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- ☐ The major challenge in wind energy production is the cost reduction.
- ☐ The cost of wind energy depends on various factors like:
 - ☐ location selection
 - ☐ farm layout design, predictive maintenance etc.
- ☐ Among these factors farm layout design is import because an inadequate layout design leads to lower power capture than the expected and leads to increased maintenance cost or so on.

□ Problem Statement

The task to find the location of wind turbines in wind farm such that the total output energy is **maximum**. This task is called wind farm layout optimization problem (WFLOP).

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- 2) Each wind turbine location is represented as two dimensional vector (x_i, y_i) , $i = 1, 2, \dots, M$ where M is number of turbines.
- 3) Turbines in the farm are considered to be homogeneous .i.e. have similar design, brand, model, power curve, capacity etc.

Problem Statement and Modelling

- 4) At a given location and height wind speed μ follows the Weibull Distribution

$$p_{\mu}(\mu, \kappa, c) = \frac{\kappa}{c} \left(\frac{\mu}{c} \right)^{(\kappa-1)} e^{-\left(\frac{\mu}{c} \right)^{\kappa}}$$

where, p_{μ} is probability density function, c is scalar parameter and κ is shape parameter.

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- 5) Proper spacing between turbines reduces the wind turbulence effect. Thus, spacing between the turbines should be proper. So, turbines locations should satisfy the inequality

$$(x_i - x_j)^2 + (y_i - y_j)^2 \geq 64R^2, \quad i \neq j$$

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- 6) All turbines must be situated within the farm. All the turbines must satisfy the constraint

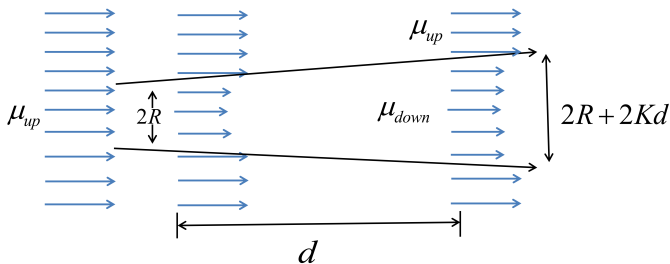
$$x_i^2 + y_i^2 \leq r^2$$

Wake Effect Model

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- Wake loss is the major factor in the wind park layout design.
- A linear expanding wake appears behind the turbine, when a uniform wind encounters a wind turbine.



$$vel_def_{ij} = 1 - \frac{\mu_{down}}{\mu_{up}} = \frac{1 - \sqrt{1 - C_r}}{(1 + Kd_{ij}/R)^2}$$

Optimization Problem

- The mathematical model of wind farm layout optimization problem is:

$$\max \sum_{i=1}^M E(P_i)$$

s.t.

$$(x_i - x_j)^2 + (y_i - y_j)^2 \geq 64R^2 \quad i = 1, 2, \dots, M, i \neq j$$
$$x_i^2 + y_j^2 \leq r^2$$

where, $E(P_i)$ is the power output of i^{th} turbine.

Optimization Problem

$$\begin{aligned}
 E(P_i) = & \alpha \sum_{j=1}^{M_\mu+1} \left(\frac{\mu_{j-1} + \mu_j}{2} \right) \sum_{t=1}^{M_\phi+1} \left[(\phi_t - \phi_{t-1}) \right. \\
 & \left. \left\{ e^{-\left(\mu_{j-1}/c_i \left(\frac{\phi_t + \phi_{t-1}}{2} \right) \right)^{\kappa \left(\frac{\phi_t + \phi_{t-1}}{2} \right)}} - e^{-\left(\mu_j/c_i \left(\frac{\phi_t + \phi_{t-1}}{2} \right) \right)^{\kappa \left(\frac{\phi_t + \phi_{t-1}}{2} \right)}} \right\} \right] \\
 & + P_{rated} \sum_{t=1}^{M_\phi+1} (\phi_t - \phi_{t-1}) \omega_{t-1} e^{-\left(\mu_{rated}/c_i \left(\frac{\phi_t + \phi_{t-1}}{2} \right) \right)^{\kappa \left(\frac{\phi_t + \phi_{t-1}}{2} \right)}} \\
 & + \beta \sum_{t=1}^{M_\phi+1} \left[(\phi_t - \phi_{t-1}) \omega_{t-1} \left\{ e^{-\left(\mu_{cut.in}/c_i \left(\frac{\phi_t + \phi_{t-1}}{2} \right) \right)^{\kappa \left(\frac{\phi_t + \phi_{t-1}}{2} \right)}} \right. \right. \\
 & \left. \left. - e^{-\left(\mu_{rated}/c_i \left(\frac{\phi_t + \phi_{t-1}}{2} \right) \right)^{\kappa \left(\frac{\phi_t + \phi_{t-1}}{2} \right)}} \right\} \right]
 \end{aligned}$$

Genetic Algorithm

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 - ☐ Selection
 - ☐ Crossover
 - ☐ Mutation
 - ☐ Elitism.

Selection and Crossover

- In selection process the fittest chromosome/solutions are selected to participate in mating pool.

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- In tournament selection we randomly sample subsets of fixed cardinality from population and choose the best individual based on fitness
- Crossover operator combines the information of two parent solution randomly taken from the matting pool and generates child solutions
- **Simulated binary crossover(SBX) [1]:** Let P_1 and P_2 are two parent solutions randomly selected from the matting pool:

$$\begin{aligned}C_1 &= 0.5(P_1 + P_2) - 0.5\eta(P_2 - P_1) \\C_2 &= 0.5(P_1 + P_2) + 0.5\eta(P_2 - P_1)\end{aligned}$$

where, $P_2 > P_1$ and

$$\eta = \begin{cases} (2u)^{\left(\frac{1}{N_c + 1}\right)}, & \text{if } \gamma \leq 0.5 \\ \left(\frac{1}{2(1-u)}\right)^{\left(\frac{1}{N_c + 1}\right)}, & \text{if } \gamma > 0.5 \end{cases}$$

Mutation and Elitism

- Mutation operator used to maintain genetic diversity from one generation of a population to the next generation.

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- Polynomial mutation is defined as follow [1]:

$$C' = \begin{cases} C + \delta_1(C - \bar{X}^L), & \text{if } rand() \leq 0.5 \\ C + \delta_2(\bar{X}^U - C), & \text{if } rand() > 0.5 \end{cases}$$

$$rand() \in U[0, 1]$$

$$\begin{cases} \delta_1 = (2u) \left(\frac{1}{N_m + 1} \right) - 1, & \text{if } rand() \leq 0.5 \\ \delta_2 = 1 - (2(1 - u)) \left(\frac{1}{N_m + 1} \right), & \text{if } rand() > 0.5 \end{cases}$$

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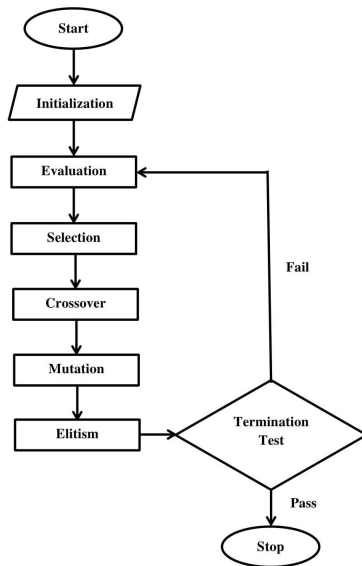
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- Elitism is a process of keeping the some proportion of elite solutions(i.e. fittest solutions) of previous generation in the next generation.

Flow Chart of GA



Experimental Results:

Experimental Results:

$t-1$	ϕ_{t-1}	ϕ_t	κ	c	ω_{t-1}
0	0	15	2	13	0
1	15	30	2	13	0.01
2	30	45	2	13	0.01
3	45	60	2	13	0.01
4	60	75	2	13	0.01
5	75	90	2	13	0.2
6	90	105	2	13	0.6
7	105	120	2	13	0.01
8	120	135	2	13	0.01
9	135	150	2	13	0.01
10	150	165	2	13	0.01
11	165	180	2	13	0.01
12	180	195	2	13	0.01
13	195	210	2	13	0.01
14	210	225	2	13	0.01
15	225	240	2	13	0.01
16	240	255	2	13	0.01
17	255	270	2	13	0.01
18	270	285	2	13	0.01
19	285	300	2	13	0.01
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Experimental Results:

□ Population size, $N = 60$

t-1	ϕ_{t-1}	ϕ_t	κ	c	ω_{t-1}
0	0	15	2	13	0
1	15	30	2	13	0.01
2	30	45	2	13	0.01
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Experimental Results:

□ Population size, $N = 60$

□ Tournament size = 3

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0	0	15	2	13	0
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□ Population size, $N = 60$

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□ Crossover probability, $C_p = 0.8$

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- ☐ Tournament size = 3
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- ☐ Mutation probability, $M_p = 0.1$
- ☐ Elitism size = 2

Experimental Results:

t-1	ϕ_{t-1}	ϕ_t	κ	c	ω_{t-1}
0	0	15	2	13	0
1	15	30	2	13	0.01
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- ☐ Mutation probability, $M_p = 0.1$
- ☐ Elitism size = 2
- ☐ Maximum generations = 100

Experimental Results:

t-1	ϕ_{t-1}	ϕ_t	κ	c	ω_{t-1}
0	0	15	2	13	0
1	15	30	2	13	0.01
2	30	45	2	13	0.01
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- ☐ Mutation probability, $M_p = 0.1$
- ☐ Elitism size = 2
- ☐ Maximum generations = 100
- ☐ Farm radius, $r = 500m$

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0	0	15	2	13	0
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- ☐ Mutation probability, $M_p = 0.1$
- ☐ Elitism size = 2
- ☐ Maximum generations = 100
- ☐ Farm radius, $r = 500\text{m}$
- ☐ Rotor radius, $R = 38.5(\text{m})$

Experimental Results:

t-1	ϕ_{t-1}	ϕ_t	κ	c	ω_{t-1}
0	0	15	2	13	0
1	15	30	2	13	0.01
2	30	45	2	13	0.01
3	45	60	2	13	0.01
4	60	75	2	13	0.01
5	75	90	2	13	0.2
6	90	105	2	13	0.6
7	105	120	2	13	0.01
8	120	135	2	13	0.01
9	135	150	2	13	0.01
10	150	165	2	13	0.01
11	165	180	2	13	0.01
12	180	195	2	13	0.01
13	195	210	2	13	0.01
14	210	225	2	13	0.01
15	225	240	2	13	0.01
16	240	255	2	13	0.01
17	255	270	2	13	0.01
18	270	285	2	13	0.01
19	285	300	2	13	0.01
20	300	315	2	13	0.01
21	315	330	2	13	0.01
22	330	345	2	13	0.01
23	345	360	2	13	0

- ☐ Population size, $N = 60$
- ☐ Tournament size = 3
- ☐ Crossover probability, $C_p = 0.8$
- ☐ Mutation probability, $M_p = 0.1$
- ☐ Elitism size = 2
- ☐ Maximum generations = 100
- ☐ Farm radius, $r = 500\text{m}$
- ☐ Rotor radius, $R = 38.5(\text{m})$
- ☐ Wind cut-in speed, $\mu_{cut_in} = 3.5 \text{ m/s}$

Experimental Results:

t-1	ϕ_{t-1}	ϕ_t	κ	c	ω_{t-1}
0	0	15	2	13	0
1	15	30	2	13	0.01
2	30	45	2	13	0.01
3	45	60	2	13	0.01
4	60	75	2	13	0.01
5	75	90	2	13	0.2
6	90	105	2	13	0.6
7	105	120	2	13	0.01
8	120	135	2	13	0.01
9	135	150	2	13	0.01
10	150	165	2	13	0.01
11	165	180	2	13	0.01
12	180	195	2	13	0.01
13	195	210	2	13	0.01
14	210	225	2	13	0.01
15	225	240	2	13	0.01
16	240	255	2	13	0.01
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21	315	330	2	13	0.01
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- ☐ Crossover probability, $C_p = 0.8$
- ☐ Mutation probability, $M_p = 0.1$
- ☐ Elitism size = 2
- ☐ Maximum generations = 100
- ☐ Farm radius, $r = 500m$
- ☐ Rotor radius, $R = 38.5(m)$
- ☐ Wind cut-in speed, $\mu_{cut_in} = 3.5 \text{ m/s}$
- ☐ Wind rated speed, $\mu_{rated} = 14 \text{ m/s}$

Experimental Results:

t-1	ϕ_{t-1}	ϕ_t	κ	c	ω_{t-1}
0	0	15	2	13	0
1	15	30	2	13	0.01
2	30	45	2	13	0.01
3	45	60	2	13	0.01
4	60	75	2	13	0.01
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6	90	105	2	13	0.6
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- ☐ Crossover probability, $C_p = 0.8$
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- ☐ Elitism size = 2
- ☐ Maximum generations = 100
- ☐ Farm radius, $r = 500\text{m}$
- ☐ Rotor radius, $R = 38.5(\text{m})$
- ☐ Wind cut-in speed, $\mu_{cut_in} = 3.5 \text{ m/s}$
- ☐ Wind rated speed, $\mu_{rated} = 14 \text{ m/s}$
- ☐ Rated power for rated wind speed, $P_{rated} = 1500 \text{ kW}$

Experimental Results:

t-1	ϕ_{t-1}	ϕ_t	κ	c	ω_{t-1}
0	0	15	2	13	0
1	15	30	2	13	0.01
2	30	45	2	13	0.01
3	45	60	2	13	0.01
4	60	75	2	13	0.01
5	75	90	2	13	0.2
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19	285	300	2	13	0.01
20	300	315	2	13	0.01
21	315	330	2	13	0.01
22	330	345	2	13	0.01
23	345	360	2	13	0

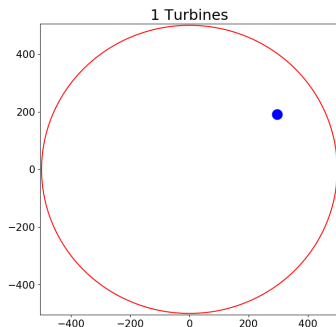
- ☐ Population size, $N = 60$
- ☐ Tournament size = 3
- ☐ Crossover probability, $C_p = 0.8$
- ☐ Mutation probability, $M_p = 0.1$
- ☐ Elitism size = 2
- ☐ Maximum generations = 100
- ☐ Farm radius, $r = 500m$
- ☐ Rotor radius, $R = 38.5(m)$
- ☐ Wind cut-in speed, $\mu_{cut_in} = 3.5 \text{ m/s}$
- ☐ Wind rated speed, $\mu_{rated} = 14 \text{ m/s}$
- ☐ Rated power for rated wind speed, $P_{rated} = 1500 \text{ kW}$
- ☐ $\alpha = 140.86, \beta = -500$

Experimental Results:

Number of turbines	Ideal Power	BBO(best)/Wake loss[2]	GA(best)/Wake loss
2	14631.37	28091.47/0.0	28091.47/0.0
3	21947.06	21947.06/0.0	21947.06/0.0
4	29262.75	29262.75/0.0	29262.75/0.0
5	36578.44	36578.44/0.0	36522.05/56.3867
6	43894.12	43894.12/0.0	43854.78/39.34

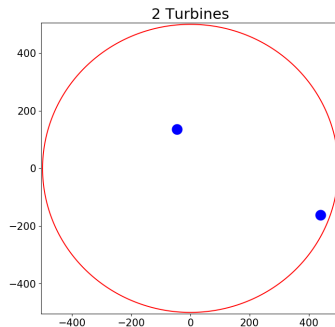
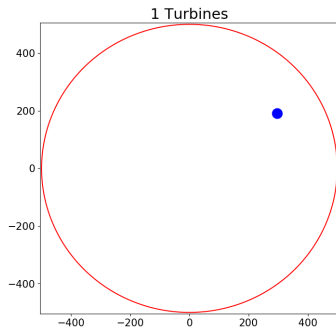
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6	43894.12	43894.12/0.0	43854.78/39.34



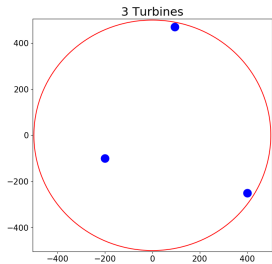
Experimental Results:

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5	36578.44	36578.44/0.0	36522.05/56.3867
6	43894.12	43894.12/0.0	43854.78/39.34

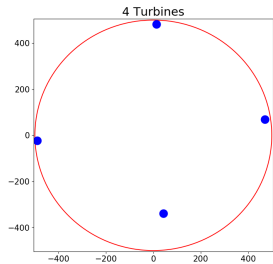
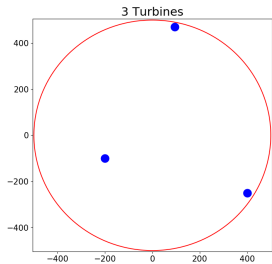


Experimental Results:

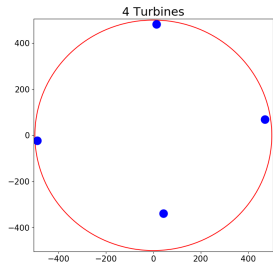
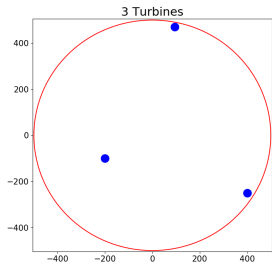
Experimental Results:



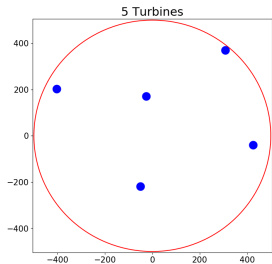
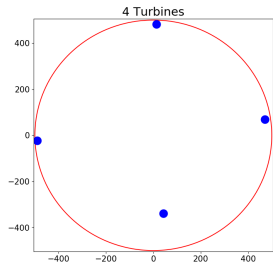
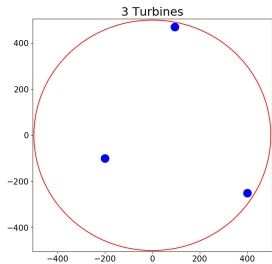
Experimental Results:



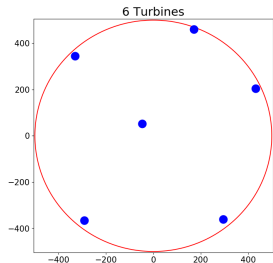
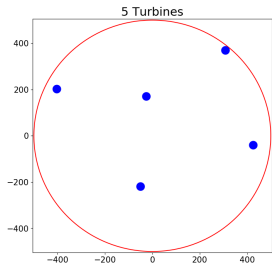
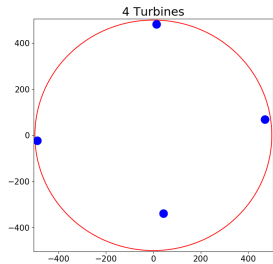
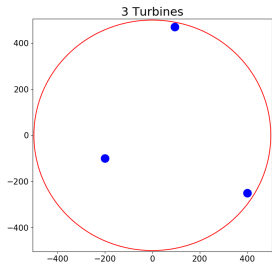
Experimental Results:



Experimental Results:



Experimental Results:



References

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References

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Thank you