人工智慧 Lab3 - Pacman Agents

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實驗內容描述:

此次實驗透過修改 search.zip 裡面的 search.py 跟 searchAgenets.py 裡頭的程式碼片段. 程式碼的撰寫部分主要包含:

- searchAgents.py 中的:
 - class CornerProblem(search.SearchProblem) 底下的
 __init__()、getStartState()、isGoalState()、getSuccessors()。

```
class CornersProblem(search.SearchProblem):
    This search problem finds paths through all four corners of a layout.
   You must select a suitable state space and successor function
    def __init__(self, startingGameState):
        Stores the walls, pacman's starting position and corners.
        self.walls = startingGameState.getWalls()
        self.startingPosition = startingGameState.getPacmanPosition()
        top, right = self.walls.height-2, self.walls.width-2
        self.corners = ((1,1), (1,top), (right, 1), (right, top))
        for corner in self.corners:
            if not startingGameState.hasFood(*corner):
                print('Warning: no food in corner ' + str(corner))
        self._expanded = 0 # DO NOT CHANGE; Number of search nodes expanded
       # in initializing the problem
        "*** YOUR CODE HERE ***"
        self.startState = (self.startingPosition, tuple())
```

```
class CornersProblem(search.SearchProblem):

def getStartState(self):
    """

Returns the start state (in your state space, not the full Pacman state space)
    """

"*** YOUR CODE HERE ***"

return self.startState

def isGoalState(self, state):
    """

Returns whether this search state is a goal state of the problem.
    """

Returns whether this search state is a goal state of the problem.
    """

**** YOUR CODE HERE ***"

return len(state[1]) == 4
```

```
class CornersProblem(search.SearchProblem):
    def getSuccessors(self, state):
        Returns successor states, the actions they require, and a cost of 1.
            As noted in search.py:
            For a given state, this should return a list of triples, (successor,
            action, stepCost), where 'successor' is a successor to the current
            state, 'action' is the action required to get there, and 'stepCost'
            is the incremental cost of expanding to that successor
       .....
        successors = []
        for action in [Directions.NORTH, Directions.SOUTH, Directions.EAST, Directions.WEST]:
            # Add a successor state to the successor list if the action is legal
            "*** YOUR CODE HERE ***"
            x, y = state[0]
            dx, dy = Actions.directionToVector(action)
            nextx, nexty = int(x + dx), int(y + dy)
            if not self.walls[nextx][nexty]:
               nextPosition = (nextx, nexty)
                visitedCorners = list(state[1])
                if nextPosition in self.corners and nextPosition not in visitedCorners:
                    visitedCorners.append(nextPosition)
                successors.append( ( (nextPosition, tuple(visitedCorners)), action, 1 ) )
        self._expanded += 1 # DO NOT CHANGE
        return successors
```

 class ClosestDotSearchAgent(SearchAgent) 底下的 findPathToClosestDot()。

```
class ClosestDotSearchAgent(SearchAgent):

def findPathToClosestDot(self, gameState):
    """

Returns a path (a list of actions) to the closest dot, starting from gameState.
    """

# Here are some useful elements of the startState
startPosition = gameState.getPacmanPosition()

food = gameState.getFood()
walls = gameState.getWalls()
problem = AnyFoodSearchProblem(gameState)

"*** YOUR CODE HERE ***"
return search.bfs(problem)
```

 class AnyFoodSearchProblem(PositionSearchProblem) 底 下的 isGoalState()。

```
class AnyFoodSearchProblem(PositionSearchProblem):

def isGoalState(self, state):

The state is Pacman's position. Fill this in with a goal test that will complete the problem definition.

x,y = state

x,y = state

"*** YOUR CODE HERE ***"

return self.food[x][y]
```

○ **cornerHeuristic()**: 尋找四格角落的 searchAgent 使用 A* 演算 法時的啟發函式, 這部分依照註解要求, 可以比較粗略的估計, 因此我僅讓他去計算從當前點開始到最近的未被拜訪的角落, 再 從該角落去到相對於當前角落最近的其他角落, 以此類推所累計

的總距離做為啟發函式的回傳值。

```
def cornersHeuristic(state, problem):
    corners = problem.corners # These are the corner coordinates
   walls = problem.walls # These are the walls of the maze, as a Grid (game.py)
    "*** YOUR CODE HERE ***"
   x, y = state[0]
   visited = state[1]
   unvisited = [corner for corner in corners if corner not in visited]
   if not unvisited:
       return 0
   totalDistance = 0
   unvisitedCorners = unvisited.copy()
   while unvisitedCorners:
       dists = [(abs(x - c[0]) + abs(y - c[1]), c) for c in unvisitedCorners]
       minDist, closestCorner = min(dists)
       totalDistance += minDist
       x, y = closestCorner
       unvisitedCorners.remove(closestCorner)
    return totalDistance
```

○ foodHeuristic():尋找食物的 searchAgent 使用 A* 演算法時的 啟發函式, 這部分依照註解要求, 需要符合 admissible 跟 consistency, 因此需要比較複雜的算法來得到夠精確, 且不能高 估的可接受的解, 因此我把啟發值分成兩部分計算, 一部分計算 與當前最近的 food 的距離. 另一部分我先假設 Pacman 先去吃 離他最近的食物,之後再從該食物開始去找其他食物,因此這涉 及食物跟食物之間的距離計算, 我透過「利用所有 food 之間的 距離製作成一個 Graph, 節點就是所有的 food, 節點跟節點之 間的邊就是任意兩個 food 之間的曼哈頓距離,並裡用 Kruskal 演算法求這個 Graph 所形成的最小生成樹」。為此, Kruskal 演 算法是以邊為主的 Greedy 演算法來獲取最小生成樹, 故我使用 了原始的 util.py 裡面提供的 PriorityQueue 來讓儲存所有的邊, 並將最小邊逐一拿出,接著,為了效率,我在 util.py 裡面實作了 自己的 DisjointSet 來維護每次加入邊不能使得當前的最小生成 樹形成 Cycle 的限制(透過檢查 parent[x]!= parent[y] 之後才把 x 跟 y 加到最小生成樹裡面)。

```
def foodHeuristic(state, problem):
   position, foodGrid = state
   "*** YOUR CODE HERE ***"
   foodList = foodGrid.asList()
   if not foodList:
       return 0
   minDist = min([abs(position[0] - food[0]) + abs(position[1] - food[1]) for food in foodList])
   vertex = foodList
   pq = util.PriorityQueue() # storing the edges in priority queue in ascending order
   for i in range(len(vertex)):
       for j in range(i + 1, len(vertex)):
           vi, vj = vertex[i], vertex[j]
           dist = abs(vi[0] - vj[0]) + abs(vi[1] - vj[1])
           pq.push((dist, i, j), dist) # use dist as the priority
   disjointSet = util.DisjointSet(n=len(vertex))
   mstCost = 0 # the cost of the MST(Minimum Spanning Tree)
   count = 0  # the count the number of edges in MST
   while not pq.isEmpty():
      dist, x, y = pq.pop() # extracting the current minimum edge in the priority queue
       rootX, rootY = disjointSet.find(x), disjointSet.find(y)
       if rootX != rootY: # check if there's cycle after we add this edge to the MST
          disjointSet.union(rootX, rootY)
           mstCost += dist
           count += 1
           if count == len(vertex) - 1: # break if we already have the MST with n - 1 edges
               break
   return minDist + mstCost
```

```
class DisjointSet:
    def __init__(self, n):
       self.rank = [0] * n
        self.parent = [0] * n
        self.n = n
        for i in range(n): self.parent[i] = i
   def find(self, x):
        if x >= self.n: return x
        while self.parent[x] != x:
            self.parent[x] = self.parent[self.parent[x]]
            x = self.parent[x]
        return x
   def union(self, x, y):
        if x >= self.n: return False
        rootX, rootY = self.parent[x], self.parent[y]
        if rootX == rootY: return;
        if self.rank[rootX] < self.rank[rootY]:</pre>
            self.parent[rootX] = rootY
        elif self.rank[rootY] < self.rank[rootX]:</pre>
            self.parent[rootY] = rootX
        else:
            self.parent[rootY] = rootX
            self.rank[rootX] += 1
        return True
```

• search.py 中的:

depthFirstSearch() 。

```
def depthFirstSearch(problem):
   Search the deepest nodes in the search tree first.
   Your search algorithm needs to return a list of actions that reaches the
   goal. Make sure to implement a graph search algorithm.
   To get started, you might want to try some of these simple commands to
   understand the search problem that is being passed in:
   print("Start:", problem.getStartState())
   print("Is the start a goal?", problem.isGoalState(problem.getStartState()))
   print("Start's successors:", problem.getSuccessors(problem.getStartState()))
   "*** YOUR CODE HERE ***"
   stack = util.Stack()
   startState = problem.getStartState()
   stack.push((startState, []))
   visited = set()
   while not stack.isEmpty():
       state, path = stack.pop()
       if problem.isGoalState(state):
            return path
       if state not in visited:
           visited.add(state)
            for successor, action, stepCost in problem.getSuccessors(state):
                stack.push((successor, path + [action]))
   return []
```

breadthFirstSearch()。

```
106 ∨ def breadthFirstSearch(problem):
          """Search the shallowest nodes in the search tree first."""
          "*** YOUR CODE HERE ***"
          queue = util.Queue()
          startState = problem.getStartState()
          queue.push((startState, []))
         visited = set()
         while not queue.isEmpty():
              state, path = queue.pop()
              if problem.isGoalState(state):
                  return path
             if state not in visited:
                  visited.add(state)
                  for successor, action, stepCost in problem.getSuccessors(state):
                      queue.push((successor, path + [action]))
          return []
```

uniformCostSearch()。

```
def uniformCostSearch(problem):
    """Search the node of least total cost first."""
    "*** YOUR CODE HERE ***"
   pq = util.PriorityQueue()
    startState = problem.getStartState()
    pq.push((startState, [], 0), 0) # (state, path, cost), priority
   visited = dict() # state: lowerest cost
   while not pq.isEmpty():
       state, path, cost = pq.pop()
       if problem.isGoalState(state):
            return path
       if state not in visited or cost < visited[state]:</pre>
            visited[state] = cost
            for successor, action, stepCost in problem.getSuccessors(state):
                newCost = cost + stepCost
                pq.push((successor, path + [action], newCost), newCost)
   return []
```

aStarSearch()。

```
def aStarSearch(problem, heuristic=nullHeuristic):
    """Search the node that has the lowest combined cost and heuristic first."""
    "*** YOUR CODE HERE ***"
    pq = util.PriorityQueue()
    startState = problem.getStartState()
    pq.push((startState, [], 0), heuristic(startState, problem))
    visited = dict()
   while not pq.isEmpty():
        state, path, cost = pq.pop()
        if problem.isGoalState(state):
            return path
       if state not in visited or cost < visited[state]:</pre>
            visited[state] = cost
            for successor, action, stepCost in problem.getSuccessors(state):
                newCost = cost + stepCost
                priority = newCost + heuristic(successor, problem)
                pq.push((successor, path + [action], newCost), priority)
    return []
```

● Addition:由於當初開啟 search.zip 時發現裡頭的 autograder.py(用於在第二步驟測試運行結果的程式碼)出現許多非單一種類的複雜問題,因此有額外花了一些時間修正並研究和修改其片段損壞的程式碼,這部分也花了一些功夫...,主要是 imp 模組在 3.12 以上的 Python 版本中已被棄用,於是我把運行環境改到 3.11.4,接著又有一些程式碼其實autograder.py 在運行時不會用到,因此將其註解掉,接著在運行後發現 grading.py 裡面原先的 cgi 函式也有問題,找了一些資料發現 cgi 僅適用於 3.8 以前的 Python 版本,但 Python 官網已經沒有提供下載

Python3.8 了, 因此我把 cgi 全面改用 html 這個 Python library, 最後 成功透過 python3.11 autograder.py --code-directory /Users/jeff/Desktop/Coding/Machine_Learning/Pacman_Agent --student-code search.py,searchAgents.py 運行了(--code-directory 後我提供了我當前執行該檔案的 Project Folder 位置)。註解:使用 python3.11 來指定在當前 PC 環境直接運行 3.11 版本的 Python

實驗結果:

運行上面提到的指令去執行 autograder.py 後, 得到了經過 q1, q2, ... q8 的所有測試結果, 包含各個測試檔案裡面的小測試案件, 可以看到總共有 25 項測試, 最後的結果是全部都通過了(可於最後一張截圖查看對於所有測試的總結 log)。

```
• jeff@Jack Pacman_Agent % python3.11 autograder.py --code-directory /Users/jeff
 /Desktop/Coding/Machine_Learning/Pacman_Agent --student-code search.py,searchA
 gents.py
 /Users/jeff/Desktop/Coding/Machine_Learning/Pacman_Agent/autograder.py:17: Dep
 recationWarning: the imp module is deprecated in favour of importlib and slate
 d for removal in Python 3.12; see the module's documentation for alternative u
   import imp
 Starting on 5-20 at 22:18:12
 Question q1
 *** PASS: test_cases/q1/graph_backtrack.test
                                  ['1:A->C', '0:C->G']
         solution:
                                  ['A', 'D', 'C']
         expanded_states:
 ***
 *** PASS: test_cases/q1/graph_bfs_vs_dfs.test
                                  ['2:A->D', '0:D->G']
         solution:
         expanded_states:
                                  ['A', 'D']
 *** PASS: test_cases/q1/graph_infinite.test
                                  ['0:A->B', '1:B->C', '1:C->G']
         solution:
 ***
                                  ['A', 'B', 'C']
         expanded states:
 ***
 *** PASS: test_cases/q1/graph_manypaths.test
                                  ['2:A->B2', '0:B2->C', '0:C->D', '2:D->E2', '0
         solution:
 ***
 :E2->F', '0:F->G']
                                  ['A', 'B2', 'C', 'D', 'E2', 'F']
         expanded_states:
 *** PASS: test_cases/q1/pacman_1.test
         pacman layout:
                                  mediumMaze
         solution length: 130
 ***
 ***
         nodes expanded:
                                  146
 ### Question q1: 3/3 ###
```

```
Question q2
*** PASS: test_cases/q2/graph_backtrack.test
                                     ['1:A->C', '0:C->G']
['A', 'B', 'C', 'D']
         solution:
         expanded states:
***
*** PASS: test_cases/q2/graph_bfs_vs_dfs.test
         solution:
                                      ['1:A->G']
***
***
         expanded_states:
                                      ['A', 'B']
*** PASS: test_cases/q2/graph_infinite.test
                                     ['0:A->B', '1:B->C', '1:C->G']
['A', 'B', 'C']
         solution:
***
         expanded_states:
***
*** PASS: test_cases/q2/graph_manypaths.test
                                     ['1:A->C', '0:C->D', '1:D->F', '0:F->G']
['A', 'B1', 'C', 'B2', 'D', 'E1', 'F', 'E2']
***
         solution:
         expanded states:
***
*** PASS: test_cases/q2/pacman_1.test
         pacman layout:
                                     mediumMaze
***
         solution length: 68
***
         nodes expanded:
                                     269
***
### Question q2: 3/3 ###
```

```
Ouestion a3
*** PASS: test_cases/q3/graph_backtrack.test
                                    ['1:A->C', '0:C->G']
['A', 'B', 'C', 'D']
         solution:
***
         expanded states:
*** PASS: test cases/g3/graph bfs vs dfs.test
         solution:
                                     ['1:A->G']
***
         expanded_states:
***
                                    ['A', 'B']
*** PASS: test_cases/q3/graph_infinite.test
                                    ['0:A->B', '1:B->C', '1:C->G']
['A', 'B', 'C']
         solution:
***
         expanded states:
***
*** PASS: test_cases/q3/graph_manypaths.test
                                    ['1:A->C', '0:C->D', '1:D->F', '0:F->G']
['A', 'B1', 'C', 'B2', 'D', 'E1', 'F', 'E2']
***
         solution:
         expanded states:
***
    PASS: test cases/q3/ucs 0 graph.test
                                    ['Right', 'Down', 'Down']
['A', 'B', 'D', 'C', 'G']
***
         solution:
***
         expanded_states:
    PASS: test_cases/q3/ucs_1_problemC.test
         pacman layout:
***
                                    mediumMaze
***
         solution length: 68
         nodes expanded:
                                    269
***
    PASS: test_cases/q3/ucs_2_problemE.test
         pacman layout:
                                    mediumMaze
***
***
         solution length: 74
***
         nodes expanded:
                                    260
    PASS: test_cases/q3/ucs_3_problemW.test
         pacman layout:
                                    mediumMaze
***
***
         solution length: 152
         nodes expanded:
***
                                    173
    PASS: test_cases/q3/ucs_4_testSearch.test
         pacman layout:
                                    testSearch
***
         solution length: 7
***
***
         nodes expanded:
                                    14
*** PASS: test_cases/q3/ucs_5_goalAtDequeue.test
                                    ['1:A->B', '0:B->C', '0:C->G']
         solution:
***
                                    ['A', 'B', 'C']
***
         expanded states:
### Question q3: 3/3 ###
```

```
Question q4
*** PASS: test_cases/q4/astar_0.test
                                    ['Right', 'Down', 'Down']
['A', 'B', 'D', 'C', 'G']
         solution:
***
        expanded_states:
***
*** PASS: test_cases/q4/astar_1_graph_heuristic.test
                                    ['0', '0', '2']
['S', 'A', 'D', 'C']
         expanded states:
***
*** PASS: test_cases/q4/astar_2_manhattan.test
         pacman layout:
                                   mediumMaze
***
        solution length: 68
***
        nodes expanded:
                                   221
***
*** PASS: test_cases/q4/astar_3_goalAtDequeue.test
                                    ['1:A->B', '0:B->C', '0:C->G']
        solution:
***
                                    ['A', 'B', 'C']
***
         expanded_states:
*** PASS: test_cases/q4/graph_backtrack.test
                                    ['1:A->C', '0:C->G']
['A', 'B', 'C', 'D']
        solution:
***
         expanded_states:
***
*** PASS: test_cases/q4/graph_manypaths.test
                                    ['1:A->C', '0:C->D', '1:D->F', '0:F->G']
        solution:
***
                                    ['A', 'B1', 'C', 'B2', 'D', 'E1', 'F', 'E2']
***
        expanded_states:
### Question q4: 3/3 ###
```

```
Question q5
=========

*** PASS: test_cases/q5/corner_tiny_corner.test

*** pacman layout: tinyCorner

*** solution length: 28

### Question q5: 3/3 ###
```

Question q6

*** PASS: heuristic value less than true cost at start state *** PASS: heuristic value less than true cost at start state *** PASS: heuristic value less than true cost at start state path: ['North', 'East', 'East', 'East', 'North', 'North', 'West', 'West', 'West', 'West', 'North', 'North', 'North', 'North', 'North', 'North', 'North', 'North', 'South', 'East', 'East', 'East', 'East', 'South', 'South', 'South', 'South', 'South', 'South', 'West', 'West', 'East', 'East', 'East', 'North', 'North', 'North', 'East', 'E t', 'South', 'South', 'East', 'East', 'East', 'East', 'East', 'North', 'North', 'South', 'East', 'East', 'East', 'North', 'North', 'East', 'East', 'North', 'South', 'South', 'South', 'South', 'East', 'East', 'North', 'North', 'East', 'East', 'North', 'North', 'North', 'North', 'North', 'North', 'North', 'North', 'North', 'West', 'North', 'North', 'East', 'East', 'North', 'North', 'North', 'East', 'East', 'North', path length: 106 *** PASS: Heuristic resulted in expansion of 901 nodes

Question q6: 3/3

```
Question q7
*** PASS: test cases/q7/food heuristic 1.test
*** PASS: test cases/q7/food heuristic 10.test
*** PASS: test_cases/q7/food_heuristic_11.test
*** PASS: test_cases/q7/food_heuristic_12.test
*** PASS: test_cases/q7/food_heuristic_13.test
*** PASS: test_cases/q7/food_heuristic_14.test
*** PASS: test_cases/q7/food_heuristic_15.test
*** PASS: test_cases/q7/food_heuristic_16.test
*** PASS: test cases/q7/food heuristic 17.test
*** PASS: test cases/q7/food heuristic 2.test
*** PASS: test cases/q7/food heuristic 3.test
*** PASS: test cases/q7/food heuristic 4.test
*** PASS: test_cases/q7/food_heuristic_5.test
*** PASS: test cases/q7/food heuristic 6.test
*** PASS: test cases/q7/food heuristic 7.test
*** PASS: test cases/q7/food heuristic 8.test
*** PASS: test_cases/q7/food_heuristic_9.test
*** FAIL: test_cases/q7/food_heuristic_grade_tricky.test
        expanded nodes: 7137
***
        thresholds: [15000, 12000, 9000, 7000]
***
### Question q7: 4/4 ###
```

```
Question q8
[SearchAgent] using function depthFirstSearch
[SearchAgent] using problem type PositionSearchProblem
*** PASS: test_cases/q8/closest_dot_1.test
        pacman layout:
                                Test 1
***
        solution length:
***
[SearchAgent] using function depthFirstSearch
[SearchAgent] using problem type PositionSearchProblem
*** PASS: test_cases/q8/closest_dot_10.test
        pacman layout:
***
                                Test 10
        solution length:
***
                                         1
[SearchAgent] using function depthFirstSearch
[SearchAgent] using problem type PositionSearchProblem
*** PASS: test cases/q8/closest dot 11.test
        pacman layout:
                                Test 11
***
        solution length:
                                         2
***
[SearchAgent] using function depthFirstSearch
[SearchAgent] using problem type PositionSearchProblem
*** PASS: test_cases/q8/closest_dot_12.test
        pacman layout:
                                Test 12
***
***
        solution length:
                                         3
[SearchAgent] using function depthFirstSearch
[SearchAgent] using problem type PositionSearchProblem
*** PASS: test_cases/q8/closest_dot_13.test
        pacman layout:
                                Test 13
***
***
        solution length:
[SearchAgent] using function depthFirstSearch
[SearchAgent] using problem type PositionSearchProblem
*** PASS: test_cases/q8/closest_dot_2.test
        pacman layout:
                                Test 2
***
        solution length:
                                         1
***
```

```
[SearchAgent] using function depthFirstSearch
[SearchAgent] using problem type PositionSearchProblem
*** PASS: test_cases/q8/closest_dot_4.test
        pacman layout:
                                 Test 4
***
***
        solution length:
[SearchAgent] using function depthFirstSearch
[SearchAgent] using problem type PositionSearchProblem
*** PASS: test cases/q8/closest dot 5.test
***
        pacman lavout:
                                 Test 5
        solution length:
***
[SearchAgent] using function depthFirstSearch
[SearchAgent] using problem type PositionSearchProblem
*** PASS: test_cases/q8/closest_dot_6.test
        pacman layout:
                                 Test 6
***
        solution length:
***
[SearchAgent] using function depthFirstSearch
[SearchAgent] using problem type PositionSearchProblem
*** PASS: test_cases/q8/closest_dot_7.test
***
        pacman layout:
                                 Test 7
        solution length:
***
[SearchAgent] using function depthFirstSearch
[SearchAgent] using problem type PositionSearchProblem
*** PASS: test_cases/q8/closest_dot_8.test
        pacman layout:
***
                                 Test 8
        solution length:
***
[SearchAgent] using function depthFirstSearch
[SearchAgent] using problem type PositionSearchProblem
*** PASS: test_cases/q8/closest_dot_9.test
        pacman layout:
***
                                 Test 9
        solution length:
                                         1
***
### Question q8: 3/3 ###
```

結果討論與實驗心得:

這次的實驗做得很累,有點心力憔悴,但是完成後的感覺很棒、很有成就感, 在這次專題中, 我訓練了自己透過 Pvthon 撰寫大量演算法(過去都是使用 C++ 在 LeetCode 上面練習), 我覺得最核心且最關鍵部分還是撰寫 foodHeuristic() 的過程, 因為要保持註解裡面提到的 admissble 跟 consistency, 否則在執行 autograder.py 時會卡在 q7, 我原先為了讓距離可 接受, 嘗試透過同個檔案底下提供的 mazeDistance() (其內部調用 bfs)來完 成,但是這會導致其中一項測資顯示擴展的點超過可接受的值,因此後來改 成粗略的計算各食物的距離(透過曼哈頓距離), 結果這也導致 q7 跳出啟發 函式不符合 consistency 的問題, 故我最後採用了一個可以更加精確且執行 速度不會太慢的方式,過程中非常煎熬,只是剛好最近在準備研究所考試的 資料結構上到最小生成樹, 跟認識的同學討論一陣子後決定至少試試看, 於 是便在 util.py 裡面寫出一個簡單的 DisjointSet(有 rank 的功能保障路經壓 縮不會花費太多時間),並使用 Kruskal 演算法,過程如同實驗內容描述,可 去上方的 foodHeuristic() 裡面查看。總之, 這次讓我更加熟悉資料結構和圖 論演算法, 也讓我更熟悉 Python 函式庫跟 Python, 最重要的是讓我面對問 題的解決能力和信心大幅提升。

另外, 如果有需要程式碼, 請聯絡我, 可以透過 gmail 或是其他方式, 我定會提供我的心血。