

COMPSCI/SFWRENG 2FA3  
Discrete Mathematics with Applications II  
Winter 2020

## Assignment 6

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Revised: March 6, 2020

Assignment 6 consists of two problems. You must write your solutions to the problems using LaTeX.

Please submit Assignment 6 as two files, `Assignment_6_YourMacID.tex` and `Assignment_6_YourMacID.pdf`, to the Assignment 6 folder on Avenue under Assessments/Assignments. *YourMacID* must be your personal MacID (written without capitalization). The `Assignment_6_YourMacID.tex` file is a copy of the LaTeX source file for this assignment (`Assignment_6.tex` found on Avenue under Contents/Assignments) with your solution entered after each problem. The `Assignment_6_YourMacID.pdf` is the PDF output produced by executing

```
pdflatex Assignment_6_YourMacID
```

This assignment is due **Sunday, March 8, 2020 before midnight**. You are allowed to submit the assignment multiple times, but only the last submission will be marked. **Late submissions and files that are not named exactly as specified above will not be accepted!** It is suggested that you submit your preliminary `Assignment_6_YourMacID.tex` and `Assignment_6_YourMacID.pdf` files well before the deadline so that your mark is not zero if, e.g., your computer fails at 11:50 PM on March 8.

Although you are allowed to receive help from the instructional staff and other students, your submission must be your own work. Copying will be treated as academic dishonesty! If any of the ideas used in your submission were obtained from other students or sources outside of the lectures and tutorials, you must acknowledge where or from whom these ideas were obtained.

## Problems

1. [10 points] Let  $L = \{a^m b^n c^p \mid 0 \leq m, n, p\}$ . Construct an NFA  $N$  (without  $\epsilon$ -transitions) and an NFA  $N'$  with  $\epsilon$ -transitions such that  $L(N) = L(N') = L$ . Present each of  $N$  and  $N'$  as both a transition table and a transition diagram.

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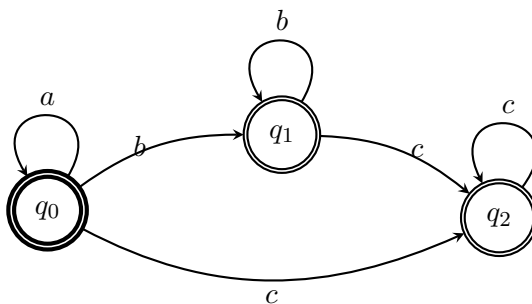
**Date:** March 8, 2020

### Solution for Problem 1:

Transition Table for  $N$ :

$Q \backslash \Sigma$		$\Sigma$		
		$a$	$b$	$c$
start & final $\rightarrow$	$q_0$	$\{q_0\}$	$\{q_1\}$	$\{q_2\}$
final $\rightarrow$	$q_1$	$\{\}$	$\{q_1\}$	$\{q_2\}$
final $\rightarrow$	$q_2$	$\{\}$	$\{\}$	$\{q_2\}$

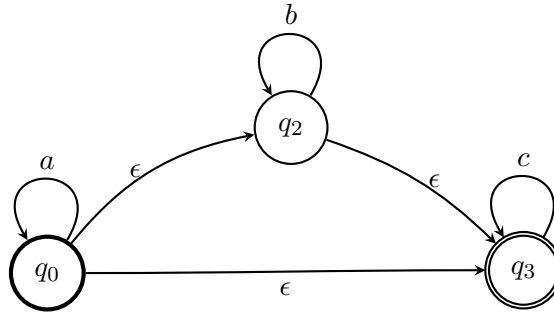
Transition diagram for  $N$ :



Transition Table for  $N'$ :

		$\Sigma$				
		$Q$	$a$	$b$	$c$	$\epsilon$
start $\rightarrow$	$q_0$	$\{q_0\}$	$\{\}$	$\{\}$	$\{\}$	$\{q_2, q_3\}$
	$q_2$	$\{\}$	$\{q_2\}$	$\{\}$	$\{\}$	$\{q_3\}$
final $\rightarrow$	$q_3$	$\{\}$	$\{\}$	$\{q_3\}$	$\{\}$	$\{\}$

Transition diagram for  $N'$ :



2. [10 points] Construct a DFA  $M$  with no inaccessible states that is equivalent to the NFA defined by the following transition table:

		$\Sigma$	
		$Q$	
		0	1
start $\rightarrow$	$p$	$\{q, s\}$	$\{q\}$
final $\rightarrow$	$q$	$\{r\}$	$\{q, r\}$
	$r$	$\{s\}$	$\{p\}$
final $\rightarrow$	$s$	$\{\}$	$\{p\}$

Present  $M$  as both a transition table and a transition diagram.

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**Solution for Problem 2:**

Transition Table for  $M$ :

		$\Sigma$	
		$Q$	
		0	1
	start $\rightarrow$	$\{p\}$	$\{q\}$
	final $\rightarrow$	$\{q\}$	$\{q, r\}$
		$\{r\}$	$\{p\}$
	final $\rightarrow$	$\{s\}$	$\{p\}$
		$\{q, s\}$	$\{p, q, r\}$
	final $\rightarrow$	$\{q, r\}$	$\{p, q, r\}$
		$\{r, s\}$	$\{p\}$
	final $\rightarrow$	$\{p, q, r\}$	$\{p, q, r\}$
	final $\rightarrow$	$\{q, r, s\}$	$\{p, q, r\}$

Transition diagram for  $M$ :

