

Fractal Rhythms and Critical Avalanches in Multi-Scale Brain Dynamics

Theoretical Models: Self-Organized Criticality and Fractal Cognition

The brain appears to operate **at the edge of chaos**, in a state often described by **self-organized criticality (SOC)**. The *critical brain hypothesis* posits that the healthy brain tunes itself near a critical setpoint – a marginally stable state with richly *multiscale* dynamics optimized for information processing ¹. In this critical regime, activity unfolds over a continuum of scales rather than a single dominant frequency or size. Such a state is “internally generated, multiscale, [and] marginally stable,” theoretically maximizing the brain’s computational capacity ¹. This perspective provides a unifying framework to understand how diverse neural processes might coordinate: at criticality, the system can seamlessly link fast and slow processes, small and large events, without preferring one scale over another.

Parallel to criticality, **fractal and holographic models of cognition** emphasize the brain’s *scale-invariance* and *distributed processing*. Fractal models suggest that patterns in neural activity or connectivity repeat across scales, echoing the self-similar structure of mathematical fractals. Indeed, recent work shows that brain networks can organize into **fractal-like patterns**: when engaged in complex thought (e.g. listening to a narrative), interactions among brain regions mirror each other at different hierarchical scales, and disrupting the thought stream scrambles these fractal patterns ². Such findings support the idea of *fractal cognition*, wherein *coherent structures emerge across nested temporal or spatial scales*. Meanwhile, the term “holographic cognition” draws from the **holonomic brain theory**, which proposes that information (like memories) is distributed across neural networks in an interference pattern—*much like a hologram, where each part contains the whole*. In Pribram’s classic formulation, **each portion of the dendritic network encodes the entire memory stored in that network**, analogous to how any fragment of a hologram contains the full image ³. This holographic analogy complements the fractal view: both imply that **parts and wholes reflect each other**, enabling robustness and integration. Together, criticality, fractality, and holographic distribution offer a theoretical lens for **multi-scale coherence** – suggesting the brain intrinsically links micro-scale events to macro-scale dynamics.

Empirical Signatures: 1/f Noise and Neuronal Avalanches

These theories are backed by distinctive **empirical hallmarks** in brain signals. One key signature is the prevalence of **1/f noise** (scale-free fluctuations) in neural recordings. In resting-state EEG, the power spectrum follows a **power-law** form $P(f) \propto 1/f^\beta$, with β typically around 1–2 ⁴. This means there is no single dominant frequency – instead, slower oscillations have higher power, but every frequency band contributes on a continuous spectrum. Crucially, this **1/f scaling** is not unique to EEG; it appears across modalities. Electrocorticograms, BOLD fMRI signals, and MEG recordings all exhibit a similar **1/f-like power spectrum**, indicating an arrhythmic, scale-free component of brain activity present at rest ⁴. Such scale-free activity is often called the “aperiodic” or fractal background, reflecting the brain’s *long-range temporal correlations*. It contrasts with narrow-band oscillations (alpha, beta, gamma rhythms), which stand out above this 1/f background. For years, the 1/f component was treated as neural “noise,” but contemporary

research has **re-evaluated its importance**. The absence of a preferred timescale suggests the brain maintains **long-memory processes** (slow fluctuations) even amid fast oscillations. In fact, the *prevailing view* ties $1/f$ dynamics to criticality – i.e. the brain may self-organize near critical states to produce scale-free activity ⁵. Critical systems naturally generate $1/f$ spectra, so the omnipresence of $1/f$ noise in neural data is seen as evidence that the brain operates *in a scale-invariant, critical regime* ⁵. (Alternative models exist – e.g. $1/f$ signals might arise from summing many damped oscillators or from an excitation-inhibition balance – but criticality provides a compelling single explanation for both the broad $1/f$ spectrum and the co-existence of distinct oscillatory bands ⁶ ⁷.)

Another striking manifestation of critical, multi-scale dynamics is the presence of **neuronal avalanches**. Avalanches are cascades of neural activity that range widely in size and duration, following no characteristic scale. In both cortical slice experiments *and* in vivo brain recordings, scientists have observed that spontaneous activity comes in **bursts that obey power-law size distributions**. For example, in resting human MEG and EEG, if one defines events and looks at clusters of co-activation, their sizes (and durations) are distributed approximately as a power law with exponent about $-3/2$ ⁸. At the same time, these cascades propagate such that each event triggers on average one subsequent event (a branching ratio ~ 1), indicating the system teeters at the critical point between quiescence and runaway excitation ⁸. This combination – a heavy-tailed distribution of event sizes and a branching parameter of 1 – is exactly what theory predicts for a system in a **critical state**. Notably, large-scale recordings confirm that the human brain at rest self-organizes into this regime: **cortical activity forms neuronal avalanches consistent with a critical branching process** ⁹. In a seminal study, resting MEG from 124 people showed that cascades of magnetically-recorded events were scale-free; at the timescale where the cascade linking was critical (branching ~ 1), the avalanche size distribution followed a power law with exponent ~ 1.5 (matching $-3/2$) ⁸. This pattern vanished in control data (shuffled or empty-room recordings), strengthening the claim that it is a genuine neural phenomenon ¹⁰. The authors conclude that **normal healthy brains maintain an optimal dynamical state at criticality**, since critical avalanches are theorized to maximize information capacity and transmission fidelity ⁹. In essence, the resting brain is perpetually **poised in a balanced, metastable state**: small activity can cascade into large events, but on average activity neither dies out too easily nor explodes chaotically.

Beyond these temporal signatures ($1/f$ spectra and avalanches), **spatial and functional patterns** in the brain also exhibit scale-free organization. Resting-state functional connectivity networks, for instance, show fractal properties in their fluctuations. Metrics like the **Hurst exponent** reveal long-range temporal correlations in BOLD signals, which tend to be higher (more persistent, more fractal) during idle or resting conditions and decrease when cognitive effort increases ¹¹ ¹². This means when the brain isn't engaged in a demanding task, its activity wanders in a *rich, self-similar way* (like a fractional Brownian motion), whereas focused tasks impose more structured, scale-limited dynamics. At the network level, researchers have even described **fractal connectivity**: nested communities of brain regions that flexibly reconfigure across multiple scales. For example, during naturalistic listening, as mentioned, the brain's network interactions exhibited **repeating patterns from the smallest (local sensory areas) to largest (cross-modal, high-order association areas) scales** ¹³. This multi-scale integration suggests that *cognitive processing links hierarchies of neural areas in a fractal-like hierarchy*. Such findings blur the line between "resting" and "active" dynamics: even active cognition leverages fractal organization to integrate information across scales. In summary, a growing body of data from EEG, MEG, fMRI, and even single-neuron spike trains (which also show $1/f$ firing variability and long-range correlations) converges on the notion that **the brain's default activity is avalanching, scale-free, and poised near criticality**. These quantitative

features (spectral slopes, power-law exponents, Hurst coefficients, branching ratios, etc.) provide concrete numbers and constraints that can inspire how we represent brain dynamics in other contexts.

Interface Implications: Visualizing Multi-Scale Coherence in a Timeline

Translating these multi-scale brain dynamics into a **user interface timeline** means designing visual elements that convey *fractal complexity*, *nested structure*, and *critical fluctuations* at a glance. We want the interface to echo the brain's layered rhythms and avalanches, creating a sense of coherence across scales. Several design cues emerge from the science:

- **Layered 1/f Textures:** We can use *visual noise patterns* that have a **1/f spectral characteristic** as the background or baseline of the timeline. For example, a subtle textured band or halo behind the timeline could be generated with *pink noise* (1/f noise) so that it contains multi-scale detail (neither purely random nor overly regular). This would symbolically represent the brain's scale-free background activity. Because 1/f textures contain structures at all sizes (much like natural textures), they give a rich, organic feel. In a UI, this could appear as a gently shifting “fractal fabric” on which other elements float – hinting that beneath any specific event lies an ongoing continuum of activity at varying scales. The **fractal dimension** or roughness of this texture might even be tunable based on data (e.g. a steeper 1/f slope vs. flatter, to reflect arousal or age-related changes in the real signal where a *whiter* spectrum indicates reduced scale-free dynamics ¹⁴ ¹⁵).
- **Nested Oscillation Halos:** To convey **rhythmic oscillations across multiple frequencies**, the interface can depict events with concentric **rings or halos** that pulse at different rates. For instance, around a point on the timeline (representing a moment or a state), draw a slow breathing outer halo (for a delta or slow cortical oscillation) and, simultaneously, an inner faster pulsating glow (for a beta/gamma oscillation). These halos would be *nested*, meaning the fast cycle is superimposed on the slow cycle – analogous to **cross-frequency coupling** in the brain (where high-frequency amplitude is often modulated by the phase of a low-frequency wave). Visually, this might look like a ripple within a ripple, or a brightening of the halo in high-frequency bursts synced to the peak of a slow wave. Such design communicates **multi-scale rhythmic coherence**: just as neurons engage in fast gamma bursts on the crest of slower theta waves, the UI element shows a unified event comprising multiple temporal layers. The use of transparency and color could differentiate the scales (e.g. a faint large ring for slow rhythm, a sharp inner ring for fast rhythm), maintaining clarity.
- **Multi-Scale “Beats” and Cascades:** To reflect **neuronal avalanches and scale-free events**, the timeline could incorporate *events of varying size* that are not evenly periodic but follow a heavy-tailed distribution of intervals or magnitudes. Practically, instead of uniform markers, one might use a mix of **small blips and occasional large spikes** on the timeline, spaced irregularly – mimicking the idea that many small events occur for each very large event (as avalanches show many tiny cascades and few huge ones). The visual spacing could be generated by an algorithm that produces power-law distributed burst sizes or inter-event gaps. This way, the timeline itself has a **fractal tempo**: zooming out, one sees patterns repeating (e.g. clusters within clusters). One could also animate *cascading highlights* to indicate a critical chain reaction: for example, when a large event marker appears, it could trigger a spread of activation along the timeline (like dominos falling) to illustrate propagation. This is inspired by how activity at criticality propagates with balanced growth and decay ¹⁶ ¹⁷ . By

tuning the “branching ratio” of these cascade animations (the spread either dies out quickly, stays constant, or blows up), the UI can even metaphorically indicate a system’s distance from criticality – a balanced cascade animation feels *alive but controlled*, whereas runaway flashes or total quenching would feel too chaotic or too idle.

- **Hierarchical Time Scales in Layout:** We might explicitly represent multiple time scales in the interface. For instance, a timeline could have **layers or tracks** corresponding to different frequency bands or scale “levels.” The lowest track might show slow trends or contexts (like a sliding window average or slow oscillation phase), while an upper track shows rapid fluctuations or events in detail. By aligning them vertically, users see how **fine-grained events nest within coarse trends**. This resembles the brain’s nested organization (e.g., the orders 1–4 of fractal network patterns in the Dartmouth study, from raw sensory detail up to integrative abstraction ¹³). Graphically, the lower layer could be a smooth curve (slow wave) and the upper layer a spiky line (fast activity), with the spikes clearly clustering at certain phases of the slow wave – thereby illustrating *phase-amplitude coupling*. Additionally, using self-similar design elements across these layers (e.g., shapes or colors that repeat across scales) can reinforce the fractal concept that each timescale is a recapitulation of the others.

By incorporating these elements, the UI timeline becomes a **living depiction of multi-scale coherence**. A viewer can intuitively sense that there are patterns within patterns: a zoomed-out structure and a zoomed-in structure might look alike (fractal self-similarity), and what happens at one moment in time is part of a larger cascade that transcends that moment. Crucially, the design should maintain *legibility*: fractal complexity doesn’t mean visual clutter. Using hierarchy and grouping (like the nested halos or multi-tier timeline) actually clarifies relationships across scales. The result could be a timeline interface that *feels organic and dynamic*, much like neural activity itself – a tapestry of **1/f-like background texture**, punctuated by **avalanche-like events**, and illuminated by **nested rhythmic glows** to denote the coupling of fast and slow. Such an interface, informed by both theory and empirical data, would not only be scientifically inspired but also engaging, giving users an intuitive grasp of the concept of **fractal, multi-scale coherence** underlying brain (and perhaps other complex system) dynamics.

Sources

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