

Literature on Cymatics and Acoustic Geometry (Sound-Induced Patterns)

Foundational Studies (Historic and Seminal Papers)

1. **Waller, M. D. (1938)** – “*Vibrations of free circular plates. Part 3: A study of Chladni's original figures.*” **Proc. Phys. Soc.** 50(1): 83–86. – Chladni (1787) famously demonstrated that fine particles on vibrating plates arrange into geometric nodal patterns, which become more intricate at higher frequencies ¹. Waller later analyzed Chladni's figures, observing their symmetries and formulating a “law of symmetry” for vibrating 2D systems ². **Why it matters:** This work laid the groundwork for visualizing sound: it proved that sound frequency, boundary conditions, and medium properties determine static “cymatic” patterns ³. **Limitations:** Early experiments were qualitative – they lacked modern measurement, and Chladni's patterns were interpreted empirically (mathematical mode theory came later).
2. **Faraday, M. (1831)** – “*On a peculiar class of acoustical figures; and on certain forms assumed by groups of particles upon vibrating elastic surfaces.*” **Phil. Trans. R. Soc. Lond.** 121: 299–340 ⁴. – Faraday extended sound-pattern experiments to fluids, discovering what are now called *Faraday waves*: standing wave ripples on liquid surfaces driven by vertical vibrations ⁵. He observed that vibration can organize particles (or fluid interfaces) into dynamic patterns at sub-harmonic frequencies (parametric resonance) and documented various “acoustical figures.” **Why it matters:** Faraday's observations revealed that not only solids but also liquids respond to acoustic forcing with ordered patterns, introducing the concept of parametric instability in fluids ⁵. This phenomenon underpins modern research in fluid acoustics and pattern formation. **Limitations:** Faraday's work was largely observational; it predated the formal development of hydrodynamic stability theory, so it did not quantify thresholds or pattern selection criteria.
3. **Jenny, H. (1967)** – *Cymatics: A Study of Wave Phenomena & Vibration*. Basel: Basilius Presse (Vol.1) – Hans Jenny coined the term “cymatics” for the study of visible sound vibrations. In his experiments, he vibrated plates and membranes coated with sand, powders, and liquids over a wide frequency range ⁶. He observed an “evolution of harmonic images,” where different frequencies produced characteristic geometric patterns in various media ⁶. Jenny's meticulous photographs showed intricate, mandala-like structures, reinforcing that specific frequencies yield repeatable patterns. **Why it matters:** Jenny's work popularized cymatics and demonstrated its cross-disciplinary resonance – he systematically visualized how sound can create order in matter, inspiring art, music, and science collaborations. **Limitations:** As a visual catalog, it lacked quantitative analysis. The experiments were phenomenological, and interpretations (e.g. invoking “invisible force fields”) went beyond mainstream physics, making some claims controversial without rigorous scientific backing.
4. **Benjamin, T. B., & Ursell, F. (1954)** – “*The stability of the plane free surface of a liquid in vertical periodic motion.*” **Proc. R. Soc. A** 225(1163): 505–515 ⁷. – This classic paper provided the first rigorous mathematical analysis of Faraday's 1831 experiment. Using linear stability theory, the authors derived

conditions under which a flat fluid surface becomes unstable to standing wave patterns when vibrated vertically. They predicted the tongues of instability in the frequency-amplitude parameter space (later called *Faraday instability tongues*⁸) and the relationship between driving frequency and the emergent pattern's wavelength. **Why it matters:** It established the theoretical foundation for parametric wave pattern formation, explaining how and when periodic forcing produces standing wave patterns^{5 9}. This helped transform Faraday's qualitative observations into quantitative physics. **Limitations:** The analysis assumed an idealized infinite depth and small amplitude oscillations (linear regime). Real fluids have viscosity and finite depth effects that required later refinements (some addressed by subsequent researchers like Kumar & Tuckerman 1994).

5. **Douady, S., & Fauve, S. (1988)** – “Pattern selection in Faraday instability.” *Europhys. Lett.* 6(3): 221–226¹⁰. – Douady & Fauve experimentally and theoretically investigated *Faraday wave pattern selection* in vibrated fluids. They showed that depending on driving conditions, the fluid surface could exhibit stripes, squares, hexagons, or more complex patterns, and they described how slight changes in frequency or amplitude select one pattern over another. Notably, they observed symmetry-breaking and coexistence of patterns, linking the results to bifurcation theory^{10 11}. **Why it matters:** This work revealed that multiple stable patterns can arise in the same system, and it introduced nonlinear pattern competition in parametrically driven systems. It marked a shift from asking “*Will a pattern form?*” to “*Which pattern will form?*”, foreshadowing chaotic and quasi-pattern states at higher drive¹¹. **Limitations:** Being a short letter, it provided snapshots of patterns without a full theoretical model for the nonlinear regime. Some phenomena (e.g. chaotic surfaces at high accelerations) were only qualitatively noted and needed deeper analysis in later studies.
6. **Melo, F., Umbanhowar, P., & Swinney, H. L. (1994)** – “Transition to parametric wave patterns in a vertically oscillated granular layer.” *Phys. Rev. Lett.* 72(1): 172–175. – This seminal study showed that *granular materials* (e.g. sand) can exhibit Faraday-like pattern formation. A thin layer of sand on a vibrated plate was found to behave like a “*granular fluid*,” developing standing wave patterns (stripes, hexagons, etc.) above a critical driving acceleration, analogous to fluid Faraday waves. The authors mapped out the phase diagram for pattern transitions and even observed localized solitary structures (“*oscillons*”) at certain parameters. **Why it matters:** It extended cymatics into *granular media*, proving that particle systems with dissipative collisions can support coherent acoustic geometry. This blurred the line between fluid and solid dynamics in vibration studies and provided a new testbed for pattern formation theories under non-equilibrium conditions. **Limitations:** Granular patterns are influenced by energy dissipation and particle size dispersity, which made them less predictable than liquid patterns. The experiment required near-monodisperse, dry grains and was primarily qualitative in identifying patterns; comprehensive theory (beyond analogy to fluids) was still lacking at this stage.
7. **Sarvazyan, A. P., Rudenko, O. V., & Fatemi, M. (2021)** – “Acoustic Radiation Force: A Review of Four Mechanisms for Biomedical Applications.” *IEEE Trans. Ultrason. Ferroelectr. Freq. Control* 68(12): 1–17 (open-access)^{12 13}. – This extensive review traces the physics of *acoustic radiation force (ARF)* – the steady force exerted by sound waves on objects – from historical observations to modern theory. It outlines four mechanisms by which acoustic waves move matter (e.g. absorption, reflection, standing-wave gradients) and notes that the first observations of ARF were by Faraday (1831) and Kundt (1874) with standing wave nodes trapping particles¹³. The paper provides the classical formulae (e.g. King and Gor'kov formulations) and surveys applications like acoustic levitation, particle manipulation, and medical ultrasound elastography. **Why it matters:** Acoustic radiation

force is the fundamental mechanism behind *cymatic pattern formation in fluids and granular media* – particles accumulate at pressure node lines due to ARF. This review connects the 19th-century cymatics experiments to modern technology, giving a rigorous basis for why particles move to form patterns ¹². **Limitations:** The focus is on biomedical and ultrasonic contexts; it does not directly discuss artistic cymatics or macro-scale demonstrations. Some derivations are presented concisely, so readers seeking detailed mathematical treatment of ARF may need to consult the cited primary sources.

Recent Advances (2015–2025)

1. **Tuan, P.-H., Wen, C.-P., Chiang, P.-Y., et al. (2015)** – “Exploring the resonant vibration of thin plates: Reconstruction of Chladni patterns and determination of resonant wave numbers.” *J. Acoust. Soc. Am.* 137(4): 2102–2123 ³. – This study combined experiment and simulation to precisely reconstruct classic Chladni figures on metal plates and extract their resonant frequencies and mode shapes. Using modern signal processing and laser vibrometry, the authors measured vibration eigenmodes and confirmed that nodal pattern geometry is dictated by plate shape and boundary conditions (as predicted historically) ³. They also quantified how closely the observed sand patterns match theoretical nodal lines by computing resonant wavenumbers. **Why it matters:** It brings Chladni’s 18th-century experiments into the quantitative era – validating that one can *predict* the cymatic patterns on an instrument or plate from first principles. This is crucial for “sci-magic” practitioners who want reproducible outcomes: it links the audible frequency to the visual pattern reliably. **Limitations:** The work focuses on relatively simple plate geometries (circular and rectangular) and small amplitudes. Real-world factors like non-uniform plates or large driving amplitudes (where nonlinearity might distort patterns) were outside its scope.
2. **Escaler, X., & De La Torre, O. (2018)** – “Axisymmetric vibrations of a circular Chladni plate in air and fully submerged in water.” *J. Fluids Struct.* 82: 432–445. – This paper explored how a surrounding fluid medium (air vs. water) affects Chladni patterns and frequencies. Using sand on a circular plate, the authors observed that in water the usual sand-at-node pattern inverted: particles were drawn towards regions of *zero transverse velocity* (antinodes) due to acoustic streaming flows ¹⁴. They also developed a coupled fluid-structure numerical model and found that submerging the plate in water dramatically lowers its resonant frequencies (~64% reduction) because of the added mass of the fluid ¹⁵. Nodal circle positions shifted between dry vs. submerged conditions. **Why it matters:** For anyone trying to create cymatic effects in different media, this demonstrates that the same solid will “sing” a different pattern when interacting with water. It highlights fluid-structure interactions: sound-based patterns can invert or alter when you go from air to water ¹⁴. **Limitations:** The study was limited to axisymmetric (circular) modes and a specific plate and grain size. More complex, non-circular modes or different fluids (viscous or shallow fluids) were not explored, so further generalization is needed for other setups.
3. **Sheldrake, M., & Sheldrake, R. (2017)** – “Determinants of Faraday wave-patterns in water samples oscillated vertically at a range of frequencies from 50–200 Hz.” *Water* 9: 1–27 ¹⁶. – This systematic investigation examined how various factors influence Faraday wave patterns on a water surface. Using a transparent cylindrical vessel and a range of pure tones, the authors tested the effects of container size, water depth, drive amplitude, temperature, and even air pressure on the resulting standing wave patterns. They found that the excitation frequency (and the vessel diameter) predominantly set the pattern’s symmetry (number of nodes) ¹⁶, whereas amplitude affected how

well-defined the pattern was (but not its shape) and water depth/temperature had no effect on pattern geometry (only on the time to reach a steady pattern)¹⁶. They also introduced a method to quantify pattern emergence time. **Why it matters:** For “sound-magic” practitioners, this study addresses reproducibility: it identifies which environmental variables *do* or *do not* significantly alter the visual outcome of a sonic experiment. Knowing that frequency and boundary size govern the pattern, while other factors (within reasonable ranges) don’t distort it, helps one reliably recreate specific cymatic images. **Limitations:** The work was published in an unconventional journal and framed within a broad theoretical context (morphic resonance), but the experimental data stand on their own. It only covered 50–200 Hz and circular containers – different frequency ranges or non-circular boundaries might yield additional complexities not captured here.

4. **Val Baker, A., Csanad, M., Fellas, N., et al. (2024)** – “Exploration of resonant modes for circular and polygonal Chladni plates.” **Entropy** 26(3): 264. – This recent open-access paper extended Chladni pattern studies to different plate geometries (beyond the classic circular plate). The researchers mapped out resonant vibration modes and their nodal patterns on plates of various shapes (including polygons), using high-speed imaging and sand pattern visualization. They proposed a unified terminology and classification for these patterns across shapes, and provided comparative images (e.g. contrasting modes on a circle vs. a square plate at analogous frequencies)¹⁷. The results showed that polygonal plates support resonant modes with predictable nodal line symmetries related to their geometry, and the authors successfully predicted those patterns using wave equations, confirming earlier theoretical expectations³. **Why it matters:** It broadens cymatics from simple shapes to more complex ones – relevant for designing custom “sigils” or acoustic sigils on different surfaces. For sci-magic enthusiasts, this means one can *engineer* plate geometry to yield a desired pattern at resonance. **Limitations:** The study focuses on linear resonant behavior; at very high drive levels, patterns can deform or mode-mix, which was not examined. Also, damping and material anisotropy in real plates may cause deviations – these idealized results assume perfectly uniform plates and support conditions.
5. **Shao, X., Bevilacqua, G., Ciarletta, P., et al. (2020)** – “Experimental observation of Faraday waves in soft gels.” **Phys. Rev. E** 102(6): 060602. – This work demonstrated that even *soft solid* surfaces (like gelatin or agar gels) can exhibit Faraday wave patterns akin to those on liquids. By vertically oscillating a soft gel layer, the team observed standing wave ripples on the gel’s surface – essentially a Faraday instability in an elastic medium. They recorded the first 15 resonant mode shapes of these gel surface waves and noted that the gel’s elasticity introduces additional restoring forces (beyond surface tension and gravity)¹⁸. Interestingly, the dispersion relation and pattern wavelength in gels differ from liquids, offering a way to measure the gel’s properties (e.g. its elastic modulus) via the wave pattern geometry¹⁸. **Why it matters:** This blurs the line between fluid and solid in acoustic patterning – showing that “solidified” liquids or biological tissues can support cymatic patterns. For practical magic/tech, it suggests one could imprint patterns in soft matter (think of manipulating biological materials or polymers with sound). **Limitations:** Soft gels have internal damping; patterns were harder to sustain and observe beyond a limited frequency range. The experiment required careful control of gel thickness and uniformity. Moreover, real biological tissues are more complex than simple gels, so direct translation to bio-systems (aside from controlled lab gels) needs caution.
6. **Hou, Z., Li, J., Zhou, Z., & Pei, Y. (2022)** – “Programmable particles patterning by multifrequency excitation radiation force of acoustic resonance modes.” **Int. J. Mech. Sci.** 222: 107232¹⁹²⁰. – This theoretical/numerical study tackled a key challenge: **actively shaping acoustic patterns** at will.

Traditional acoustic manipulation traps particles along fixed nodal lines of a single-frequency standing wave, which limits patterns to simple shapes (usually periodic nodes)¹⁹. Hou *et al.* proposed using multiple frequencies simultaneously to create an arbitrary acoustic potential landscape. By exciting several resonance modes of a cavity at once, they can superpose patterns and form almost any desired arrangement of pressure minima for particles to gather²⁰. They developed an algorithm to “program” these acoustic fields and demonstrated examples of dynamically reconfigurable particle patterns (both in simulations). **Why it matters:** This is a step towards *acoustic holography* or “sonic spell design” – instead of being limited to nature’s default patterns, one could design a composite sound that yields a custom shape. For sci-magic extractors, it means greater control: using a mix of tones to sculpt matter into complex, perhaps even moving, configurations. **Limitations:** The work is computational – it assumes an ideal chamber with known resonance modes. In practice, generating multiple precise frequencies with the required phase control is technically demanding, and acoustic interference or streaming could disturb the ideal patterns. There were no physical experiments here; real-world validation in fluids or granular media is an ongoing challenge.

7. **Guex, A. G., Di Marzio, N., Eglin, D., et al. (2021)** – “The waves that make the pattern: a review on acoustic manipulation in biomedical research.” *Mater. Today Bio* 10: 100110²¹. – This recent review provides a broad overview of how sound waves are used to organize matter, especially in bioengineering. It classifies acoustic manipulation techniques into *surface acoustic waves*, *bulk acoustic waves*, and *Faraday waves*, discussing how each can arrange particles or cells into patterns²². Key achievements highlighted include using sound to assemble polymers and cells in prescribed geometries, e.g. creating filamentous or lattice patterns, and even 3D tissue structures by standing-wave field positioning²³. Long-term acoustic stimulation effects (like influencing stem cell differentiation) are also noted. **Why it matters:** This connects cymatics to cutting-edge biofabrication – essentially the “science” parallel to the “magic.” It shows that the same acoustic forces that form sand and water patterns can be harnessed to pattern living cells and materials, which is highly relevant if one imagines sci-magic applications like healing or materializing structures via sound. **Limitations:** The review is focused on microscopic and biomedical contexts; it doesn’t cover larger-scale artistic cymatics demonstrations. Some techniques (e.g. microfluidic SAW devices) operate at ultrasonic frequencies far above hearing, so the direct visual patterns are microscopic. Nonetheless, the physical principles overlap with macro-scale cymatics.
8. **Hong, S.-H., Gorlach, A., Punzmann, H., et al. (2020)** – “Surface waves control bacterial attachment and formation of biofilms in thin layers.” *Sci. Adv.* 6(22): eaba2898²⁴. – This study applied Faraday-wave principles to *microbiology*. By vibrating a shallow water layer with bacteria, the team showed that certain resonant wave patterns could either promote or inhibit bacteria settling and biofilm formation. Specifically, dynamically controlled surface wave patterns were used to prevent bacteria from clustering in one place, effectively “stirring” them in a way that impeded their ability to attach and grow into a biofilm. Conversely, other wave conditions organized the bacteria into regular distributions. **Why it matters:** It’s a striking example of using cymatics for *functional outcomes*: here, manipulating a “living” system (biofilms) with sound. For sci-magic enthusiasts, it illustrates literal “spells” that cleanse or arrange living matter with sound. On the scientific side, it suggests non-invasive acoustic methods to control biological patterning. **Limitations:** The experiments were done in controlled lab conditions with specific bacterial strains and thin fluid layers. Complex real-world fluids (blood, soil, etc.) and mixed communities would respond differently. Also, while the study

shows correlation between wave patterns and biofilm reduction, the long-term evolutionary response of organisms to such acoustic forcing remains unknown.

Each of these references builds a piece of the cymatics puzzle – from the basic physics of how sound generates patterns, through historical demonstrations, to modern controlled experiments and applications. Together they form a comprehensive foundation and up-to-date review of how “*sonic spells*” can produce structured, often beautiful, physical effects on matter, and what constraints and possibilities govern those effects.

1 2 3 4 5 7 8 9 10 11 17 18 24 Resonant Phenomena of Faraday Waves: A Classification

According to New and Existing Terms – Water

<https://waterjournal.org/volume-14/baker/>

6 Cymatics - Wikipedia

<https://en.wikipedia.org/wiki/Cymatics>

12 13 (PDF) Acoustic Radiation Force: A Review of Four Mechanisms for Biomedical Applications

https://www.researchgate.net/publication/354587898_Acoustic_Radiation_Force_A_Review_of_Four_Mechanisms_for_Biomedical_Applications

14 15 Axisymmetric vibrations of a circular Chladni plate in air and fully submerged in water

<https://upcommons.upc.edu/entities/publication/07e1d7fc-83df-47f8-af11-e053f3f0cded>

16 Determinants of Faraday Wave-Patterns in Water Samples Oscillated Vertically at a Range of Frequencies from 50-200 Hz – Summary – Water

<https://waterjournal.org/archives/sheldrake-summary/>

19 20 Programmable particles patterning by multifrequency excitation radiation force of acoustic resonance modes - Beijing Institute of Technology

<http://pure.bit.edu.cn/en/publications/programmable-particles-patterning-by-multifrequency-excitation-ra/>

21 22 23 The waves that make the pattern: a review on acoustic manipulation in biomedical research - ScienceDirect

<https://www.sciencedirect.com/science/article/pii/S2590006421000181>