

# Sequence and Series

## Sequence

A sequence is a function that assigns real numbers to all positive integers denoted by  $u_n$ ,  $\{u_n\}$  or  $(u_n)$ .

For example:

- $1, 2, 3, 4, \dots$  where  $u_n = n$
- $-1, 1, -1, 1, \dots$  where  $u_n = (-1)^n$

## Series

A series is the sum of all terms in a sequence, or a partial amount of terms. It is usually written in the form of  $\sum$  and a variable that denotes the terms of the sequence.

Here is a list of sequences and their corresponding series:

Sequence	Series
$u_n = n$ $(1, 2, 3, 4, \dots)$	$\sum_i i$ $(1 + 2 + 3 + 4 + \dots)$
$u_n = \frac{1}{n}$ $(1, \frac{1}{2}, \frac{1}{3}, \frac{1}{4}, \dots)$	$\sum_i \frac{1}{i}$ $(1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots)$

## Partial Sum

A partial sum is a small portion of a series that starts and ends at a specific point.

$$\sum_{i=1}^n f(i)$$

This is the sum of the values of a function  $f$  from  $i = 1$  to  $i = n$ .