#### 1 Centre of mass

#### 1.1 General centre of mass

Shape  $A(x_1, y_1)$  weighted  $w_1$ ,  $B(x_2, y_2)$  weighted  $w_2$ ,  $C(x_3, y_3)$  weighted  $w_3$ , centre of mass  $G(\overline{x}, \overline{y})$ :

$$w_1 \begin{pmatrix} x_1 \\ y_1 \end{pmatrix} + w_2 \begin{pmatrix} x_2 \\ y_2 \end{pmatrix} + w_3 \begin{pmatrix} x_3 \\ y_3 \end{pmatrix} = (w_1 + w_2 + w_3) \begin{pmatrix} \overline{x} \\ \overline{y} \end{pmatrix}$$

## 1.2 Centre of mass of uniform triangular lamina

$$G\left(\frac{x_1+x_2+x_3}{3}, \frac{y_1+y_2+y_3}{3}\right)$$

#### 1.3 Centre of mass of uniform sector of a circle

Make the origin at the centre of the circle, make x-axis crossing the symmetry of the sector, then

$$distance = \frac{2r\sin\alpha}{3\alpha}$$

$$G\left(0,\frac{2r\sin\alpha}{3\alpha}\right)$$

## 1.4 Combined centre of mass of two laminae

Shape A,  $G_A(x_a, y_a)$  area  $A_a$ ;

Shape B,  $G_B(x_b, y_b)$  area  $A_b$ .

Combined centre of mass:

$$A_a \begin{pmatrix} x_a \\ y_a \end{pmatrix} + A_b \begin{pmatrix} x_b \\ y_b \end{pmatrix} = (A_a + A_b) \begin{pmatrix} \overline{x} \\ \overline{y} \end{pmatrix}$$

#### 1.5 Centre of mass of an arc of a circle

Make the origin at the centre of the circle, make x-axis crossing the symmetry of the sector, then

$$distance = \frac{r \sin \alpha}{\alpha}$$

## 1.6 Centre of mass of a frame

Consider all lines as a dedicated shape, use the general method to calculate its centre then use centre point to represent the shape then apply the general method again.

#### 2 Momentum

## 2.1 Coefficients of restitution

$$e = \frac{v_2 - v_1}{u_1 - u_2}$$

When e = 1, perfect elastic

#### 2.2 Collisions with wall

$$e = \frac{v}{u}$$

## 3 Stiffness coefficient

## 3.1 Force by extended string

$$F = \frac{\lambda x}{L}$$

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# 3.2 Energy stored in string

$$W = \frac{\lambda x^2}{2L}$$