

Some Common Continous Random Variables

Normal	Exponential	Uniform	Erlang	Chi Squared
$X \sim N(\mu, \sigma^2)$ $x \in [-\infty, \infty]$ $f(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$ $E(X) = \mu$ $Var(X) = \sigma^2$ $\phi_X(\omega) = e^{j\mu\omega - \frac{\sigma^2\omega^2}{2}}$	$X \sim Exp(\lambda)$ $x \in [0, \infty]$ $f(x) = \lambda e^{-\lambda x}$ $E(X) = \frac{1}{\lambda}$ $Var(X) = \frac{1}{\lambda^2}$ $\phi_X(\omega) = \frac{\lambda}{\lambda - j\omega}$	$X \sim U(a, b)$ $x \in [a, b]$ $f(x) = \frac{1}{b-a}$ $E(X) = \frac{a+b}{2}$ $Var(X) = \frac{(b-a)^2}{12}$ $\phi_X(\omega) = \frac{e^{j\omega b} - e^{j\omega a}}{j\omega(b-a)}$	$X \sim Erlang(\lambda, k)$ $x \in [0, \infty]$ $f(x) = \frac{\lambda^k}{(k-1)!} x^{k-1} e^{-\lambda x}$ $E(X) = \frac{k}{\lambda}$ $Var(X) = \frac{k}{\lambda^2}$ $\phi_X(\omega) = \left(\frac{\lambda}{\lambda - j\omega} \right)^k$	$X \sim \chi^2(k)$ $x \in [0, \infty]$ $f(x) = \frac{1}{2^{k/2}\Gamma(k/2)} x^{k/2-1} e^{-x/2}$ $E(X) = k$ $Var(X) = 2k$ $\phi_X(\omega) = \left(\frac{1}{1-j2\omega} \right)^{k/2}$
Laplacian Random Variable				
$X \sim Lap(\alpha)$ $x \in [-\infty, \infty]$ $f(x) = \frac{\alpha}{2} e^{-\alpha x }$ $E(X) = 0$ $Var(X) = \frac{2}{\alpha^2}$ $\phi_X(\omega) = \frac{\alpha^2}{\alpha^2 + \omega^2}$				

The Erlang distribution is the sum of k independent exponential random variables with rate λ . The Chi Squared distribution is the sum of the squares of k independent standard normal random variables.