

Discussed topics:

Meson-exchange models

Hyperons in matter

• Brueckner-Goldstone

Hartree-Fock approach

Chiral effective field theory

MTHS24 - Exercise sheet 9

Morning: Laura Tolos / Andrew Jackura Afternoon: XXX, YYY



Wednesday, 24 July 2024

Lecture material

References:

- R. Machleidt, Advances in Nuclear Physics 19, 189 (1989)
- R. Machleidt, D. R. Entem, Phys. Rept. 503, 1 (2011)
- A Pich Rep. Prog. Phys. 58, 563 (1995)
- V. Koch, Int. J. Mod. Phys. E 6, 203 (1997)
- S. Petschauer, J. Haidenbauer, N. Kaiser,
 U. G. Meißner and W. Weise, Front. in Phys.
 8, 12 (2020)
- B. D. Day, Reviews of Modern Physics 39, 719 (1967); 50, 495 (1978)
- R.D. Mattuck, A guide to Feynman Diagrams in the Many-Body problem, Dover, New York, 1992. Editor McGraw-Hill, Inc.

Exercices

Brueckner-

9.1 Effecitve Theory Questions

(a) Explain the Yukawa's idea (for NN interaction)

Hyperon-nucleon and hyperon-hyperon interac-

Theory:

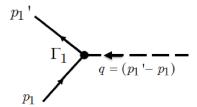
- (b) Explain what an effective theory is and indicate the four pillars where the power of an effective theory lies in.
- (c) Explain the many-body problem (for NN interaction)

9.2 Gradient Coupling

Consider the pseudo-vector (or gradient coupling) to the nucleon described by the Lagrangian

$$\mathcal{L} = -\frac{f_{\pi NN}}{m_{\pi}} \bar{\psi} \gamma^{\mu} \gamma_5 \vec{\tau} \psi \cdot \partial_{\mu} \vec{\phi}^{(\pi)}, \tag{1}$$

and compute the contribution of the following diagram to the one-pion exchange potential (OPEP)



Some hints:

- You should compute $\bar{u}(p_1',s_1)\Gamma_{\pi NN}u(p_1,s_1)$, with $\Gamma_{\pi NN}=(i)^2\frac{f_{\pi NN}}{m_\pi}\gamma^\mu\gamma_5\vec{\tau}q_\mu$ for the incoming pion. Note that i is the imaginary unit, (γ^μ,γ_5) are the gamma matrices, $\vec{\tau}$ is the isospin vector, q is the four-momentum carried by the pion $(q_\mu=p_1'-p_1)$, $f_{\pi NN}$ is the πNN coupling and m_π is the pion mass.
- Consider the static limit $(q_0 \to 0)$
- The Dirac spinors u(p,s) in the non-relativistic approach are given by $u(p,s)=\begin{pmatrix} \chi_s \\ 0 \end{pmatrix}$, with χ_s the two-component Pauli spinor.
- The gamma matrices are defined as

$$\gamma^0 = \left(\begin{array}{cc} \mathbb{1} & 0 \\ 0 & -\mathbb{1} \end{array} \right), \quad \gamma^k = \left(\begin{array}{cc} 0 & \sigma^k \\ -\sigma^k & 0 \end{array} \right), \quad \gamma^5 = \gamma_5 = \left(\begin{array}{cc} 0 & \mathbb{1} \\ \mathbb{1} & 0 \end{array} \right)$$

with σ^k the three Pauli matrices (k running from 1 to 3). Also $\{\gamma^\mu,\gamma^\nu\}=2g^{\mu\nu}$ and $\{\gamma_5,\gamma^\mu\}=0$, with μ and ν running from 0 to 3. The metric tensor is $g_{00}=+1$, $g_{kk}=-1$, $g_{\mu\neq\nu}=0$.

9.3 Nucleon-nucleon potential with scalar meson exchange

Calculate the nucleon-nucleon potential due to scalar meson exchange. Things to be considered:

- you have to reproduce the expression on the slides;
- the scalar propagator is given by

$$\frac{i}{q^2 - m_s^2},$$

where m_s is the scalar mass and q the four-momentum;

• work in the center-of-mass frame. If $\vec{p_1}$ y $\vec{p_2}$ are the momenta of initial particles 1 y 2, respectively, and $\vec{p'}_1$ y $\vec{p'}_2$ are the momenta of the final particles 1 y 2, respectively, then we can define

$$\vec{p}_1 = -\vec{p}_2 = \vec{p}, \vec{p'}_1 = -\vec{p'}_2 = \vec{p'}.$$

With these definitions, we define

$$\begin{aligned} \vec{k} &=& 1/2(\vec{p}+\vec{p'}), \\ \vec{q} &=& \vec{p'}-\vec{p}; \end{aligned}$$

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- work in the non-relativistic approximation: $E+M\sim 2M$;
- ullet the angular momentum $ec{L}$ is defined as $ec{L}=\mathrm{i}~(ec{k} imesec{q}).$