

# Natural Language Processing

## Assignment 4

### Type of Question: MCQ

Number of Questions: 7 Total Marks:  $(4 \times 1) + (3 \times 2) = 10$

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1.

Baum-Welch algorithm is an example of -

**[Marks 1]**

- A) Forward-backward algorithm
- B) Not a case of the Expectation-maximisation algorithm
- C) Both A and B
- D) None

**Answer:** A

**Solution:** Theory.

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2.

Marks 2

Once a day (e.g. at noon), the weather is observed as one of state 1: rainy state 2: cloudy state 3: sunny The state transition probabilities are :

0.4	0.3	0.3
0.2	0.6	0.2
0.1	0.1	0.8

Given that the weather on day 1 ( $t = 1$ ) is sunny (state 3), what is the probability that the weather for the next 7 days will be “sun-sun-rain-rain-sun-cloudy-sun”?

- A)  $1.54 \times 10^{-4}$
- B)  $8.9 \times 10^{-2}$
- C)  $7.1 \times 10^{-7}$
- D)  $2.5 \times 10^{-10}$

**Answer: A**

**Solution:**

$O = \{S3, S3, S3, S1, S1, S3, S2, S3\}$

$P(O \mid \text{Model})$

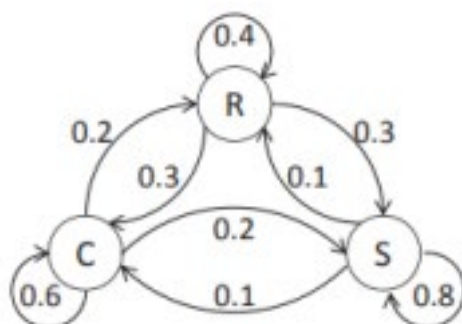
$= P(S3, S3, S3, S1, S1, S3, S2, S3 \mid \text{Model})$

$= P(S3) P(S3|S3) P(S3|S3) P(S1|S3) P(S1|S1) P(S3|S1) P(S2|S3)$

$P(S3|S2) = Q3 \cdot a33 \cdot a33 \cdot a31 \cdot a11 \cdot a13 \cdot a32 \cdot a23$

$= (1)(0.8)(0.8)(0.1)(0.4)(0.3)(0.1)(0.2)$

$= 1.536 \times 10^{-4}$



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3.

In the question 2, the expected number of consecutive days of sunny weather is:

- A) 2
- B) 3
- C) 4
- D) 5

**[Marks 1]**

**Answer: D**

**Solution:**

$\text{Exp}(i) = 1/(1-p_{ii})$  So for rainy, the expected no of days =  $1/(1-0.8) = 5$

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4.

**[Marks 2]**

You are building a model distribution for an infinite stream of word tokens. You know that the source of this stream has a vocabulary of size 1200. Out of these 1200 words you know of 200 words to be stop words each of which has a probability of 0.001. With only this knowledge what is the maximum possible entropy of the modelled distribution. (Use log base 10 for entropy calculation)

- A) 2.079
- B) 4.5084
- C) 2.984
- D) 3.0775

**Answer: D**

**Solution:** There are 200 stopwords with each having an occurrence probability of 0.001. Hence,

$$P(\text{Stopwords}) = 200 * 0.001 = 0.2$$

$$P(\text{non-stopwords}) = 1 - 0.2 = 0.8$$

For maximum entropy, the remaining probability should be uniformly distributed. For every non-stopword  $w$ ,  $P(w) = 0.8/(1200 - 200) = 0.8/1000 = 0.0008$ . Finally, the value of the entropy would be,

$$\begin{aligned} H &= E(\log(1/p)) \\ &= -200(0.001 * \log(0.001)) - 1000(0.0008 \log(0.0008)) \\ &= -200(0.001 * (-3)) - 1000(0.0008 * (-3.0969)) \\ &= 0.6 + 2.4775 \\ &= 3.0775 \end{aligned}$$

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5.

[Marks 1]

Suppose you have the input sentence "Sachin is a great cricketer".

And you know the possible tags each of the words in the sentence can take.

- Sachin: NN, NNS, NNP, NNPS
- is: VB
- a: DT
- great: ADJ
- cricketer: NN, NNS, NNP

How many possible hidden state sequences are possible for the above sentence and States?

- A)  $4 \times 3 \times 3$
- B)  $3 \times 4$
- C)  $2^4 \times 2^3 \times 2^3$
- D)  $3 \times 4^2$

**Answer: B**

**Solution:** Each possible hidden sequence can take only one POS tag for each of the words. Hence the total possibility will be a product of the number of candidates for each word.

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6.

[Marks 1]

What are the time and space complexity order of the Viterbi algorithm? K is the number of states and N number of time steps.

- A) KN,  $K^2N$
- B)  $K^2N$ , KN
- C)  $K^2N$ ,  $K^2N$
- D) KN, KN

**Answer: B**

**Solution:** The sum-product algorithm is polynomial. The time complexity is

$O(K^2N)$ , the space complexity is  $O(KN)$ , where  $K$  is the number of states and  $N$  number of time steps.

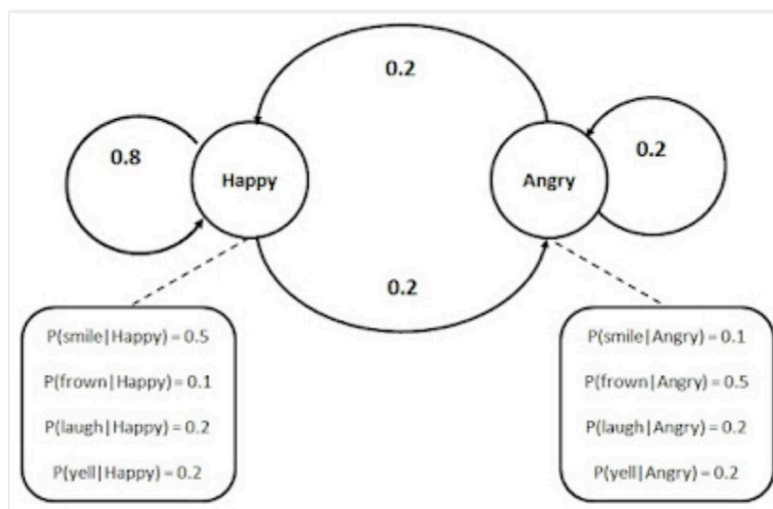
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7.

[Marks 2]

Mr. X is happy someday and angry on other days. We can only observe when he smiles, frowns, laughs, or yells but not his actual emotional state. Let us start on day 1 in a happy state. There can be only one state transition per day. It can be either a happy state or an angry state. The HMM is shown below-

Assume that  $q_t$  is the state on day  $t$  and  $o_t$  is the observation on day  $t$ . Answer the following questions;



What is  $P(o_2 = \text{frown})$ ?

- A) 0.56
- B) 0.18
- C) 0.03
- D) 0.78

**Answer: B**

**Solution:** We need to find the probability of observation **frown** on day 2. But we don't know whether he is happy or not on day 2 (we know he was happy on day 1). Hence, the probability of the observation is the sum of products of observation probabilities and all possible hidden state transitions.

$$\begin{aligned} P(o_2 = \text{frown}) &= P(o_2 = \text{frown} \mid q_2 = \text{Happy}) + P(o_2 = \text{frown} \mid q_2 = \text{Angry}) \\ &= P(\text{Happy} \mid \text{Happy}) * P(\text{frown} \mid \text{Happy}) + P(\text{Angry} \mid \text{Happy}) * P(\text{frown} \mid \text{Angry}) \\ &= (0.8 * 0.1) + (0.2 * 0.5) = 0.08 + 0.1 = 0.18 \end{aligned}$$