

Tema 4
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A d)

$$d) \begin{cases} 2x_1 + 4x_3 + x_4 = 7 \\ 2x_2 + 4x_3 + x_4 = 7 \\ 2x_1 + 4x_2 + 3x_3 = 9 \\ x_1 + 2x_2 + 2x_4 = 5 \end{cases}$$

$$A = \begin{bmatrix} 2 & 0 & 4 & 1 \\ 0 & 2 & 4 & 1 \\ 2 & 4 & 3 & 0 \\ 1 & 2 & 0 & 2 \end{bmatrix} \quad B = \begin{bmatrix} 7 \\ 7 \\ 9 \\ 5 \end{bmatrix}$$

$$\begin{bmatrix} 2 & 0 & 4 & 1 & 7 \\ 0 & 2 & 4 & 1 & 7 \\ 2 & 4 & 3 & 0 & 9 \\ 1 & 2 & 0 & 2 & 5 \end{bmatrix} \xrightarrow{I:2} \begin{bmatrix} 1 & 0 & 2 & 1/2 & 7/2 \\ 0 & 2 & 4 & 1 & 7 \\ 2 & 4 & 3 & 0 & 9 \\ 1 & 2 & 0 & 2 & 5 \end{bmatrix} \xrightarrow{I:2} \begin{bmatrix} 1 & 0 & 2 & 1/2 & 7/2 \\ 0 & 2 & 4 & 1 & 7 \\ 0 & 4 & -1 & -1 & 2 \\ 1 & 2 & -2 & 3/2 & 3/2 \end{bmatrix} \xrightarrow{I:2} \begin{bmatrix} 1 & 0 & 2 & 1/2 & 7/2 \\ 0 & 1 & 2 & 1/2 & 7/2 \\ 0 & 4 & -1 & -1 & 2 \\ 0 & 2 & -2 & 3/2 & 3/2 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 2 & 1/2 & 7/2 \\ 0 & 1 & 2 & 1/2 & 7/2 \\ 0 & 4 & -1 & -1 & 2 \\ 0 & 2 & -2 & 3/2 & 3/2 \end{bmatrix} \xrightarrow{I:2} \begin{bmatrix} 1 & 0 & 2 & 1/2 & 7/2 \\ 0 & 1 & 2 & 1/2 & 7/2 \\ 0 & 0 & -9 & -3 & -12 \\ 0 & 0 & -6 & 0.5 & -5.5 \end{bmatrix} \xrightarrow{I:2} \begin{bmatrix} 1 & 0 & 2 & 1/2 & 7/2 \\ 0 & 1 & 2 & 1/2 & 7/2 \\ 0 & 0 & 1 & 1/3 & 4/3 \\ 0 & 0 & -6 & 0.5 & -5.5 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & -1/6 & 5/6 \\ 0 & 1 & 0 & -1/6 & 5/6 \\ 0 & 0 & 1 & 1/3 & 4/3 \\ 0 & 0 & 0 & 2.5 & 2.5 \end{bmatrix} \xrightarrow{I:2.5} \begin{bmatrix} 1 & 0 & 0 & -1/6 & 5/6 \\ 0 & 1 & 0 & -1/6 & 5/6 \\ 0 & 0 & 1 & 1/3 & 4/3 \\ 0 & 0 & 0 & 1 & 1 \end{bmatrix} \xrightarrow{I:2.5} \begin{matrix} X_1 = 5/6 + 1/6 \cdot 1 = 1 \rightarrow x_1 = 1 \\ X_2 = 5/6 + 1/6 \cdot 1 = 1 \rightarrow x_2 = 1 \\ X_3 = 4/3 - 1/3 \cdot 1 = 1 \rightarrow x_3 = 1 \\ X_1 = 1 \rightarrow x_4 = 1 \end{matrix} \Rightarrow X = \begin{pmatrix} 1 \\ 1 \\ 1 \\ 1 \end{pmatrix}$$

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C

```
function x = gaussTotal(a,b)
n = length(b);
[lin,col] = size(a);
if lin ~= col
    error('Matricea nu e patratica');
else
    if det(a) == 0
        error('Matricea este singulara, det(A) = 0');
    end
end
a = [a b]; % matricea extinsa
x = zeros(n,1);
tic % pornim cronometrul
for i = 1:n
    if ((a(i,i)~=0) || (max(abs(a(i:n,i:n)))) ~= 0 )
```

```

        [m, k] = max(abs(a(i:n,i:n))); % retin cea mai mare valoare de pe
coloana i
        [max_val, col_index] = max(m);
        k = k(col_index) + i - 1;
        % fixam linia k ca sa fie intotdeauna pt linii de sub pivot
        % schimbam linia i cu linia k pt toate coloanele
        a([i k],1:n+1)=a([k i],1:n+1);
        % o data fixat pivotul, putem imparti linia la pivot
        a(i,i:n+1) = a(i,i:n+1)/a(i,i);
        % aplicam regula de pivotare
        for j = i+1:n
            a(j,i+1:n+1) = a(j,i+1:n+1) - a(j,i)*a(i,i+1:n+1)/a(i,i);
        end
    else
        error('impartire la 0. Sistemul nu este compatibil determinat');
    end
end
toc % oprim cronometrul (afiseaza secunde)
for k = n:-1:1
    x(k) = a(k,n+1) - a(k,k+1:n)*x(k+1:n); % calcularea vectorului cu solutiile
end
fprintf('\nSolutiile sub forma de fractii:\n')
disp(rats(x')) % ne afiseaza valorile lui x sub forma de fractii (rats)
end

```

APEL DE FUNCTIE

```
c=[2, -5, 4; -3, 1, 1; 2, -1, 0], d=[7;-1;1], y=gaussTotal(c,d);
```

>> Tema4

c =

```

2  -5  4
-3  1  1
2  -1  0

```

d =

```

7
-1
1

```

Elapsed time is 0.001084 seconds.

Solutiile sub forma de fractii:

-1/2 -2 -1/2
>>