

To smoothen out the data variability and differences in the three datasets and account for global outliers found, here is the recommendation on smoothing out the data:

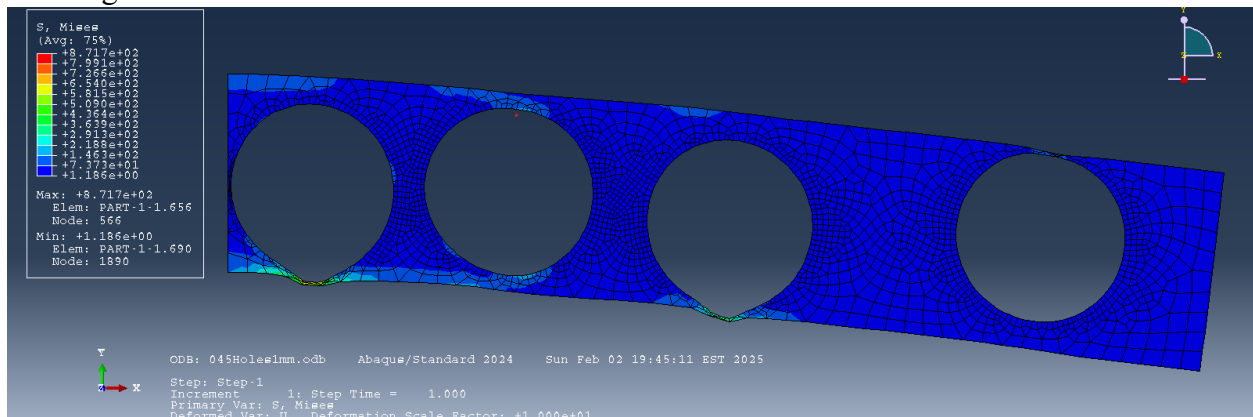
Units for Max Stress MPA						
Max stress at 1 mm cantilever end displacement				Max stress at 5 mm cantilever end displacement		
Volume Fraction	Holes	Mat A	Mat B	Holes	Mat A	Mat B
0.1	447.3	357		226	2236	1785
0.15	270.9	233.6		217.9	1355	1168
0.2	513.7	377.3		233.1	2568	1887
0.25	481.6	349.2		226.1	2408	1746
0.3	435.5	325.5		227.4	2178	1628
0.35	472.1	438		238.2	2361	1740
0.4	461.6	376.3		253.3	2308	1881
0.45	871.7	580.1		256	4358	2900
0.5	278.2	258.8		235.6	1391	1294
0.55	485.6	347.2		273.7	2428	1736
0.6	284.1	293		265.1	1421	1465
0.65	195.5	399		309	977.4	1995
0.7	455.4	415.5		313.8	2277	415.5
1.2357647 0.959243407 1.081596621 1.235474899 -0.104406797 1.084013971 SKEW						
Data Set 2						
Direction Down	Max stress at 1 mm cantilever end displacement			Max stress at 5 mm cantilever end displacement		
Volume Fraction	Holes	Mat A	Mat B	Holes	Mat A	Mat B
0.1	622.2448	382.41037		281.1238	3111.224	1912.052
0.15	338.8414	247.766159		270.4947	1694.207	1238.831
0.2	627.9702	421.764526		257.462	3139.851	2108.822
0.25	596.8199	400.048889		284.4005	2984.1	2000.244
0.3	344.0836	270.011566		280.1042	1720.418	1350.058
0.35	534.295	288.397522		278.4342	2671.475	1441.988
0.4	384.0533	270.313843		285.0964	1920.267	1351.569
0.45	562.757	403.45932		310.4611	2813.785	2017.297
0.5	425.7577	333.556854		305.1353	2128.788	1667.784
0.55	330.0016	340.363647		322.4433	1650.008	1701.818
0.6	411.0307	393.639832		322.5807	2055.154	1968.199
0.65	485.8028	451.577881		322.5977	2429.014	2257.889
0.7	436.1982	390.22345		328.4326	2180.991	1951.117
0.2216839 -0.3312122 0.025807323 0.22168399 -0.331212396 0.025807323 SKEW						
Data Set 1						
Direction Down	Max stress at 1 mm cantilever end displacement			Max stress at 5 mm cantilever end displacement		
Volume Fraction	Holes	Mat A	Mat B	Holes	Mat A	Mat B
0.1	347.613	310.234		291.05	1738.07	1551.17
0.15	359.08	256.346		293.229	1795.4	1281.73
0.2	454.594	247.325		299.539	2272.97	1236.63
0.25	305.303	282.48		296.22	1526.51	1412.4
0.3	337.884	272.717		308.474	1689.42	1363.58
0.35	589.65	343.193		308.453	2948.25	1715.37
0.4	520.482	334.245		302.148	2602.42	1671.22
0.45	532.067	286.829		315.039	2660.34	1434.15
0.5	396.119	394.028		313.111	1980.59	1970.14
0.55	377.361	294.543		325.115	1886.8	1472.21
0.6	208.163	405.615		333.695	1040.81	2028.08
0.65	212.252	387.345		327.577	1061.26	1936.73
0.7	162.654	458.921		359.343	813.269	2294.6
0.0739044 0.645456802 1.141165051 0.073908428 0.645613333 1.141212188 SKEW						

Units for Displacement mm						
Displacement at cantilever end at 100 N end load				Displacement at cantilever end at 500 N end load		
Volume Fraction	Holes	Mat A	Mat B	Holes	Mat A	Mat B
0.1	0.88	0.81	0.63	4.41	4.06	3.14
0.15	0.76	0.73	0.65	3.82	3.64	3.23
0.2	1.16	0.95	0.60	5.79	4.74	3.02
0.25	0.97	0.84	0.62	4.85	4.20	3.10
0.3	1.11	0.90	0.60	5.53	4.48	3.02
0.35	1.30	0.96	0.59	6.48	4.82	2.94
0.4	1.63	1.13	0.57	8.14	5.65	2.86
0.45	2.68	1.24	0.55	13.38	6.20	2.74
0.5	1.54	1.03	0.56	7.68	5.17	2.82
0.55	3.87	1.69	0.50	19.20	8.46	2.51
0.6	3.08	1.36	0.52	15.41	6.78	2.59
0.65	7.38	1.54	0.49	36.89	7.72	2.46
0.7	9.17	1.91	0.46	45.84	9.52	2.32
1.75944 0.8649346 -0.400895686 1.764110289 0.865435 -0.403095298 SKEW						
U Magnitude						
Displacement at cantilever end at 100 N end load				Displacement at cantilever end at 500 N end load		
Volume Fraction	Holes	Mat A	Mat B	Holes	Mat A	Mat B
0.1	0.97549	0.8118544	0.63321126	5.852968693	4.871127	3.79926753
0.15	0.77769	0.7183398	0.65866578	4.66616714	4.310039	3.95199466
0.2	1.01017	0.8148219	0.63839102	6.061004639	4.888932	3.83034611
0.25	1.20768	0.910269	0.62354016	7.246062279	5.461614	3.74124074
0.3	0.98537	0.8390453	0.62064612	5.912212372	5.034271	3.72387695
0.35	1.11887	0.877953	0.60921901	6.713216782	5.267718	3.65531397
0.4	1.21136	0.8696523	0.61592317	7.268157482	5.217913	3.695539
0.45	1.8259	1.2023917	0.55895829	10.95540524	7.21435	3.35374975
0.5	1.95962	1.1775166	0.55060107	11.7577076	7.0651	3.30360651
0.55	2.42762	1.2991489	0.54038113	14.56569672	7.794894	3.24226668
0.6	2.55957	1.4082384	0.51242006	15.35739136	8.44943	3.07452035
0.65	3.95264	1.5463021	0.49870613	23.71582222	9.277812	2.99223685
0.7	5.85599	1.6380326	0.49126866	35.13594055	9.828196	2.94761205
1.85157 0.6031756 -0.354720782 1.851567485 0.603176 -0.35472068 SKEW						
Displacement at cantilever end at 100 N end load				Displacement at cantilever end at 500 N end load		
Volume Fraction	Holes	Mat A	Mat B	Holes	Mat A	Mat B
0.1	-0.739	-0.735191	-0.63744	-3.6948	-3.67595	-3.1872
0.15	-0.8555	-0.723759	-0.63121	-4.27761	-3.61879	-3.15605
0.2	-0.8488	-0.750971	-0.61675	-4.24409	-3.75458	-3.08375
0.25	-0.8525	-0.774226	-0.614885	-4.26225	-3.87113	-3.07442
0.3	-0.9859	-0.833196	-0.596528	-4.92966	-4.16598	-2.98264
0.35	-1.2457	-0.899816	-0.592495	-6.22836	-4.49908	-2.96247
0.4	-1.4191	-0.977682	-0.575703	-7.09561	-4.88841	-2.87851
0.45	-1.6689	-0.9663	-0.577702	-8.34452	-4.8315	-2.88851
0.5	-2.1589	-1.10828	-0.558918	-10.7947	-5.54139	-2.79459
0.55	-2.7256	-1.19047	-0.535038	-13.628	-5.95235	-2.67519
0.6	-9.344	-1.35998	-0.507666	-46.7202	-6.7999	-2.53833
0.65	-16.488	-1.40595	-0.509413	-82.4393	-7.02977	-2.54706
0.7	-233.19	-1.55324	-0.474383	-1165.93	-7.76622	-2.37192
-3.5736 -0.708228 0.545881746 -3.573627059 -0.7082 0.5458864249 SKEW						

Given the skewness in the data (ranging from -3.57 to 1.76), the Box-Cox transformation can be an appropriate method to normalize the data and make it more suitable for analysis. This transformation is effective when data is positively skewed, as it helps to reduce skewness and achieve a normal distribution. Since the outlier appears to be caused by a physical effect influencing structural behavior, it would be important to perform the transformation both with and without the outlier. If the Box-Cox transformation is heavily distorted by this outlier, alternative transformations like the Yeo-Johnson or log transformation could be explored to see if they yield better results.

After applying the Box-Cox transformation, if successful in normalizing the skewed data, Kernel Density Estimation (KDE) could be used to smooth the distribution further. This technique can help visualize the underlying distribution and address any irregularities in the data that might not be immediately apparent from histograms.

Another key observation from scatter plots is that the primary deviation between my data and the provided datasets is due to a hole positioned too close to the beam's edge. This resulted in unrealistic deformation/resulting in unrealistic stress concentration in ABAQUS, which is unlikely to occur in a real-life scenario. In this case, removing the corresponding data point might be justified, as it appears to be an artifact of the simulation setup rather than a physically meaningful result.



Additionally, comparing different simulation runs, for example, those with and without voids, and Material A versus Material B—requires a fair comparison of stress and displacement results. Standardization is a useful approach here, as it eliminates differences in units and scales. This ensures that variations, such as changes in hole placement, can be analyzed more effectively without being influenced by differences in magnitude or units.