

COMPSCI/SFWRENG 2FA3
Discrete Mathematics with Applications II
Winter 2020

Assignment 10

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Assignment 10 consists of two problems. You must write your solutions to the problems using LaTeX.

Please submit Assignment 10 as two files, `Assignment_10_YourMacID.tex` and `Assignment_10_YourMacID.pdf`, to the Assignment 10 folder on Avenue under Assessments/Assignments. *YourMacID* must be your personal MacID (written without capitalization). The `Assignment_10_YourMacID.tex` file is a copy of the LaTeX source file for this assignment (`Assignment_10.tex` found on Avenue under Contents/Assignments) with your solution entered after each problem. The `Assignment_10_YourMacID.pdf` is the PDF output produced by executing

```
pdflatex Assignment_10_YourMacID
```

This assignment is due **Sunday, April 5, 2020 before midnight**. You are allow to submit the assignment multiple times, but only the last submission will be marked. **Late submissions and files that are not named exactly as specified above will not be accepted!** It is suggested that you submit your preliminary `Assignment_10_YourMacID.tex` and `Assignment_10_YourMacID.pdf` files well before the deadline so that your mark is not zero if, e.g., your computer fails at 11:50 PM on April 5.

Although you are allowed to receive help from the instructional staff and other students, your submission must be your own work. Copying will be treated as academic dishonesty! If any of the ideas used in your submission were obtained from other students or sources outside of the lectures and tutorials, you must acknowledge where or from whom these ideas were obtained.

Problems

1. [10 points] Construct an NPDA that accepts the language

$$\{a^m b^n \mid m, n \geq 1 \text{ with } m \neq n\}.$$

Name: Hishmat Salehi

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Date: April 4, 2020

Solution:

Let $M = (Q, \Sigma, \Gamma, \delta, s, \perp, F)$ be the NPDA where:

$$Q = \{s, f\}.$$

$$F = \{f\}$$

$$\Sigma = \{a, b\}.$$

$$\Gamma = \{\perp, a, b\}.$$

δ contains the following transitions:

a. $((s, a, \perp), (s, a\perp)).$

b. $((s, a, a), (s, aa)).$

c. $((s, b, a), (s, \epsilon)).$

d. $((s, b, \perp), (f, \perp)).$

e. $((s, \epsilon, a), (f, \perp)).$

M clearly accepts $\{a^m b^n \mid m, n \geq 1 \text{ with } m \neq n\}$. by final state.

2. [10 points] Let $G = (N, \Sigma, P, S)$ be the CFG where $N = \{S, A, B\}$, $\Sigma = \{a, b\}$, and P contains the following productions:

$$S \rightarrow bA \mid aB.$$

$$A \rightarrow bAA \mid aS \mid a.$$

$$B \rightarrow aBB \mid bS \mid b.$$

Construct an NPDA that accepts $L(G)$.

Name: Hishmat Salehi

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Date: April 4, 2020

Solution:

Let $M = (Q, \Sigma, \Gamma, \delta, q, S, \emptyset)$ be the NPDA where:

$$Q = \{q\}.$$

$$F = \{\}$$

$$\Sigma = \{a, b\}.$$

$$\Gamma = \{S, A, B\}.$$

δ contains the following transitions:

1. $((q, b, S), (q, A))$.
2. $((q, a, S), (q, B))$.
3. $((q, b, A), (q, AA))$.
4. $((q, a, A), (q, S))$.
5. $((q, a, A), (q, \epsilon))$.
6. $((q, a, B), (q, BB))$.
7. $((q, b, B), (q, S))$.
8. $((q, b, B), (q, \epsilon))$.

M clearly accepts $L(G)$. by empty stack.