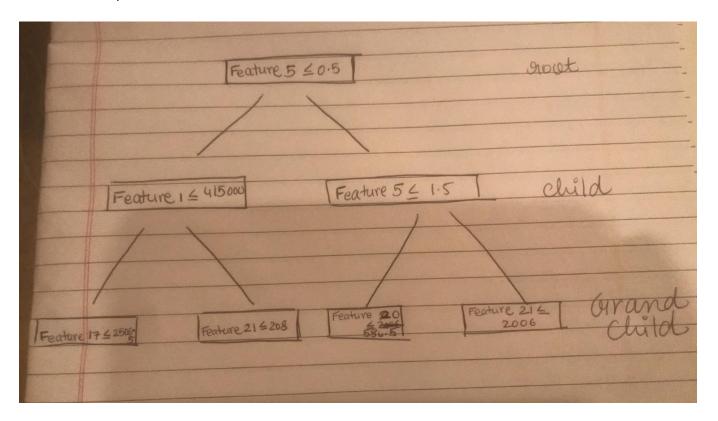
Q1. The below picture are the decision rules selected.



Root Feature 5 <= 0.5 The training points are 2000

Left Child Feature 1 <= 415000 The training points are 1319

Right Child Feature 5 <= 1.5 The training points are 681

Left Left Grandchild Feature 17 <= 2505.6 The training points are 1284 Left Right Grandchild Feature 21 <= 208 The training points are 35

Right Left Grandchild Feature 20 <= 584.5 The training points are 292

Right Right Grandchild Feature 21 <= 2006 The training points are 389

- Q2. The training error is 0.0 The test error is 0.498
- Q3. Validation error before pruning: 0.461

Pruning
Decision rule is feature 1 <= 415000
Validation error is 0.442
Test error is 0.485

Pruning
Decision rule is feature 4 <= 2.5
Validation error is 0.442
Test error is 0.485

Q4. Feature 5 which is payment delay September

import numpy as np from collections import Counter import math import random

text = np.loadtxt('./pa2train.txt')
validate = np.loadtxt('./pa2validation.txt')
other = np.loadtxt('./pa2test.txt')

def total_entropy(values):
 counts = Counter([x for x in values])
 total_length = len(values)
 probability = []
 for i in counts.values():

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probability.append(i/total length)
  return [sum([-x*math.log(x) for x in probability]), counts]
def information_gain(values, rule, rule_Value):
  split = []
  sp = []
  for i in values:
    if i[rule] > rule Value:
       split.append(i)
    else:
       sp.append(i)
  split_labels = []
  for j in split:
    split labels.append(j[len(j)-1])
  label = []
  for a in sp:
    label.append(a[len(a)-1])
  proability_split = total_entropy(split_labels)[0]
  probability label = total entropy(label)[0]
  probaility s = len(split labels)/ len(values)
  probality = len(label)/ len(values)
  conditional = (probaility_s*proability_split) + (probality*probability_label)
  value ttoal = []
  for b in values:
    value_ttoal.append(b[len(b)-1])
  return [total_entropy(value_ttoal)[0] - conditional, total_entropy(value_ttoal)[1]]
def candidate_rules(values):
  temp = []
  for y in range(22):
    temp_values = []
    for x in values:
       temp_values.append(x[y])
    sort_value = sorted(np.unique(temp_values))
    for i in range(len(sort_value)-1):
       temp.append([(sort value[i]+sort value[i+1])/2, y])
  return temp
def id3(values):
```

```
root = Tree()
root.data = values
root.left = Tree()
root.right = Tree()
value_label = []
ig = []
for x in values:
  value_label.append(x[len(x)-1])
counts = Counter([x for x in value_label])
if (len(counts) == 1):
  print(value_label[0])
  root.data = value_label[0]
  root.left = None
  root.right = None
  return root
elif(len(value_label) <= 0):
  return
else:
  cr = candidate_rules(values)
  for j in cr:
    i = information_gain(values, j[1], j[0])
    ig.append([i[0], [j[1], j[0]], i[1]])
max_value = -1
for c in ig:
  if c[0] > max_value:
    max_value = c[0]
max_ig = []
for c in ig:
  if c[0] == max_value:
    max_ig.append(c)
random_ig = random.choice(max_ig)
decison_feature = random_ig[1][0]
decison_value = random_ig[1][1]
keys = []
value counts = []
for i in random_ig[2].items():
  keys.append(i[0])
  value_counts.append(i[1])
```

```
count_feature = [keys[0], value_counts[0]]
  count_other = [keys[1], value_counts[1]]
  split left = []
  split_right = []
  for d in values:
    if d[decison_feature] <= decison_value:</pre>
         split_left.append(d)
    else:
         split_right.append(d)
  root.feature = decison feature
  root.threshold = decison_value
  root.pure = False
  root.count = count_feature
  root.other = count_other
  decison = decison_feature+1
  print("decision rule", decison, "<=", decison_value)</pre>
  root.left = id3(split_left)
  root.right = id3(split_right)
  return root
class Tree:
  def __init__(self):
    self.left = None
    self.right = None
    self.data = None
    self.threshold = None
    self.count = None
    self.pure = False
    self.other = None
    self.feature = None
def e(train, other):
  c = 0
  for i in range(len(other)):
    if other[i][-1] != train[i]:
      c = c+1
  return (c/len(other))
def make_predict(tree, values):
  a = []
```

```
for i in values:
    def make_redict(tree, values):
      if (tree.pure == True):
         if(tree.count[1] > tree.other[1]):
           a.append(tree.count[0])
           return
         else:
           a.append(tree.other[0])
           return
      else:
        if( tree.left == None and tree.right == None):
           a.append(tree.data)
           return
        if values[tree.feature] <= tree.threshold:</pre>
           make_redict(tree.left, values)
         else:
           make_redict(tree.right, values)
    make_redict(tree, i)
  return a
a = id3(text)
b = make_predict(a, text)
c = e(b, other)
d = e(b, text)
print(c)
print(d)
def tr(tree):
  queue = []
  queue.append(tree)
  counter = 0
  while queue and counter <= 6:
    want = queue.pop(0)
    print(want.feature, want.threshold, want.count, want.other)
    queue.append(want.left)
    queue.append(want.right)
    counter = counter +1
tr(a)
def prune(tree):
  queue = []
  queue.append(tree.left)
  queue.append(tree.right)
  before = e(b, validate)
```

```
print(before, "b")
  counter = 0
  while queue and counter < 2:
    wanted = queue.pop(0)
    print(wanted.feature, wanted.threshold)
    wanted.pure = True
    counter =counter +1
    after = e(make_predict(a, text), validate)
    t_after = e(make_predict(a, text), other)
    print(after, "a")
    print(t_after)
    if after <= before:
      wanted.left = None
      wanted.right = None
      before = after
    if after > before:
      wanted.pure = False
      counter = counter -1
    if wanted.left != None:
      queue.append(wanted.left)
    if wanted.right != None:
      queue.append(wanted.right)
  return tree
pruned = prune(a)
print(pruned)
```