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1  #include<bits/stdc++.h>
2
3  using namespace std;
4
5  struct Point{
6      double x,y;
7      Point(double x=0,double y=0):x(x),y(y){}
8  };
9
10 typedef Point Vector;
11
12 struct Circle{
13     Point c;
14     double r;
15     Circle(Point c,double r):c(c),r(r){}
16
17     //通过圆心角确定圆上坐标
18     Point point(double a){
19         return Point(c.x + cos(a)*r,c.y+sin(a)*r);
20     }
21 };
22
23 struct Line{
24     Point p;
25     Vector v;
26     double ang;
27     Line(){}
28     Line(Point p,Vector v):p(p),v(v){}
29     bool operator < (const Line &L) const {
30         return ang < L.ang;
31     }
32 };
33
34
35 const double eps = 1e-10;
36 const double PI = acos(-1);
37
38 Vector operator + (Vector A,Vector B){ return Vector(A.x+B.x,A.y+B.y); }
39 Vector operator - (Point A,Point B){ return Vector(A.x-B.x,A.y-B.y); }
40 Vector operator * (Vector A,double p){ return Vector(A.x*p,A.y*p); }
41 Vector operator / (Vector A,double p){ return Vector(A.x/p,A.y/p); }
42
43 bool operator < (const Point &a,const Point &b){
44     return a.x < b.x || (a.x == b.x && a.y < b.y);
45 }
46
47 int dcmp(double x){
48     if( fabs(x) < eps ) return 0;
49     else return x < 0 ? -1 : 1;
50 }
51
52 bool operator == (const Point &a,const Point &b){
53     return dcmp(a.x-b.x) == 0 && dcmp(a.y-b.y);
54 }
55

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56 double Dot(Vector A,Vector B){ return A.x*B.x + A.y*B.y; }
57 double Length(Vector A){ return sqrt(Dot(A,A)); }
58 double Angle(Vector A,Vector B){ return acos( Dot(A,B)/Length(A)/Length(B)
); }
59
60 double Cross(Vector A,Vector B){ return A.x*B.y - A.y*B.x; }
61 double Area2(Point A,Point B,Point C){ return Cross(B-A,C-A); }
62
63 Vector Rotate(Vector A,double rad){
64     return Vector( A.x*cos(rad)-A.y*sin(rad),A.x*sin(rad)+A.y*cos(rad) );
65 }
66
67 bool OnSegment(Point p,Point a1,Point a2){
68     return dcmp(Cross(a1-p,a2-p)) == 0 && dcmp(Dot(a1-p,a2-p)) < 0;
69 }
70
71 //直线与圆的交点，返回交点个数，结果存在sol中
72 //没有清空sol
73
74 int getLineCircleIntersecion(Line L,Circle C,double &t1,double
&t2,vector<Point> &sol){
75     double a = L.v.x, b = L.p.x - C.c.x,
76             c = L.v.y, d = L.p.y - C.c.y;
77     double e = a*a + c*c, f = 2*(a*b + c*d),
78             g = b*b + d*d - C.r*C.r;
79     double delta = f*f - 4*e*g;
80     if( dcmp(delta) < 0 ) return 0; //相离
81     if( dcmp(delta) == 0 ){ //相切
82         t1 = t2 = -f/(2*e);
83         sol.push_back(C.point(t1));
84         return 1;
85     }
86     t1 = (-f - sqrt(delta)) / (2*e);
87     t2 = (-f + sqrt(delta)) / (2*e);
88     sol.push_back(C.point(t1));
89     sol.push_back(C.point(t2));
90     return 2;
91 }
92
93 double angle(Vector v){ return atan2(v.y,v.x); }
94
95 //两圆相交
96
97 int getCircleCircleIntersection(Circle c1,Circle c2,vector<Point> &sol){
98     double d = Length(c1.c - c2.c);
99     if( dcmp(d) == 0 ){
100         if( dcmp(c1.r - c2.r) == 0 ) return -1; //两圆重合
101         return 0; //内含
102     }
103     if( dcmp(c1.r+c2.r-d) < 0 ) return 0; //相离
104     if( dcmp(fabs(c1.r - c2.r) - d) > 0 ) return 0;
105
106     double a = angle(c2.c - c1.c); // 向量c1 c2 的极角
107     double da = acos( (c1.r*c1.r + d*d - c2.r*c2.r) / (2*c1.r*d) );
108
109     Point p1 = c1.point(a-da),p2 = c1.point(a+da);
110
111     sol.push_back(p1);

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112     if( p1 == p2 ) return 1;
113     sol.push_back(p2);
114     return 2;
115 }
116
117 //过点做圆切线
118
119 int getTangents(Point p,Circle C,Vector* v){
120     Vector u = C.c - p;
121     double dist = Length(u);
122     if( dist < C.r ) return 0;
123     else if( dcmp(dist - C.r) == 0 ){ //p在圆上
124         v[0] = Rotate(u,PI/2);
125         return 1;
126     }
127     else{
128         double ang = asin(C.r / dist);
129         v[0] = Rotate(u, -ang);
130         v[1] = Rotate(u, +ang);
131         return 2;
132     }
133 }
134
135 //返回切线的数量 两圆的公切线
136 //a[i] 和 b[i] 表示 第 i 条切线在 圆A 和 圆B 上的 切点
137
138 int getTangents(Circle A,Circle B,Point* a,Point* b){
139     int cnt = 0;
140     if( A.r < B.r ){ swap(A,B);swap(a,b); }
141     int d2 = (A.c.x - B.c.x)*(A.c.x - B.c.x) + (A.c.y - B.c.y)*(A.c.y -
142 B.c.y);
143     int rdifff = A.r - B.r;
144     int rsum = A.r + B.r;
145     if( d2 < rdifff*rdifff ) return 0; // 内含
146
147     double base = atan2(B.c.y - A.c.y,B.c.x - A.c.x);
148     if( d2 == 0 && A.r == B.r ) return -1;
149     if( d2 == rdifff*rdifff ){ //内切
150         a[cnt] = A.point(base);b[cnt] = B.point(base); cnt++;
151         return 1;
152     }
153
154     double ang = acos( (A.r - B.r) / sqrt(d2) );
155     a[cnt] = A.point(base + ang);b[cnt] = B.point(base + ang); cnt++;
156     a[cnt] = A.point(base - ang);b[cnt] = B.point(base - ang); cnt++;
157
158     if( d2 == rsum*rsum ){
159         a[cnt] = A.point(base);b[cnt] = B.point(base + PI); cnt++;
160     }
161     else if( d2 > rsum*rsum ){
162         ang = acos( (A.r + B.r) / sqrt(d2) );
163         a[cnt] = A.point(base + ang);b[cnt] = B.point(base + ang + PI);
164         cnt++;
165         a[cnt] = A.point(base - ang);b[cnt] = B.point(base - ang + PI);
166         cnt++;
167     }
168     return cnt;
169 }

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167  
168 int main(int argc, char ** argv){  
169  
170     return 0;  
171 }
```