

ECE 141 Homework 4

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Problem 1

We have that

$$\beta = \arctan\left(\frac{l_r}{l_r + l_f} \tan(u)\right)$$

therefore

$$\tan(\beta) = \frac{l_r}{l_r + l_f} \tan(u)$$

therefore since the range of \tan is $-\infty$ to ∞ for any β we can find a u that satisfies the equation.

Problem 2

We have that

$$\frac{d}{dt}y = v \sin(\psi + \beta)$$

$$\frac{d}{dt}\psi = \frac{v}{l_R} \sin(\beta)$$

$$\beta = \arctan\left(\frac{l_r}{l_r + l_f} \tan(u)\right)$$

Linearizing around $\psi = 0$ $\beta = 0$, we have

$$\frac{d}{dt}y = v(\psi + \beta)$$

$$\frac{d}{dt}\psi = \frac{v}{l_R}\beta$$

therefore taking the laplace transform we have

$$sY = v(\psi + \beta)$$

$$s\psi = \frac{v}{l_r}\beta$$

Therefore we get

$$sY = v\left(\frac{v}{l_r s} + 1\right)\beta$$

Therefore the transfer function is

$$\frac{Y(s)}{\beta} = \frac{v(v + l_r s)}{l_r s^2}$$

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