LAB3_Part1_TeacherUse_Hideki_v1.

February 8, 2021

1 Linear Regression with Health Datasets

Datasets: from kaggles https://www.kaggle.com/nareshbhat/health-care-data-set-on-heart-attack-possibility?select=heart.csv

Objective: Trying to figure out the correlation between choosing variables.

Plan: choose continuous values: age, trestbps, chol, thalach, oldpeak. Ignore other variables since they're binary

1.1 1. Import libraries

[1]:
```
import matplotlib.pyplot as plt
import pandas as pd
import numpy as np
import seaborn as sns
```

1.2 2. Import excel data file into pandas data frame

Data Info:

`Attribute Information`

1) age
2) sex
3) cp = chest pain type (4 values)
4) trestbps = resting blood pressure
5) chol = serum cholestoral in mg/dl
6) fbs = fasting blood sugar > 120 mg/dl
7) restecg = resting electrocardiographic results (values 0,1,2)
8) thalach = maximum heart rate achieved

9) exang = exercise induced angina

10) oldpeak = ST depression induced by exercise relative to rest

11) slope = the slope of the peak exercise ST segment

12) ca = number of major vessels (0-3) colored by flourosopy

13) thal: 0 = normal; 1 = fixed defect; 2 = reversable defect

14) target: 0= less chance of heart attack 1= more chance of heart attack

[2]:
```
df = pd.read_csv("health2.csv")
```

[3]:
```
# to check dataframe, use display()
display(df)
```

```
     age  sex  cp  trestbps  chol  fbs  restecg  thalach  exang  oldpeak  \
0     63    1   3       145   233    1        0      150      0      2.3
1     37    1   2       130   250    0        1      187      0      3.5
2     41    0   1       130   204    0        0      172      0      1.4
3     56    1   1       120   236    0        1      178      0      0.8
4     57    0   0       120   354    0        1      163      1      0.6
..   ...  ...  ..       ...   ...  ...      ...      ...    ...      ...
298   57    0   0       140   241    0        1      123      1      0.2
299   45    1   3       110   264    0        1      132      0      1.2
300   68    1   0       144   193    1        1      141      0      3.4
301   57    1   0       130   131    0        1      115      1      1.2
302   57    0   1       130   236    0        0      174      0      0.0

     slope  ca  thal  target
0        0   0     1       1
1        0   0     2       1
2        2   0     2       1
3        2   0     2       1
4        2   0     2       1
..     ...  ..   ...     ...
298      1   0     3       0
299      1   0     3       0
300      1   2     3       0
301      1   1     3       0
302      1   1     2       0

[303 rows x 14 columns]
```

1.3 Data Cleaning

There might be a possiblity that the data is missing its values. use "print(df.isnull().sum))" to check if the data is ready to be processed.

[4]:
```
print(df.isnull().sum())
```

```
age         0
sex         0
cp          0
trestbps    0
chol        0
fbs         0
restecg     0
thalach     0
exang       0
oldpeak     0
slope       0
ca          0
thal        0
target      0
dtype: int64
```

1.4 Technique to fill Nan if data is missing its value

1.5 Won't need to use in this notebook since the dataset is perfect

#Fill NaN with ' '
df['col'] = df['col'].fillna(' ')
#Fill NaN with 99
df['col'] = df['col'].fillna(99)
#Fill NaN with the mean of the column
df['col'] = df['col'].fillna(df['col'].mean())

1.6 Feature Selection

Now that the data is good to go, we are ready to move on to the next step of the process. As there are 14 features in the dataset, we do not want to use all of these features for training our model, because not all of them are relevant. Instead, we want to choose those features that directly influence the result (that is, prices of houses) to train the model. For this, we can use the corr() function. The corr() function computes the pairwise correlation of columns:

[5]:
```
corr = df.corr()
display(corr)
```

```
              age       sex        cp  trestbps      chol       fbs  \
age       1.000000 -0.098447 -0.068653  0.279351  0.213678  0.121308
sex      -0.098447  1.000000 -0.049353 -0.056769 -0.197912  0.045032
cp       -0.068653 -0.049353  1.000000  0.047608 -0.076904  0.094444
trestbps  0.279351 -0.056769  0.047608  1.000000  0.123174  0.177531
chol      0.213678 -0.197912 -0.076904  0.123174  1.000000  0.013294
fbs       0.121308  0.045032  0.094444  0.177531  0.013294  1.000000
```

```
restecg  -0.116211 -0.058196  0.044421 -0.114103 -0.151040 -0.084189
thalach  -0.398522 -0.044020  0.295762 -0.046698 -0.009940 -0.008567
exang     0.096801  0.141664 -0.394280  0.067616  0.067023  0.025665
oldpeak   0.210013  0.096093 -0.149230  0.193216  0.053952  0.005747
slope    -0.168814 -0.030711  0.119717 -0.121475 -0.004038 -0.059894
ca        0.276326  0.118261 -0.181053  0.101389  0.070511  0.137979
thal      0.068001  0.210041 -0.161736  0.062210  0.098803 -0.032019
target   -0.225439 -0.280937  0.433798 -0.144931 -0.085239 -0.028046

           restecg   thalach     exang   oldpeak     slope        ca  \
age      -0.116211 -0.398522  0.096801  0.210013 -0.168814  0.276326
sex      -0.058196 -0.044020  0.141664  0.096093 -0.030711  0.118261
cp        0.044421  0.295762 -0.394280 -0.149230  0.119717 -0.181053
trestbps -0.114103 -0.046698  0.067616  0.193216 -0.121475  0.101389
chol     -0.151040 -0.009940  0.067023  0.053952 -0.004038  0.070511
fbs      -0.084189 -0.008567  0.025665  0.005747 -0.059894  0.137979
restecg   1.000000  0.044123 -0.070733 -0.058770  0.093045 -0.072042
thalach   0.044123  1.000000 -0.378812 -0.344187  0.386784 -0.213177
exang    -0.070733 -0.378812  1.000000  0.288223 -0.257748  0.115739
oldpeak  -0.058770 -0.344187  0.288223  1.000000 -0.577537  0.222682
slope     0.093045  0.386784 -0.257748 -0.577537  1.000000 -0.080155
ca       -0.072042 -0.213177  0.115739  0.222682 -0.080155  1.000000
thal     -0.011981 -0.096439  0.206754  0.210244 -0.104764  0.151832
target    0.137230  0.421741 -0.436757 -0.430696  0.345877 -0.391724

              thal    target
age       0.068001 -0.225439
sex       0.210041 -0.280937
cp       -0.161736  0.433798
trestbps  0.062210 -0.144931
chol      0.098803 -0.085239
fbs      -0.032019 -0.028046
restecg  -0.011981  0.137230
thalach  -0.096439  0.421741
exang     0.206754 -0.436757
oldpeak   0.210244 -0.430696
slope    -0.104764  0.345877
ca        0.151832 -0.391724
thal      1.000000 -0.344029
target   -0.344029  1.000000
```

1.7 Choose one independent variable for looking for its correlation with other variables

[6]:
```
#---get the top 3 features that has the highest correlation---
#select "Age" to see which variables has a strong correlation with age.

print(df.corr().abs().nlargest(3, 'age').index)

#---print the top 3 correlation values---
print(df.corr().abs().nlargest(3, 'age').values[:,13])
```

```
Index(['age', 'thalach', 'trestbps'], dtype='object')
[0.22543872 0.42174093 0.14493113]
```

1.8 This is testing for looking for a best correlation values.

1.8.1 In this data, I found that [age], [thalach], [taget] has a high value

*** Target is exception for now in this practice notebook ***

[7]:
```
#---get the top 3 features that has the highest correlation---
#select "chol" to see which variables has a strong correlation with serum␣
 ↪cholestoral.

print(df.corr().abs().nlargest(5, 'thalach').index)

#---print the top 3 correlation values---
print(df.corr().abs().nlargest(5, 'thalach').values[:,13])
```

```
Index(['thalach', 'target', 'age', 'slope', 'exang'], dtype='object')
[0.42174093 1.         0.22543872 0.34587708 0.43675708]
```

[8]:
```
%matplotlib inline
plt.figure(figsize=(20,5))
plt.scatter(df['age'], df['thalach'], marker='*')
plt.xlabel('age')
plt.ylabel('thalach')
```

[8]:
```
Text(0, 0.5, 'thalach')
```

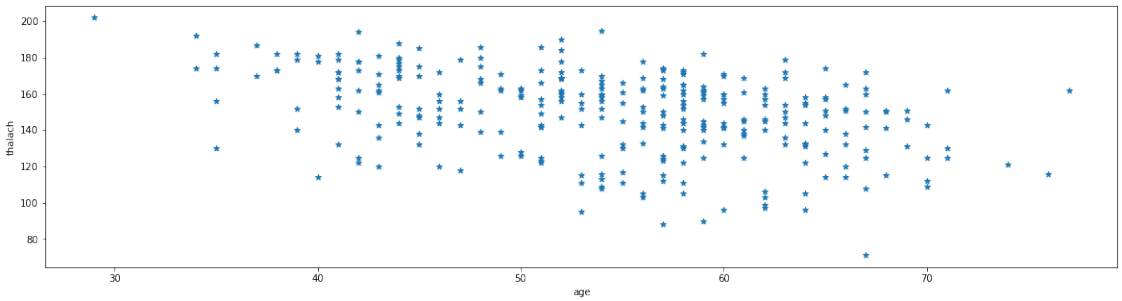


fig1: Scatter plot showing the relationship between “age” and “thalach”

[9]:
```
sns.regplot(df['age'], df['thalach'], ci=None)
```

[9]:
```
<matplotlib.axes._subplots.AxesSubplot at 0x7fa41db36760>
```

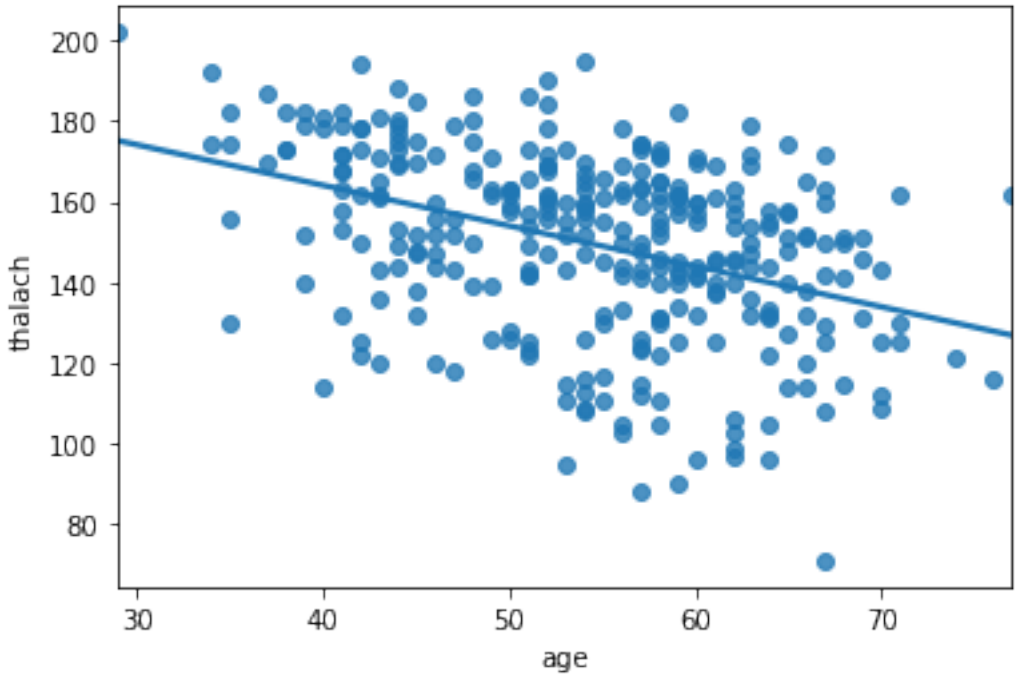


fig1.1: using seaborn to make it more clear in linear regression line

[10]:
```
sns.regplot(df['age'],df['trestbps'], ci=None)
```

[10]:
```
<matplotlib.axes._subplots.AxesSubplot at 0x7fa41dd20340>
```

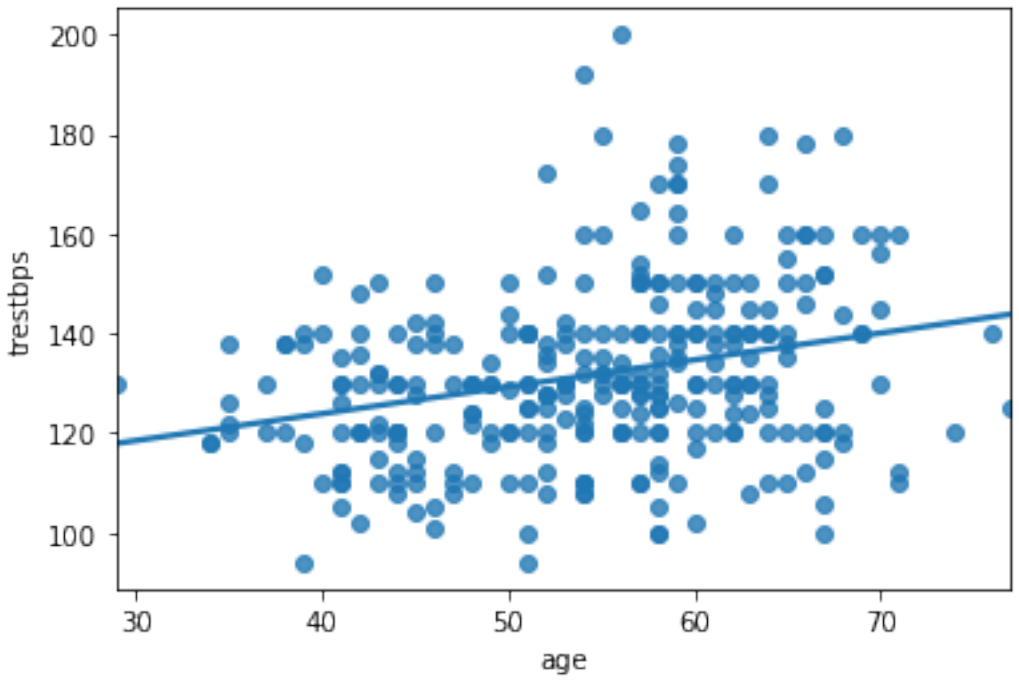


fig2: Scatter plot showing the relationship between “age” and “trestbps”

[11]:
```
sns.regplot(df['age'],df['chol'], ci=None)
```

[11]:
```
<matplotlib.axes._subplots.AxesSubplot at 0x7fa41dde53d0>
```

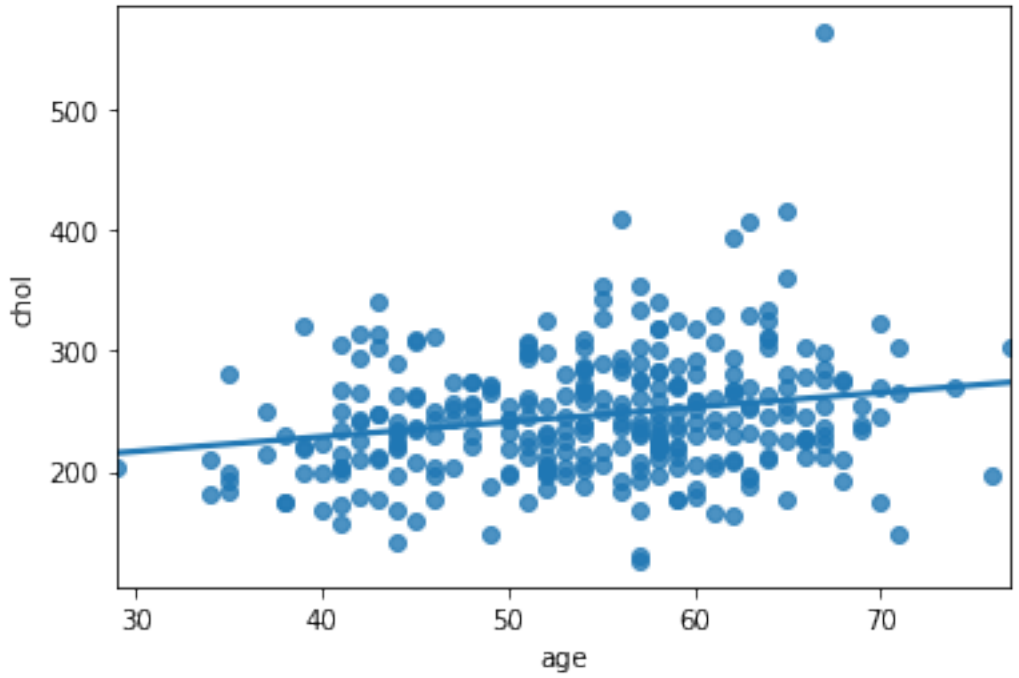


fig3: Scatter plot showing the relationship between “age” and “chol”

[12]:
```
from mpl_toolkits.mplot3d import Axes3D

fig = plt.figure(figsize=(18,15))
ax = fig.add_subplot(111, projection='3d')

ax.scatter(df['trestbps'],
                    df['thalach'],
                    df['age'],
                    c='b')

ax.set_xlabel("trestbps")
ax.set_ylabel("thalach")
ax.set_zlabel("age")
plt.show()
```

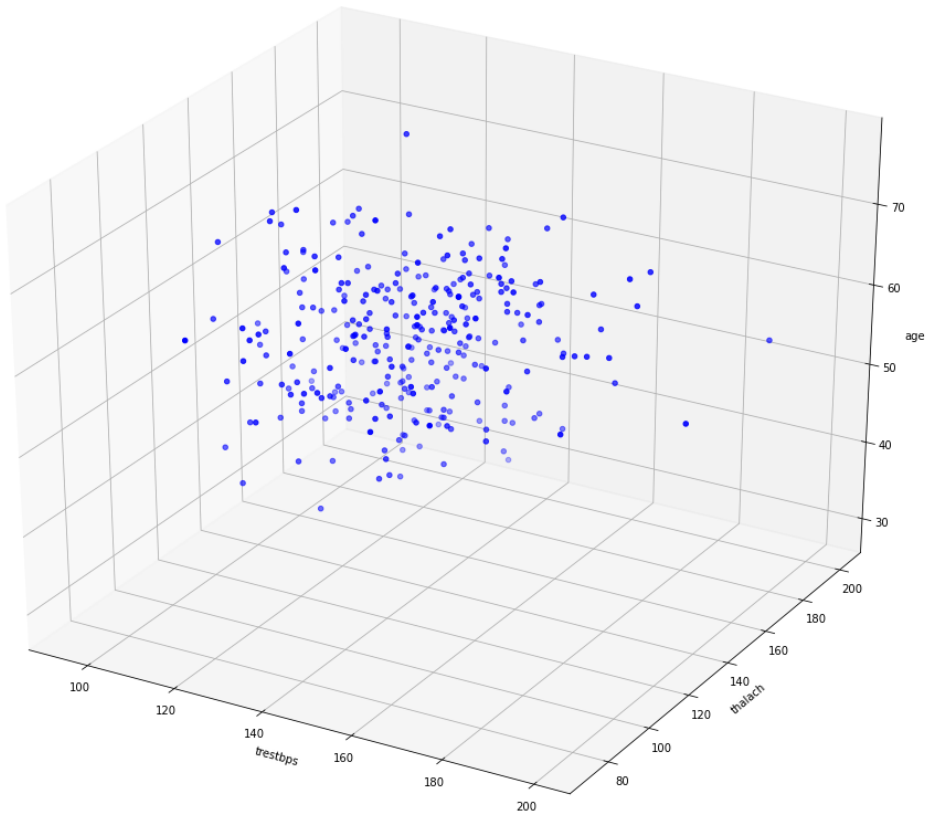


Figure4: shows the 3D chart of trestbps and thalach plotted against age.

1.9 Training the Model

We can now train the model. First, create two DataFrames: x and Y. The x DataFrame will contain the combination of the thalach and trestbps features, while the Y DataFrame will contain the age label:

[107]:
```
x = pd.DataFrame(np.c_[df['thalach']], columns = ['thalach'])
Y = df['age']
```

We will split the dataset into 70 percent for training and 30 percent for testing:

[108]:
```
from sklearn.model_selection import train_test_split
x_train, x_test, Y_train, Y_test = train_test_split(x, Y, test_size = 0.
 ↪3,random_state=5)
```

[109]:
```
# Print out the shape of the training sets:
print(x_train.shape)
print(Y_train.shape)
```

```
(212, 1)
(212,)
```

[110]:
```
# Print out the shape of the testing set
print(x_test.shape)
print(Y_test.shape)
```

```
(91, 1)
(91,)
```

[111]:
```
# Perform Linear Regression
from sklearn.linear_model import LinearRegression

model = LinearRegression()
model.fit(x_train, Y_train)
```

[111]:
```
LinearRegression()
```

Once the model is trained, we will use the testing set to perform some predictions:

[112]:
```
age_pred = model.predict(x_test)
```

To learn how well our model performed, we use the R-Squared method that you learned in the previous chapter. The R-Squared method lets you know how close the test data fits the regression line. A value of 1.0 means a perfect fit. So, you aim for a value of R-Squared that is close to 1:

[113]:
```
print('R-Squared: %.4f' % model.score(x_test,Y_test))
```

```
R-Squared: 0.1143
```

2 Issues: R-Squared is lower than acceptance line (>80%)

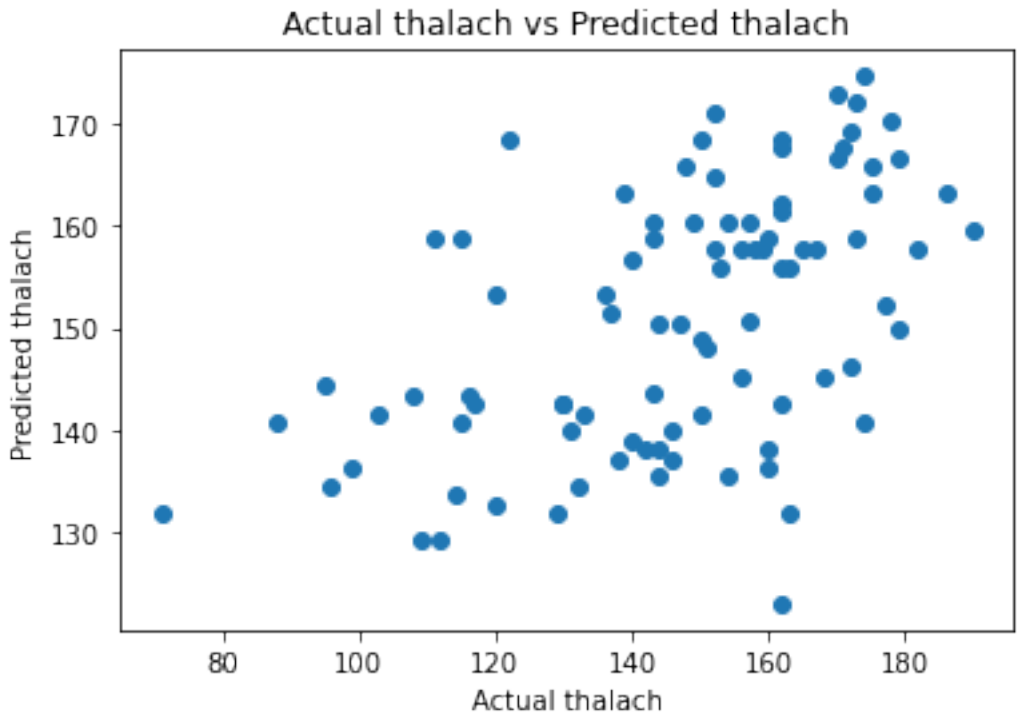
[20]:
```
from sklearn.metrics import mean_squared_error

mse = mean_squared_error(Y_test, age_pred)
print(mse)

plt.scatter(Y_test, age_pred)
plt.xlabel("Actual thalach")
plt.ylabel("Predicted thalach")
plt.title("Actual thalach vs Predicted thalach")
```

```
447.0611138492073
```

[20]:
```
Text(0.5, 1.0, 'Actual thalach vs Predicted thalach')
```



2.0.1 Getting the Intercept and Coefficients

[21]:
```
print(model.intercept_)
print(model.coef_)
```

```
191.26422222062155
[-0.88572785 14.31158955]
```

[ ]:

[22]:
```
# polynomial_task if that improve the accuracy in tthe model/
```

2.1 Polynomial Regression

In the previous section, you saw how to apply linear regression to predict the prices of houses in the Boston area. While the result is somewhat acceptable, it is not very accurate. This is because sometimes a linear regression line might not be the best solution to capture the relationships between the features and label accurately. In some cases, a curved line might do better.

[23]:
```
display(df)
```

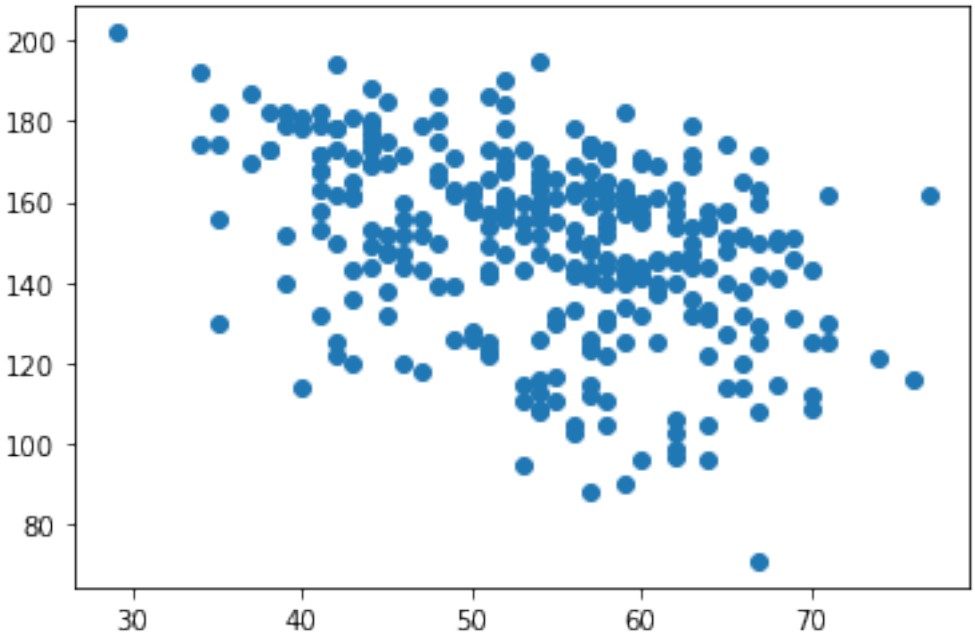
```
     age  sex  cp  trestbps  chol  fbs  restecg  thalach  exang  oldpeak  \
0     63    1   3       145   233    1        0      150      0      2.3
1     37    1   2       130   250    0        1      187      0      3.5
2     41    0   1       130   204    0        0      172      0      1.4
3     56    1   1       120   236    0        1      178      0      0.8
4     57    0   0       120   354    0        1      163      1      0.6
..   ...  ...  ..       ...   ...  ...      ...      ...    ...      ...
298   57    0   0       140   241    0        1      123      1      0.2
299   45    1   3       110   264    0        1      132      0      1.2
300   68    1   0       144   193    1        1      141      0      3.4
301   57    1   0       130   131    0        1      115      1      1.2
302   57    0   1       130   236    0        0      174      0      0.0

     slope  ca  thal  target
0        0   0     1       1
1        0   0     2       1
2        2   0     2       1
3        2   0     2       1
4        2   0     2       1
..     ...  ..   ...     ...
298      1   0     3       0
299      1   0     3       0
300      1   2     3       0
301      1   1     3       0
302      1   1     2       0

[303 rows x 14 columns]
```

[24]:
```
plt.scatter(df['age'],df['thalach'])
```

[24]:
```
<matplotlib.collections.PathCollection at 0x7fa41fe33f70>
```



Using linear regression, you can try to plot a straight line cutting through most of the points:

[51]:
```
model = LinearRegression()

x = df['age'][0:302, np.newaxis] #--- convert to 2D array
y = df['thalach'][0:302, np.newaxis] #---convert to 2D array

model.fit(x,y)
```

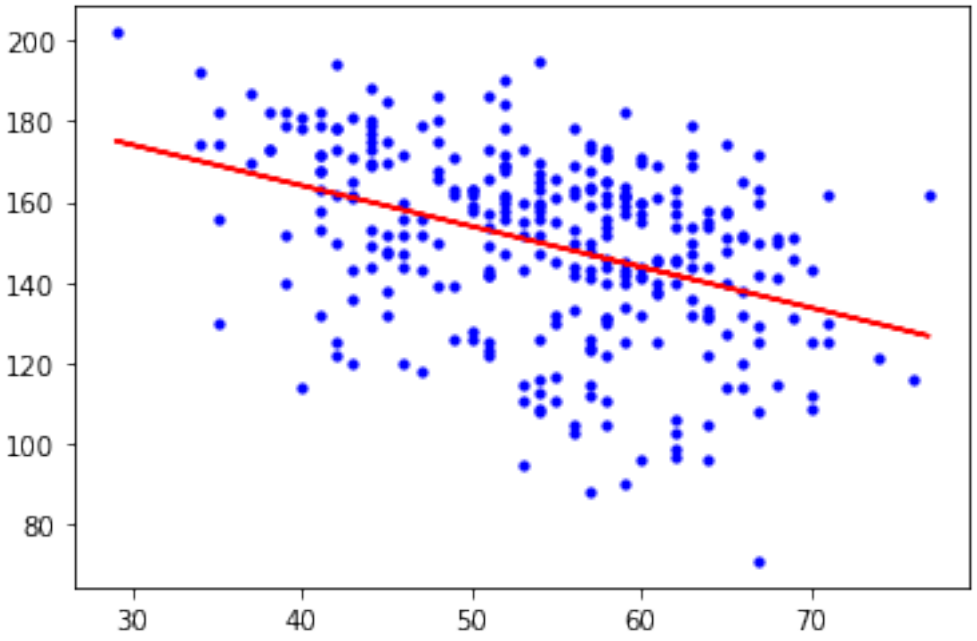
[51]:
```
LinearRegression()
```

[52]:
```
# ---perform prediction
y_pred = model.predict(x)

#---plot the training points---
plt.scatter(x,y, s=10, color='b')

#---plot the straight line---
plt.plot(x, y_pred, color='r')
plt.show()

#---calculate R-Squared---
print('R-Squared for training set: %.4f' % model.score(x,y))
```




```
R-Squared for training set: 0.1603
```

2.2 Polynomial Regression in Scikit-learn

[75]:
```
from sklearn.preprocessing import PolynomialFeatures
degree = 2
polynomial_features = PolynomialFeatures(degree = degree)

x_poly = polynomial_features.fit_transform(x)
print(x_poly)
```

```
[[1.000e+00 6.300e+01 3.969e+03]
 [1.000e+00 3.700e+01 1.369e+03]
 [1.000e+00 4.100e+01 1.681e+03]
 [1.000e+00 5.600e+01 3.136e+03]
 [1.000e+00 5.700e+01 3.249e+03]
 [1.000e+00 5.700e+01 3.249e+03]
 [1.000e+00 5.600e+01 3.136e+03]
 [1.000e+00 4.400e+01 1.936e+03]
 [1.000e+00 5.200e+01 2.704e+03]
 [1.000e+00 5.700e+01 3.249e+03]
 [1.000e+00 5.400e+01 2.916e+03]
 [1.000e+00 4.800e+01 2.304e+03]
 [1.000e+00 4.900e+01 2.401e+03]
 [1.000e+00 6.400e+01 4.096e+03]
 [1.000e+00 5.800e+01 3.364e+03]
```

```
[1.000e+00 5.000e+01 2.500e+03]
[1.000e+00 5.800e+01 3.364e+03]
[1.000e+00 6.600e+01 4.356e+03]
[1.000e+00 4.300e+01 1.849e+03]
[1.000e+00 6.900e+01 4.761e+03]
[1.000e+00 5.900e+01 3.481e+03]
[1.000e+00 4.400e+01 1.936e+03]
[1.000e+00 4.200e+01 1.764e+03]
[1.000e+00 6.100e+01 3.721e+03]
[1.000e+00 4.000e+01 1.600e+03]
[1.000e+00 7.100e+01 5.041e+03]
[1.000e+00 5.900e+01 3.481e+03]
[1.000e+00 5.100e+01 2.601e+03]
[1.000e+00 6.500e+01 4.225e+03]
[1.000e+00 5.300e+01 2.809e+03]
[1.000e+00 4.100e+01 1.681e+03]
[1.000e+00 6.500e+01 4.225e+03]
[1.000e+00 4.400e+01 1.936e+03]
[1.000e+00 5.400e+01 2.916e+03]
[1.000e+00 5.100e+01 2.601e+03]
[1.000e+00 4.600e+01 2.116e+03]
[1.000e+00 5.400e+01 2.916e+03]
[1.000e+00 5.400e+01 2.916e+03]
[1.000e+00 6.500e+01 4.225e+03]
[1.000e+00 6.500e+01 4.225e+03]
[1.000e+00 5.100e+01 2.601e+03]
[1.000e+00 4.800e+01 2.304e+03]
[1.000e+00 4.500e+01 2.025e+03]
[1.000e+00 5.300e+01 2.809e+03]
[1.000e+00 3.900e+01 1.521e+03]
[1.000e+00 5.200e+01 2.704e+03]
[1.000e+00 4.400e+01 1.936e+03]
[1.000e+00 4.700e+01 2.209e+03]
[1.000e+00 5.300e+01 2.809e+03]
[1.000e+00 5.300e+01 2.809e+03]
[1.000e+00 5.100e+01 2.601e+03]
[1.000e+00 6.600e+01 4.356e+03]
[1.000e+00 6.200e+01 3.844e+03]
[1.000e+00 4.400e+01 1.936e+03]
[1.000e+00 6.300e+01 3.969e+03]
[1.000e+00 5.200e+01 2.704e+03]
[1.000e+00 4.800e+01 2.304e+03]
[1.000e+00 4.500e+01 2.025e+03]
[1.000e+00 3.400e+01 1.156e+03]
[1.000e+00 5.700e+01 3.249e+03]
[1.000e+00 7.100e+01 5.041e+03]
[1.000e+00 5.400e+01 2.916e+03]
[1.000e+00 5.200e+01 2.704e+03]
```

```
[1.000e+00 4.100e+01 1.681e+03]
[1.000e+00 5.800e+01 3.364e+03]
[1.000e+00 3.500e+01 1.225e+03]
[1.000e+00 5.100e+01 2.601e+03]
[1.000e+00 4.500e+01 2.025e+03]
[1.000e+00 4.400e+01 1.936e+03]
[1.000e+00 6.200e+01 3.844e+03]
[1.000e+00 5.400e+01 2.916e+03]
[1.000e+00 5.100e+01 2.601e+03]
[1.000e+00 2.900e+01 8.410e+02]
[1.000e+00 5.100e+01 2.601e+03]
[1.000e+00 4.300e+01 1.849e+03]
[1.000e+00 5.500e+01 3.025e+03]
[1.000e+00 5.100e+01 2.601e+03]
[1.000e+00 5.900e+01 3.481e+03]
[1.000e+00 5.200e+01 2.704e+03]
[1.000e+00 5.800e+01 3.364e+03]
[1.000e+00 4.100e+01 1.681e+03]
[1.000e+00 4.500e+01 2.025e+03]
[1.000e+00 6.000e+01 3.600e+03]
[1.000e+00 5.200e+01 2.704e+03]
[1.000e+00 4.200e+01 1.764e+03]
[1.000e+00 6.700e+01 4.489e+03]
[1.000e+00 6.800e+01 4.624e+03]
[1.000e+00 4.600e+01 2.116e+03]
[1.000e+00 5.400e+01 2.916e+03]
[1.000e+00 5.800e+01 3.364e+03]
[1.000e+00 4.800e+01 2.304e+03]
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[1.000e+00 5.400e+01 2.916e+03]
[1.000e+00 4.500e+01 2.025e+03]
[1.000e+00 5.300e+01 2.809e+03]
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[1.000e+00 6.800e+01 4.624e+03]
[1.000e+00 6.900e+01 4.761e+03]
[1.000e+00 4.500e+01 2.025e+03]
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[1.000e+00 6.400e+01 4.096e+03]
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[1.000e+00 6.400e+01 4.096e+03]
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[1.000e+00 5.500e+01 3.025e+03]
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[1.000e+00 4.600e+01 2.116e+03]
[1.000e+00 6.400e+01 4.096e+03]
[1.000e+00 5.900e+01 3.481e+03]
[1.000e+00 4.100e+01 1.681e+03]
[1.000e+00 5.400e+01 2.916e+03]
[1.000e+00 3.900e+01 1.521e+03]
[1.000e+00 3.400e+01 1.156e+03]
[1.000e+00 4.700e+01 2.209e+03]
[1.000e+00 6.700e+01 4.489e+03]
[1.000e+00 5.200e+01 2.704e+03]
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[1.000e+00 5.400e+01 2.916e+03]
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[1.000e+00 4.100e+01 1.681e+03]
[1.000e+00 4.100e+01 1.681e+03]
[1.000e+00 4.900e+01 2.401e+03]
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[1.000e+00 6.600e+01 4.356e+03]
[1.000e+00 7.100e+01 5.041e+03]
[1.000e+00 6.400e+01 4.096e+03]
[1.000e+00 6.600e+01 4.356e+03]
[1.000e+00 3.900e+01 1.521e+03]
[1.000e+00 5.800e+01 3.364e+03]
[1.000e+00 4.700e+01 2.209e+03]
[1.000e+00 3.500e+01 1.225e+03]
[1.000e+00 5.800e+01 3.364e+03]
```

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[1.000e+00 5.600e+01 3.136e+03]
[1.000e+00 5.600e+01 3.136e+03]
[1.000e+00 5.500e+01 3.025e+03]
[1.000e+00 4.100e+01 1.681e+03]
[1.000e+00 3.800e+01 1.444e+03]
[1.000e+00 3.800e+01 1.444e+03]
[1.000e+00 6.700e+01 4.489e+03]
[1.000e+00 6.700e+01 4.489e+03]
[1.000e+00 6.200e+01 3.844e+03]
[1.000e+00 6.300e+01 3.969e+03]
[1.000e+00 5.300e+01 2.809e+03]
[1.000e+00 5.600e+01 3.136e+03]
[1.000e+00 4.800e+01 2.304e+03]
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[1.000e+00 5.800e+01 3.364e+03]
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[1.000e+00 6.000e+01 3.600e+03]
[1.000e+00 6.400e+01 4.096e+03]
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[1.000e+00 6.100e+01 3.721e+03]
[1.000e+00 5.800e+01 3.364e+03]
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[1.000e+00 4.400e+01 1.936e+03]
[1.000e+00 6.000e+01 3.600e+03]
[1.000e+00 5.400e+01 2.916e+03]
[1.000e+00 5.000e+01 2.500e+03]
[1.000e+00 4.100e+01 1.681e+03]
[1.000e+00 5.100e+01 2.601e+03]
[1.000e+00 5.800e+01 3.364e+03]
[1.000e+00 5.400e+01 2.916e+03]
[1.000e+00 6.000e+01 3.600e+03]
[1.000e+00 6.000e+01 3.600e+03]
[1.000e+00 5.900e+01 3.481e+03]
[1.000e+00 4.600e+01 2.116e+03]
[1.000e+00 6.700e+01 4.489e+03]
[1.000e+00 6.200e+01 3.844e+03]
[1.000e+00 6.500e+01 4.225e+03]
[1.000e+00 4.400e+01 1.936e+03]
[1.000e+00 6.000e+01 3.600e+03]
[1.000e+00 5.800e+01 3.364e+03]
[1.000e+00 6.800e+01 4.624e+03]
[1.000e+00 6.200e+01 3.844e+03]
[1.000e+00 5.200e+01 2.704e+03]
[1.000e+00 5.900e+01 3.481e+03]
```

```
[1.000e+00 6.000e+01 3.600e+03]
[1.000e+00 4.900e+01 2.401e+03]
[1.000e+00 5.900e+01 3.481e+03]
[1.000e+00 5.700e+01 3.249e+03]
[1.000e+00 6.100e+01 3.721e+03]
[1.000e+00 3.900e+01 1.521e+03]
[1.000e+00 6.100e+01 3.721e+03]
[1.000e+00 5.600e+01 3.136e+03]
[1.000e+00 4.300e+01 1.849e+03]
[1.000e+00 6.200e+01 3.844e+03]
[1.000e+00 6.300e+01 3.969e+03]
[1.000e+00 6.500e+01 4.225e+03]
[1.000e+00 4.800e+01 2.304e+03]
[1.000e+00 6.300e+01 3.969e+03]
[1.000e+00 5.500e+01 3.025e+03]
[1.000e+00 6.500e+01 4.225e+03]
[1.000e+00 5.600e+01 3.136e+03]
[1.000e+00 5.400e+01 2.916e+03]
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[1.000e+00 5.700e+01 3.249e+03]
[1.000e+00 5.500e+01 3.025e+03]
[1.000e+00 6.400e+01 4.096e+03]
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[1.000e+00 5.100e+01 2.601e+03]
[1.000e+00 5.800e+01 3.364e+03]
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[1.000e+00 3.500e+01 1.225e+03]
[1.000e+00 7.000e+01 4.900e+03]
[1.000e+00 5.900e+01 3.481e+03]
[1.000e+00 6.400e+01 4.096e+03]
[1.000e+00 5.700e+01 3.249e+03]
[1.000e+00 5.600e+01 3.136e+03]
[1.000e+00 4.800e+01 2.304e+03]
[1.000e+00 5.600e+01 3.136e+03]
[1.000e+00 6.600e+01 4.356e+03]
[1.000e+00 5.400e+01 2.916e+03]
[1.000e+00 6.900e+01 4.761e+03]
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[1.000e+00 4.300e+01 1.849e+03]
[1.000e+00 6.200e+01 3.844e+03]
[1.000e+00 6.700e+01 4.489e+03]
[1.000e+00 5.900e+01 3.481e+03]
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```
[1.000e+00 4.500e+01 2.025e+03]
[1.000e+00 5.800e+01 3.364e+03]
[1.000e+00 5.000e+01 2.500e+03]
[1.000e+00 6.200e+01 3.844e+03]
[1.000e+00 3.800e+01 1.444e+03]
[1.000e+00 6.600e+01 4.356e+03]
[1.000e+00 5.200e+01 2.704e+03]
[1.000e+00 5.300e+01 2.809e+03]
[1.000e+00 6.300e+01 3.969e+03]
[1.000e+00 5.400e+01 2.916e+03]
[1.000e+00 6.600e+01 4.356e+03]
[1.000e+00 5.500e+01 3.025e+03]
[1.000e+00 4.900e+01 2.401e+03]
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[1.000e+00 5.600e+01 3.136e+03]
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[1.000e+00 6.100e+01 3.721e+03]
[1.000e+00 6.700e+01 4.489e+03]
[1.000e+00 5.800e+01 3.364e+03]
[1.000e+00 4.700e+01 2.209e+03]
[1.000e+00 5.200e+01 2.704e+03]
[1.000e+00 5.800e+01 3.364e+03]
[1.000e+00 5.700e+01 3.249e+03]
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[1.000e+00 4.200e+01 1.764e+03]
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[1.000e+00 5.900e+01 3.481e+03]
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[1.000e+00 6.100e+01 3.721e+03]
[1.000e+00 4.600e+01 2.116e+03]
[1.000e+00 5.900e+01 3.481e+03]
[1.000e+00 5.700e+01 3.249e+03]
[1.000e+00 5.700e+01 3.249e+03]
[1.000e+00 5.500e+01 3.025e+03]
[1.000e+00 6.100e+01 3.721e+03]
[1.000e+00 5.800e+01 3.364e+03]
[1.000e+00 5.800e+01 3.364e+03]
[1.000e+00 6.700e+01 4.489e+03]
[1.000e+00 4.400e+01 1.936e+03]
[1.000e+00 6.300e+01 3.969e+03]
[1.000e+00 6.300e+01 3.969e+03]
[1.000e+00 5.900e+01 3.481e+03]
[1.000e+00 5.700e+01 3.249e+03]
[1.000e+00 4.500e+01 2.025e+03]
[1.000e+00 6.800e+01 4.624e+03]
[1.000e+00 5.700e+01 3.249e+03]]
```

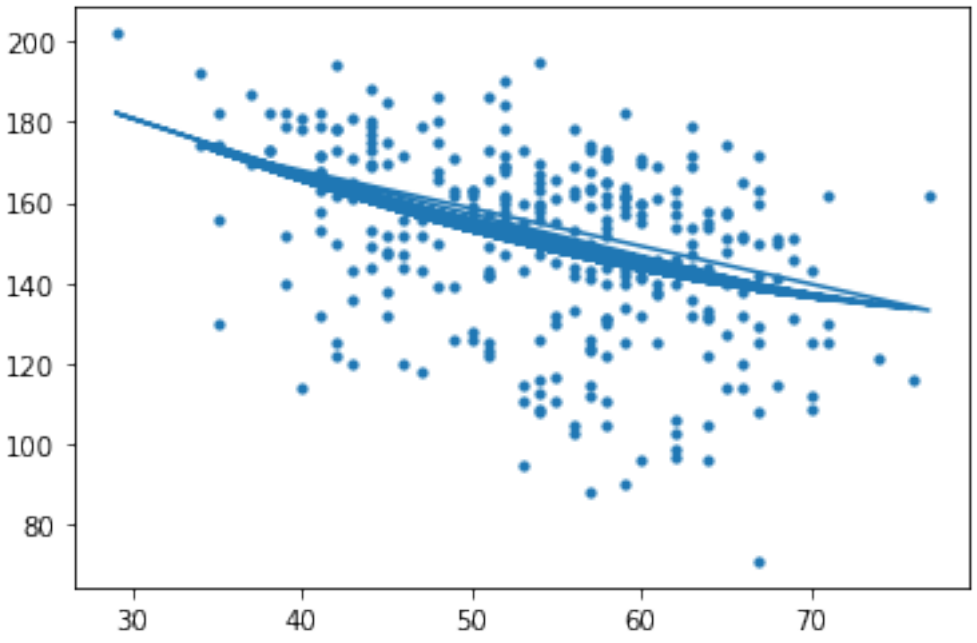
The matrix that you see is generated as follows:
The first column is always 1.
The second column is the value of x.
The third column is the value of x2.

[76]:
```
print(polynomial_features.get_feature_names('x'))
```

```
['1', 'x', 'x^2']
```

[77]:
```
model = LinearRegression()
model.fit(x_poly, y)
y_poly_pred = model.predict(x_poly)
  #---plot the points---
plt.scatter(x, y, s=10)
  #---plot the regression line---
plt.plot(x, y_poly_pred)
plt.show()

print(model.intercept_)
print(model.coef_)
```




```
[242.66086202]
[[ 0.         -2.48409126  0.01380695]]
```

[78]:
```
print('R-Squared for training set: %.4f' % model.score(x_poly,y))
```

```
R-Squared for training set: 0.1638
```

Can the R-Squared value be improved? Let's try a degree 3 polynomial. Using the same code and changing degree to 3, you should get the curve shown in Figure 6.13 and a value of 0.9889 for R-Squared.

3 Polynomial Regression did improve a bit of accuracy and R-Squared value But still not an acceptable value which is less than 80%

3.1 Possible Reasons:

1) Less Input Datasets

2) High Variance with bias

3.2 What to do?

1) Boosting / bagging methods

2) cross-validation is a better approximation. Moreover instead of only measuring accuracy, efforts should be on improving the algorithm. If the algorithm is improved, accuracy will also improve vis-a-vis the earlier approaches.

[ ]: