

# Announcements

- ▶ Project 7 due tonight 11pm
- ▶ Project 8 out soon

#### Which is True about Function Files?

- A. May contain only one function definition
- B. May contain any number, but only the first can be called from command window
- May contain any number, but the second one can only be called by the first
- May contain any number, any can be called from anywhere
- E. None of the above

#### Subfunctions

- ▶ A function (.m) file may contain multiple function definitions
  - ▶ The first is the primary function and should correspond to the name of the file
  - ▶ Subsequent functions are called subfunctions
- Primary and subfunctions may call each other
  - regardless of order of appearance in file
  - only primary function may be called from main scope
- ▶ Each (sub)function has its own scope for local variables

#### **Nested Function Definitions**

 can also define a function within another function definition

```
function [a, b] = SomeFunction (x, y)
...
  function c = NestOne(z)
  ...
  end
...
end
NestOne is a nested function of SomeFunction
SomeFunction is the nesting function of NestOne
```

```
Example: Recursive Helper
function b = IsPalindrome( s )

PalindromeAux(1,length(s));

function PalindromeAux(low,high)
  if low >= high
    b = true;
  elseif s(low) ~= s(high)
    b = false;
  else PalindromeAux(low+1,high-1);
  end
  end
end
```

#### What if PalindromeAux were a Subfunction?

```
function b = IsPalindrome( s )
   PalindromeAux(1,length(s));
end
function PalindromeAux(low,high)
   if low >= high
      b = true;
   elseif s(low) ~= s(high)
      b = false;
   else
      PalindromeAux(low+1,high-1);
   end
end
```

- A It would work fine.
- B It would run, but produce no result.
- C Error: b undefined
- D Error: s undefined
- E None of the above

# Nested Functions: Scope

- Unlike subfunctions, nested functions share the scope of their nesting function
  - > can access and modify variables in nesting function's scope
  - variables introduced in nested function are accessible within nesting function's scope
  - formal parameters (input and output) of nested function not accessible to nesting function
- A function can call its nested functions
- A nested function can call its nesting function (recursion), as well as any functions its nesting function can call

```
Multiple Nested Functions (Same Level)
function [a, b] = SomeFunction (x, y)
...
  function c = NestOne(z)
...
  end
...
  function d = NestTwo(w)
...
  end
  NestOne and NestTwo are nested functions of SomeFunction
  SomeFunction is the nesting function of NestOne and NestTwo
```

```
Multilevel Function Nesting
function y = A (a1,a2)
                              function scope
   function z = B(b1,b2)
                              What can A call?
                                B, D (and itself, of course)
      function w = C(c1, c2)
                              ▶ What can B call?
      end
                                ▶ C,A, D, B
                              What can't C call?
   function u = D(d1, d2)
                              What can't D call?
      function h = E(e1, e2)
      end
   end
end
```

# Multilevel Function Nesting

```
function y = A (a1,a2)
...
    function z = B(b1,b2)
...
        function w = C(c1,c2)
...
        end
    end
    function u = D(d1,d2)
...
        function h = E(e1,e2)
...
        end
    end
    end
end
end
end
```

#### variable scope

- Which fns have access to a1, a2, and y?
  - all of them
- other formal parameters?
- other variables (e.g., if B introduces b3)?
  - Accessible to A and C, and also D and E but only if A refers to b3.

#### Example: Newton's Method

▶ Solve for *x*:

$$f(x) = 0$$

- Approach:
  - ► Guess a value, g
  - ▶ If f(g) close enough to zero, return g
  - ▶ Otherwise, generate an improved guess, repeat...
- ▶ Guess improvement formula:

$$g \leftarrow g - \frac{f(g)}{f'(g)}$$

double squareRoot(double s, double eps)

double residual = abs(guess \* guess - s);

double guess = 1.0;

return guess;

while ( residual > eps ) {
 guess = newGuess(guess,s);
 residual = abs(guess \* guess - s);

```
Newton's Method in MATLAB

function root = newton(guess)
% newton help line goes here

function y = f(x)
    y = x^3 + x - 3;
end

Nested "helper" functions, defining equation to be solved and its derivative.

function y = df(x)
    y = 3*x^2 + 1;
end

(to be continued)

adapted from Hahn & Valentine, Essential MATLAB
```

## Functions as Input

- ▶ Subfunction and nested function facility make it relatively easy to encapsulate helper fns with their primary function
- What we would really like, for an example like newton, is to supply the functions f and df as part of the input.
  - So far, only way to invoke a function is to call based on name associated with definition in program text
  - Passing functions as input requires a way to construct a function as a data element
- ...here's where function handles come in

#### **Function Handles**

- Create a function handle by prepending @ before a function name.
- For example, suppose we have defined:

function 
$$y = myfunc(x)$$
  
 $y = x^3 + x - 3$ ;

- then @myfunc is a function handle, and:
- feval(@myfunc,expr) behaves just like myfunc(expr)
- if we assign myf2 = @myfunc, then myf2(expr) also behaves just like myfunc(expr)

# Newton's Method with Function Inputs

# **Anonymous Functions**

- ▶ Function objects without names
- Form:

```
@ (paramList) expr
```

- paramList: comma-separated list of arguments (just as in function definitions)
- expr: a MATLAB expression
- ▶ To associate with a function handle variable:

```
handlevar = @ (paramList) expr
```

**>** 

# Calling Anon Fns with Handle Variables

► Examples:

```
calcThis = @ (m) m^2 - 2*m + 1;
calcThis(5) → 16

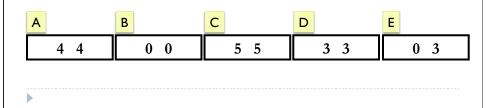
calcThat = @ (m,n,p) n - 2*p + m;
calcThat(5,4,3) → 3

calcIt = @ (m) m.^2;
calcIt([3 4 5]) → [9 16 25]
```

#### Exercise

▶ What is b after executing the following code?

```
func = @ (x,y) sqrt(x.^2-y.^2);
a = func([5 5], [3 3]);
b = 3 + func(a,a);
```



## Using Anonymous Functions

Example:

$$f = @(x) x.^3 + x - 3$$
  
 $df = @(x) 3*x.^2 + 1$ 

Use in expressions:

$$z = 0:0.05:2;$$
  
plot(z, f(z))

▶ Pass into functions:

Assigning handle to name not actually needed:

## Anonymous Functions: Scope

@ (paramList) expr

- Variables in paramList have scope local to anonymous function
- Body expr may also refer to any variables or functions available in scope where anonymous function defined
  - External references evaluated at definition time

#### Try this in MATLAB

```
x = 999;
z = -111;
myFunc = @(z) sqrt(x+z);
y = myFunc(601)
x = 24;
y2 = myFunc(601)
myFunc2 = @(y) 2*myFunc(y);
y3 = myFunc2(601)
myFunc = @(x) x^2;
y4 = myFunc2(601)
```

# Functions with Multiple Return Values

- ▶ Suppose fun0 is defined to return two values
- Various ways to use these values:

$$a = \text{fun0}(x)$$
  
 $[a] = \text{fun0}(x)$ 

one return value (first)

$$[\sim,a] = \text{fun0}(x)$$

one return value (second)

$$[a,b] = fun0(x)$$

two return values

#### Built-In size Function

- returns the size of each dimension of input array
- various ways to use return value (for matrix M):

```
sz = size(M)
```

one return value (a vector)

nrows = sz(1)ncols = sz(2)

two return values (scalars)

[nrows ncols] = size(M)

two-argument version

nrows = size(M, 1)
ncols = size(M, 2)

# Flexible Function Parameters

- ▶ Many MATLAB functions can handle varying numbers of arguments and return values
  - ▶ Examples: ones, fopen, fprintf, save, ...
  - Purpose:
    - ▶ Provide default values
    - Varying dimensions
    - Varying number of operands
- User-defined functions may also offer this flexibility

#### Supporting Varying Number of Parameters

- MATLAB exposes two key variables:
  - nargin: number of input arguments passed to the function
  - nargout: number of return values requested by the caller
- Idea: condition function behavior on these values

```
function myFunc (optArg)
  if nargin == 0
    optArg = defaultVal
  end
...
```

# Example with Optional Default

```
function val = simulate(time, startval)
  val = zeros(time);
  if nargin<2 | isempty(startval)
    val(1) = 0;
  else
    val(1) = startval;
  end
  for t = 2:time
    val(t) = SomeFunction(val(t-1));
  end
end</pre>
```

Example with Optional Return Value

```
function [m,v]=MeanVar(X)
% MeanVar computes mean and variance

n = size(X,1);  % #rows
m = mean(X);
if nargout>1
    temp = X - ones(n,1)*m;
    v = sum(temp.*temp)/(n-1);
end
```