

Q

Rolling Median (Abhishek Saini) :-

Find the median of all subarrays of size $\text{len}(k)$

Ans

Intuition :-

- since we're going to iterate to every window of size k
- So for a window we'll add elem, remove elem, get median of the window

(Sort all the numbers
+
get the middle no)

- we cannot just sort each window manually & then get get median bcz then T.C'll be

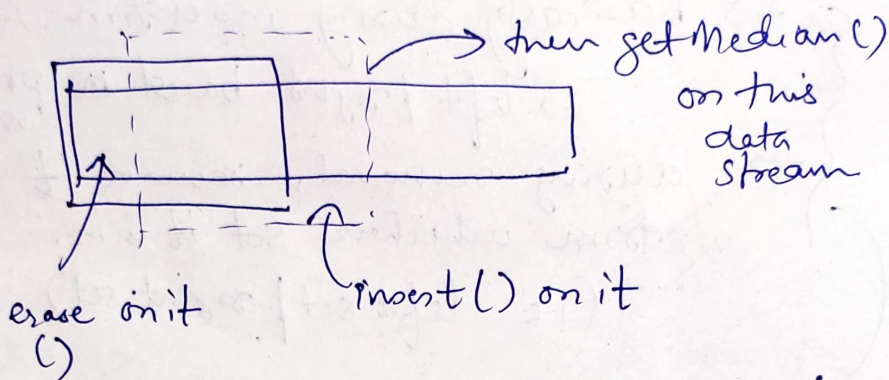
$$\begin{aligned} & \# \text{ windows} \times (\text{T.C to get median of} \\ & \quad \parallel \quad \parallel \text{ a window}) \\ & (n-k+1) \quad \parallel (k \log k) \end{aligned}$$

$$\approx O(n^2 \times \log n)$$

→ To design a data Structure

on which we'll easily be able to

perform $\boxed{\text{insert}(n), \text{erase}(n), \text{getMedian}()}$



* How to get the median?

10, 5, 2, 3, 6, 12, 9

↓ sorted order

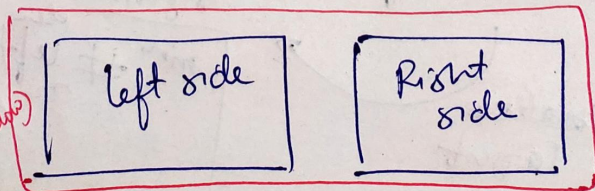
2 3 5 6 9 10 12

if $\left[\begin{array}{l} \text{(If we can maintain} \\ \text{these 2 parts then largest elem in} \\ \text{the left side is the median)}$ \end{array} \right.

we can use 2 ordered sets.

(to maintain sorted order in each half)

(this is the data struct. to maintain for every window)



If we can maintain half sorted elems in left & remaining in right set.

Then largest elem in left set is median

how??

→ basically during insertion, insert in left / right based on prev median

→ during removal, remove it from whichever set it is in.

(ie left set / right set)

So size of left / right might not be what it should be or elems in it might not be sorted from left → right.

So after every insert / remove

there should be some Rebalance

ideally ($\#_{\text{left}} \approx \#_{\text{elem in right}}$)

unless $k = \text{odd}$, then left has 1 more

So $\# \text{elem left} > \# \text{elem right}$

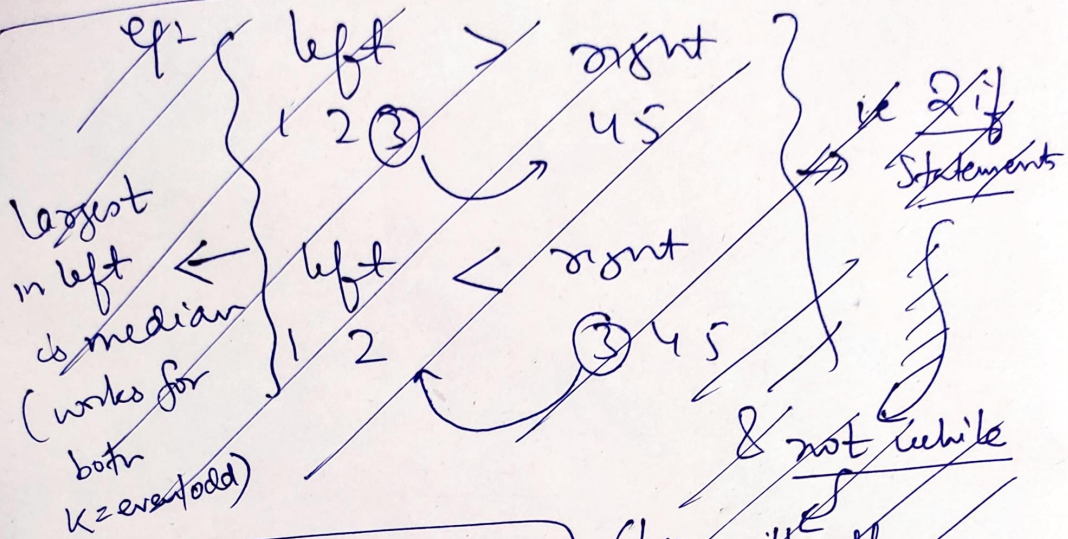
~~smallest~~
largest

right
min

elem
 $\#_{\text{left}} < \# \text{elem right}$

smallest

→ we'll call $\text{getMedian}()$ ~~if~~ when left & right have equal no of elem
 → (then we'll return largest from the left)



T.C :- $O(\log n)$

(bcoz we'll call rebalance after every insertion or deletion)