



# Normalisation – Part 1

## BCNF

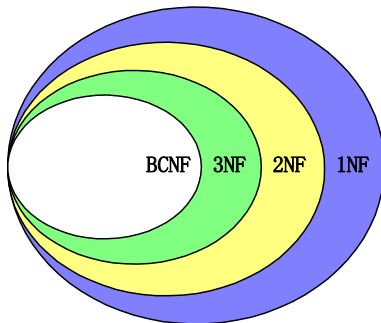


## Schema Design

- A driving force for **the study of dependencies** has been **schema design**.
- The goal of schema design is to select **the most appropriate schema** for a particular database application.
- The **choice of a schema** is guided by **semantic information** about the application data provided by users and captured by dependencies.
- A common approach starts with a **universal relation** and applies decomposition to create new relations that satisfy certain normal forms (i.e. **normalization**).

## Normal Forms

Normal forms	Test criteria
1NF	
↓	
2NF	weak
↓	
3NF	↓
↓	
BCNF	strong
...	



● **Note that:**

- 1NF is not based on any constraints.
- 2NF, 3NF and BCNF are based on keys and functional dependencies.
- 4NF and 5NF are based on other constraints (will not be covered).



## Normalisation

- Decomposing a relation into **smaller relations in a certain normal form**
  - Each normal form reduces certain kind of data redundancy.
  - Each normal form does not have certain types of (undesirable) dependencies.
- What normal forms will we learn?
  - 1 Boyce-Codd normal form (**BCNF**)
  - 2 Third normal form (**3NF**)



## BCNF - Definition

- A relation schema  $R$  is in **BCNF** if whenever a non-trivial FD  $X \rightarrow A$  holds in  $R$ , then  **$X$  is a superkey**.
- When a relation schema is in BCNF, all data redundancy based on functional dependency are removed.
  - Note: this does not necessarily mean a good design.

**Do not represent the same fact twice (within a relation)!**



## Normalisation to BCNF

- Consider the relation schema TEACH with the following FDs:
  - $\{\text{StudentID}, \text{CourseName}\} \rightarrow \{\text{Instructor}\};$
  - $\{\text{Instructor}\} \rightarrow \{\text{CourseName}\}.$

TEACH		
StudentID	CourseName	Instructor
u123456	Operating Systems	Jane
u234567	Operating Systems	Jane
u234567	Databases	Mark

- Is TEACH in BCNF?**
  - Not in BCNF because of  $\{\text{Instructor}\} \rightarrow \{\text{CourseName}\}.$



## Normalisation to BCNF

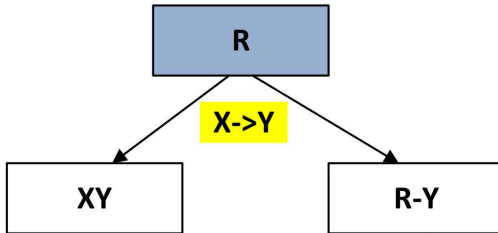
- **Algorithm** for a BCNF-decomposition

**Input:** a relation schema  $R'$  and a set  $\Sigma$  of FDs on  $R'$ .

**Output:** a set  $\mathcal{S}$  of relation schemas in BCNF, each having a set of FDs

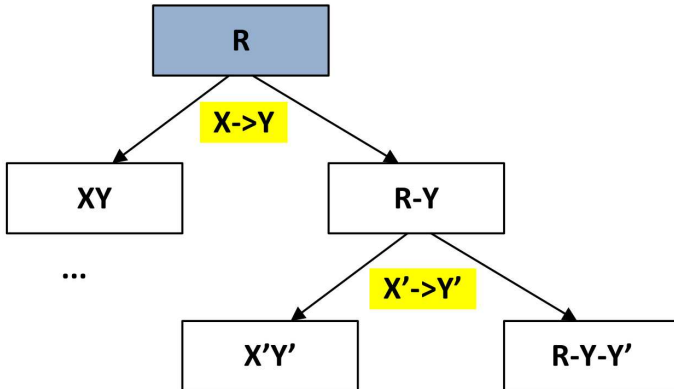
- Start with  $\mathcal{S} = \{R'\}$ ;
- Do the following for each  $R \in \mathcal{S}$  iteratively until no changes on  $\mathcal{S}$ :
  - Find a (non-trivial) FD  $X \rightarrow Y$  on  $R$  that violates BCNF, if any;
  - Replace  $R$  in  $\mathcal{S}$  by two relation schemas  $XY$  and  $(R - Y)$  and project the FDs to these two relation schemas.

## Normalisation to BCNF





## Normalisation to BCNF





## BCNF - Example

- Consider TEACH with the following FDs again:
  - $\{\text{StudentID}, \text{CourseName}\} \rightarrow \{\text{Instructor}\};$
  - $\{\text{Instructor}\} \rightarrow \{\text{CourseName}\}.$

TEACH		
StudentID	CourseName	Instructor
u123456	Operating Systems	Jane
u234567	Operating Systems	Jane
u234567	Databases	Mark

- Can we normalise TEACH into BCNF?

## BCNF - Example

- Consider TEACH with the following FDs again:
  - $\{\text{StudentID}, \text{CourseName}\} \rightarrow \{\text{Instructor}\};$
  - $\{\text{Instructor}\} \rightarrow \{\text{CourseName}\}.$

TEACH		
StudentID	CourseName	Instructor
u123456	Operating Systems	Jane
u234567	Operating Systems	Jane
u234567	Databases	Mark

- Replace TEACH with  $R_1$  and  $R_2$ :

$R_1$	
CourseName	Instructor
Operating Systems	Jane
Databases	Mark

$R_2$	
StudentID	Instructor
u123456	Jane
u234567	Jane
u234567	Mark

## BCNF - Example

- Consider the relation schema TEACH with the following FDs:
  - $\{ \text{StudentID}, \text{CourseName} \} \rightarrow \{ \text{Instructor} \};$
  - $\{ \text{Instructor} \} \rightarrow \{ \text{CourseName} \}.$

TEACH		
StudentID	CourseName	Instructor
u123456	Operating Systems	Jane
u234567	Operating Systems	Jane
u234567	Databases	Mark

$R_1$	
CourseName	Instructor
Operating Systems	Jane
Databases	Mark

$R_2$	
StudentID	Instructor
u123456	Jane
u234567	Jane
u234567	Mark

- Does this decomposition preserve all FDs on TEACH?**

## BCNF - Example

- Consider the relation schema TEACH with the following FDs:
  - $\{\text{StudentID}, \text{CourseName}\} \rightarrow \{\text{Instructor}\}; \text{Lost!}$
  - $\{\text{Instructor}\} \rightarrow \{\text{CourseName}\}.$

TEACH

StudentID	CourseName	Instructor
u123456	Operating Systems	Jane
u234567	Operating Systems	Jane
u234567	Databases	Mark

$R_1$

CourseName	Instructor
Operating Systems	Jane
Databases	Mark

$R_2$

StudentID	Instructor
u123456	Jane
u234567	Jane
u234567	Mark

- No. We only have  $\{\text{Instructor}\} \rightarrow \{\text{CourseName}\}$  on  $R_1$ .**



## Two Properties

- We need to consider the following properties when decomposing a relation:

- 1 **Lossless join** – “**capture the same data**”

To disallow the possibility of generating spurious tuples when a NATURAL JOIN operation is applied to the relations after decomposition.

- 2 **Dependency preservation** – “**capture the same meta-data**”

To ensure that each functional dependency can be inferred from functional dependencies after decomposition.



## Two Properties

- **Facts**

- (1) There exists an algorithm that can generate **a lossless decomposition into BCNF**.
- (2) However, a BCNF-decomposition that is **both lossless and dependency-preserving** does not always exist.

- Does there exist **a less restrictive normal form** such that a lossless and dependency preserving decomposition can always be found?