

Listing 1 "Nadaraya Watson Estimator of rectangular kernel."

```

1  import numpy as np
2  import scipy.stats as stats
3  import matplotlib.pyplot as plt
4
5  from matplotlib import rc
6
7  rc('text', usetex=True)
8
9  def Nadaraya_Watson(x, Xi, Yi, h):
10     k = []
11     nw = 0
12     for (x_i, y_i) in zip(Xi, Yi):
13         u = ( x_i - x ) / h
14         k_u = Rect(u)
15
16         nw += y_i * k_u
17         k.append(k_u)
18
19     s = sum(k)
20
21     if s == 0:
22         return 0
23     else:
24         return nw / s
25
26  def Rect(u):
27     if( abs(u) <= 1 ):
28         return 0.5
29     else:
30         return 0
31
32  def f(x):
33     return 2 * x * x - x + 3
34
35  def AddNoise(x):
36     xi = stats.norm.rvs(loc=0, scale = 0.3, size=x.size, random_state=0)
37     return x + xi
38
39  def Example_1_2(Xi, Yi, f_x, h, ax):
40     fn_nw = []
41     for _x in Xi:
42         fn_nw.append(Nadaraya_Watson(_x, Xi, Yi, h))
43
44     ax.plot(Xi, Yi, 'b+')
45     ax.plot(Xi, f_x, 'k--')
46     ax.plot(Xi, fn_nw, 'r_')
47
48     ax.set_title('h={0:.2f}'.format(h))
49     ax.set_xlabel('x', fontsize=13)
50     ax.set_ylabel('y', fontsize=13)
51
52  def main():
53
54     sz = 100
55     x = np.linspace(start=-1, stop=2.1, num = sz)
56
57     f_x = f(x)
58     y = AddNoise(f_x)
59
60     fig, ax = plt.subplots(2, 2, sharex="col", sharey="row")
61
62     Example_1_2(x, y, f_x, 5, ax[0,0])
63     Example_1_2(x, y, f_x, 1, ax[0,1])
64     Example_1_2(x, y, f_x, 0.1, ax[1,0])
65     Example_1_2(x, y, f_x, 0.01, ax[1,1])
66
67     fig.suptitle(r'$Y_{i_{\omega}} = (2X_{i_{\omega}}^2 - X_{i_{\omega}} + 3)_{\omega} + \xi_{i_{\omega}} \sim \text{quad}_{\omega} \xi_{i_{\omega}} \sim N(0, 0.3^2)_{\omega} (i_{\omega} = 1, \dots, 100)$', fontsize
68                 =16)
69
70     plt.show()
71
72  if __name__ == "__main__":
73     main()

```