Data Analytics with Python Prof. Ramesh Anbanandam Department of Management Studies Indian Institute of Technology - Roorkee

Lecture – 56 Hierarchical Method of Clustering - II

In a previous lecture, I have explained introduction to hierarchical clustering and different types of distance measures. In this lecture, I have taken a numerical example, with the help of the numerical example, I am going to explain how to do hierarchical clustering method, for that same problem, I am going to explain how to use Python for doing hierarchical clustering.

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Agenda

- · Agglomerative hierarchical algorithm
- · Python demo

So, the agenda for this lecture is agglomerative hierarchical algorithm, the second one is python demo.

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Example for Hierarchical Agglomerative Clustering (HAC)

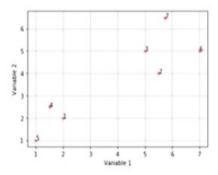
 A data set consisting of seven objects for which two variables were measured.

Object	Variable 1	Variable 2
1	2.00	2.00
2	5.50	4.00
3	5.00	5.00
4	1.50	2.50
5	1.00	1.00
6	7.00	5.00
7	5.75	6.50

So the example of hierarchical agglomerative clustering, HAC; a data set consists of 7 objects for which 2 variables were measured. There are 7 objects; 1, 2, 3, 4, 5, 6, 7, variable 1 and variable 2. So, variable 1 is 2, 5, 5.5, 5 and so on. Variable 2 is 2, 4, 5, 2, 1, 5, 6 and so on.

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Scatter plot



When you plot in the scatterplot, it is appearing that there are 7 data set, variable 1 in x axis, variable 2 in y axis. Now, we are going to do hierarchical clustering for this data set.

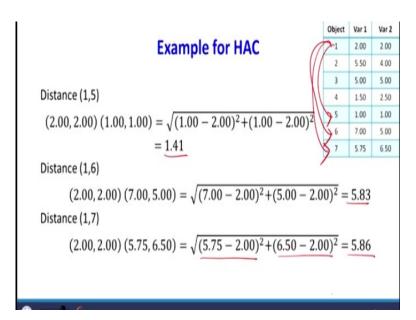
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	Object	Var 1	Var
Example for HAC		2.00	2.00
	C 2	5.50	4.00
NOT 8 10 000 NOS 00 00 00 00 00 00 00 00 00 00 00 00 00	3	5.00	5.00
 Calculate Euclidean Distance and create the distance matrix. 	54	1.50	2.50
Distance[$(x_1, y_1), (x_2, y_2)$] = $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$	5	1.00	1.00
	6	7.00	5.00
Distance (1,2)	7	5.75	6.50
$(2.00, 2.00) (5.50, 4.00) = \sqrt{(5.50 - 2.00)^2 + (4.00 - 2.00)^2}$	00)2	= 4.02	2
Distance (1,3)			
$(2.00, 2.00) (5.00, 5.00) = \sqrt{(5.00 - 2.00)^2 + (5.00 - 2.00)^2}$	00)2	= 4.24	4
Distance (1,4)			

What is the first one; calculate the Euclidean distance and create a distance matrix, what we are going to do; first we are going to create a distance matrix, for that we are going to find out the distance between 1 and 2, 1 and 3, 1 and 4, 1 and 5, 1 and 6, 1 and 7 and 2 and 3, 2 and 4, 2 and 5, 2 and 6 and 2 and 7, then 3 and 4, 3 and 5, 3 and 6 and 3 and 7 then 4 and 5, 4 and 6 and 4 and 7, then 5 and 6 and 5 and 7 finally, 6 and 7.

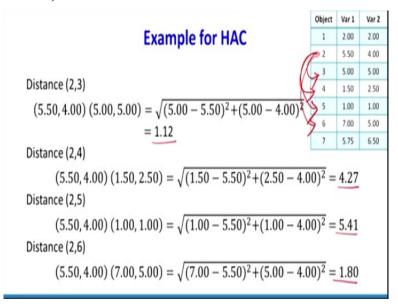
First we will find the distance between object 1 and 2, so the object 1 is 2, 2, object 2 is 5.5, 4, after finding the Euclidean distance, we know the formula is $x^2 - x^2 + y^2 - y^2 + y^2$

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Now, we will find the distance between 1 and 5, so this 1 and 5 because this we have done it, so 1 and 5 is 2, 2; the position of the 5th object is 1, 1, so it is 1 - 2 whole square + 1 - 2 whole square, it is 1.41. Now, we will find the distance 1 and 6 that is 2, 2, then 7, 5, so it is 7 - 2 whole square + 5 - 2 whole square that is 5.83. Similarly, we can find the distance between 1 and 7 that is 2, 2 versus 5.75 and 6.5.

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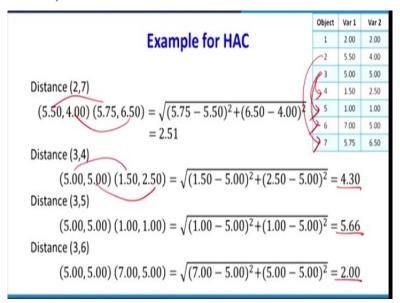


So, it is a 5.75 - 2 whole square + 6.5 - 2 whole square, we got 5.86, now we have done 1 versus all the point, now we go second versus 3, the distance between 2 and 3, the position of 2 is 5, 5, 4; 3 is 5, 5, so the distance is 5 - 5.5 whole square + 5 - 4 whole square, it is 1.12. Now, 2 and 4;

5.5, 4 is the position of 2, 4 is the position of 2, the position of object 4 is 1.5, 2.5, so the distance is 1.5 - 5.5 whole square + 2.5 - 4 whole square that is 4.27.

Next we will find the distance between 2 and 5; we know the position of 2 is 5.5, 4, the position of object 5 is 1, 1, see this point, the distance is (1 - 5.5) whole square + (1 - 4) whole square that is 5.41. Now, we can find the distance between 2 and 6, so the position of object 6 is 7, 5, so the distance is (7 - 5.5) whole square + (5 - 4) whole square that is 1.81.

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The next one; we are going to find the distance between 2 and 7, so 2 and 7, so the position of object 7 is 5.75, 6.5, so the distance is 5.75 - 5.5 whole square + 6.5 - 4 whole square, so this difference whole square and this difference whole square that is 2.51. Now, 2; the point 2, the object 2 and other all 7's we compare, now we will compare 3; 3 and 4, 3 and 5, 3 and 6 and 3 and 7.

So, the 3 and 4 distance is the position of point '3' is 5, 5 and 4 is 1.5, 2.5, so this distance versus this distance, this difference, so 1.5 - 5 whole square + 2.5 - 5 whole square that is 4.30. Next 3 and 5, so 5, 5 and the 1; 1, 1 is the position of object 5, so what will happen; 1 - 5 whole square + 1 - 5 whole square, 5.66. Now, 3 and 6; so 3 is 5, 5; 6 is 7, 5, so the difference is 7 - 5 whole square + 5 - 5 whole square, the distance is 2.

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	Object	Var 1	Var 2
Example for HAC	1	2.00	2.00
	2	5.50	4.00
2 (2.7)	<u>_3</u>	5.00	5.00
Distance (3,7)	14	1.50	2.50
$(5.00, 5.00) (5.75, 6.50) = \sqrt{(5.75 - 5.00)^2 + (6.50 - 5.00)^2}$	95	1.00	1.00
= 1.68	6	7.00	5.00
Distance (4,5)) 1	5.75	6.50
$(1.50, 2.50) (1.00, 1.00) = \sqrt{(1.00 - 1.50)^2 + (1.00 - 2.50)^2}$	$(0)^2 =$	1.58	
Distance (4,6)			
$(1.50, 2.50) (7.00, 5,00) = \sqrt{(7.00 - 1.50)^2 + (5.00 - 2.5)^2}$	$\overline{(0)^2} =$	6.04	
Distance (4,7)			
$(1.50, 2.50) (5.75, 6.50) = \sqrt{(5.75 - 1.50)^2 + (6.50 - 2.50)^2}$	(0)2 -	E 01	

Now, we are going to find the next one; 3, 7, so 3, 7 what is the distance; we know position of 3 is 5, 5; 7 is 5.75 - 6.50, so this difference whole square versus this difference whole square, so 5.75 - 5 whole square + 6.5 - 5 whole square that is 1.68. Now, we have to find out 3 versus all the point, now we will take 4, 5 and 4, 6 and 4, 7. So, the distance between 4 and 5 is 1.5 - 2.5 is a the position of object 4, for the 5th one it is 1, 1.

When you look at the distance, it is 1.58, then 4 and 6 we have done that one, now we will go for 4 and 6. The 4 and 6 is the 4th 1.5, 2.5, the 6th position is 7, 5, so the difference is 7 - 1.5 whole square + 5 - 2.5 whole square equal to 6.04. Now, we will find out 4 versus 7, the distance between 4 and 7, the 1.5, 2.5, the position of object 7 is 5.75, 6.50, so the this difference whole square plus this difference whole square.

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Example for HAC 2.00 2.00 5.50 4.00 5.00 5.00 Distance (5,6) 1.50 2.50 1.00 1.00 $(1.00, 1.00) (7.00, 5.00) = \sqrt{(7.00 - 1.00)^2 + (5.00 - 1.00)^2}$ = 7.215.75 Distance (5,7) $(1.00, 1.00) (5.75, 6.50) = \sqrt{(5.75 - 1.00)^2 + (6.50 - 1.00)^2} = 7.27$ Distance (6,7) $(7.00, 5.00) (5.75, 6.50) = \sqrt{(5.75 - 7.00)^2 + (6.50 - 5.00)^2} = 1.95$

So, 5.5; 5.75 - 1.5 whole square +6.5 - 2.5 whole square that is 5.84, 5 we have completed, now we will go 5 and 6 and 5 and 7, the distance between 5 and 6 is 1, 1 is a position of object 5, for 6th one, it is 7, 5, so it is 7 - 1 whole square +5 - 1 whole square that is 7.21. Now, we will find out distance between 5 and 7 that is 1, 1 versus 5.75 - 6.5, so it is 5.75 - 1 whole square +6.5 - 1 whole square, 7.27.

Now, 6 versus 7, we will find out the distance, so that is position of object 6 is 7, 5, position of object 7 is 5.75, 6.5, so the distance is 5.75 - 7 whole square + 6.5 - 5.00 whole square that is 1.95.

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Distance Matrix

· The distance matrix is-

	1	2	3	4	5	6	7
1	0.0						
2	4.0	0.0					
3	4.2	1.1	0.0				
4	0.7	4.3	4.3	0.0			
5	1.4	5.4	5.7	1.6	0.0		
6	5.8	1.8	2.0	6.0	7.2	0.0	
7	5.9	2.5	1.7	5.8	7.3	2.0	0.0

Now, we have compared all the distance, as I told you this is a distance matrix, see that in the diagonal it is '0' because the distance is 0, we got distance between 2 and 1, 3 and 1, 4 and 1, 5 and 1, 6 and 1, 7 and 1, this value which we got from our previous slides, so we got the distance matrix.

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Example for HAC

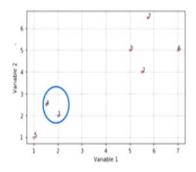
· Select minimum element to build first cluster formation-

	1	2	3	4	5	6	7
1	.0.0						
2	4.0	0.0					
3	4.2	1.1	0.0				
4	0.7	4.3	4.3	0.0			
5	1.4	5.4	5.7	1.6	0.0		
6	5.8	1.8	2.0	6.0	7.2	0.0	
7	5.9	2.5	1.7	5.8	7.3	2.0	0.0

After the distance matrix, for that hierarchical agglomerative method, select minimum element to build the first cluster formation, so among this, find out where there is a minimum distance, so the minimum distance is this one; 0.7. What are the 2 objects between 4 and 1, so what is going to do; we are going to form a cluster, in that there are 2 element is going to be there; 4 and 1.

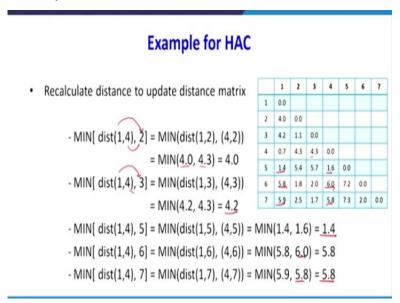
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Example for HAC



So, the 4 and 1 will form a cluster, so we got this one, 4 and 1, this is our first cluster.

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We are going to find the distance between that cluster 1, 4 forming a distance versus 2, so what we are going to do; we are going to find out distance between 1 and 2 and 4 and 2, whichever is minimum, we are going to take that distance because in cluster 1, already there are 2 object is there, we are going to consider the minimum distance. So, the distance between 1, 2, see that this value 4 and 4, 2 is 4.3, this value we take from the table.

So, the minimum distance is 4, the next one 1, 4 versus 3, similarly 1, 4 versus 5, 1, 4 versus 6, 1, 4 versus 7, so if you want to know this cluster versus 3, so minimum distance between 1, 3 and 4, 3; this 1, 3 and 4, 3, so 1, 3 it is a 4.2; 4, 3 it is a 4.3, this value, so minimum is 4.2. Now, 4th we cannot go, already the 4th one is already gone to that cluster, so we will go to 5th, so 1, 4 versus 5th object, for that we have to find out the minimum distance between 1, 5 and 4, 5.

So, 1, 5 is 1.4, this value and 4, 5 is your this value, 1.6 that 1.6, the minimum is 1.4, then 1, 4 with 6, now what happened here; we have to find out the minimum distance 1, 6 and 4, 6. So 1, 6 is 5.8 this value and 4, 6 that is 6, this value, so minimum is 5.8. Now, why we are taking 1.4 because this we formed one cluster, so from this cluster there are 2 point; 2 object 1 and 4. From 1 and 4, this 7 is how far away?

So, 2 way we have to do; 1 and 7 we have to find the distance and 4 and 7 we have to find the distance whichever minimum that has to be kept. So, 1 and 7, 4 and 7, so 1 and 7 is this one, 5.9, 4 and 7 that is your 5.8, so minimum value is 4.8.

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Example for HAC

Updated distance matrix for the cluster (1, 4)

	1,4,	2	3	5	6	7
1,4	0.0					
2	4.0	0.0				
3	4.2	1.1	0.0			
5	1.4	5.4	5.7	0.0		
6	5.8	1.8	2.0	7.2	0.0	
7	5.8	2.5	1.7	7.3	2.0	0.0

Now, we are going to update this value, so what update we have done that one; since 1 and 4 form a new cluster, so now we will find this value, how we got this value? So, 2, 1, 4; so 2, 1, 4 is 4, so we updated. Now, so updated the distance, this distance matrix is going to be used for were further steps.

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Example for HAC

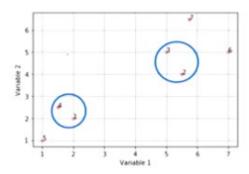
· Select minimum element to build next cluster formation-

	1,4	2	3	5	6	7
1,4	0.0					
2	4.0	0.0				
3	4.2	1.1	0.0			
5	1.4	5.4	5.7	0.0		
6	5.8	1.8	2.0	7.2	0.0	
7	5.8	2.5	1.7	7.3	2.0	0.0

So, now in that updated matrix, again you find out which is minimum, so this 1.1 is minimum that forms 3 and 2. So, now what is happening; the 3 and 2 is going to form one cluster.

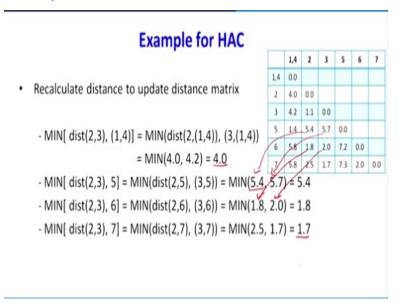
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Example for HAC



Yeah, 3 and 2 is formed one cluster.

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Now, since 2 and 3 is formed a distance and already there is 1 cluster; 1, 4, so we are going to find out the distance between 2 and 1, 4 and 3 and 1, 4. So, 2 and 1, 4 you can find out this is 4 because 1 and 4 formed a cluster, then 3 and 1, 4; 3 and 1, 4 is 4.2, in this minimum is 4. Similarly, the distance between this newly formed cluster 2, 3 versus 5, 5th point, we are not go

to 4th one because 4 is already formed a cluster, so the 5th one, we have to find out the minimum distance of 2, 5 versus 3, 5.

So, in 2, 5, the distance is 5.4 this value, this value; 3, 5; 5.7, so we got this value, in between 5.4 and 5.7, minimum is 5.4. Now, 2, 3 versus 6, now we have to find out the distance between 2, 6 and 3, 6. So, 2, 6; where is 2, 6; 6, 2, this is 1.8, this value and 3, 6, 6, 3, see these 2 value, so in that minimum is 1.8. Now, the last point is 2, 3 versus 7, so what we have to do; we have to find the minimum distance is 2 and 7 and 3 and 7. So, between 2 and 7, minimum distance is 2.5, 3 and 7 minimum distance is 1.7, so out of this minimum is 1.7, now we are going to update this new distance.

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Example for HAC

Updated distance matrix for the cluster (2, 3)

	1,4	2,3	5	6	7
1,4	0.0				
2,3	4.0	0.0			
5	1.4	5.4	0.0		
6	5.8	1.8	7.2	0.0	
7	5.8	1.7	7.3	2.0	0.0

So, this was updated distance but you see that 2 and 3 is formed 1 cluster, previously 1 and 4 will formed a cluster, now in the next slides what we are going to do; among these new updated distance matrix which is the lowest value.

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Example for HAC

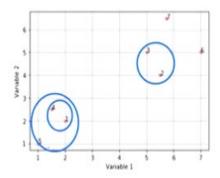
· Select minimum element to build next cluster formation-

	1,4	2,3	5	6	7
1,4	0.0				
2,3	4.0	0.0			
5	1.4	5.4	0.0		
6	5.8	1.8	7.2	0.0	
7	5.8	1.7	7.3	2.0	0.0

So, select the minimum element to build the next cluster formation, in that the minimum point is this 1.4, so what is going to happen; this object 5 is going to join with this cluster 1, 4.

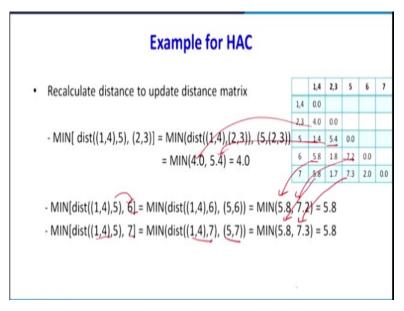
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Example for HAC



You see that the object 5 is going to form with cluster 1, 4.

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Now, what we are going to do; you see that already there is; this is a new cluster, this is not new cluster, already 1, 4 is there, one cluster that again, the object 5 is added, so the distance between this cluster versus another cluster, in that there are 2 point; 2 object you see 2, 3. So, what we have to do; minimum distance between 1 and 4 and 2, 3 and 5 and 2, 3, so what is happening here; 1 and 4 is there, 2, 3 is there, the distance is 4, this value we got it.

The distance between 5, 2, 3 so this is 5.4, so this value we got it here, this value got it, the distant minimum is 4, similarly minimum distance between 1, 4, 5 versus 6, so what you have to do; 1, 4 versus 6 and 5 and 6, so 1, 4 versus 6, 1, 4 and 6, this is 5.8 right, so this value got here. So 5, 6; 7.2 we got this value here, the minimum is 5.8 now, there is a 7th object is there, let us see how far away the object 7. So, what you have to do; we have to find the minimum distance 1, 4 and 7; 1, 4 and 7 and 5, 7, so the distance between 1, 4 and 7 is 5.8 is this value and 5, 7 is our 7.3, so the minimum is 5.8.

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Example for HAC

Updated distance matrix for the cluster ((1,4), 5)

	1,4,5	2,3	6	7
1,4,5	0.0			
2,3	4.0	0.0		
6	5.8	1.8	0.0	
7	5.8	1.7	2.0	0.0

Again, we will update our distance matrix, so what happen now, you see that the 5 has entered into this cluster because already there is 1, 4 is there, so this is our updated distance matrix.

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Example for HAC

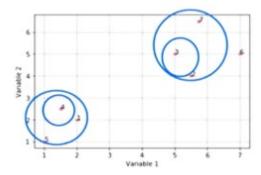
· Select minimum element to build next cluster formation-

	1,4,5	2,3	6	7
1,4,5	0.0			
2,3	4.0	0.0		
6	5.8	1.8	0.0	
7	5.8	1.7	2.0	0.0

The next step what we are going to do; in the updated distance matrix look at where there is a minimum distance is there, so the 1.7 is a minimum distance. So, what is going to do that the object 7 is going to add in to the cluster 2, 3, so now we will update this distance.

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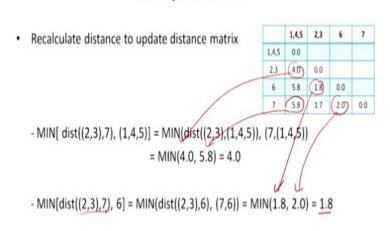
Example for HAC



What happen, see that this 7 is going to form in that cluster.

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Example for HAC



Now, what happened, we are going to you see that already there is a cluster, in that 2 object is there because 7 also joined there, so the distance between this cluster versus 1, 4, 5, this is the another cluster. So, what we are going to do; so, 2, 3, 1, 4, 5 and 7, 1, 4, 5, so 2, 3 this 1; 2, 3, 1.45, yes the distance is 2, 3 1.45, this is; this 4 has come here. Second one; the distance between 7, 1, 4, 4, 5, so this one 5.8, so this distance has come here, out of this minimum is 4.

Now, this newly formed clustered versus 6, so here one point is 2, 3 versus 6 and 7, 6, so 2, 3 versus 6, what is a distance; 2, 3 versus 6 this is 1.8, so that distance is came here, so between 7

and 6, the distance is 2, so that distance has come here. Now, the minimum is 1.8, we cannot go next one because 7 is already gone in to that cluster.

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Example for HAC

Updated distance matrix for the cluster ((2,3), 7)

	1,4,5	2,3,7	6
1,4,5	0.0		
2,3,7	4.0	0.0	
6	5.8	1.8	0.0

Now, again we will update that now, in the updation you see that we have formed 2 clusters, in that 1, 4, 5 is one group, 2, 3, 7 is another group, this is updated distance matrix. This value 4 we got from here, this 1.8 we got from here.

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Example for HAC

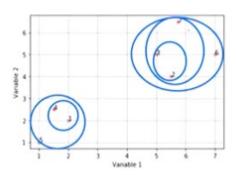
Select minimum element to build next cluster formation-

	1,4,5	2,3,7	6
1,4,5	0.0		
2,3,7	4.0	0.0	
6	5.8	1.8	0.0

Now, in the next stage select minimum element to build the next cluster formation, so after this the minimum value is 1.8, this gives the minimum distance between 6 and the cluster 2, 3, 7, so what is going to do now; the 7 is going to join with this cluster where 2, 3, 7 is there.

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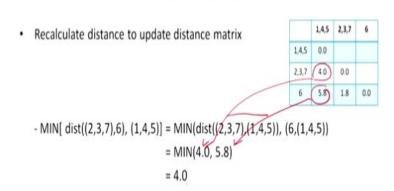
Example for HAC



See that it is gone to 2, 3, 7.

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Example for HAC



Now, recalculate the distance to update the distance matrix, so the distance between 2, 3, 7, 6 versus 1, 4, 5, so what you have to do the distance is 2, 3, 7 versus 1.45, you have to find out this distance, so 2, 3, 7, 1.45 the minimum distance is that one we brought it here. The next one 6, 1, 4.5, so 6, 1.45 that is a 5.8, so in that the minimum distance is 4.

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Example for HAC

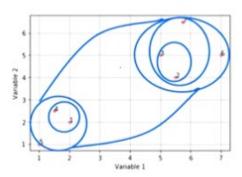
• Updated distance matrix for the cluster ((2,3,7), 6)

	1,4,5	2,3,7,6
1,4,5	0.0	
2,3,7,6	4.0	0.0

This is our updated matrix, now what happened in that the minimum value is 4, so what happened this 2, 3, 7, 6 will join with 1, 4, 5.

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Example for HAC



So that is nothing but the everything is joined together.

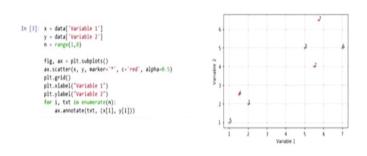
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Python demo for HAC

Now, let us see how to do this agglomerative hierarchical clustering method with the help of python, so we have imported the data; import numpy as np, import pandas as pd, import matplotlib.pyplot as plt, import scipy. from scipy.cluster.hierarchy import fcluster, from scipy.cluster.hierarchy import cophenet, from scipy.spatial.disatnce import pdist.

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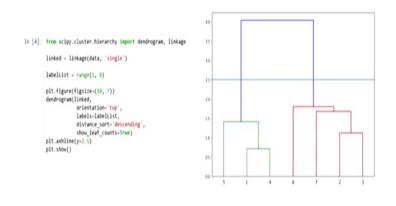
Python demo for HAC



So, I have data in hierarchical clustering, so what happened this was our data set, for this data set, we have plotted the 2 dimensional picture, so in that all the objects are displayed.

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Python demo for HAC



Now, when you run this comment that is from scipy.cluster.hierarchy import dendrogram, linkage, you will get a this kind of pictures, So, what is happening you see that this is the way 1 and 4 are joining together this stage, after that along with 1 and 4, the 5 is joined, initially 2 and 4; 2 and 3 is a joined, so along with 2 and 3, 7 is joined, after sometime along with the 7, 2, 3, 6 also joined.

At the end, see that the blue line which says all are forming one clustering, this picture shows the dendrogram, so for that from scipy dot cluster dot hierarchy import dendrogram, linkage, so linked equal to linkage data, single, we are going to have single linkage, the label is this, range 1 to 8 that is a figure size. So, when you run that you are getting the dendrogram.

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Python demo for HAC

Now, here what it shows that, here we have entered k equal to 2, you look at this value from sklearn; from sklearn dot cluster import AgglomerativeClustering, when you put k equal to 2, we are going to say Euclidean distance and single linkage, so when you; k equal to 2, so the cluster name is into 2 category; one is 0 is one group, 1 is another group, so this was the labels; 1, 0.

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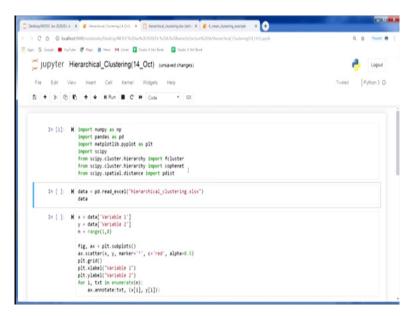
Python demo for HAC

```
In [8]: x - data['Variable 1']
y - data['Variable 2']
n - range(1,8)

fig, ax - plt.subplots()
ax.scatter(x, y, c-Hclustering.labels_, cmap-'rainbow')
plt.grid()
plt.xlabel('Variable 1')
plt.ylabel('Variable 2')
for i, tx in enumerate(n):
ax.annotate(txt, (x[i], y[i]))
```

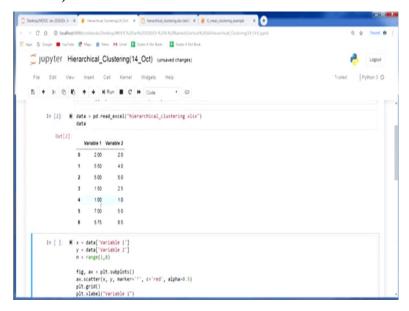
So, when you run this, you see that there are 2 clustering, so this is forms 1 cluster, this is form another cluster, suppose if you write k equal to 3 here, you may get with 3 clusters now, I am going to the python demo for doing this agglomerative hierarchical clustering.

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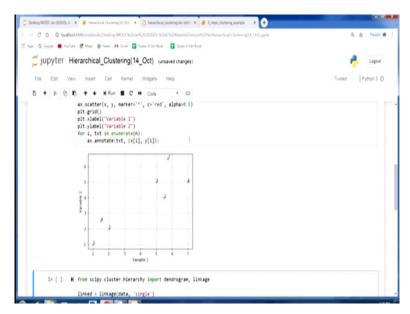
Now, I am going to show how to do agglomerative hierarchical clustering in python, so import this necessary library; I an running this, I have stored the data in the file name hierarchical clustering.

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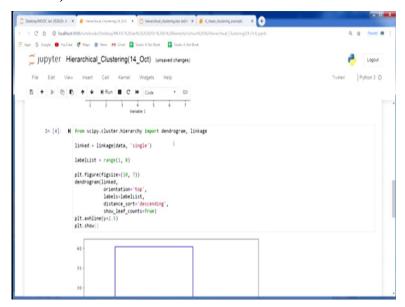
So, this is our data, for this I am going to do this hierarchical clustering.

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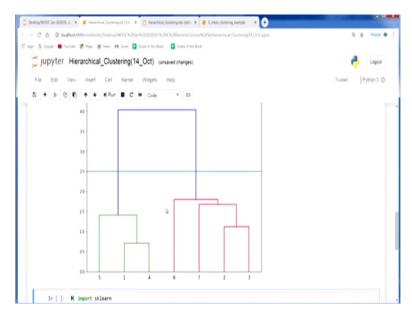
So, first I am going to show the scatterplot, in that it is showing all the objects, while looking at the object itself, you see that if you go for 2 clustering that will be good.

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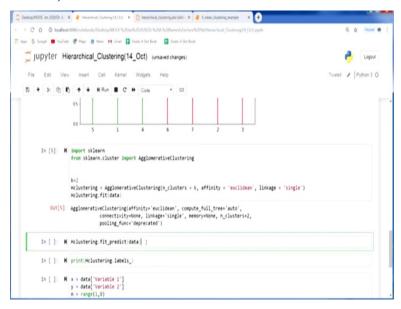
So, what we are going to do; we are going to do the single linkage, here I am going to show the figure size here also, so this picture you know we are going to get the dendrogram.

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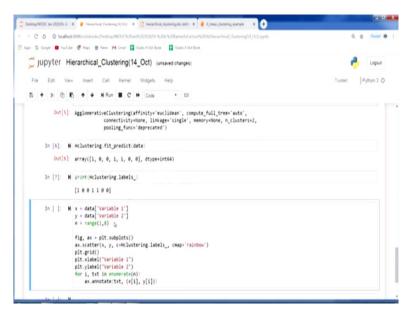
So, this is the dendrogram, so 2 and 3 is forming one cluster, out of that this 7 is joining, out of that 6 is joining. Here at level 1, it is 1 and 4 is joining, then 5 is joining there at the end, it is going to; all are going to be in the same cluster.

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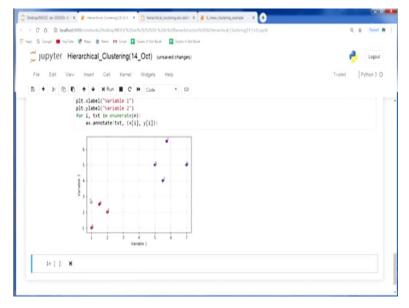
Now, from sklearn dot cluster import AgglomerativeClustering, suppose we will start with 2, so 2, so run this, let us see hierarchical clustering, how we are doing, see that there are 2 clustering, it is one is named as 1, another one is 0.

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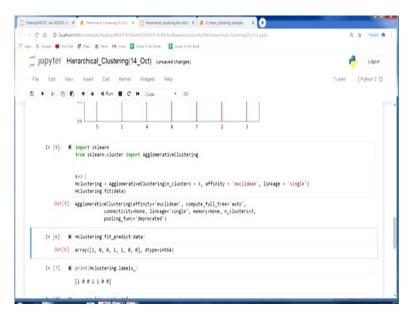
So, let us see what are the labels so, this is labels; 1, 0, 0, 1, 1, 0, 0.

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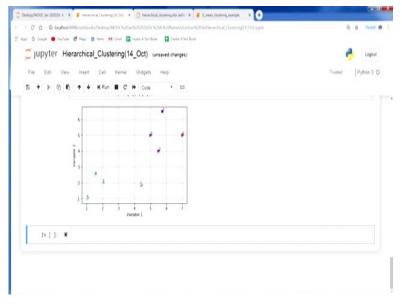
So, now if you run this, what you are getting; now there are 2 clusters, so the red colour point, say 1 cluster, the purple is another cluster. Suppose, if we go for k equal to 3, let us see what kind of answer we are getting.

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Suppose, if we go for k equal to 3, again you run it, you see that the level is 0, 1, 2, again you run it, level is see that.

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Now, if you run this, you see that there are 3 cluster; green, purple and red because red is only one cluster, there is only one element, so the optimal number of cluster for this kind of data set is k equal to 2 that is a purpose we can visualise how the cluster is formed and quality of cluster also. In this lecture, what I have done, I have started agglomerative hierarchical algorithm with the help of a numerical example.

In that example, I have first I found the distance matrix, after finding the distance matrix, I formed a cluster wherever there is a minimum value is there, I connected that 2 objects, then I have updated the distance matrix, again I have gone to where there is a minimum point is there, so that point and that objects are clubbed together. At the end, for the same data set, I have explained how to do python programming.

And I also shown how the result is appearing, so here the number of cluster I have initially started with k equal to 2, then again I changed k equal to 3 but when I changed k equal to 3, I get some other result that is not looking good, so I kept only k equal to 2 is the right number of clusters, so optimal number of clusters.