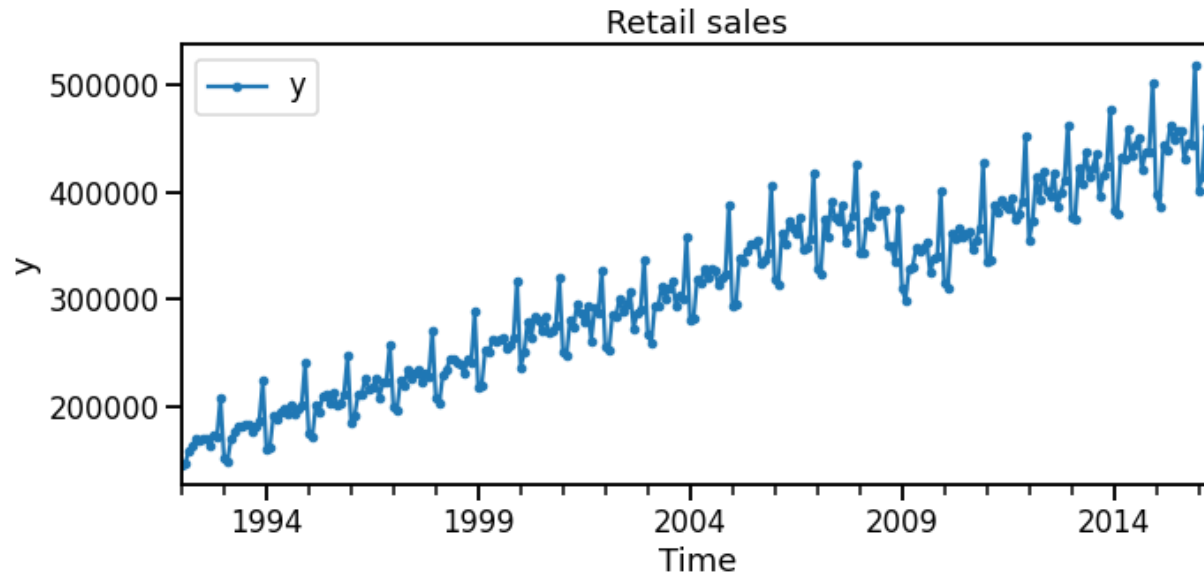


# Multi-seasonal time series

---

Time series  
decomposition

# So far we've shown time series with one seasonality



Additive decomposition

$$y_t = \hat{T}_t + \hat{S}_t + \hat{R}_t$$

Multiplicative decomposition

$$y_t = \hat{T}_t \times \hat{S}_t \times \hat{R}_t$$

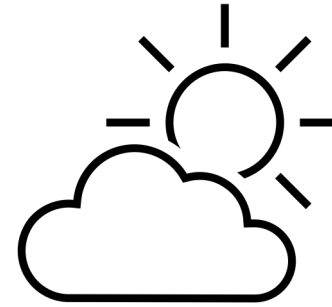
Trend component      Seasonal component      Residual component

Arrows point from the labels "Trend component", "Seasonal component", and "Residual component" to the corresponding terms  $\hat{T}_t$ ,  $\hat{S}_t$ , and  $\hat{R}_t$  in the multiplicative decomposition equation.

- Retail sales at monthly granularity just shows yearly seasonality.
- This is partly an artifact of aggregating.
- If we had more granular data we might uncover other seasonal components (e.g., daily, weekly).

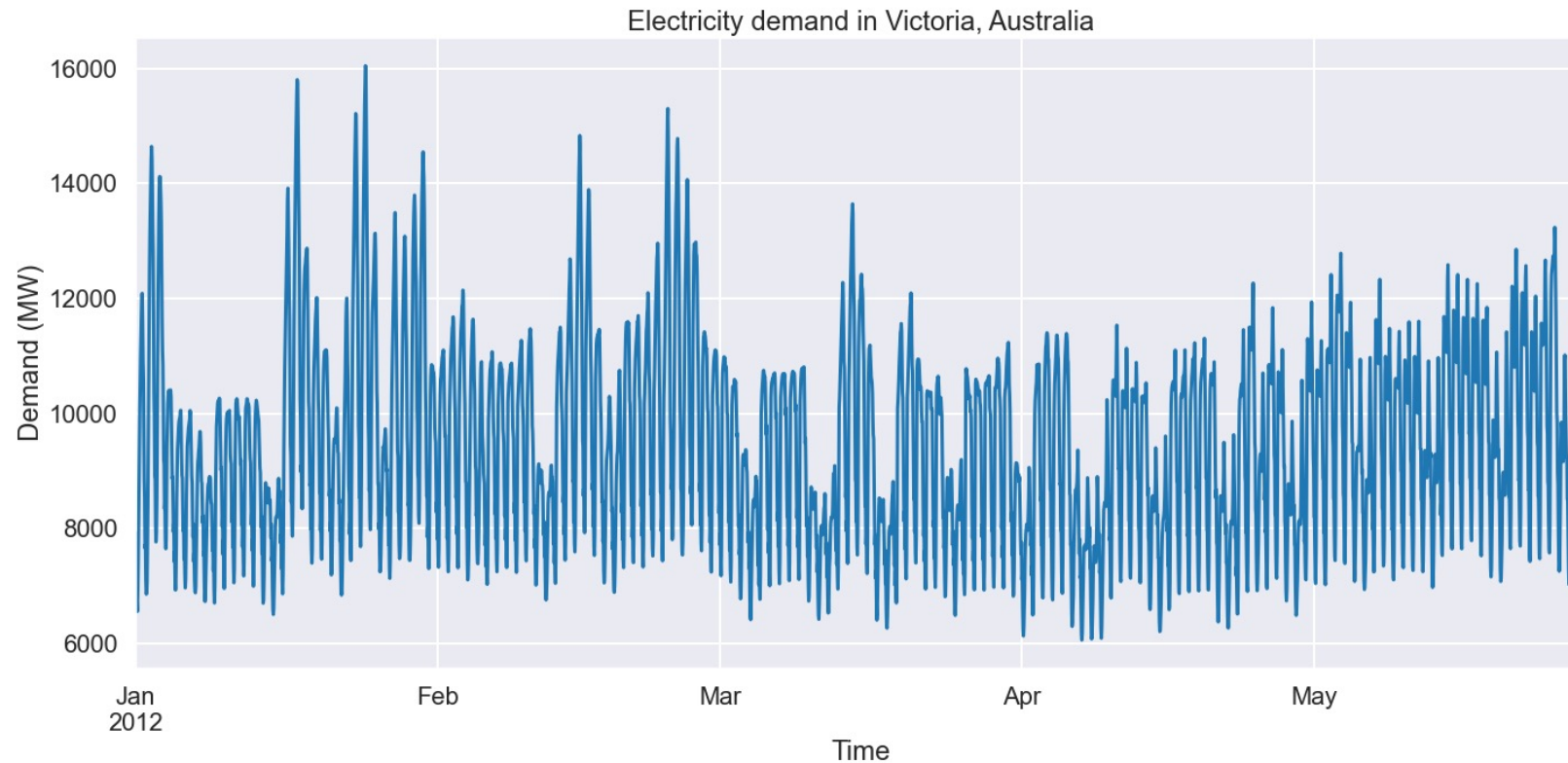
# What about multi-seasonal time series?

- Multi-seasonality: time series has multiple repeating patterns at different time scales (e.g., daily and weekly)
- What can cause multi-seasonality?
- Weather
  - Sunshine & daylight (daily and yearly)
  - Temperature (daily and yearly)
  - Monsoon seasons (yearly)
- Human behaviour
  - Workday patterns (daily)
  - Weekdays vs weekends (weekly)
  - Monthly pay checks (monthly)
  - Summer holidays (yearly)
- Time series from air pollution to restaurant demand have multiple seasonalities.



# Electricity demand example

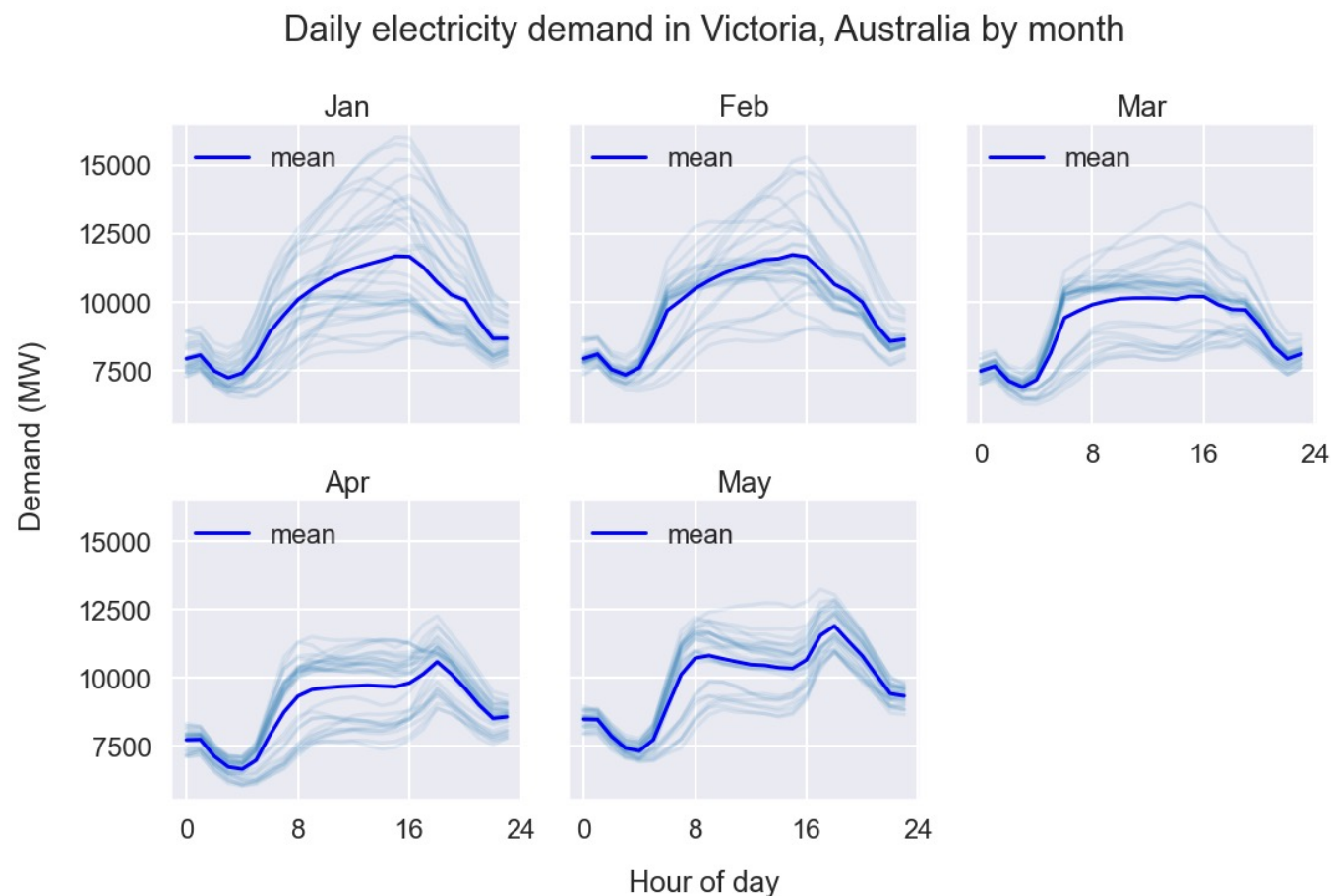
- Hourly electricity demand in Victoria, Australia.



Source: O'Hara-Wild, M., Hyndman, R.J., Wang, E., 2021. tsibbledata: Diverse Datasets for 'tsibble'. URL: <https://CRAN.R-project.org/package=tsibbledata>. R package version 0.3.0. ([Creative Commons License](#))

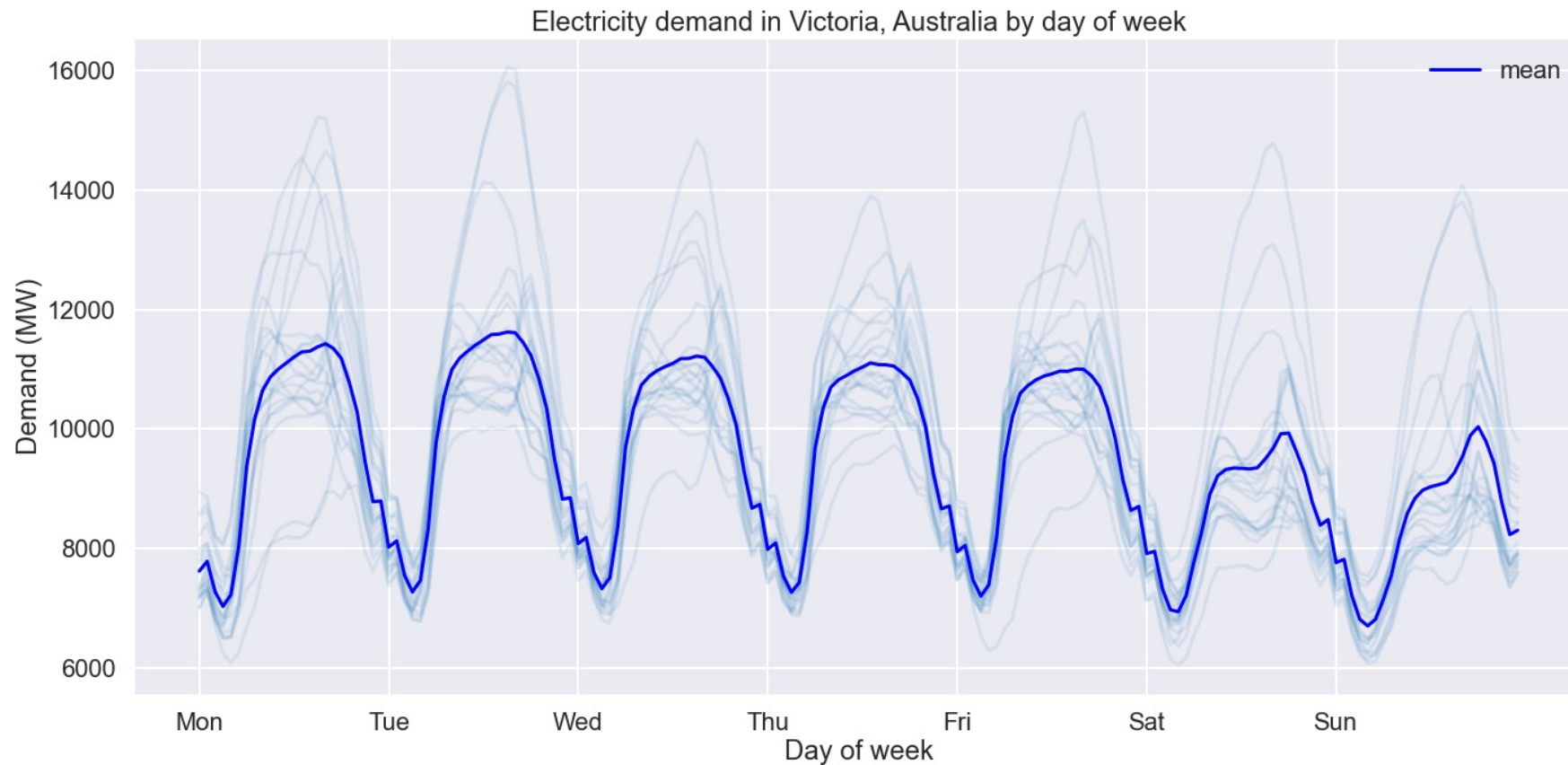
# Electricity demand example

- There is daily seasonality which changes with the time of year.



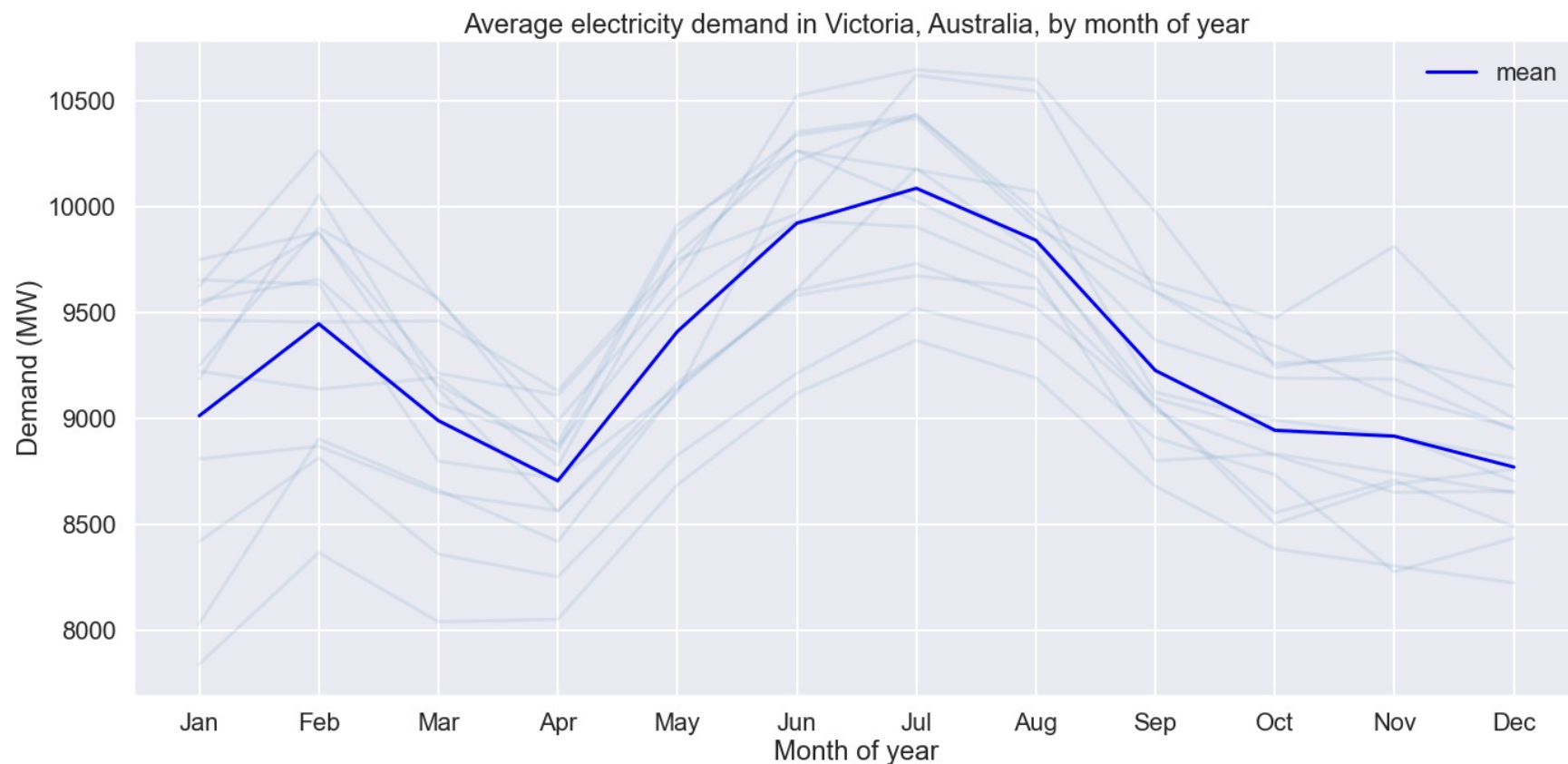
# Electricity demand example

- There is weekly seasonality from changes in demand in the weekdays vs the weekends.



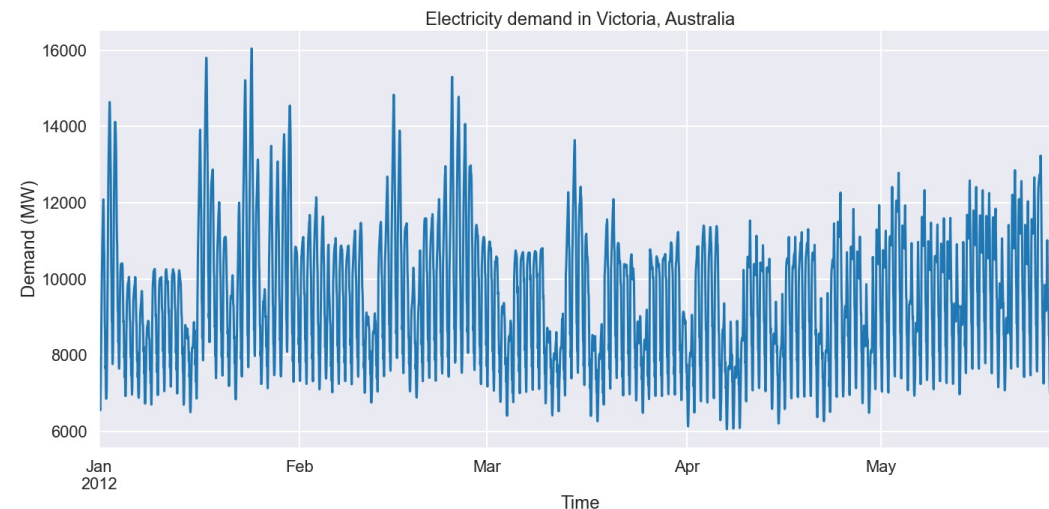
# Electricity demand example

- There is yearly seasonality from changes in temperature over the winter and summer.



# Electricity demand example

- This time series has daily, weekly, and yearly seasonality.
- In general, as data becomes more granular we start to see more seasonal patterns.
- We want to be able to decompose it into a trend and multiple seasonal components.
- In the next lecture we'll discuss multi-seasonal decomposition methods.



$$y_t = \hat{T}_t + \underbrace{\hat{S}_t^{(1)} + \hat{S}_t^{(2)} + \dots + \hat{S}_t^{(N)}}_{\text{Seasonal components}} + \hat{R}_t$$

Trend component
Residual component



# Summary

Time series can have multiple seasonal components (e.g., daily and weekly).

This can be driven by a range of factors from weather to human behaviour.

Need to use specific methods to decompose multi-seasonal time series.