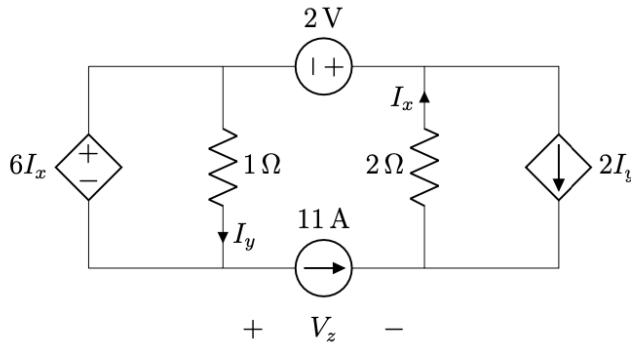
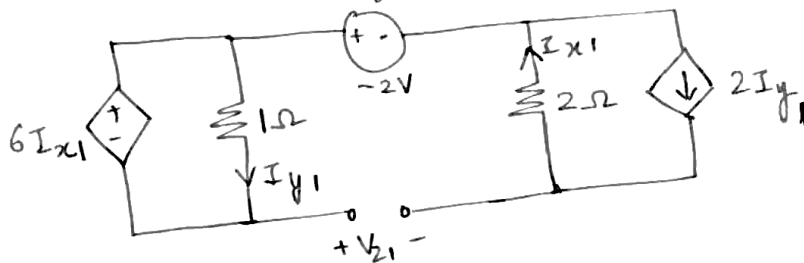


Que 1.

Determine I_x , I_y and V_z using superposition:



Ans 4. (i) Contribution of $-2V$ source:



$$6I_{x1} = 1 \times I_{y1} \quad \text{--- (1)}$$

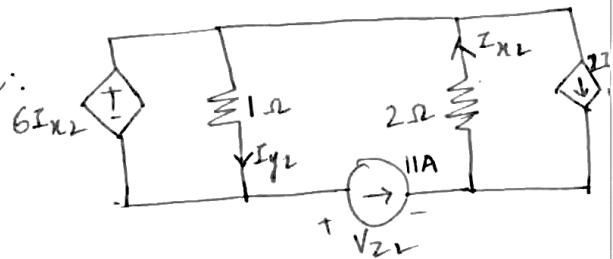
$$2I_{y1} = I_{x1} \quad \text{--- (2)}$$

$$\Rightarrow I_{x1} = I_{y1} = 0$$

$$\text{Also, } -V_{z1} - 1 \times I_{y1} + (-2V) - 2 \times I_{x1} = 0$$

$$\therefore V_{z1} = -2V$$

(ii) Contribution of $11A$ source:



$$V_{12} = 6I_{x2}$$

$$V_{12} = 1 \times I_{y2}$$

$$\Rightarrow 6I_{x2} = I_{y2}$$

$$11 = I_{x2} - 2I_{y2}$$

$$\therefore I_{x2} = -1A, I_{y2} = -6A$$

$$\text{also, } 2I_{x2} + I_{y2} + V_{22} = 0$$

$$\Rightarrow V_{22} = 8V$$

$$\therefore I_x = I_{x1} + I_{x2} = -1A$$

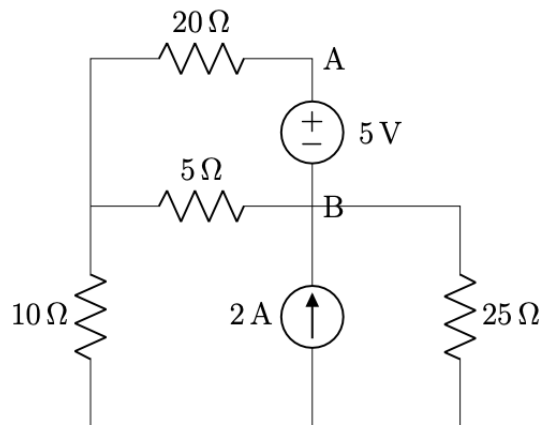
$$I_y = I_{y1} + I_{y2} = -6A$$

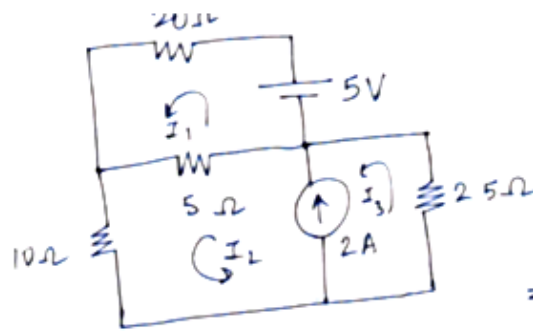
$$V_2 = V_{21} + V_{22} = 6V$$

Que 2

Determine the power supplied by the 5V source using

- Mesh analysis
- Nodal analysis
- Superposition principle
- Thevenin's equivalent circuit between terminals A and B.





$$20I_1 + 10I_2 + 25I_3 = 5$$

$$I_2 - I_3 = 2$$

$$\therefore 20I_1 + 10I_2 + 25I_2 = 55$$

$$\Rightarrow 20I_1 + 35I_2 = 55$$

$$\Rightarrow 4I_1 + 7I_2 = 11 \quad \text{--- (1)}$$

$$20I_1 + 5(I_1 - I_2) = 5$$

$$\Rightarrow 25I_1 - \frac{5}{7}(11 - 4I_1) = 5$$

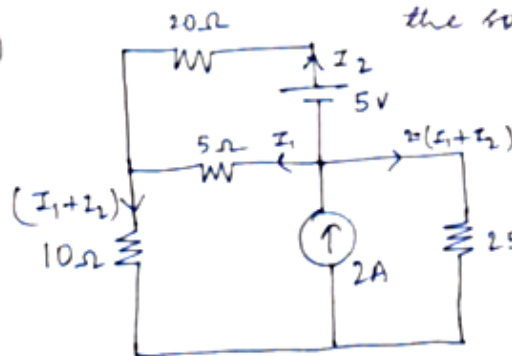
$$\Rightarrow 25I_1 - \frac{55}{7} + \frac{20}{7}I_1 = 5$$

$$\Rightarrow I_1 = \frac{\left(5 + \frac{55}{7}\right)}{\left(25 + \frac{20}{7}\right)} = 0.46 \text{ A}$$

$$\therefore P_{5V} = -0.46 \times 5 \text{ W} = -2.31 \text{ W}$$

Shows that power is supplied by the source.

(b)



$$[10(I_1 + I_2) + 20I_2] -$$

$$[25(2 - I_1 - I_2)] = 5$$

$$\Rightarrow 10I_1 + 30I_2 - 50 + 25I_1 + 25I_2 = 5$$

$$\Rightarrow 11I_2 + 7I_1 = 11 \quad \text{--- (1)}$$

$$10(I_1 + I_2) + 5I_1 = (2 - I_1 - I_2)25$$

$$\Rightarrow 15I_1 + 10I_2 = 50 - 25I_1 - 25I_2$$

$$\Rightarrow 40I_1 + 35I_2 = 50$$

$$\Rightarrow 8I_1 + 7I_2 = 10 \quad \text{--- (2)}$$

From (1) and (2),

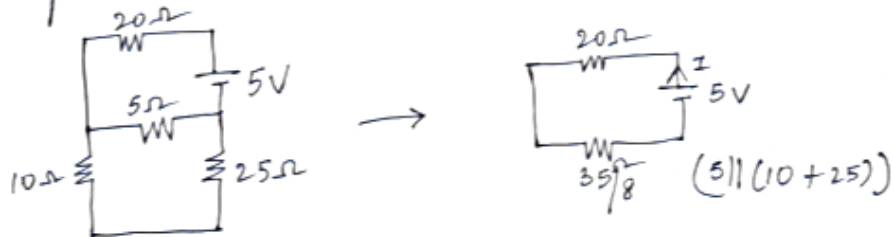
$$11I_2 + \frac{7}{8}(10 - 7I_2) = 11$$

$$\Rightarrow \left(11 - \frac{49}{8}\right) I_2 = 11 - \frac{70}{8}$$

$$\Rightarrow I_2 = 0.46 \text{ A}$$

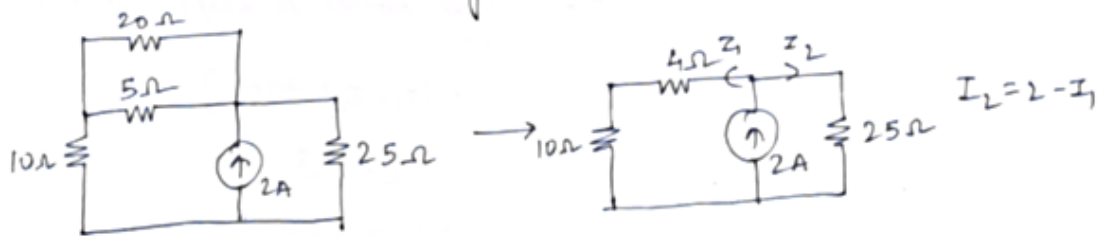
$$\therefore P_{5V} = -0.46 \times 5 \text{ W} = -2.31 \text{ W}$$

(c) Open circuit current source:



$$\therefore I = \frac{5}{20 + \frac{35}{8}} \text{ A} = 0.2 \text{ A}$$

Short circuit voltage source:



$$25(2 - I_1) = I_1(10 + 4) \Rightarrow I_1 = 1.28 \text{ A}$$



$$5(1.28) - 5i_A = 20(I_1 - i_A)$$

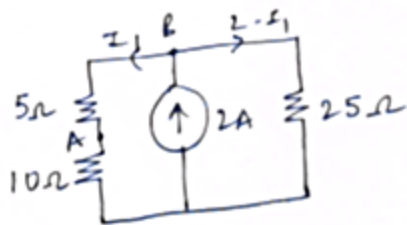
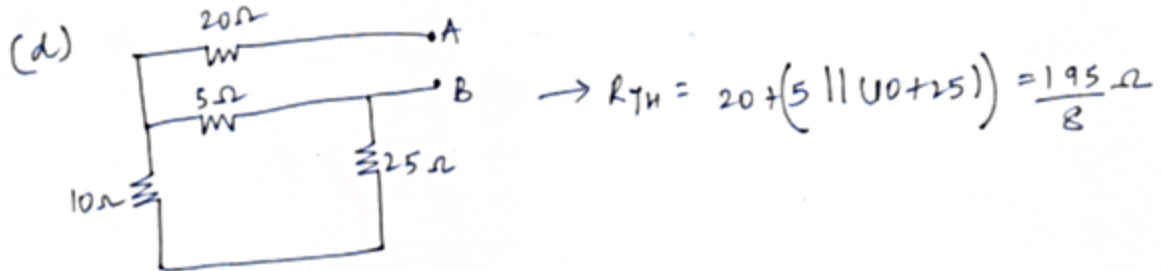
$$\Rightarrow i_A(5 + 20) = 20I_1$$

$$\Rightarrow i_A = \frac{4}{5} I_1$$

$$\Rightarrow I_1 - i_A = \frac{I_1}{5} = 0.26 \text{ A}$$

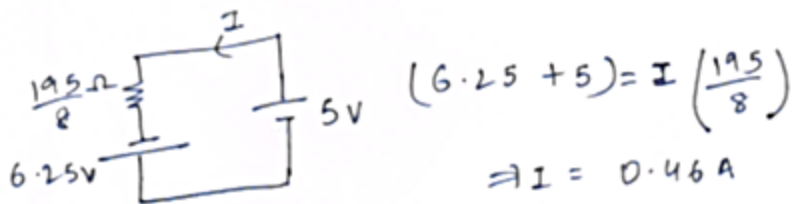
$$\therefore I = 0.2A + 0.26A = 0.46A$$

$$P_{5V} = -0.46A \times 5V = -2.31W$$



$$I_1 = \frac{2 \times 25}{25 + 10 + 5} A = 1.25 A$$

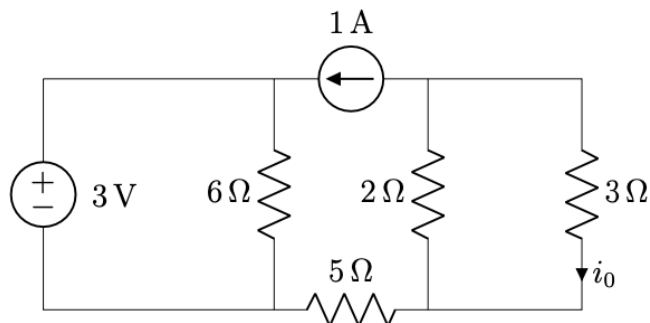
$$\therefore V_{AB} = -5I_1 = -6.25V = V_{TH}$$

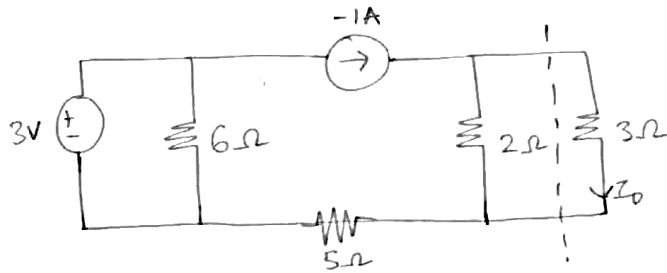


$$\therefore P_{5V} = -0.46 \times 5W = -2.31W$$

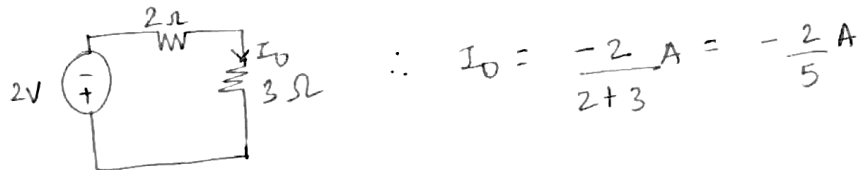
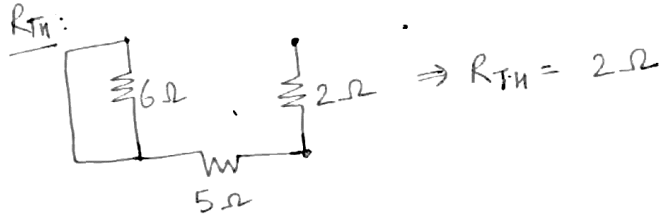
Que 3

Use Thevenin's theorem to determine i_o .



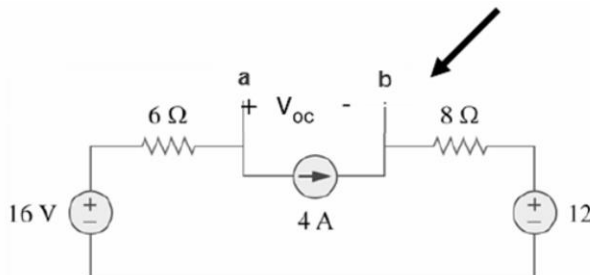
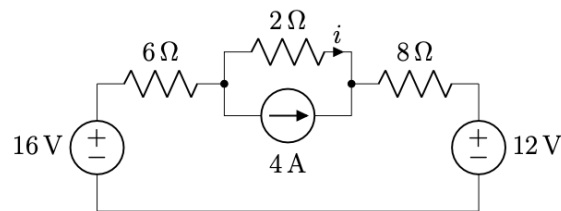


$$I_{2\Omega} = -1A \Rightarrow V_{TH} = 2 \times -1V = -2V$$



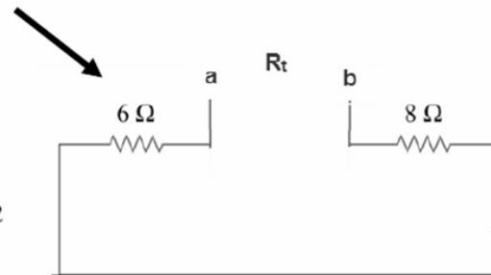
Que 4

Determine current i through 2Ω resistor by building Thevenin's equivalent for the rest of the circuit.



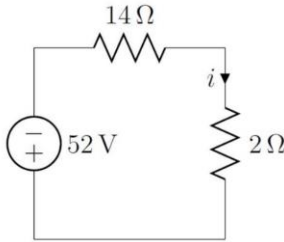
$$-16 + 4 \times 6 + v_{oc} + 4 \times 8 + 12 = 0$$

$$v_{oc} = -52V$$



$$R_t = 14\Omega$$

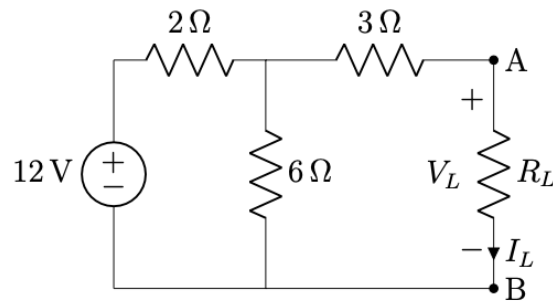
Now, the original circuit can be represented as,



Clearly $i = -3.25A$.

Que 5.

Find Voltage V_L across the load resistor R_L , and the current I_L flowing through the load resistor R_L , in the below circuit, by using Norton's Theorem. Where $R_L = 1.5\Omega$.



To compute I_N , we will short circuit terminal AB. Then the current supplied from 12V source is

$$I = \frac{12V}{2 + 6||3} = 3A$$

From current division, the current in AB is 2A. Hence, $I_N = 2A$,

To calculate the R_N , we will short circuit the voltage source. Looking from terminal A-B, the resistance is $(2||6 + 3) = 4.5 \text{ ohm}$.

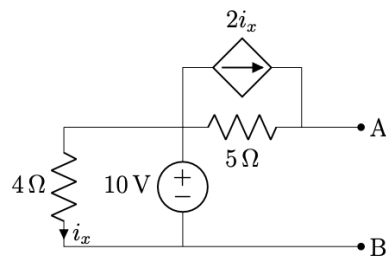
Now, from current division, the current in R_L will be

$$I_L = I_N \frac{4.5}{4.5 + 1.5} = 1.5A$$

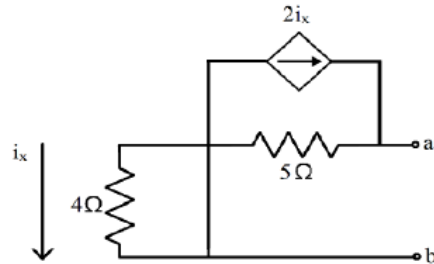
Voltage across R_L is $V_L = I_L R_L = 2.25V$.

Que 6.

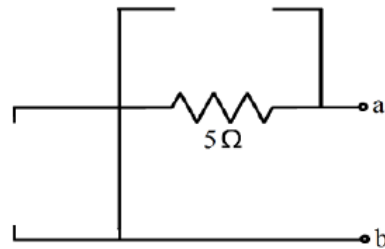
Find the Norton resistance R_N , and the Norton current I_N , at the terminals $A - B$.



Solution: Short the independent voltage source as shown below.

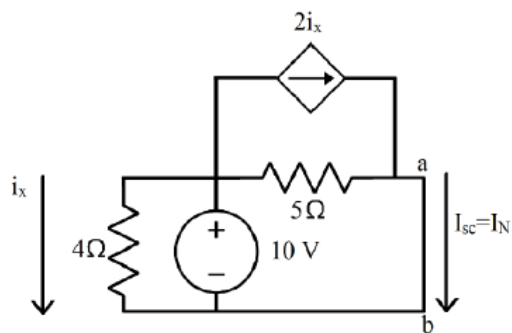


Now, $i_x = 0 \Rightarrow 2i_x = 0$, i.e. the dependent current source is open.



Therefore, $R_N = 5\Omega$

To find the Norton Current, short a-b, as shown below.



All the branches are in parallel. Therefore,

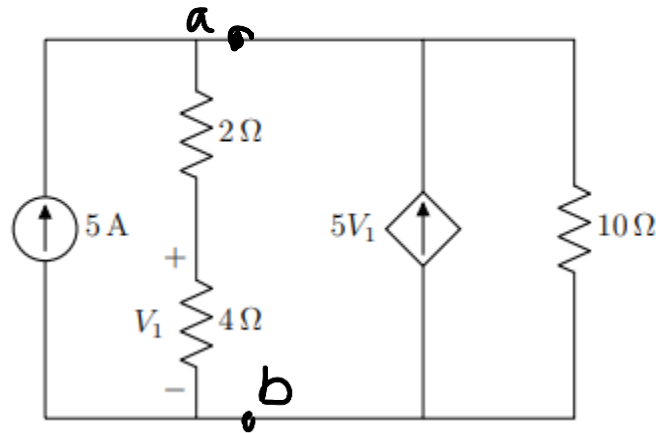
$$i_x = \frac{10}{4} = 2.5A$$

Applying KCL at node a,

$$I_{sc} = I_N = \frac{10}{5} + 2i_x = 7A$$

Que 7.

Determine the power dissipated in the 10Ω resistor in the following circuit



Take at node 'a' be V and let 'b' be reference node. Applying KCL at node 'a',

$$-5 + \frac{V}{6} - 5V_1 + \frac{V}{10} = 0 \quad \text{--- (1)}$$

also, by voltage division,

$$V_1 = \frac{V \times 4}{2+4} = \frac{4V}{6} = \frac{2V}{3} \quad \text{--- (2)}$$

From (1) and (2),

$$-5 + \frac{V}{6} - 5\left(\frac{2V}{3}\right) + \frac{V}{10} = 0$$

$$\Rightarrow \frac{V}{6} - \frac{10V}{3} + \frac{V}{10} = 5$$

$$\Rightarrow \frac{5V - 100V + 3V}{30} = 5$$

$$\Rightarrow -92V = 5 \times 30$$

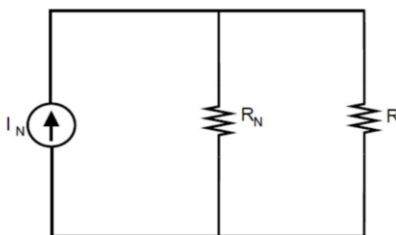
$$\Rightarrow V = -\frac{5 \times 30}{92} V$$

$$\begin{aligned} \therefore \text{Power across } 10\Omega &= \left(\frac{5 \times 30}{92}\right)^2 \times \frac{1}{10} W \\ &= \frac{25 \times 900}{920 \times 92} W = 265.83 \text{ mW} \end{aligned}$$

Que 8.

A practical current source provides $10W$ to 250Ω load and, $20W$ to 80Ω load. A resistance R_L with voltage v_L across it, and with current i_L through it, is connected to the source. Find the values of R_L , v_L , and i_L if,

- (a) $v_L \cdot i_L$ is maximum.
- (b) v_L is maximum.
- (c) i_L is maximum.



10 W to $250\ \Omega$ corresponds to 200mA . Similarly, 20W to $80\ \Omega$ corresponds to 500 mA .

By Voltage division, we have

$$I_R = I_N \frac{R_N}{R + R_N}$$

So, we have

$$0.2 = I_N \frac{R_N}{250 + R_N}$$

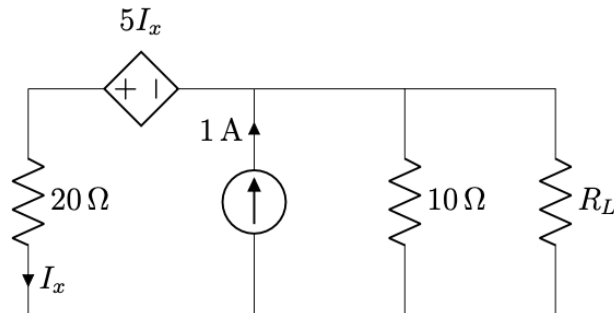
$$0.5 = I_N \frac{R_N}{80 + R_N}$$

Solving, we get $I_N = 1.7\text{ A}$ and $R_N = 33.33\ \Omega$.

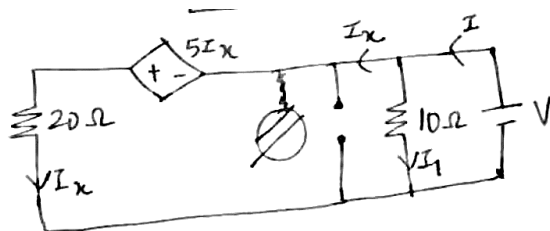
- (a) If $v_L i_L$ is a maximum, then we have $R_L = R_N = 33.33\ \Omega$, $i_L = 1.7 \times \frac{33.33}{33.33 + 33.33} = 850\text{ mA}$, $v_L = 33.33\ i_L = 28.33\text{ V}$
 - (b) If v_L is a maximum, then $v_L = I_N (R_N || R_L)$. Then v_L is a maximum when $R_N || R_L$ is a maximum, which occurs at $R_L = \infty$. Then $i_L = 0$ and $v_L = 1.7 \times R_N = 56.66\text{ V}$.
 - (c) If i_L is a maximum, then $i_L = I_N \frac{R_N}{R_N + R_L}$ is maximum when $R_L = 0\ \Omega$. So, $i_L = 1.7\text{ A}$, and $v_L = 0\text{ V}$.
-

Que 9.

Determine the value of R_L in the below circuit, such that maximum power is delivered into R_L . Calculate the value of the maximum power.



For maximum power transfer, $R_L = R_{TH}$.

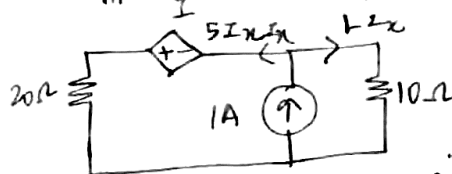


$$\frac{V + 5I_x}{20} = I_x$$

$$\Rightarrow V = 15I_x \quad (1)$$

$$\frac{V}{10} = I_1 \Rightarrow I = I_1 + I_x = \frac{V}{10} + \frac{V}{15} = \frac{V}{6}$$

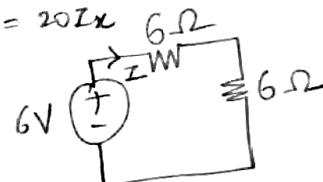
$$\therefore R_{TH} = \frac{V}{I} = V / V\left(\frac{1}{6}\right) = 6 \Omega$$



$$\text{KVL: } 10(1 - 2I_x) + 5I_x = 20I_x$$

$$\Rightarrow I_x = \frac{2}{5} \text{ A}$$

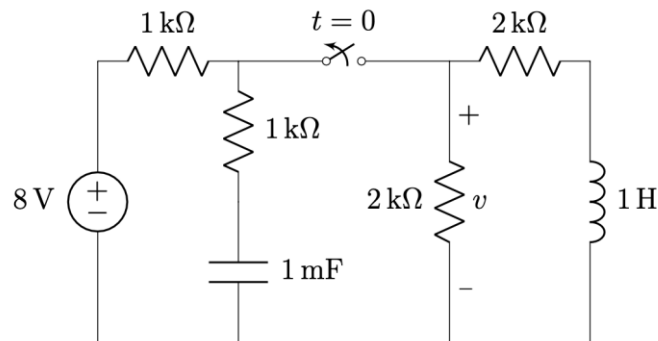
$$\therefore V_{OC} = \left(1 - \frac{2}{5}\right) \times 10 = 6 \text{ V}$$



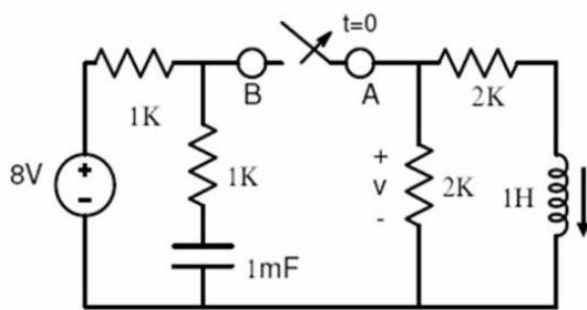
$$I = \frac{6 \text{ V}}{12 \Omega} = 0.5 \text{ A}$$

$$\therefore P_{max} = (0.5)^2 \times 6 \text{ W} = 1.5 \text{ W}$$

10. For the circuit shown below, determine the voltage across the 2K resistor (vertical) as a function of time after the switch is opened at $t = 0$.



Solution:



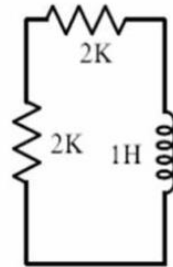
First find the inductor current

$$i_L(t) = i_L(\infty) + \{i_L(0^+) - i_L(\infty)\} \times e^{-\frac{t}{\tau}}$$

Circuit after opening the switch ($t > 0$)

$$R_{eq} = 2K + 2K = 4K$$

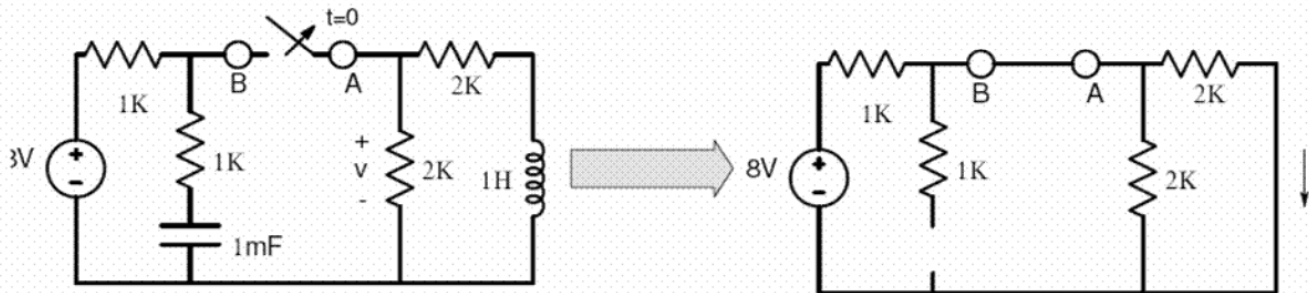
$$\tau = \frac{L}{R_{eq}} = 0.25ms$$



One can also see that : $i_L(\infty) = 0$

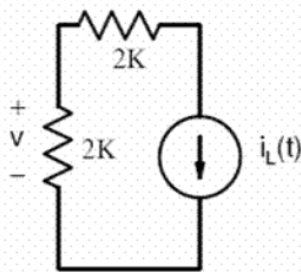
$$i_L(0^+) = i_L(0^-)$$

Circuit before opening the switch ($t < 0$) and assuming steady state condition:



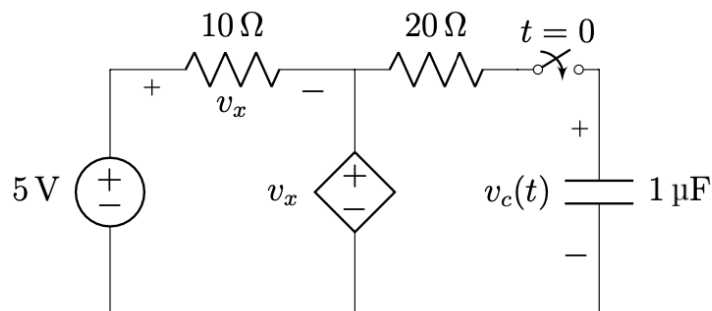
$$i_L(0^+) = i_L(0^-) = \frac{8}{(2K \parallel 2K) + 1K} \times 0.5 = 2mA \Rightarrow i_L(t) = 2 \times e^{-4000t} mA$$

Voltage across the 2K resistor:



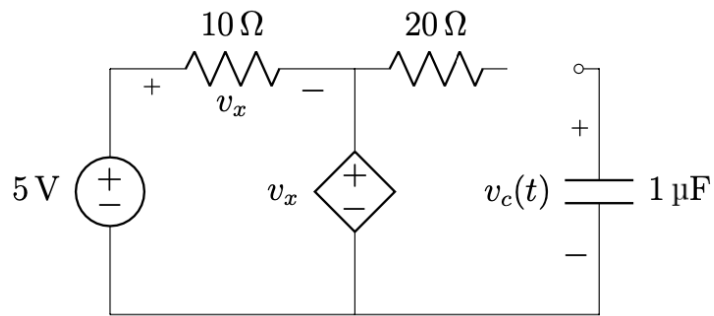
$$v(t) = -2 \times 10^3 \times i_L(t) = -4 \times e^{-4000t} V$$

11. Find $v_c(t)$ for $t > 0$ in the following circuit if the capacitor voltage is zero for $t < 0$.



Solution:

Before the circuit is closed:



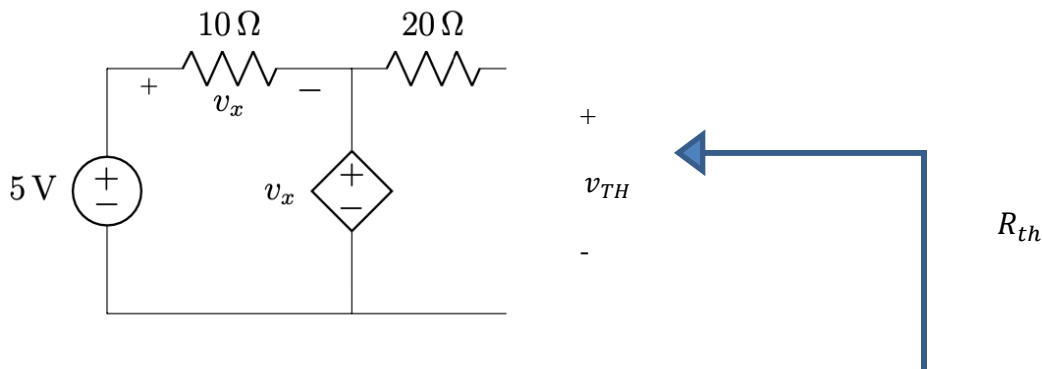
Applying KVL in the first loop

$$5 - V_x - V_x = 0$$

or

$$V_x = 2.5V$$

After the switch is closed



Thevenin voltage

$$V_{th} = 2.5V$$

Short circuit current=

$$I_{sc} = \frac{2.5V}{20} = 125mA$$

$$R_{th} = \frac{2.5V}{125mA} = 20\Omega$$

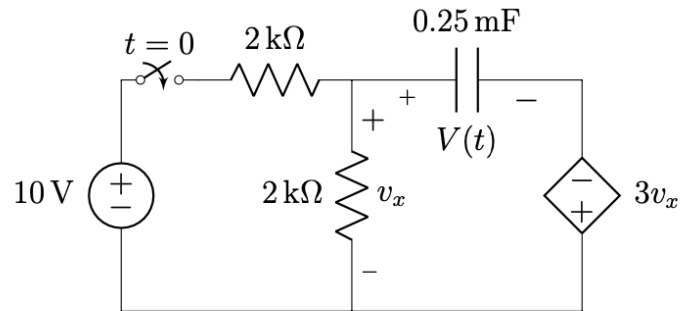
Hence, the time constant is

$$\tau = 20 \times 10^{-6} = 20\mu s$$

The voltage is given as

$$\begin{aligned} V_c(t) &= V_c(\infty) + [V_c(0) - V_c(\infty)]e^{-\frac{t}{\tau}} \\ &= 2.5 + (0 - 2.5)e^{-\frac{t}{2 \times 10^{-5}}} V \\ &= 2.5 \left(1 - e^{-\frac{t}{2 \times 10^{-5}}} \right) V \end{aligned}$$

12. Assuming that the capacitor does not have any initial charge, determine the voltage across the capacitor $V(t)$ as a function of time after the switch is closed at $t = 0$.



Solution:

$$v(t) = v(\infty) + \{v(0^+) - v(\infty)\}e^{-t/\tau}$$

$$v(0^+) = 0 \quad [1]$$

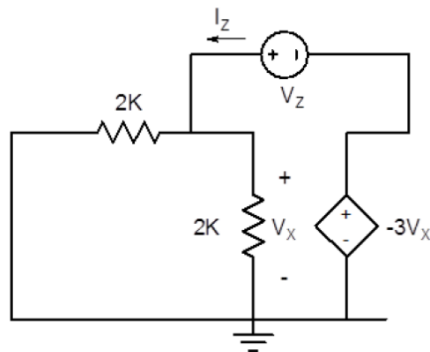
At $t \rightarrow \infty$, the capacitor is open circuit. Therefore,

$$v_X = \frac{2K}{2K + 2K} * 10 = 5V$$

$$v(\infty) = V_X - (-3V_X) = 4V_X = 20V \quad [1]$$

$$\tau = CR_{eq}$$

R_{eq} can be found from the circuit:



$$R_{eq} = \frac{v_Z}{i_Z}$$

$$v_Z = v_X - (-3v_X) = 4v_X$$

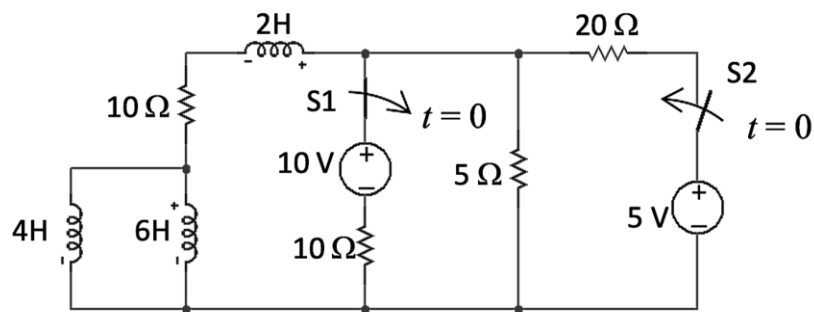
$$i_Z = \frac{v_X}{1K}$$

$$R_{eq} = \frac{v_Z}{i_Z} = 4K \quad [1]$$

$$\tau = CR_{eq} = 1s \quad [1]$$

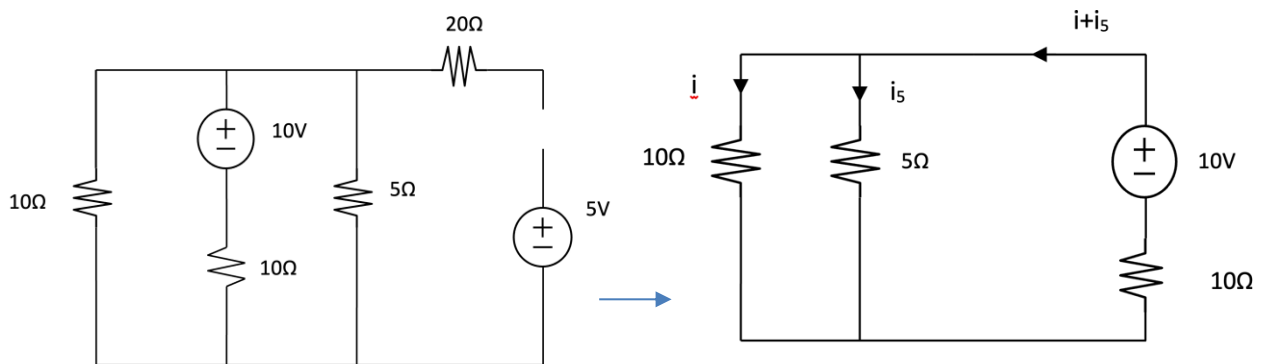
$$v(t) = 20\{1 - e^{-t}\} \quad [1]$$

13. In the following circuit the switch S1 is closed and S2 is left open for a long time. At $t=0$, S1 is opened and S2 is closed. Determine the current, i_5 , through the 5Ω resistor for all time



Solution:

For $t = 0^-$



$$R_{eq} = 10 + \left(10 \times \frac{5}{15}\right) = \left(10 + \frac{50}{15}\right) \Omega = \left(10 + \frac{10}{3}\right) \Omega$$

$$i_{5\Omega} = \left(\frac{10}{10 + \frac{10}{3}}\right) \times \frac{10}{15} A = 0.5 A$$

$$10 - 10i - 10i - 10i_5 = 0$$

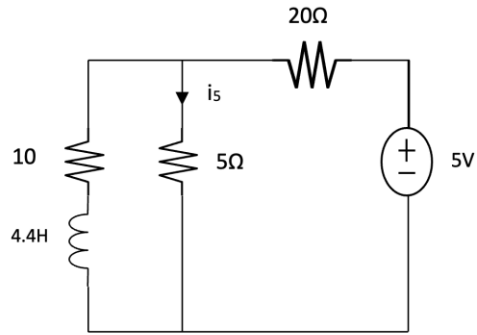
$$1 - i_5 = 2i$$

$$10 - 5i_5 - 10i - 10i_5 = 0$$

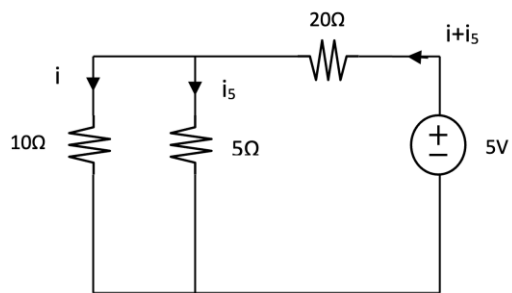
$$i = \left(\frac{1}{4}\right) A$$

$$i(0^-) = (1/4)A = i(0^+)$$

At $t > 0$



$t \rightarrow \infty$



$$5 - 20i - 20v_5 - 5i_s = 0$$

$$5 - 20i - 20i_s - 10i = 0$$

$$i = 5/70 \text{ A}, i_s = 10/70 \text{ A}$$

$$R_{th} = (20 \parallel 5) + 10 = 14 \Omega$$

$$\text{Therefore, } \tau = 4.4/14 = 0.314 \text{ s}$$

$t > 0$

$$i(t) = i(\infty) + [i(0^+) - i(\infty)]e^{-t/\tau}$$

$$\text{therefore, } i(t) = (1/14) + ((1/4) - (1/14))e^{-3.2t} \text{ A}$$

$$v_{5\Omega} = 10i + L \left(\frac{di}{dt} \right) = \frac{5}{7} + \left(\frac{5}{2} - \frac{5}{7} \right) e^{-3.2t} + (4.4) \left(\frac{1}{4} - \frac{1}{14} \right) e^{-3.2t} (-8.2) V$$

$$\text{therefore, } V_{5\Omega} = \left(\frac{10}{14} \right) (1 - e^{-3.2t}) V$$

therefore,

$$i_{5\Omega} = \left(\frac{1}{7} \right) (1 - e^{-3.2t}) A$$