

Câu 1:

$$F = \text{Tìm } (0, 2, 6, 7, 8, 15) \cdot D(4, 10, 11, 13)$$

a,

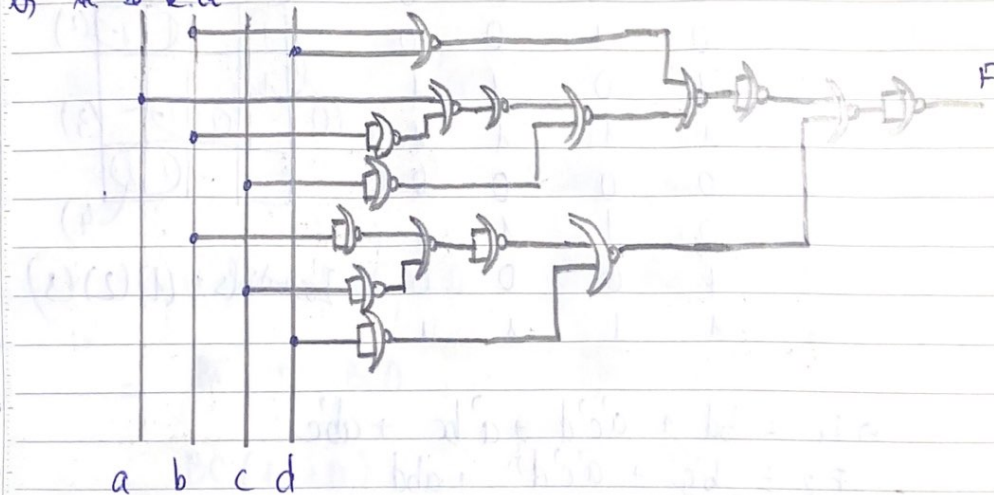
		cd		
		00	01	11
ab	00	0		0
	01	D	0	0
	11		D	0
	10	0		D

Essential: ①, ④

$$\rightarrow F = ① \times ③ \times ④$$

$$= (b'd')(a' + b + c)(b + c + d)$$

b, ~~a~~ ~~b~~ ~~c~~ ~~d~~



Câu 2:

Ta sử dụng đầu vào là 4bit abcd để biểu diễn với:

+, a để quy định nhà máy (a=0 là nhà máy X, a=1 là nhà máy Y)

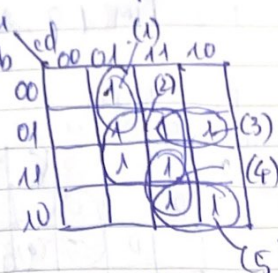
+, b, c, d là 3 bit biểu diễn cho loại rác (từ 1 đến 8)

Với đầu ra sẽ có 2 bit F₁ F₂ tương ứng cho 4 trạm (từ 1 đến 4)

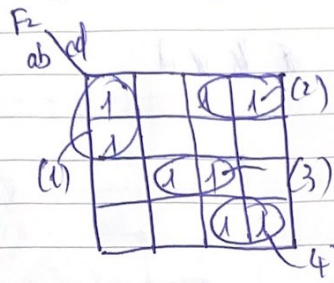
Bảng chân lý:

a	b	c	d	F ₁	F ₂
0	0	0	0	0	1
0	0	0	1	1	0
0	0	1	0	0	1
0	0	1	1	0	1
0	1	0	0	0	1
0	1	0	1	1	0
0	1	1	0	1	0
0	1	1	1	1	0
1	0	0	0	0	0
1	0	0	1	0	0
1	0	1	0	1	1
1	0	1	1	1	1
1	1	0	0	0	0
1	1	0	1	1	1
1	1	1	0	0	0
1	1	1	1	1	1

K-map



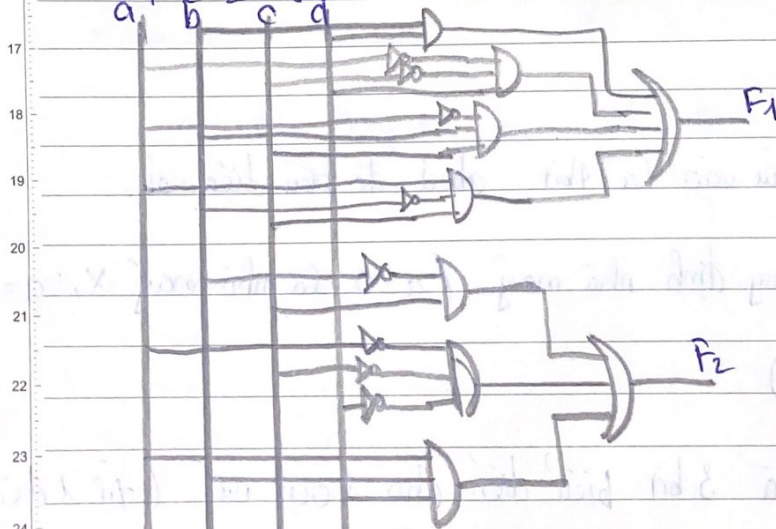
Essentials: (1)(2)(3)(5)



Essentials: (1)(2)(3)

$$\Rightarrow F_1 = bd + a'c'd + a'bc + ab'c$$

$$F_2 = b'c + a'c'd' + abd$$



Câu 3.

a. $BC + B'CD = BC + CD$

$$\begin{aligned} VT &= BC + B'CD \\ &= BC(1) + B'CD \quad \text{(Bù)} \\ &= BCD + BC + B'CD \quad \text{(phân phối)} \\ &= CD(B+B') + BC \quad \text{(kết hợp)} \\ &= BC + CD \quad \text{(Bù)} \\ &= VP \rightarrow \text{đpcm} \end{aligned}$$

b. $[(B' + CD)' + (BC)']' = BC$

$$\begin{aligned} VT &= [(B' + CD)' + (BC)']' \\ &= (B + CD) \cdot (BC) \quad \text{(DeMorgan)} \\ &= B \cdot BC + BC \cdot CD \quad \text{(phân phối)} \\ &= BC + BCD \quad \text{(bù)} \\ &= BC(1 + D) \quad \text{(kết hợp)} \\ &= BC = VP \rightarrow \text{đpcm} \quad \text{(bù)} \end{aligned}$$

c. $[(B' + C')' + (B'C'D')' + AD']' = B'C'D$

$$\begin{aligned} VT &= [(B' + C')' + (B'C'D')' + AD']' \\ &= (B' + C') \cdot (B'C'D') \cdot (A + D) \quad \text{(DeMorgan)} \\ &= (B' \cdot B'C'D' + C' \cdot B'C'D') (A + D) \quad \text{(phân phối)} \\ &= (B'C'D' + B'C'D') (A + D) \quad \text{(thu hút)} \\ &= B'C'D' (A + D) \quad \text{(lưu ý)} \\ &= A'B'C'D' + B'C'D' \cdot D \quad \text{(phân phối)} \\ &= B'C'D' (A' + 1) \quad \text{(kết hợp)} \end{aligned}$$

$$= B'C'D = VP \rightarrow \text{dpem}$$

$$d) W = (A' + B' + C + D)(A + C' + D)(A' + B' + C' + D)$$

$$= [(A' + B' + C + D)(A' + B' + C' + D)(A + C' + D)]$$

$$= [ABC'D' + ABCD' + (A + C' + D)']'$$

$$= [ABD'(C' + C) + (A + C' + D)']'$$

$$= [ABD' + (A + C' + D)']'$$

$$= [ABD'(1 + C) + (A + C' + D)']'$$

$$= [ABD' + ABCD' + A'CD']'$$

$$= [ABD' + ABCD' + A'(1 + B)CD']'$$

$$= (BCD' + ABD' + A'CD)'$$

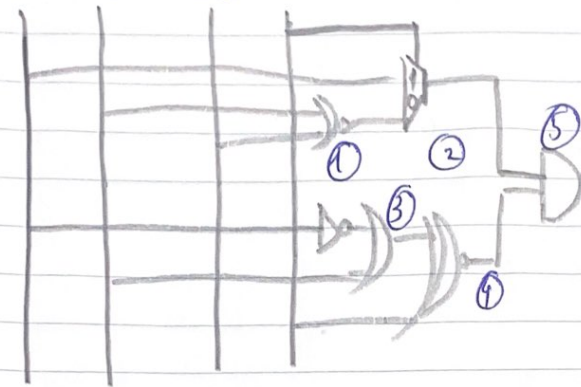
$$= (A'BCD' + ABD' + A'CD)'$$

$$= (A + B' + C' + D)(A' + B' + D)(A + C' + D)$$

$$= VP \rightarrow \text{dpem}$$

Câu 4:

A B C D



$$\textcircled{1} (B+C)' = B'C'$$

$$\textcircled{2} AD + B'C'D'$$

$$\textcircled{3} A' + B$$

$$\textcircled{4} (A' + B)D + (A' + B')D'$$

$$= A'D + BD + ABD'$$

$$\Rightarrow \textcircled{5} = F = (A'D + BD + ABD')$$

$$(AB'D' + A'D + BD)$$

$$= ABD + AB'C'D'$$