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Đề 02

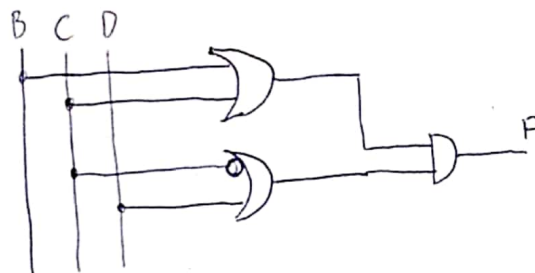
①

$$F(A, B, C, D) = M(0, 1, 2, 6, 14, 10) \cdot D(8, 9)$$

a)

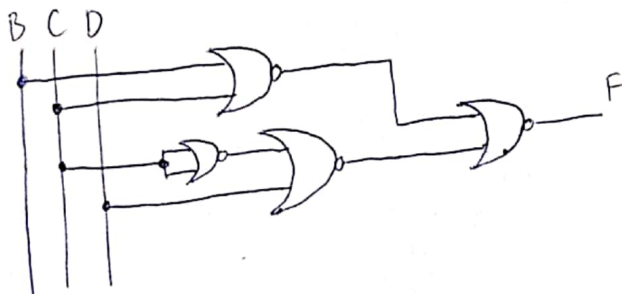
F	CD \ AB	00		01		11		10	
		00	01	11	10	00	01	11	10
	00	0	0	1	0	0	0	1	0
	01	1	1	1	0	1	1	1	0
	11	1	1	1	0	1	1	1	0
	10	d	d	1	0	1	1	1	0

$$F = (B + C)(C' + D)$$



b)

$$F = (B + C)(C' + D) = \overline{\overline{(B + C)} \overline{(C' + D)}} = \overline{\overline{(B + C)} + \overline{(C' + D)}}$$



2

Bảng chân lý:

A	B	C	D	X	Y	Z
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	0	1	0	0	0	0
0	0	1	1	0	0	0
0	1	0	0	1	0	0
0	1	0	1	0	0	1
0	1	1	0	0	0	1
0	1	1	1	1	0	0
1	0	0	0	0	0	1
1	0	0	1	0	0	1
1	0	1	0	0	1	0
1	0	1	1	0	1	0
1	1	0	0	0	0	1
1	1	0	1	0	0	1
1	1	1	0	0	0	1
1	1	1	1	0	0	1

X	CD	AB			
		00	01	11	10
	00	0	0	0	0
	01	1	0	1	0
	11	0	0	0	0
	10	0	0	0	0

$$X = A'BC'D + A'BCD$$

$$= A'B(C'D + CD)$$

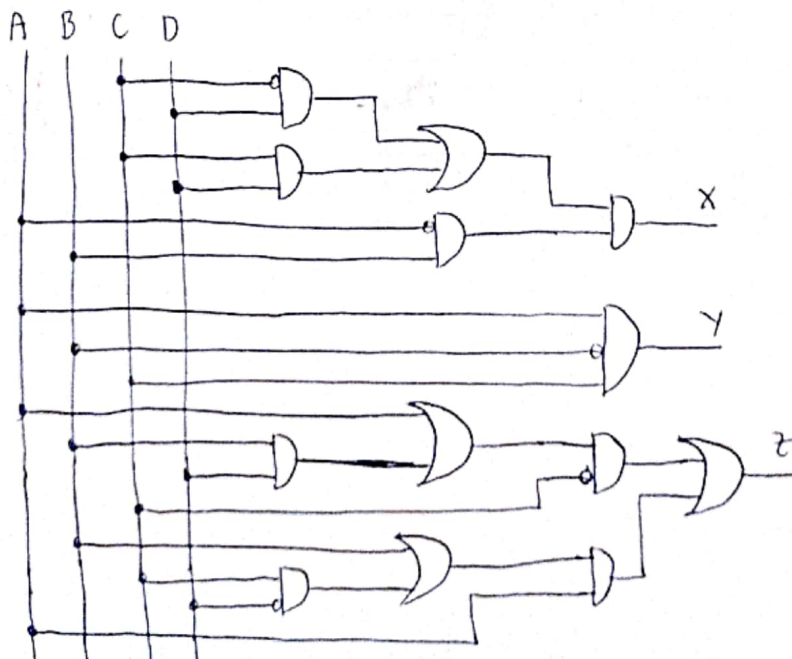
Y	CD	AB			
		00	01	11	10
	00	0	0	0	0
	01	0	0	0	0
	11	0	0	0	0
	10	0	0	1	1

$$Y = AB'C$$

Z	CD	AB			
		00	01	11	10
	00	0	0	0	0
	01	0	1	0	1
	11	1	1	1	1
	10	1	1	0	0

$$Z = AC' + AB + BC'D + ACD'$$

$$= C'(A + BD) + A(B + CD)$$



③

$$a) \quad AC' + A'B' = ABC' + B'C' + A'B'C$$

$$\text{xét } VP = ABC' + B'C' + A'B'C$$

$$= ABC'D + ABC'D' + AB'C'D + A'B'C'D + AB'C'D' + A'B'C'D' + A'B'CD + A'B'CD' \quad (\text{Bù})$$

$$= AC'(BD + BD' + B'D + B'D') + A'B'(C'D + C'D' + CD + CD') \quad (\text{Phân phối})$$

$$= AC' + A'B' \quad (\text{Bù})$$

$$= VT \quad (\text{ct pđm})$$

b) $AC + A'B'C + BC = C$

Xét VT = $AC + A'B'C + BC$

= $C(A + A'B' + B)$ (phân phối)

= $C \cdot 1 = C$

= VP (ctpcm)

c) $(A' + B' + C')(A + B' + C)(A + C' + D) = B'C' + AB + A'CD$

Xét VT = $(A' + B' + C')(A + B' + C)(A + C' + D)$

= $(A'B' + A'C + AB + BC + AC' + B'C')(A + C' + D)$ (phân phối)

= $A'B'C' + A'B'D + A'CD + AB + ABC' + ABD + ABC + BCD + AC' + AC'D + A'BC' + B'C' + B'C'D$ (phân phối)

= $A'B'C' + A'B'D + A'CD + ABC' + ABD + ABC + BCD + AC'D + A'BC' + B'C'D + AB + AC' + B'C'$ (luỹ đẳng)

= ~~$B'C'(A' + A + D + 1) + AB(C' + D + C + 1) + A'CD + BCD + AC'$~~

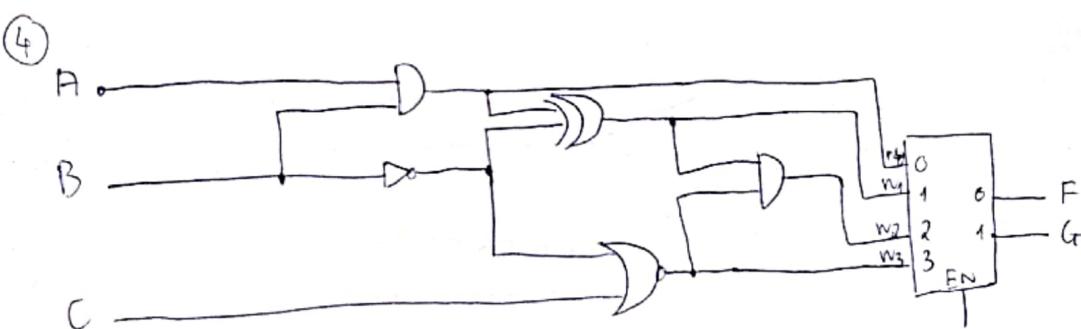
= $B'C'(A' + A + D + 1) + AB(C' + D + C + 1) + AC'(B + D + B' + 1) + A'B'D + A'CD + BCD$ (phân phối)

= $B'C' + AB + AC' + A'B'D + A'CD + BCD$ (bù)

= $B'C' + AB + AC' + A'B'CD + A'B'C'D + ABCD + A'BCD + A'CD$ (bù)

= $B'C'(1 + A'D) + AB(1 + CD) + A'CD(B' + B + 1)$ (phân phối)

= $B'C' + AB + A'CD = VP$ (ctpcm)



$w_0 = AB \quad w_1 = A'B' + AB + B' \quad w_2 = ABC' \quad w_3 = BC'$

Do $EN = 1$, ta có bảng chân lý:

w_3	w_2	w_1	w_0	F	G
0	0	0	1	0	0
0	0	1	0	0	1
0	1	0	0	1	0
1	0	0	0	1	1

F	$w_3 w_2$	00	01	11	10
00	d	0	d	0	
01	1	d	d	d	
11	d	d	d	d	
10	1	d	d	d	

G	$w_3 w_2$	$w_1 w_0$	00	01	11	10
00	d	0	d	1		
01	0	d	d	d		
11	d	d	d	d		
10	1	d	d	d		

$F = w_2 + w_3$
 $= ABC' + BC'$

$= F(m, B, C) = \bar{Z}_m(2, 6)$

$G = w_3 + w_1$
 $= BC' + A'B' + AB + B'$

$= G(A, B, C) = \bar{Z}_m(0, 1, 2, 4, 5, 6, 7)$