# hw3p3

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## 0.1 Homework 3, Problem 3 on inhomogeneous Poisson processes

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In this problem, we will use the same simulated neuron as in Problem 2, but now the reaching angle s will be time-dependent with the following form:

$$s(t) = t^2 \cdot \pi,$$

where t ranges between 0 and 1 second. This will be referred as s(t) equation in the questions.

```
[1]:

ECE C143/C243 Homework-3 Problem-3

"""

import numpy as np
import matplotlib.pyplot as plt
import nsp as nsp # these are helper functions that we provide.
import scipy.special
from scipy.stats import poisson

# Load matplotlib images inline
%matplotlib inline

# Reloading any code written in external .py files.
%load_ext autoreload
%autoreload 2
```

#### 0.1.1 (a) (6 points) Spike trains

Generate 100 spike trains, each 1 second in duration, according to an inhomogeneous Poisson process with a firing rate profile defined by tuning equation,

$$\lambda(s) = r_0 + (r_{\text{max}} - r_0)\cos(s - s_{\text{max}})$$

and the s(t) equation,

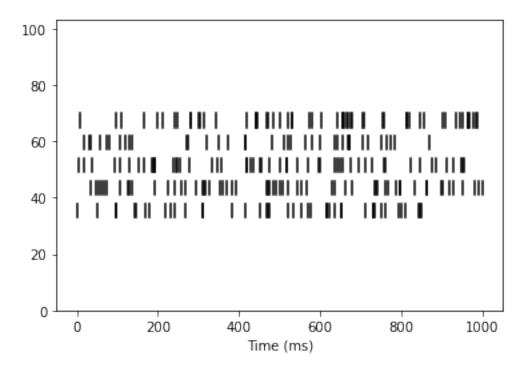
$$s(t) = t^2 \cdot \pi$$

```
s_max = np.pi/2 # (radians)
T = 1000 # trial length (ms)
```

[3]: np.random.exponential(1.0/r\_max \* 1000)

[3]: 19.359532842136645

```
[4]: ## 3a
   num_trials = 100 # number of total spike trains
   num_rasters_to_plot = 5 # number of spike trains to plot
   # YOUR CODE HERE:
   # Generate the spike times for 100 trials of an inhomogeneous
   # Poisson process. Plot 5 example spike rasters.
   spike_times = np.empty((num_trials), dtype=list)
   for trial in range(num_trials):
       #generate a homogeneous possion process
      spike_train=list(nsp.GeneratePoissonSpikeTrain( T, r_max ))
       #thin it
      spikes_to_keep=[]
      for t in spike_train:
         s=(t/1000)**2*np.pi
         l=r_0+(r_max-r_0)*np.cos(s-s_max)
         p=1/r_max
          if np.random.random()<p:</pre>
             spikes_to_keep.append(t)
       spike_times[trial]=np.array(spikes_to_keep)
   nsp.PlotSpikeRaster(spike_times[:num_rasters_to_plot])
   # END YOUR CODE
```



## 0.1.2 (b) (5 points) Spike histogram

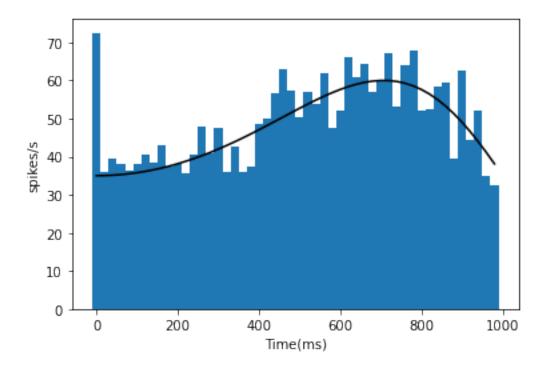
Plot the spike histogram by taking spike counts in non-overlapping 20 ms bins, then averaging across the 100 trials. The spike histogram should have firing rate (in spikes / second) as the vertical axis and time (in msec, not time bin index) as the horizontal axis. Plot the expected firing rate profile defined by equations tuning equation and s(t) equation on the same plot.

```
[5]: # 3b
   bin_width = 20 # (ms)
   # YOUR CODE HERE:
      Plot the spike histogram
   bins=np.arange(0,1000//bin_width)*bin_width
   counts=np.zeros(1000//bin_width)
   for rep in range(num_trials):
      rbins,rcounts=np.unique(spike_times[rep][0:]//bin_width,return_counts=True)
      for i,b in enumerate(rbins):
         counts[int(b)]+=rcounts[i]
   plt.bar(bins,(counts/num_trials)/(20*10**-3),width=20)
   s=(bins/1000)**2*np.pi
   1=r_0+(r_max-r_0)*np.cos(s-s_max)
   plt.plot(bins,1,color="black")
   # END YOUR CODE
```

```
#======#

plt.ylabel('spikes/s')
plt.xlabel('Time(ms)')
```

## [5]: Text(0.5, 0, 'Time(ms)')



Question: Does the spike histogram agree with the expected firing rate profile?

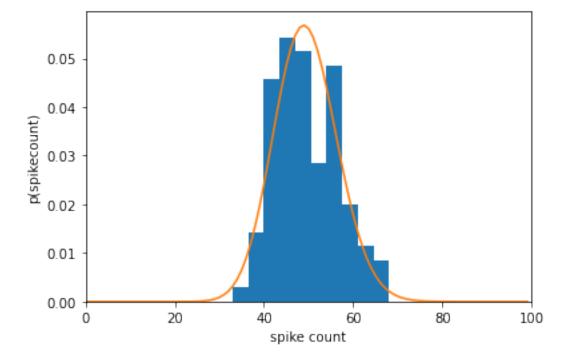
Your Answer: Yes

## 0.1.3 (c) (6 points) Count distribution

For each trial, count the number of spikes across the entire trial. Plot the normalized distribution of spike counts. Fit a Poisson distribution to this empirical distribution and plot it on top of the empirical distribution.

```
[6]: #========#
# YOUR CODE HERE:
# Plot the normalized distribution of spike counts
#=========#
N_spikes=np.empty(num_trials)
for trial in range(num_trials):
    N_spikes[trial]=spike_times[trial].shape[0]
```

```
plt.hist(N_spikes,density=True)
plt.xlim(0,100)
plt.plot(np.arange(0,100),poisson.pmf(np.arange(0,100), np.mean(N_spikes)))
#========#
# END YOUR CODE
#========#
plt.xlabel('spike count')
plt.ylabel('p(spikecount)')
plt.show()
```



Question: Should we expect the spike counts to be Poisson-distributed?

**Your Answer:** Yes, because the spike counts of a inhomogeneous Possion process is still a possion distribution.

## 0.1.4 (d) (5 points) ISI distribution

Plot the normalized distribution of ISIs. Fit an exponential distribution to the empirical distribution and plot it on top of the empirical distribution.

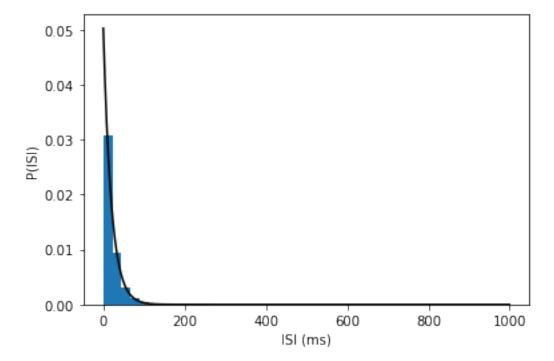
```
[7]: #=======#

# YOUR CODE HERE:

# Plot the normalized distribution of ISIs

#==========#

ISI=[]
```



**Question:** Should we expect the ISIs to be exponentially-distributed? (Note, it is possible for the empirical distribution to strongly resemble an exponential distribution even if the data aren't exponentially distributed.)

Your Answer: No, because it is an inhomogenous possion process