

# How to choose the lags

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Lag features

# How to choose the lags

|            | target<br>↓ | feature<br>↓ |
|------------|-------------|--------------|
| Date       | Sales       | Ad<br>spend  |
| 2020-02-12 | 23          | 100          |
| 2020-02-13 | 30          | 120          |
| 2020-02-14 | 35          | 90           |
| 2020-02-15 | 30          | 80           |
| 2020-02-16 | ?           | 100          |

# Lag feature

| target     |       | lag features <b>from target</b> |             | original features | lag features <b>from original features</b> |                |
|------------|-------|---------------------------------|-------------|-------------------|--|----------------|
| Date       | Sales | Sales Lag 1                     | Sales Lag 3 | Ad spend          | Ad spend Lag 1                             | Ad spend Lag 2 |
| 2020-02-12 | 23    | NaN                             | NaN         | 100               | NaN  | NaN            |
| 2020-02-13 | 30    | 23                              | NaN         | 120               | 100  | NaN            |
| 2020-02-14 | 35    | 30                              | NaN         | 90                | 120  | 100            |
| 2020-02-15 | 30    | 35                              | 23          | 80                | 90   | 120            |
| 2020-02-16 | ?     | 30                              | 30          | 100               | 80   | 90             |

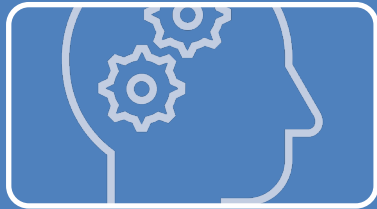
We can create multiple lag features with different lags from the target and features.

Problem: Which lags to use? How many lag features to create?

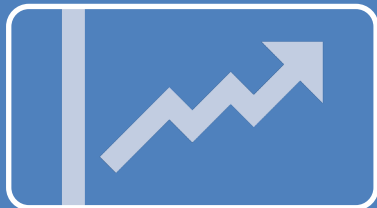
# How to choose the lags



Domain knowledge



Feature selection and modelling

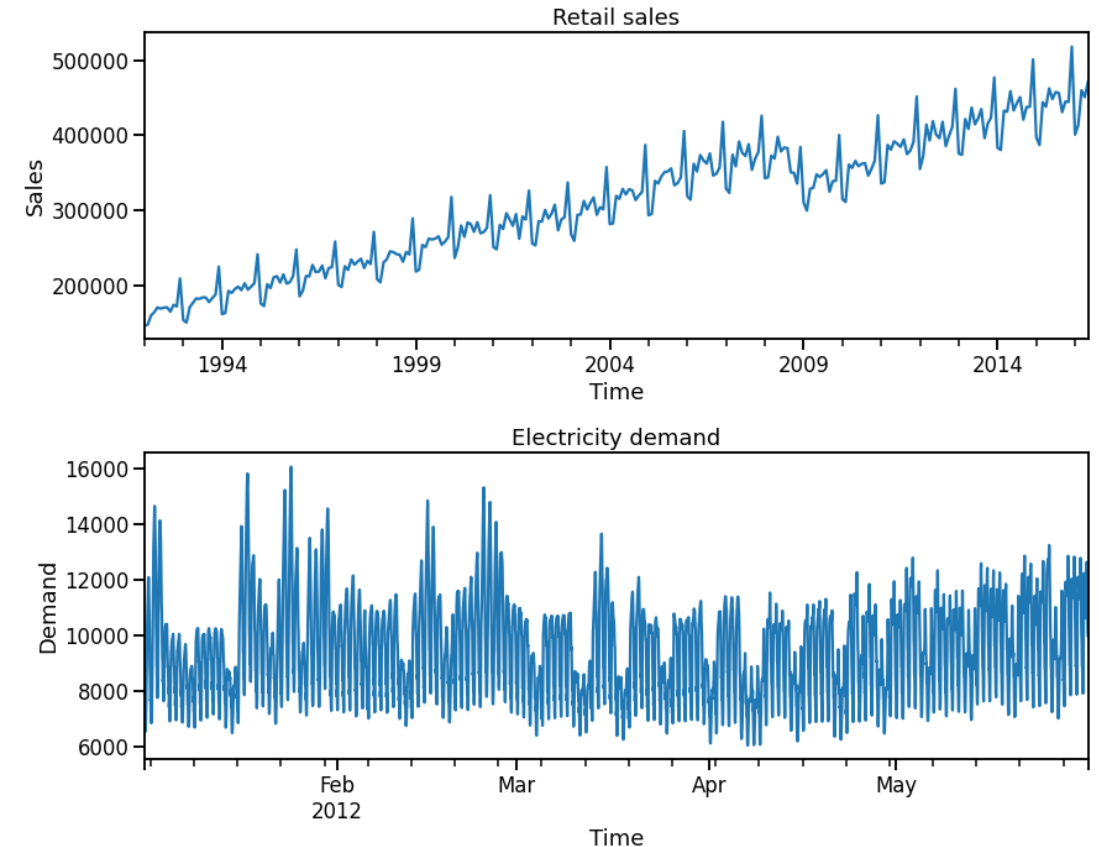


Time-series correlation methods

# Domain knowledge

## When lagging the target

- If seasonality is known use a lag of the same seasonal order (aka seasonal lag).
- Example retail sales: yearly seasonality → use lag of 1 year.
- Example electricity demand: multiple seasonalities such as yearly, weekly, and daily → use lag of 1 year, 1 week, and 1 day.
- Most recent values tend to be predictive → use small lags.



# Domain knowledge

## When lagging the features

- Use the subset of features you think are most important in affecting the target.
- Only use the value of the feature that you know at predict time to avoid data leakage.
- Most recent values tend to be predictive  
→ use small lags.

|            | target | features |         |
|------------|--------|----------|---------|
|            | ↓      |          |         |
| Date       | Sales  | Ad spend | weekend |
| 2020-02-12 | 23     | 100      | 0       |
| 2020-02-13 | 30     | 120      | 0       |
| 2020-02-14 | 35     | 90       | 0       |
| 2020-02-15 | 30     | 80       | 1       |
| 2020-02-16 | ?      | 100      | 1       |

# Domain knowledge

## Pros

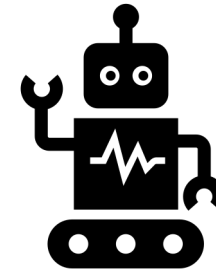
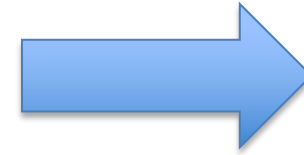
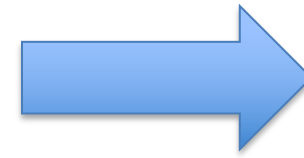
- Likely to result in fewer additional features as we will pick a small number of lags and features known to be important.

## Cons

- We may not know all the seasonal patterns or which ones are most important.
- We may not know which features are important to lag.
- Not scalable.

# Feature selection and modelling

| Sales Lag 1 | Sales Lag 3 | Ad spend Lag 1 | Ad spend Lag 2 |
|-------------|-------------|----------------|----------------|
| NaN         | NaN         | NaN            | NaN            |
| 23          | NaN         | 100            | NaN            |
| 30          | NaN         | 120            | 100            |
| 35          | 23          | 90             | 120            |
| 30          | 30          | 80             | 90             |



- Create a bunch of different lags which are reasonable given the feature and use case (e.g., ad spend more than 1 year ago unlikely to be help for sales forecasting).
- Use feature selection and/or modelling (e.g., LASSO) to best utilize the features and determine a subset which minimizes forecast error.



# Feature selection and modelling

## Pros

- Automatic. Less hands-on decision making.
- May find useful features which you may not have been used otherwise.

## Cons

- Will create very large number of features.
- The lags of the same features will be highly correlated to each other.
- More complex model than necessary.
- Computationally expensive.

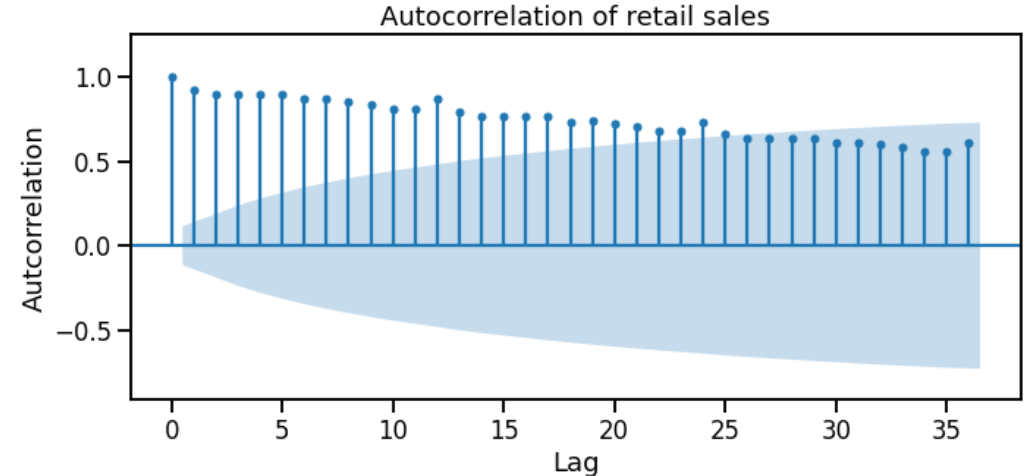
# Time-series correlation methods

## The main idea

- Measure how correlated the lag features are with the target.
- If the lag feature is highly correlated to the target then it might be helpful.

## Three main methods

- Autocorrelation function (ACF)
- Partial autocorrelation function (PACF)
- Cross-correlation function (CCF)



# Time-series correlation methods

## Pros

- More robust way to find relevant lags.
- Can indicate whether there is any predictive information in the historic time series at all.
- Can help identify important seasonalities.

## Cons

- Can be difficult to interpret correlation plots.
- Time consuming to interpret and read correlation plots → not scalable to large number of features.
- Even if one feature is not highly correlated with the target it could still be predictive in the presence of other features → not captured in these methods.
- These methods only measure linear relationship between variables.

# Summary

Lags of the target and other features can create predictive features for forecasting.

User must decide which lag features to create.

Domain knowledge, feature selection & modelling, and time-series correlation methods can help inform this decision.