

ECE 131A Quiz 1

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Problem 1

(a)

Since $P(A^c \cap B^c) = \frac{2}{3}$, we have

$$P((A \cap B^c) \cup (A^c \cap B) \cup (A \cap B)) = 1 - P(A^c \cap B^c) = \boxed{\frac{1}{3}}$$

.

(b)

We have

$$\begin{aligned} P(C \cap D) &= P(C, D) \\ P(C|D) &= \frac{P(C, D)}{P(D)} \\ P(C^c|D) &= 1 - \frac{P(C, D)}{P(D)} \end{aligned}$$

$$P(C^c \cap D) = P(C^c, D) = P(D)P(C^c|D) = P(D)(1 - \frac{P(C, D)}{P(D)})$$

$$P(C^c \cap D) = P(D) - P(C, D) = 0.45 - 0.1 = \boxed{0.35}$$

Problem 2

Let the bernoulli random variable T represent if a page from a textbook have a theorem on it. Likewise let M be a random variable that represents the type of textbook a student is reading given it is a math textbook, therefore we have

$$P(M = \text{probability}) = \frac{10}{100 - 72}$$

$$P(M = \text{algebra}) = \frac{13}{100 - 72}$$

$$P(M = \text{real analysis}) = \frac{5}{100 - 72}$$

And thus we have

$$P(M = \text{probability}|T = 1) = \frac{P(M = \text{probability})P(T = 1|M = \text{probability})}{P(T = 1)}$$

Since

$$\begin{aligned} P(T = 1) &= P(M = \text{probability})P(T = 1|M = \text{probability}) \\ &\quad + P(M = \text{algebra})P(T = 1|M = \text{algebra}) \\ &\quad + P(M = \text{real analysis})P(T = 1|M = \text{real analysis}) \\ &= \frac{10}{100 - 72} \frac{20}{100} + \frac{13}{100 - 72} \frac{29}{100} + \frac{5}{100 - 72} \frac{37}{100} \\ &= 0.272142857143 \end{aligned}$$

Therefore we have

$$\begin{aligned} P(M = \text{probability}|T = 1) &= \frac{P(M = \text{probability})P(T = 1|M = \text{probability})}{P(T = 1)} \\ &= \frac{\frac{10}{100 - 72} \frac{20}{100}}{0.272142857143} \\ &= \boxed{0.262467191601} \end{aligned}$$