



# INFO20003 Database Systems

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Tutorial 5  
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- 1. Relational algebra (RA) review - 15 min**
- 2. Relational algebra and SQL statements  
- 35 min**
- 3. Lab - 1 hour**

## Relation algebra

- procedural query language for relational model
- provide theoretical foundation for RD and SQL
- consists of a collection of **operators** (unary/binary)
- **operand**: instance(s) of a relation, returns a relation instance.
- **Five basic operators** of Relational Algebra that can form other compound operators

# Fundamental operations

## Removal operators: Selection ( $\sigma$ ) and Projection ( $\pi$ )

- **Projection:**

- $\pi_{A_1, A_2, \dots, A_n}(R)$  where  $R$  is relation and  $A$  are attributes that ‘projected’
- Create new relation with a **subset of attributes**
- All tuples are included, but only **chosen attributes** are kept
- Projection operator has to *eliminate duplicates*

- **Selection:**

- $\sigma_C(R)$  where  $R$  is relation and  $C$  is condition used to **filter rows**
- Create new relation consisting of those **rows** for which  $C$  is true

## Projection Example

FirstName	LastName	Phone	Email
Jon	Snow	0551-999-210	knowsnothing@hotmail.com
Daenerys	Targaryen	0569-988-112	bendtheknee@gmail.com
Jamie	Lannister	0531-987-654	handsfree@gmail.com
Night	King	0566-123-456	killerstare@gmail.com

The expression  $\pi_{\text{FirstName, LastName}}(\text{Person})$  will result in:

FirstName	LastName
Jon	Snow
Daenerys	Targaryen
Jamie	Lannister
Night	King



## Selection Example

FirstName	LastName	Phone	Email
Jon	Snow	0551-999-210	knowsnothing@hotmail.com
Daenerys	Targaryen	0569-988-112	bendtheknee@gmail.com
Jamie	Lannister	0531-987-654	handsfree@gmail.com
Night	King	0566-123-456	killerstare@gmail.com

$\sigma_{\text{FirstName} = \text{'Jon'} \vee \text{LastName} = \text{'King'}} (\text{Person})$

FirstName	LastName	Phone	Email
Jon	Snow	0551-999-210	knowsnothing@hotmail.com
Night	King	0566-123-456	killerstare@gmail.com



## Selection Projection Combination

FirstName	LastName	Phone	Email
Jon	Snow	0551-999-210	knowsnothing@hotmail.com
Daenerys	Targaryen	0569-988-112	bendtheknee@gmail.com
Jamie	Lannister	0531-987-654	handsfree@gmail.com
Night	King	0566-123-456	killerstare@gmail.com

$\pi_{\text{FirstName, LastName}} (\sigma_{\text{FirstName} = \text{'Jon'} \vee \text{LastName} = \text{'King'}} (\text{Person}))$

FirstName	LastName
Jon	Snow
Night	King



## Fundamental operations

### Set operators: Set-difference ( $-$ ) and Union ( $\cup$ )

- **constraint:** both relations must have the **same attributes** with the **same domains**. the **ordering** of attributes should be kept **consistent**.
- **Set-difference:**
  - $R - S$ . result will be every row which is in R but not in S
- **Union:**
  - $R \cup S$ . result will be every row which is either in R or S
  - Duplicates are removed



## Union Example

GoodGuys

FirstName	LastName
Jon	Snow
Daenerys	Targaryen

BadGuys

FirstName	LastName
Cersei	Lannister
Night	King

GoodGuys  $\cup$  BadGuys will result in:

FirstName	LastName
Jon	Snow
Daenerys	Targaryen
Cersei	Lannister
Night	King

## Difference Example

RandomCombo1

FirstName	LastName
Jon	Snow
Daenerys	Targaryen
Jamie	Lannister
Night	King

RandomCombo2

FirstName	LastName
Night	King
Arya	Stark
Cersei	Lannister
Daenerys	Targaryen

RandomCombo1 – RandomCombo2 will result in:

FirstName	LastName
Jon	Snow
Jamie	Lannister



## Fundamental operations

### Set operators: Cross Product ( $\times$ )

- **Cross Product ( $\times$ ):**
  - Each row of R pairs with each row of S. The resulting schema has all the attributes from both relations. If some attributes have same name, rename them by using renaming operator.

$$\rho(C(1 \rightarrow sid1, 5 \rightarrow sid2), S1 \times R1)$$

Result relation name



## Cross Product Example

Person

FirstName	LastName	Email
Jon	Snow	knowsnothing@hotmail.com
Night	King	killerstare@gmail.com

Weapon

Weapon	Metal
Sword	Valyrian steel
Dagger	Dragon glass

Person  $\times$  Weapon will result in:

FirstName	LastName	Email	Weapon	Metal
Jon	Snow	knowsnothing@hotmail.com	Sword	Valyrian steel
Jon	Snow	knowsnothing@hotmail.com	Dagger	Dragon glass
Night	King	killerstare@gmail.com	Sword	Valyrian steel
Night	King	killerstare@gmail.com	Dagger	Dragon glass



## Compound operations

- operators are not adding any computational power to the language but are useful shorthand.
- All these operators can be expressed using the basic operators



## Compound operations

### set operator: Intersection( $\cap$ )

- **Intersection ( $\cap$ ):**
  - union compatible
  - result is a relation containing all the tuples which are present in both relations

$$R \cap S = R - (R - S)$$

## Intersection Example

RandomCombo1

FirstName	LastName
Jon	Snow
Daenerys	Targaryen
Jamie	Lannister
Night	King

RandomCombo2

FirstName	LastName
Night	King
Arya	Stark
Cersei	Lannister
Daenerys	Targaryen

RandomCombo1  $\cap$  RandomCombo2 will result in:

FirstName	LastName
Daenerys	Targaryen
Night	King



## Compound operations

### set operator: Natural Join( $\bowtie$ )

- **Natural Join( $\bowtie$ ):**
  - identifies **attributes common** to each relation
  - pairing each tuple from R and S where the common attributes are **equal**
  - In general are compound operators involving cross product, selection and occasionally projection
  - omit duplicate attributes





## Compound operations

### set operator: Natural Join( $\bowtie$ )

- **Natural Join( $\bowtie$ ) steps:**
  - Compute  $R \times S$
  - Select rows where attributes that appear in both relations have equal values.
  - Project all unique attributes and one copy of each of the common ones.

## Natural Join Example

Person

FirstName	LastName	Email
Jon	Snow	knowsnothing@hotmail.com
Daenerys	Targaryen	bendtheknee@gmail.com
Tyrion	Lannister	idrinkandiknow@gmail.com
Night	King	killerstare@gmail.com

WeaponOwner

Weapon	LastName	Metal
Sword	Snow	Valyrian steel
Dagger	Lannister	Dragon glass

**Person  $\times$  Weapon (intermediate result):**



## Natural Join Example

FirstName	LastName	Email	Weapon	LastName	Metal
Jon	Snow	knowsnothing@hotmail.com	Sword	Snow	Valyrian steel
Jon	Snow	knowsnothing@hotmail.com	Dagger	Lannister	Dragon glass
Daenerys	Targaryen	bendtheknee@gmail.com	Sword	Snow	Valyrian steel
Daenerys	Targaryen	bendtheknee@gmail.com	Dagger	Lannister	Dragon glass
Tyrion	Lannister	idrinkandiknow@gmail.com	Sword	Snow	Valyrian steel
Tyrion	Lannister	idrinkandiknow@gmail.com	Dagger	Lannister	Dragon glass
Night	King	killerstare@gmail.com	Sword	Snow	Valyrian steel
Night	King	killerstare@gmail.com	Dagger	Lannister	Dragon glass



## Natural Join Example

**Person  $\bowtie$  Weapon** will result in:

FirstName	LastName	Email	Weapon	Metal
Jon	Snow	knowsnothing@hotmail.com	Sword	Valyrian steel
Tyrion	Lannister	idrinkandiknow@gmail.com	Dagger	Dragon glass

# Compound operations

## set operator: Condition Join (Theta/Inner Join)

- **Condition Join( $\bowtie_c$ ) steps:**
  - $R \bowtie_c S$  joins rows from relation  $R$  and  $S$  such that the Boolean condition  $C$  is true
  - commonly  $C$  is of the type  $A = B$ , making an “equi-join”.

$$R \bowtie_c S = \sigma_C(R \times S)$$

## Condition Join Example

Person

FirstName	LastName	Email
Jon	Snow	knowsnothing@hotmail.com
Daenerys	Targaryen	bendtheknee@gmail.com
Tyrion	Lannister	idrinkandiknow@gmail.com
Night	King	killerstare@gmail.com

WeaponOwner

Weapon	Name	Metal
Sword	Snow	Valyrian steel
Dagger	Lannister	Dragon glass

**Person  $\times$  Weapon (intermediate result):**

## Condition Join Example

FirstName	LastName	Email	Weapon	Name	Metal
Jon	Snow	knowsnothing@hotmail.com	Sword	Snow	Valyrian steel
Jon	Snow	knowsnothing@hotmail.com	Dagger	Lannister	Dragon glass
Daenerys	Targaryen	bendtheknee@gmail.com	Sword	Snow	Valyrian steel
Daenerys	Targaryen	bendtheknee@gmail.com	Dagger	Lannister	Dragon glass
Tyrion	Lannister	idrinkandiknow@gmail.com	Sword	Snow	Valyrian steel
Tyrion	Lannister	idrinkandiknow@gmail.com	Dagger	Lannister	Dragon glass
Night	King	killerstare@gmail.com	Sword	Snow	Valyrian steel
Night	King	killerstare@gmail.com	Dagger	Lannister	Dragon glass



## Natural Join Example

**Person** ⋈<sub>LastName = Name</sub> **Weapon** will result in:

FirstName	LastName	Email	Weapon	Name	Metal
Jon	Snow	knowsnothing@hotmail.com	Sword	Snow	Valyrian steel
Tyrion	Lannister	idrinkandiknow@gmail.com	Dagger	Lannister	Dragon glass





**Any questions?**

## Structured Query Language(SQL)

- Domain-specific language
- Language for data manipulation in RD
- Allow to create/delete tables, add/update/remove data, etc

## Structured Query Language(SQL)

- **Data Definition Language (DDL):** To define and setup the database `CREATE`, `ALTER`, `DROP`
- **Data Manipulation Language (DML):** To maintain and use the database, `SELECT`, `INSERT`, `DELETE`, `UPDATE`
- **Data Control Language (DCL):** To control access to the database, `GRANT`, `REVOKE`
- **Other Commands:** Administer the databas, Transaction Control

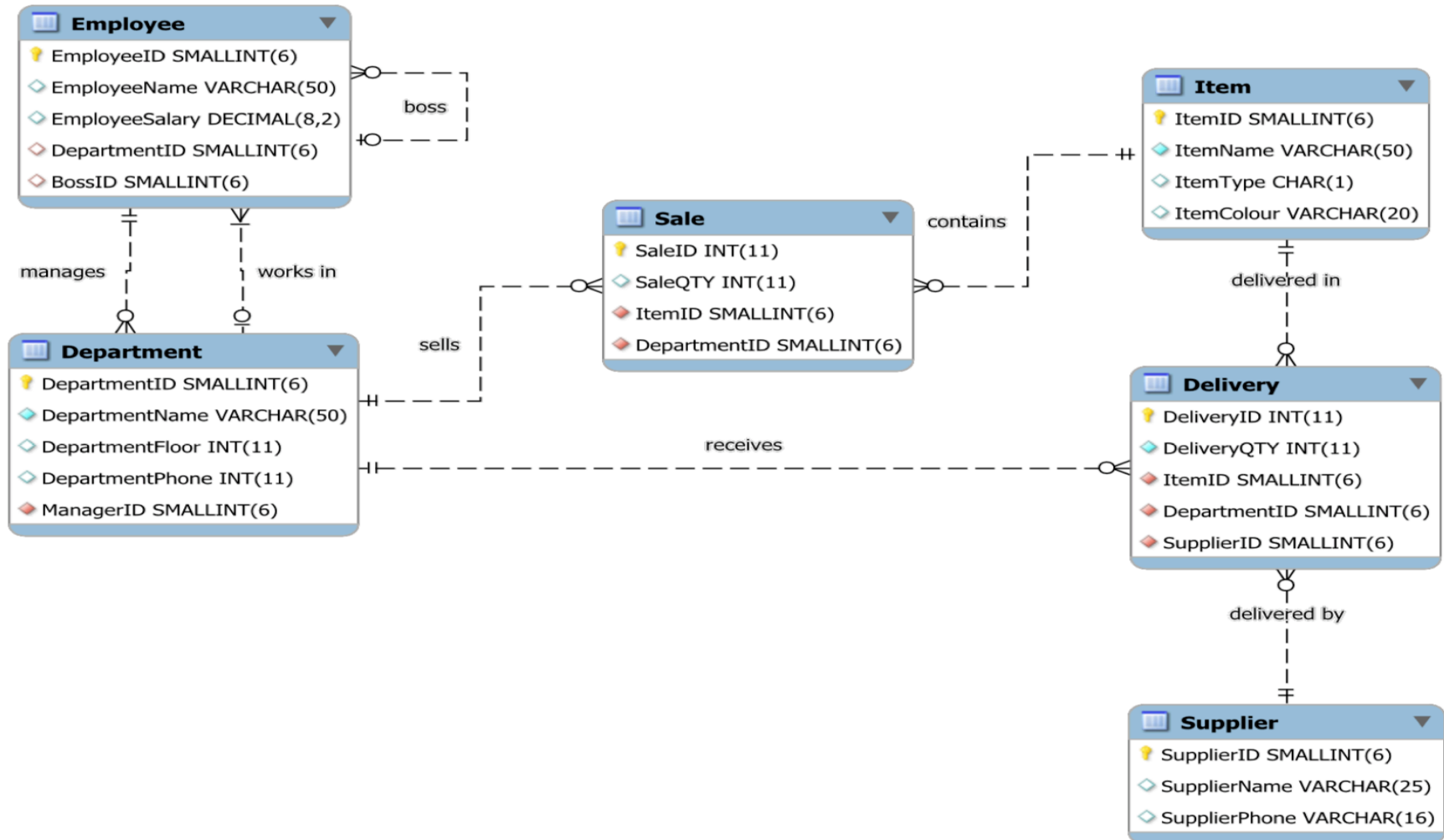
## Structured Query Language(SQL)

- **SELECT** [ALL | DISTINCT] *select\_expr* [, *select\_expr* ...]
  - List the columns (and expressions) that are returned from the query
- **[FROM *table\_references* ]**
  - Indicate the table(s) or view(s) from where the data is obtained
- **[WHERE *where\_condition*]**
  - Indicate the conditions on whether a particular row will be in the result
- **[GROUP BY {*col\_name* | *expr*} [ASC | DESC], ...]**
  - Indicate categorisation of results
- **[HAVING *where\_condition*]**
  - Indicate the conditions under which a particular category (group) is included in the result
- **[ORDER BY {*col\_name* | *expr* | *position*} [ASC | DESC], ...]**
  - Sort the result based on the criteria
- **[LIMIT {[*offset*,] *row\_count* | *row\_count* OFFSET *offset*}]**
  - Limit which rows are returned by their return order (ie 5 rows, 5 rows from row 2)



**Any questions?**

Consider the following schema:



**a. Find the names of all employees.**

**Relational Algebra:**  $\pi_{\text{EmployeeName}}(\text{Employee})$

**SQL:** `SELECT EmployeeName  
FROM Employee;`

**b. Find the names of all employees in department number 1.**

**Relational Algebra:**  $\pi_{\text{EmployeeName}}(\sigma_{\text{DepartmentID} = 1}(\text{Employee}))$

**SQL:** `SELECT EmployeeName  
FROM Employee  
WHERE DepartmentID = 1;`

**c. List the names of green items of type C.**

**Relational Algebra:**  $\pi_{\text{ItemName}} (\sigma_{\text{ItemColour} = \text{'Green'} \wedge \text{ItemType} = \text{'C'}} (\text{Item}))$

**SQL:** `SELECT ItemName  
FROM Item  
WHERE ItemType = 'C' AND ItemColour = 'Green';`

**d. Find the items sold by the departments on the second floor (only show ItemID).**

**Relational Algebra:**  $\pi_{\text{ItemID}} (\sigma_{\text{DepartmentFloor} = 2} (\text{Sale} \bowtie \text{Department}))$

**SQL:** `SELECT DISTINCT ItemID  
FROM Sale NATURAL JOIN Department  
WHERE DepartmentFloor = 2;`



**e. Find the names of brown items sold by the Recreation department.**

**Relational Algebra:**  $\pi_{\text{ItemName}} (\sigma_{\text{DepartmentName} = \text{'Recreation'} \wedge \text{ItemColour} = \text{'Brown'}} (\text{Item} \bowtie \text{Sale} \bowtie \text{Department}))$

**SQL:** `SELECT ItemName  
FROM Item NATURAL JOIN Sale NATURAL JOIN Department  
WHERE DepartmentName = 'Recreation'  
AND ItemColour = 'Brown';`

**f. Find the employees whose salary is less than half that of their managers.**

$$\begin{aligned} &\rho(\text{Emp}(\text{EmployeeName} \rightarrow \text{EmpName}, \text{EmployeeSalary} \rightarrow \text{EmpSalary}, \\ &\quad \text{BossID} \rightarrow \text{EmpBossID}), \text{Employee}) \\ &\rho(\text{Boss}(\text{EmployeeID} \rightarrow \text{BossEmployeeID}, \\ &\quad \text{EmployeeSalary} \rightarrow \text{BossSalary}), \text{Employee}) \\ &\pi_{\text{EmpName}} (\sigma_{\text{EmpSalary} < (\text{BossSalary} / 2)} (\text{Emp} \bowtie_{\text{EmpBossID} = \text{BossEmployeeID}} \text{Boss})) \end{aligned}$$

*Or you could use an SQL-like notation:*

$\text{Emp} := \text{Employee}$

$\text{Boss} := \text{Employee}$

$$\pi_{\text{Emp.EmployeeName}} (\sigma_{\text{Emp.EmployeeSalary} < (\text{Boss.EmployeeSalary} / 2)} (\text{Emp} \bowtie_{\text{Emp.BossID} = \text{Boss.EmployeeID}} \text{Boss}))$$

**SQL:** **SELECT** Emp.EmployeeName  
**FROM** Employee **AS** Emp  
**INNER JOIN** Employee **AS** Boss  
**ON** Emp.BossID = Boss.EmployeeID  
**WHERE** Emp.EmployeeSalary < (Boss.EmployeeSalary / 2);



**Any questions?**



## Please refer to Lab 5 on LMS

Let me know if you encounter with  
any problem

**More practice on SQL Skills**