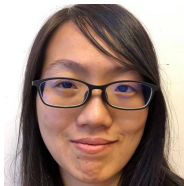


Discovering conflicting groups in signed networks

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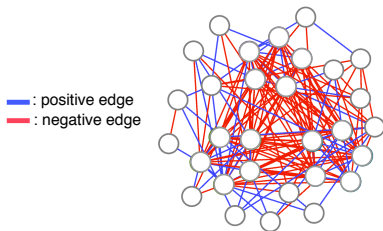
²Aalto University



34th Conference on Neural Information Processing Systems

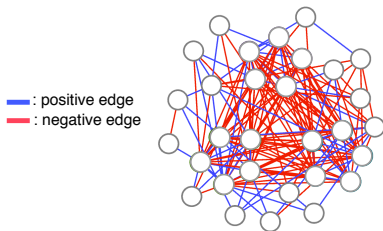
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- ▶ Given a signed network, e.g., social networks with edge sign indicating agree/disagree.



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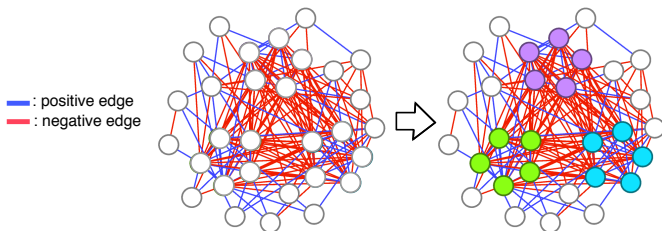
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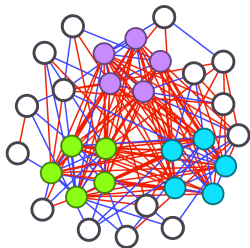
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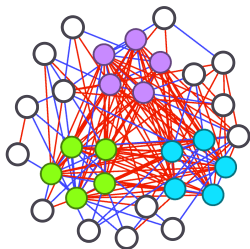
- ▶ People form into groups with likely-minded or common enemies.
- ▶ Our goal: find the conflicting groups with mostly + intra-group edges and mostly - inter-group edges.

Challenge: existence of neutral nodes



- ▶ Reason: e.g., not all people have strong opinions or firm stances.
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- ▶ Neutral nodes might behave differently to both the conflicting groups or to themselves.
- ▶ Methods partitioning the entire network such as signed clustering [4, 5] and correlation clustering [1] are not efficient.

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- ▶ **Our contribution:** a framework SCG so that each group S_j can be found by solving

$$x^* = \operatorname{argmax}_{x \in \{k-j, 0, -1\}^n} \frac{x^T A^{(j-1)} x}{x^T x}, \quad (1)$$

where $A^{(j-1)}$ is the adjacency matrix of the graph after removing $\cup_{h < j} S_h$.

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- ▶ The j -th group $S_j = \{i : x_i^* = k - j\}$.
- ▶ Nodes in other groups: $\{i : x_i^* = -1\}$.
- ▶ Neutral nodes: $\{i : x_i^* = 0\}$.

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- ▶ It is APX-hard [2] to solve Eq (1) for $k = 2$.
- ▶ **Our contribution:** approximation algorithms by rounding the leading eigenvector of $A^{(j-1)}$.

(Minimum Angle) competitive in practice but hard to be analyzed.

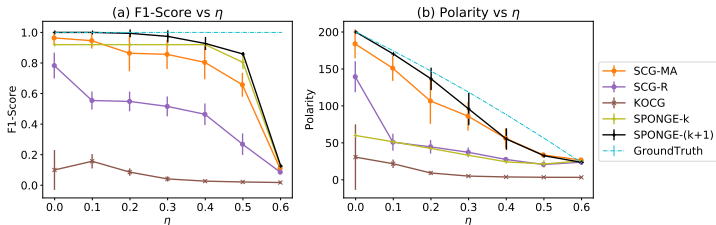
(Randomized) tight $\mathcal{O}(\sqrt{n})$ integrality gap when $k = 2$.

Experiment Results

► Real-world networks:

	Bitcoin	WikiVote	Referendum	Slashdot	WikiConflict	Epinions	Wikipolitics
$ V $	5881	7115	10884	82140	116717	131580	138587
$ E $	21492	100693	251406	500481	2026646	711210	715883
$ E_- / E $	0.2	0.2	0.1	0.2	0.6	0.2	0.1
SCG-MA	14.6	45.5	84.9	37.8	102.6	88.8	57.5
SCG-R	5.0	9.7	39.8	7.3	16.2	39.4	5.5
KOCG	4.4	5.5	8.8	2.6	4.5	8.7	4.8
SPONGE-k	5.0	15.8	41.5	—	—	—	—
SPONGE-(k+1)	0.8	1.0	1.0	—	—	—	—

► Synthetic:



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