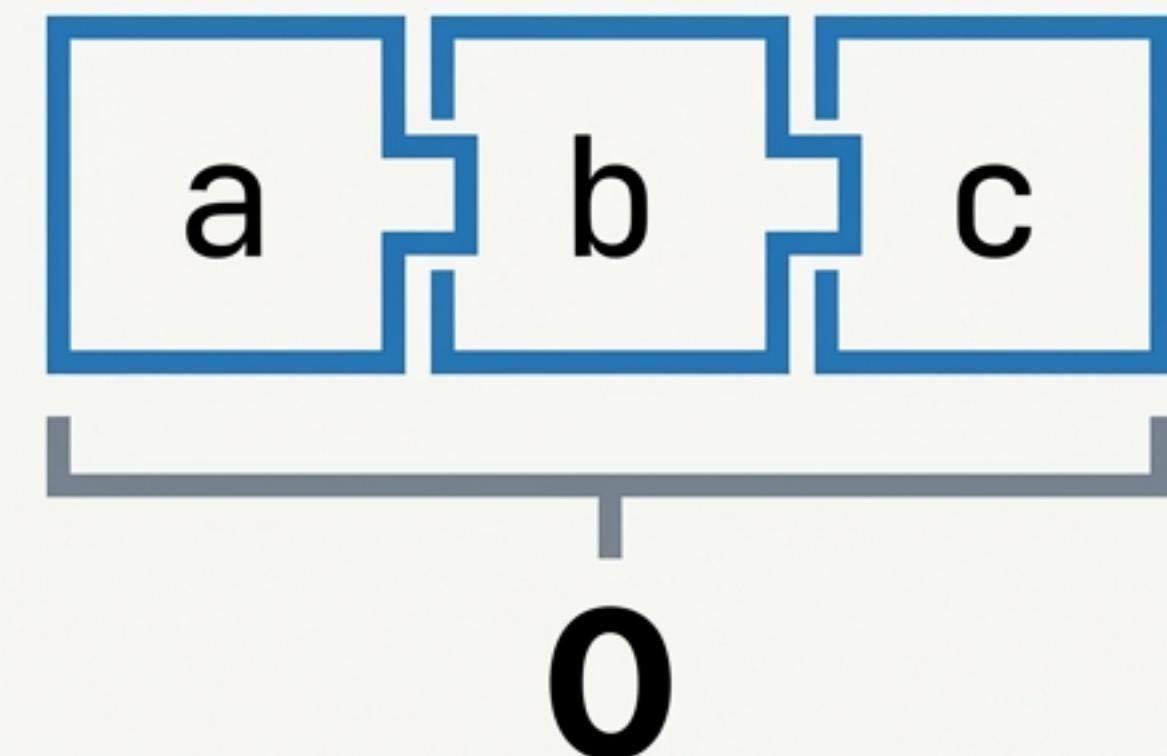


# Mastering 3 Sum

## The Two-Pointer Approach

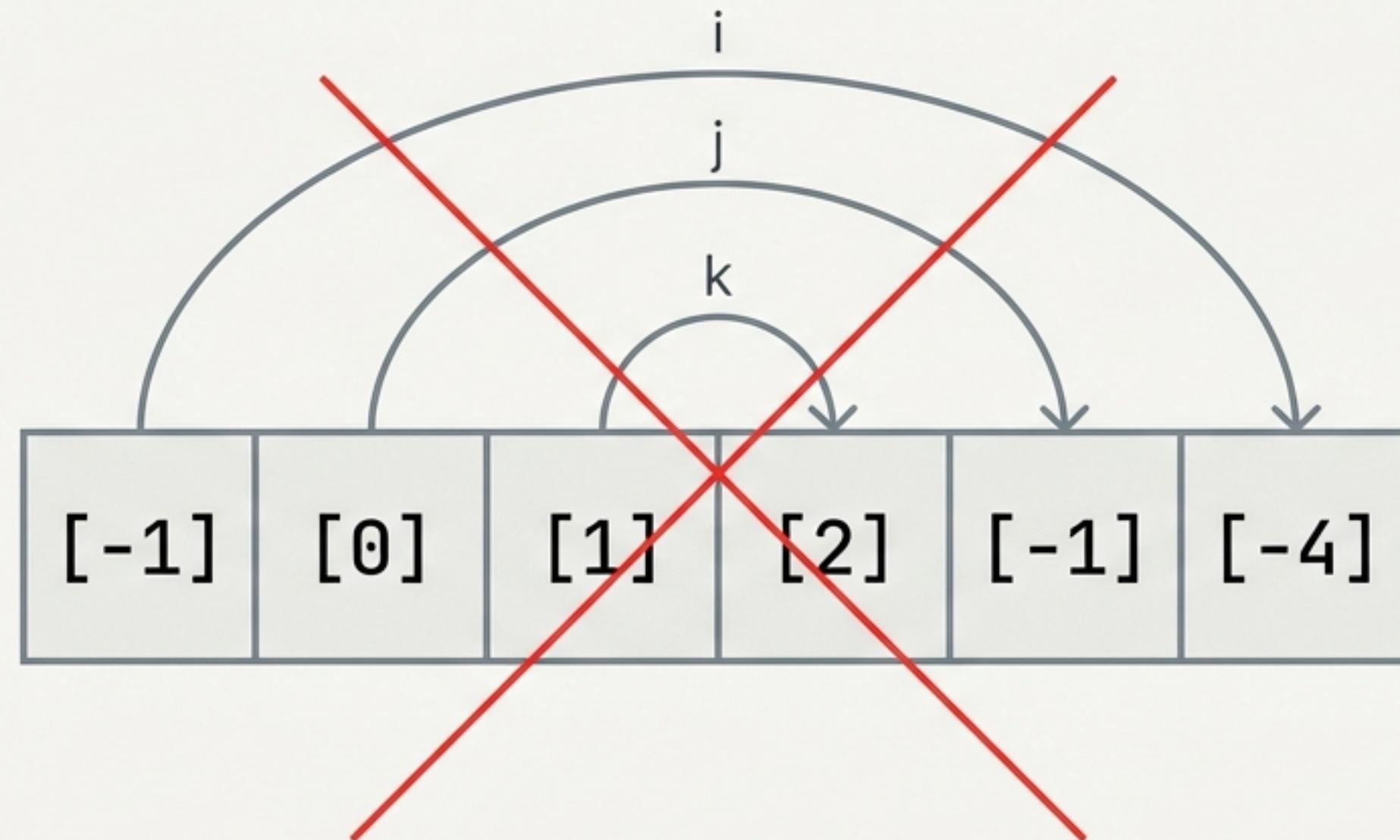


Finding unique triplets efficiently  
without the  **$O(N^3)$**  brute force trap.

# The Brute Force Bottleneck

## THE GOAL

Find all unique  $[a, b, c]$  where  $a + b + c = 0$ .



## THE TRAP

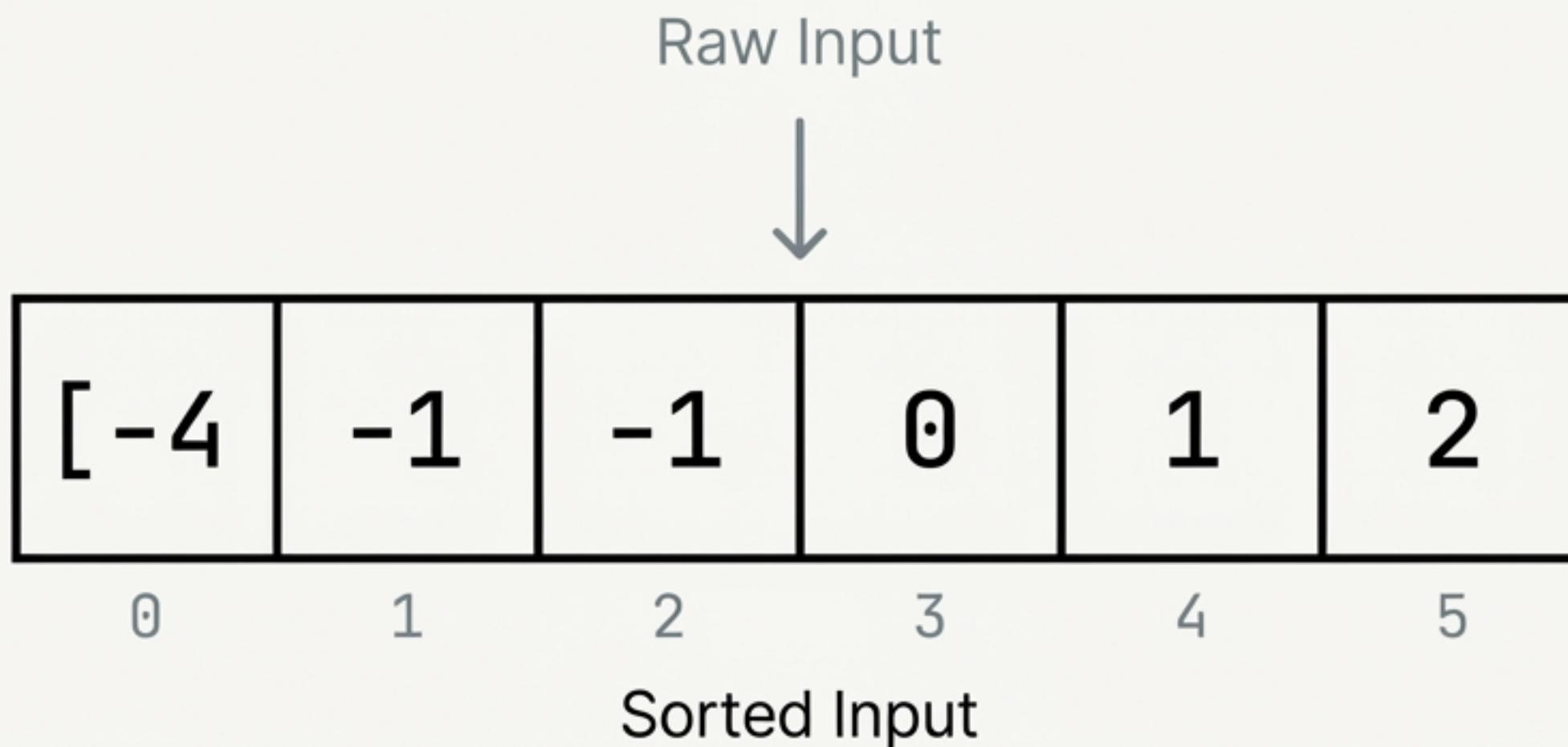
Checking every combination requires three nested loops.

**Complexity:**  
**O( $N^3$ )**

# Step 1: Sort the Input

[ -1	0	1	2	-1	-4 ]
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`nums.sort()`



Sorting unlocks predictable decision-making. If the sum is too small, move right. If too large, move left.

Eliminates the need for a third loop.

# The Strategy: Fix One, Solve Two

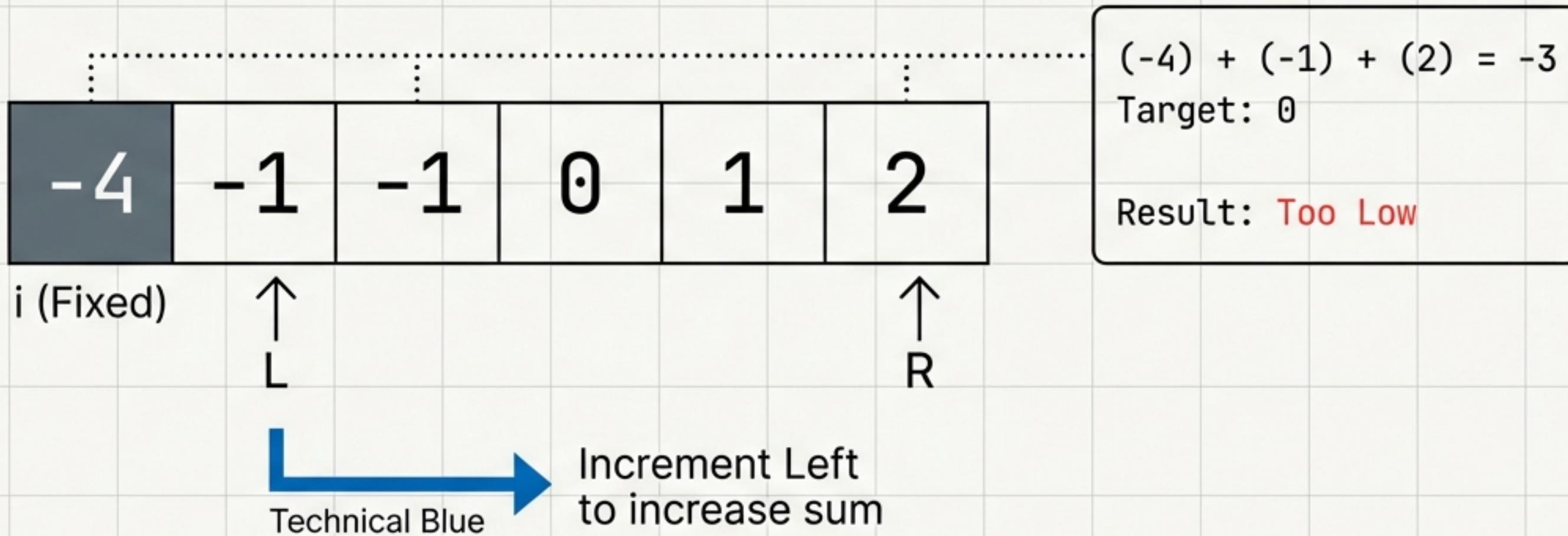


Iterate through 'i'. For each step, the problem becomes finding two numbers in the remaining window that sum to  $-\text{nums}[i]$ .

Transform the Equation

$$a + b + c = 0 \rightarrow b + c = -a$$

# Scenario A: Sum is Too Small



# Scenario B: Sum is Too Big

-4	-1	-1	0	1	2
----	----	----	---	---	---

i (Fixed)



L



R



Decrement Right to  
decrease sum

$$(-1) + (0) + (2) = 1$$

Target: 0

Result: Too High

# Scenario C: Target Hit!

-4	-1	-1	0	1	2
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i (Fixed)



$$(-1) + (0) + (1) = 0$$

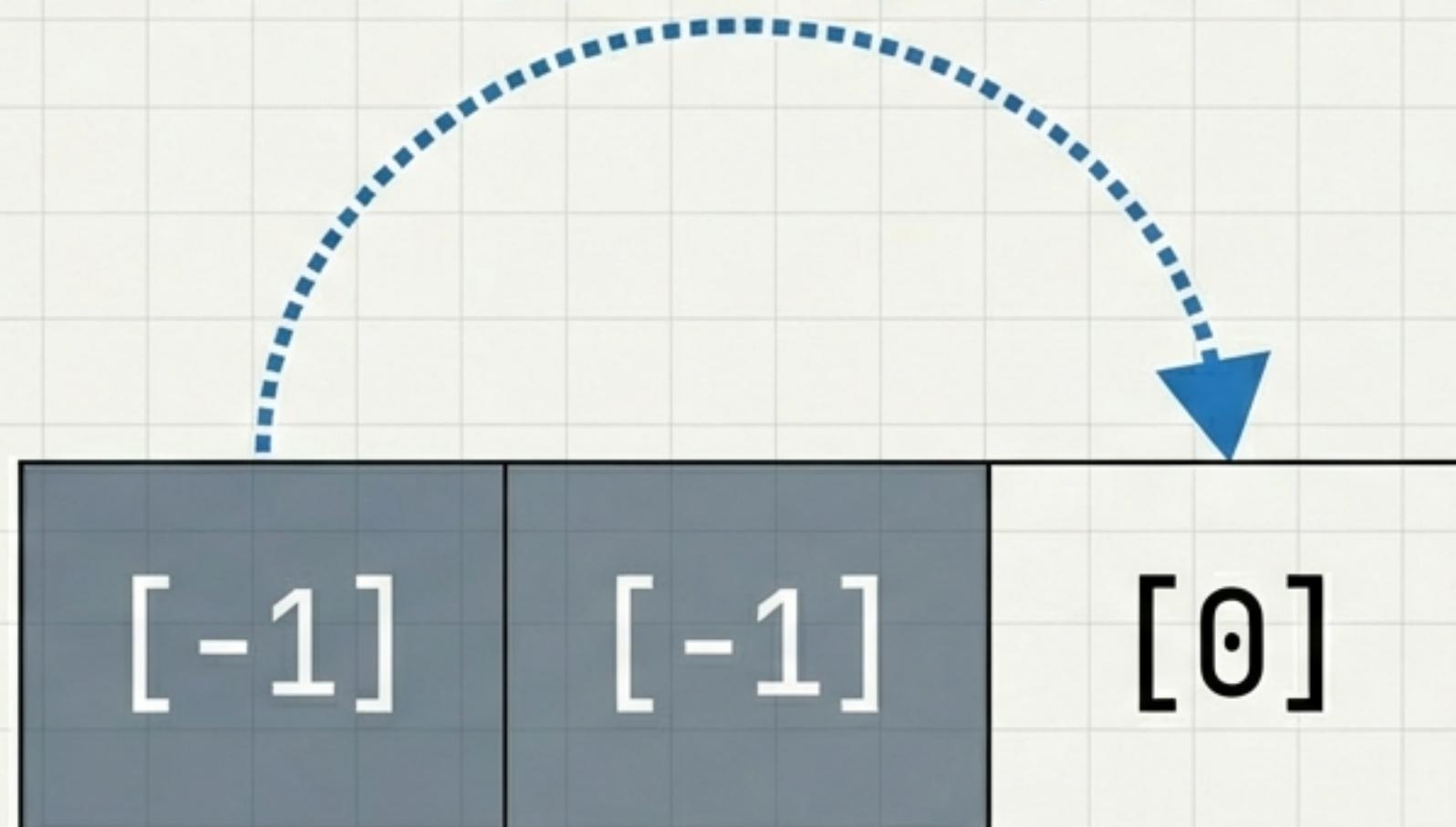
Found Triplet: [-1, 0, 1]



Record result, then pinch BOTH  
pointers inward to find other pairs.

# The Critical Edge Case: Skipping Duplicates

While `nums[i] == nums[i-1]`, continue



## **The Requirement:**

Return only unique triplets.

## **Outer Loop Logic:**

Skip the current index if it is identical to the previous one. We have already solved for this value.

## **Inner Loop Logic:**

Apply same logic to 'Left' pointer after finding a match.

# The Implementation

## Sort is Prerequisite

Sorting the array is the foundational step for the two-pointer approach.

## Skip Outer Duplicates

This condition prevents duplicate triplets from the same starting number.

## Skip Inner Duplicates

After finding a valid triplet, this loop advances the left pointer past any duplicates.

```
1 def threeSum(self, nums):
2     res = []
3     nums.sort() # 1
4
5     for i, a in enumerate(nums):
6         if i > 0 and a == nums[i-1]:
7             continue # 2
8
9         l, r = i + 1, len(nums) - 1
10        while l < r:
11            threeSum = a + nums[l] + nums[r]
12            if threeSum > 0:
13                r -= 1
14            elif threeSum < 0:
15                l += 1
16            else:
17                res.append([a, nums[l], nums[r]])
18                l += 1 # 3
19
20    return res
```

# Complexity & Key Takeaways

## Time Complexity

**$O(N^2)$**

Sorting:  $N \log N$ . Loops:  $N^2$ . Overall dominated by  $N^2$ .

## Space Complexity

**$O(1)$  or  $O(N)$**

Depends on sorting implementation (timsort uses  $O(N)$ ).

## The Recipe

1. Sort.
2. Loop 'i'.
3. Two Pointers (Left/Right).

## The Pitfall

Always skip duplicates for both 'i' and 'Left' to ensure unique triplets.