ECE 131A HW 1

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Problem 1

(a)

The sample space is just all the combinations of the two dice, with r denoting the bottom face of the red die and g denoting the bottom face of the green die. Therefore the sample space is just all the 16 orderd sets possible combinations of the possible results of r and g. In other words, the sample space is

$$\{(1,1),(1,2),(1,3),(1,4),(2,1),(2,2),(2,3),(2,4),$$

 $(3,1),(3,2),(3,3),(3,4),(4,1),(4,2),(4,3),(4,4)\}$

(b)

(i)

$$E = \boxed{\{(1,1), (1,3), (3,1), (3,3)\}}$$
$$F = \boxed{\{(1,4), (2,3), (3,2), (4,1)\}}$$

(ii)

Since E requires all values to be odd, and thus their sum to be even and F requires the sum of the values to be odd (5), these sets are disjoint, thus:

$$E \cap F = \boxed{\emptyset}$$

(iii)

$$E \cup F = \boxed{\{(1,1), (1,3), (3,1), (3,3), (1,4), (2,3), (3,2), (4,1)\}}$$

(iv)

 G^c is effectively just all value sof g and g such that $g+r\geq 7$, thus

$$G^c = \left[\{ (3,4), (4,3), (4,4) \} \right]$$