

HANOI UNIVERSITY OF SCIENCE AND  
TECHNOLOGY  
**SCHOOL OF ELECTRICAL AND  
ELECTRONICS ENGINEERING**

**Sample no.: 1 Pages: 6**

**FINAL EXAM OF SEMESTER I/2022-2023**

**Module: DATA STRUCTURES AND**

**ALGORITHMS (ET2101E)**

**Date: Mar/16/2023 - 12:30**

**Duration: 90 minutes**

(Paper documents allowed. Write directly on this sheet.)

**Signatures** Lecturer in charge:

Group leader:

**Student name: ..... Student ID: ..... Signature: .....**

**(Number of questions: 60)**

**1.** In the software development process, in which step(s) are algorithms used?

- a) Analysis
- b) Design
- c) Testing
- d) Evolution
- e) Implementation

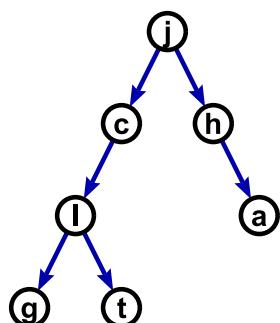
**2.** Given an array [13, 14, 12, 11, 16, 15]. Rewrite the values of this array after make it a Max Heap.

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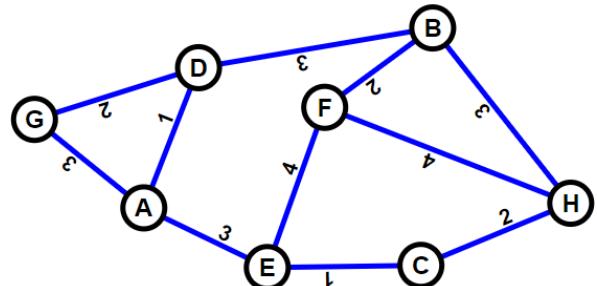
**3.** How many swap operations does the Bubble Sort algorithm need to sort the array [26, 34, 27, 32, 20, 24, 28, 22, 30, 21] in ascendant order?

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**4.** Given a tree as in the figure. Which node is visited right after node g when traversing the tree with DFS method in LVR order?



**5.** Is this graph cyclic?

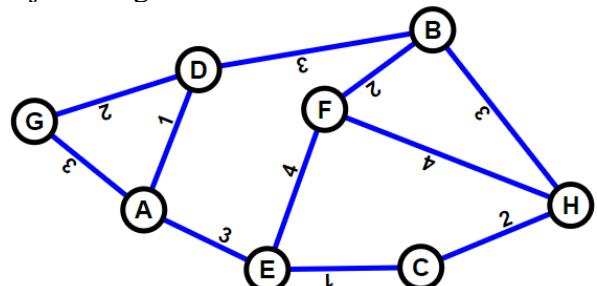


- a) True
- b) False

**6.** If edge  $\langle i,j \rangle$  is present in a directed graph G, then edge  $\langle j,i \rangle$  also is?

- a) True
- b) False

**7.** List the first 5 visited nodes in order when traversing this graph starting from G using Dijkstra algorithm



**8.** There may exist only one spanning tree for a graph?

- a) True
- b) False

9. After 4 steps of the Selection Sort algorithm in ascendant order, an array becomes [21, 22, 23, 24, 30, 27, 29, 26, 28]. Rewrite the values of this array after 3 next step(s).

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10. Given two elements a and b in a linked list, write the expression to check if a is the previous element of b

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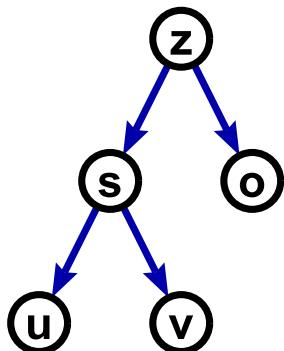
11. Given a stack with the elements added in the following order: <2, 7, 8, 3, 4, 7>. Rewrite the elements of this stack after doing Pop 2 times, then Push 5 and 9 respectively.

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12. Linked lists are more efficient than arrays in accessing a random element?

- a) True
- b) False

13. What is the depth of the following tree?



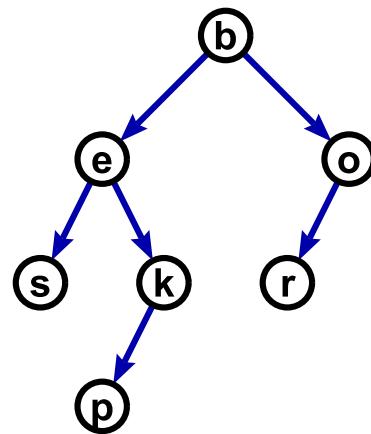
14. The constant complexity for a problem with size of n is

- a)  $O(n^2)$
- b)  $O(n)$
- c)  $O(1)$

15. Write the expression to check if a given element e is not the 2nd last element

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16. Given a tree as in the figure. Which node is visited right before node k when traversing the tree with DFS method in LRV order?



17. What is the asymptotic complexity of finding the next element (assumed existing) of a given element in a singly-linked list?

- a)  $O(i^2)$
- b)  $O(n)$
- c)  $O(1)$
- d)  $O(i)$
- e)  $O(n+i)$
- f)  $O(n^2)$

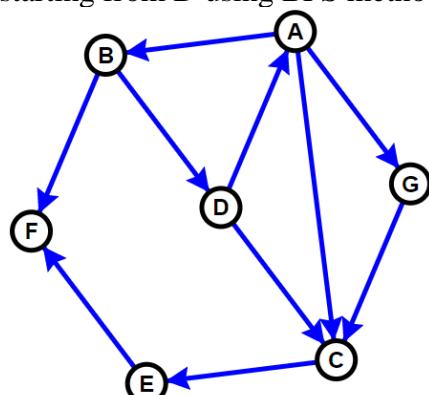
18. The linear complexity for a problem with size of n is

- a)  $O(1)$
- b)  $O(n^2)$
- c)  $O(n)$

19. What is needed to traverse a graph using the iterative DFS method?

- a) A stack
- b) A queue
- c) A linked list

20. Which one(s) of the following sequences is/are possibly visited when traversing this graph starting from D using BFS method?



- a) D A C G E B F
- b) D A F G B E C
- c) D A C G B F E
- d) D A C G B E F

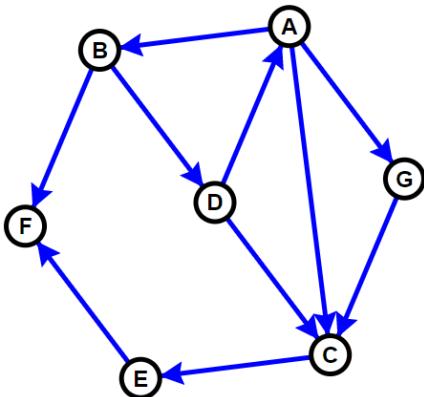
**21.** In a queue, the Dequeue operation allows to

- a) Remove the element at the tail
- b) Add an element to the tail
- c) Remove the element at the head
- d) Add an element to the head

**22.** In a Hash Table, the keys of elements must not duplicate?

- a) True
- b) False

**23.** List all the nodes that are reachable from D



**24.** At most, how many iterations are needed to find a value in an array of 200 elements using the Binary Search algorithm?

**25.** What is the asymptotic complexity of finding the previous element (assumed existing) of a given element in a singly-linked list?

- a) O(n)
- b) O(n^2)
- c) O(n+i)
- d) O(i^2)
- e) O(i)
- f) O(1)

**26.** What is the asymptotic complexity of an algorithm with  $2n^2 + 3\log(m)$  operations?

- a) O(log(m))
- b) O(n^2)
- c) O(n^2 + \log(m))

**27.** What is the memory asymptotic complexity of the in-place (not using auxiliary memory) Merge Sort algorithm?

- a) O(n^2)
- b) O(\log(n))
- c) O(n)
- d) O(1)

**28.** The number of hash values

- a) Can be determined by the programmer
- b) Equals the number of elements
- c) Is fixed by the algorithm

**29.** Given a Self Organizing List [21, 18, 22, 19, 17, 23, 20] using the Move-to-Front method. Rewrite the values of this list after respectively searching the following values: 21, 18, 20, 18, 17.

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**30.** Which one(s) of the following operations are of a stack?

- a) Enqueue
- b) Push
- c) Dequeue
- d) Pop

**31.** Nút lá của cây là nút

- a) Has the most number of children
- b) Does not have any child
- c) Has the most number of parents
- d) Does not have parent

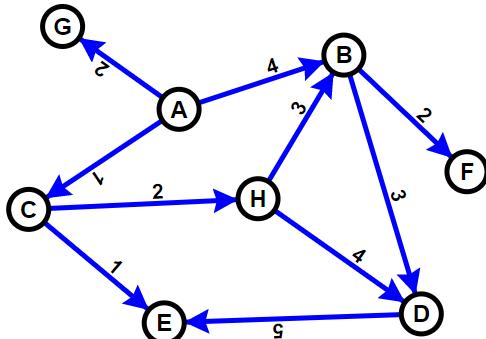
**32.** Which complexity(-ies) does an algorithm with  $13n^2 + 14n$  operations satisfy?

- a) O(2n^2)
- b) O(n^2 + n)
- c) O(n)
- d) O(n^2)
- e) O(2^n)

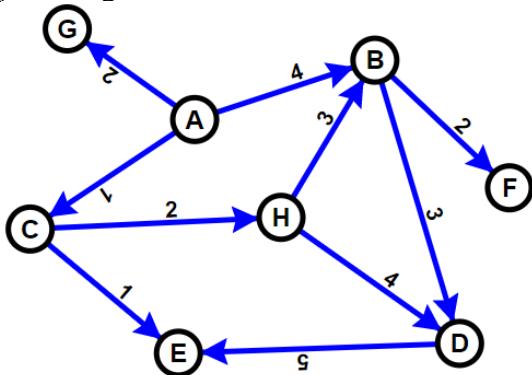
- 33.** Which data structure is last-in-first-out (LIFO)?
- Linked list
  - Stack
  - Tree
  - Hash table
  - Queue
- 34.** What pairs of elements are examined by the Bubble Sort algorithm?
- Pairs of two adjacent elements
  - Pairs of two arbitrary elements
- 35.** What is the asymptotic complexity of accessing the  $i$ -th element in a linked list?
- $O(n)$
  - $O(i+n)$
  - $O(i)$
  - $O(1)$
- 36.** The elements of a linked list are contiguously in memory?
- True
  - False
- 37.** Given a Binary Search Tree as in the figure. Write the nodes visited in order when searching for the value 12.
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graph TD
    15 --> 9
    15 --> 18
    9 --> 14
    9 --> 17
    14 --> 13
    14 --> 11
    11 --> 12
  
```
- .....
- 38.** For a given array of values, there are many Binary Search Trees that can be established?
- True
  - False
- 39.** What is needed to traverse a tree using the iterative BFS method?
- A queue
  - A linked list
  - A stack
- 40.** There can be many leaf nodes in a tree?
- True
  - False
- 41.** Given a Binary Search Tree as in the figure. How many nodes are visited to find the value 25?
- 
- ```

graph TD
    23 --> 21
    23 --> 27
    21 --> 20
    21 --> 25
    25 --> 26
  
```
- .....
- 42.** What is the memory asymptotic complexity of the standard (using auxiliary memory) Merge Sort algorithm?
- $O(n)$
  - $O(n^2)$
  - $O(\log(n))$
  - $O(1)$
- 43.** Does the Linear Search algorithm require the array to be sorted first?
- True
  - False
- 44.** Given two elements  $a$  and  $b$  in a linked list, write the expression to check if  $a$  is the 2nd next element of  $b$
- .....
- 45.** List all the nodes that are reachable from B



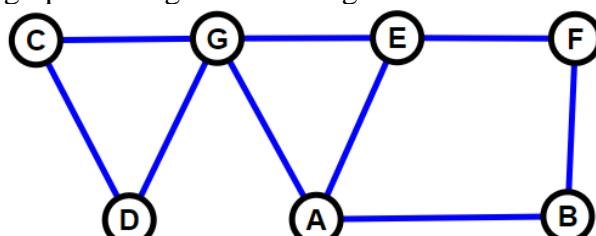
46. List the first 5 visited nodes in order when traversing this graph starting from C using Dijkstra algorithm



47. What is the asymptotic complexity of traversing a linked list of n elements from the beginning to the end?

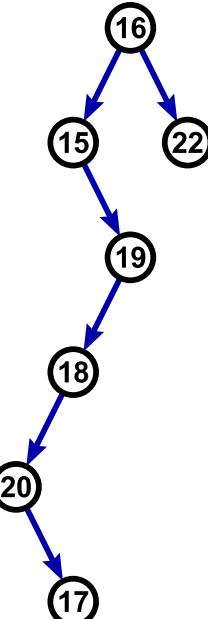
- a) O(1)
- b) O(log(n))
- c) O(n^2)
- d) O(n)

48. Which one(s) of the following sequences is/are possibly visited when traversing this graph starting from C using BFS method?



- a) C E D G A F A B
- b) C G D E A F A B
- c) C B D E A A F G
- d) C G D E A A F B

49. A Hash Table is used to
- a) Improve the efficiency in storing data
  - b) Improve the efficiency in searching data
50. Is the tree given in the figure a Binary Search Tree?



51. The root node of a tree
- a) Has the most number of children
  - b) Does not have any child
  - c) Does not have parent
  - d) Has the most number of parents
52. When does the Heap Sort algorithm establishes a Max Heap or Min Heap?
- a) At every step
  - b) Only once at the beginning
53. Is a connected acyclic graph a tree?
- a) True
  - b) False
54. There can be many root nodes in a tree?
- a) True
  - b) False
55. What is the time asymptotic complexity of the Quicksort algorithm in the worst case?
- a) O(1)
  - b) O(n^2)
  - c) O(log(n))
  - d) O(n)

**56.** Given a queue with the elements added in the following order: <22, 21, 24, 25>. Rewrite the elements of this queue after doing Dequeue 2 times, then Enqueue a value of 23.

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- 57.** An element in a doubly-linked list
- a) Points to the next element
  - b) Points to the next and the previous elements
  - c) Points to the previous element

**58.** After 4 steps of the Insertion Sort algorithm in descendant order, an array becomes [26, 19,

17, 15, 12, 22, 14, 23, 25, 10, 21]. Rewrite the values of this array after 3 next step(s).

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**59.** Does the Binary Search algorithm require the array to be sorted first?

- a) True
- b) False

**60.** Arrays are more efficient than linked lists in using memory?

- a) True
- b) False

----- *End* -----