

# 3D Geometry Objects

10 Questions

1. What is the name of 2 presenters today?

1 POINT

- 0/11 ☐ A Nguyen Duc Anh Phuc & Ngo Van Tan Luu
- 0/11 ☐ B Ngo Van Tan Luu & Huynh Viet Tuan Kiet
- 0/11 ☐ C Nguyen Duc Anh Phuc & Truong Thanh Thang
- 11/11 ☒ D Huynh Viet Tuan Kiet & Nguyen Duc Anh Phuc
- 0/11 ☐ E Ngo Van Tan Luu & Truong Thanh Thang

2. Which is a correct statement?

2 POINTS

- 2/12 ☐ A 3 collinear points are 3 points in only one plane
- 2/12 ☐ B There is only one plane going through 3 collinear points
- 5/12 ☒ C 3 coplanar points may not be collinear
- 3/12 ☐ D 3 points that are not collinear are definitely not coplanar

3. Why must use matrices in order to represent linear transformations?

3 POINTS

- 0/11 ☐ A Matrices allow arbitrary linear transformations to be displayed in a consistent format suitable for computation
- 0/11 ☐ B Matrices are easily represented as a computer data structure
- 0/11 ☐ C The transformation represented as a matrix  $M$  can be undone by applying the inverse of the matrix  $M^{-1}$
- 0/11 ☐ D Every linear transformation is a matrix transformation
- 0/11 ☐ E Both A, B, D are correct
- 1/11 ☐ F A and C are correct
- 5/11 ☒ G Both A, B, C are correct
- 5/11 ☐ H Both A, B, C, D are correct
- 0/11 ☐ I B and C are correct

4. Square matrices are used so that we can perform all transformations using matrix **multiplications**.

1 POINT

10/11 **T** True

1/11 **F** False

$$\begin{bmatrix} 1 & 0 & 0 & T_X \\ 0 & 1 & 0 & T_Y \\ 0 & 0 & 1 & T_Z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

5. Based on the equation, which is the matrix that rotates around the Oy axis?

3 POINTS

1/11 **A**  $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta & 0 \\ 0 & \sin \theta & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$

10/11 **B**  $\begin{bmatrix} \cos \theta & 0 & \sin \theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \theta & 0 & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$

0/11 **C**  $\begin{bmatrix} \cos \theta & 0 & -\sin \theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \theta & 0 & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$

0/11 **D**  $\begin{bmatrix} \sin \theta & 0 & \cos \theta & 0 \\ 0 & 1 & 0 & 0 \\ -\cos \theta & 0 & \sin \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$

$$X' = X \times \cos \theta + Z \times \sin \theta$$

$$Y' = Y$$

$$Z' = -X \times \sin \theta + Z \times \cos \theta$$

$$\rightarrow \begin{bmatrix} X' \\ Y' \\ Z' \\ 1 \end{bmatrix} = [?] \times \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

6. Which matrix represents this 3D scaling transformation visualization?

3 POINTS

2/11 **A**  $S = \begin{bmatrix} \frac{1}{2}, 0, 0, 0 \\ 0, \frac{1}{2}, 0, 0 \\ 0, 0, \frac{1}{2}, 0 \\ 0, 0, 0, 0 \end{bmatrix}$

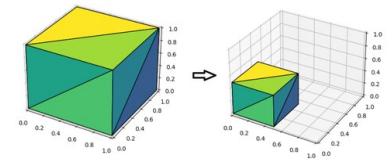
3/11 **B**  $S = \begin{bmatrix} 2, 0, 0, 0 \\ 0, 2, 0, 0 \\ 0, 0, 2, 0 \\ 0, 0, 0, 1 \end{bmatrix}$

1/11 **C**  $S = \begin{bmatrix} 1, 0, 0, 0 \\ 0, 1, 0, 0 \\ 0, 0, 1, 0 \\ 0, 0, 0, \frac{1}{2} \end{bmatrix}$

4/11 **D**  $S = \begin{bmatrix} \frac{1}{2}, 0, 0, 0 \\ 0, \frac{1}{2}, 0, 0 \\ 0, 0, \frac{1}{2}, 0 \\ 0, 0, 0, \frac{1}{2} \end{bmatrix}$

1/11 **E**  $S = \begin{bmatrix} 1, 0, 0, 0 \\ 0, 1, 0, 0 \\ 0, 0, 1, 0 \\ 0, 0, 0, 2 \end{bmatrix}$

0/11 **F**  $S = \begin{bmatrix} 2, 0, 0, 0 \\ 0, 2, 0, 0 \\ 0, 0, 2, 0 \\ 0, 0, 0, \frac{1}{2} \end{bmatrix}$



7. What transformation does this matrix perform?

2 POINTS

0/11 **A** Reflection through the XY plane

0/11 **B** Reflection through the YZ plane

11/11 **C** Reflection through the XZ plane

$$\begin{bmatrix} X' \\ Y' \\ Z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

8. What transformation does this matrix perform?

3 POINTS

5/11 **A** Rotation around the Ox axis 90 degrees

3/11 **B** Rotation around the Oy axis 90 degrees

3/11 **C** Rotation around the Oz axis 90 degrees

$$\begin{bmatrix} X' \\ Y' \\ Z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

9. Which of the following coordinate performs the translation  $(2, 4, 5)$  and rotates about the z-axis at an angle of 90 degrees at the point  $(1, 1, 1)$ ?

3 POINTS

- 1/11 **A**  $(5, 3 - 6)$   
 7/11 **B**  $(-5, 3, 6)$   
 1/11 **C**  $(-3, 3, 6)$   
 2/11 **D**  $(3, 3, -6)$

10. Which of the following matrices performs the reflection  $(2, 4, 5)$  through the YZ plane and shear in the X directions with the parameter  $(0, 4, 7)$  degrees at any point?

5 POINTS

- 6/11 **A**  $S = \begin{bmatrix} -1, 0, 0, 0 \\ -4, 1, 0, 0 \\ -7, 0, 1, 0 \\ 0, 0, 0, 1 \end{bmatrix}$   
 3/11 **B**  $S = \begin{bmatrix} -1, 0, 0, 0 \\ 4, 1, 0, 0 \\ 7, 0, 1, 0 \\ 0, 0, 0, 1 \end{bmatrix}$   
 1/11 **C**  $S = \begin{bmatrix} -1, 0, 0, 0 \\ -4, 1, 0, 0 \\ 7, 0, 1, 0 \\ 0, 0, 0, 1 \end{bmatrix}$   
 1/11 **D**  $S = \begin{bmatrix} -1, 0, 0, 0 \\ 4, 1, 0, 0 \\ -7, 0, 1, 0 \\ 0, 0, 0, 1 \end{bmatrix}$