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BATCH	C
SUBJECT	Design and Analysis of Algorithms
EXPERIMENT NO	3
DATE OF PERFORMANCE	27-02-2023
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AIM	To understand and implement Strassen's Matrix Multiplication.
THEORY	<p>Given two square matrices A and B of size $n \times n$ each, find their multiplication matrix.</p> <p>Naive Method takes the Time Complexity of $O(N^3)$.</p> <p>Divide and Conquer:</p> <p>Following is a simple Divide and Conquer method to multiply two square matrices.</p> <ol style="list-style-type: none"> 1 Divide matrices A and B in 4 sub-matrices of size $N/2 \times N/2$ as shown in the below diagram. 2 Calculate following values recursively. $ae + bg$, $af + bh$, $ce + dg$ and $cf + dh$. <p>Simple Divide and Conquer also leads to $O(N^3)$, can there be a better way?</p> <p>In the above divide and conquer method, the main component for high time complexity is 8 recursive calls. The idea of Strassen's method is to reduce the number of recursive calls to 7. Strassen's method is similar to above</p>

	<p>simple divide and conquer method in the sense that this method also divides matrices to sub-matrices of size $N/2 \times N/2$ as shown in the above diagram, but in Strassen's method, the four sub-matrices of result are calculated using following formulae.</p> <p>Time Complexity of Strassen's Method</p> <p>Addition and Subtraction of two matrices takes $O(N^2)$ time. So, time complexity can be written as</p> $T(N) = 7T(N/2) + O(N^2)$ <p>Generally, Strassen's Method is not preferred for practical applications for the following reasons.</p> <p>The constants used in Strassen's method are high and for a typical application Naive method works better. For Sparse matrices, there are better methods especially designed for them.</p> <p>The submatrices in recursion take extra space.</p> <p>Because of the limited precision of computer arithmetic on non-integer values, larger errors accumulate in Strassen's algorithm than in Naive Method.</p>
ALGORITHM	<ol style="list-style-type: none"> 1 Start 2 Declare two matrices A and B and take the values from the user. 3 Find S1 to S10 using provided formulae. 4 Find P1 to P7 using provided formulae. 5 Find the elements of matrix C which is the multiplication of A and B. 6 Print the result.

PROGRAM	<pre>#include <stdio.h> #include <stdlib.h> int main() { int n, i, j; printf("Enter the dimensions of the matrix.\n"); scanf("%d", &n); int A[n][n], B[n][n]; int C[n][n]; printf("Enter the contents of matrix 'A' \n"); for (i = 0; i < n; i++) { for (j = 0; j < n; j++) { scanf("%d", &A[i][j]); } } printf("Enter the contents of matrix 'B' \n"); for (i = 0; i < n; i++) { for (j = 0; j < n; j++) { scanf("%d", &B[i][j]); } } int s1 = B[0][1] - B[1][1]; int s2 = A[0][0] + A[0][1]; int s3 = A[1][0] + A[1][1]; int s4 = B[1][0] - B[0][0]; int s5 = A[0][0] + A[1][1]; int s6 = B[0][0] + B[1][1]; int s7 = A[0][1] - A[1][1]; int s8 = B[1][0] + B[1][1];</pre>
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int s9 = A[0][0] - A[1][0];  
int s10 = B[0][0] + B[0][1];
```

```
int p1, p2, p3, p4, p5, p6, p7;  
p1 = A[0][0] * s1;  
p2 = s2 * B[1][1];  
p3 = s3 * B[0][0];  
p4 = s4 * A[1][1];  
p5 = s5 * s6;  
p6 = s7 * s8;  
p7 = s9 * s10;
```

```
C[0][0] = p5 + p4 - p2 + p6;  
C[0][1] = p1 + p2;  
C[1][0] = p3 + p4;  
C[1][1] = p5 + p1 - p3 - p7;
```

```
printf("Matrix A*B is \n");  
for (i = 0; i < n; i++)  
{  
    for (j = 0; j < n; j++)  
    {  
        printf("%d\t", C[i][j]);  
    }  
    printf("\n");  
}  
}
```

RESULT (SNAPSHOT):

```
Enter the dimensions of the matrix.  
2  
Enter the contents of matrix 'A'  
3  
4  
2  
1  
Enter the contents of matrix 'B'  
1  
5  
3  
7  
Matrix A*B is  
15      43  
5       17
```

CONCLUSION:

With the help of this experiment, I was successfully able to understand and implement the concept of Strassen's multiplication.