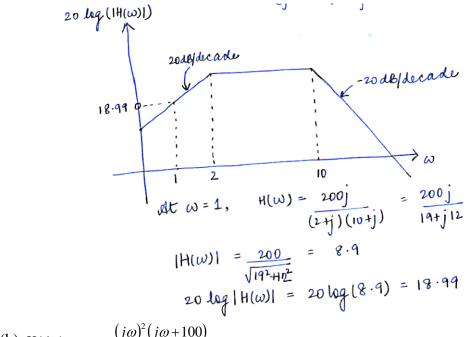
1. Draw the Bode magnitude plot for the following transfer functions.

(a)
$$H(j\omega) = \frac{200j\omega}{(j\omega+2)(j\omega+10)}$$

(b)
$$H(j\omega) = \frac{(j\omega)^2(j\omega+100)}{(j\omega+1)(j\omega+10)(j\omega+1000)}$$

Solutions:

(a) a)
$$H(j\omega) = \frac{200j\omega}{(j\omega+2)(j\omega+10)}$$



(b)
$$H(j\omega) = \frac{(j\omega)^2(j\omega+100)}{(j\omega+1)(j\omega+10)(j\omega+1000)}$$

(b)
$$H(j \omega)! = (j\omega)^{2} (j\omega+100)$$

$$(j\omega+1)(j\omega+10)(j\omega+1000)$$

$$20 \log H(\omega)!)$$

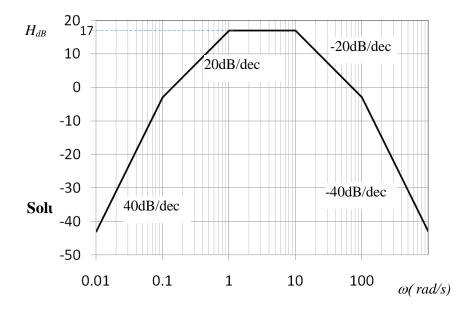
$$-80 \circ (j\omega+1)(j\omega+10)(j\omega+1000)$$

$$-80 \circ (j\omega+1)(j\omega+10)(j\omega+1000)$$

$$-80 \circ (j\omega+1)(j\omega+100)(j\omega+1000) = 10^{4}$$

$$20 \log (H(\omega)!) = -80 \log (10) = -80$$

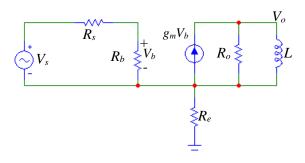
2. Find the transfer function for the following Bode plot.



H(w) =
$$\frac{A(j\omega)^{2}}{(1+j\omega)(1+j\omega)(1+j\omega)(1+j\omega)}$$

 $H(\omega=1) = 17 dB$
 $\Rightarrow 17 = 20 log \frac{A}{(1+j0)(1+j)(1+0.01j)}$
 $= 20 log (\frac{A}{10 \times 1 \times 1 \times 1})$
 $\Rightarrow 20 log A = 17 + 20 = 37$
 $\therefore A = 10^{3/20} = 70.79$
 $\therefore H(\omega) = \frac{7079(j\omega)^{2}}{(j\omega+0.1)(j\omega+10)(j\omega+100)}$

3. Determine the transfer function (V_o/V_s) for the following circuit.



Solution:

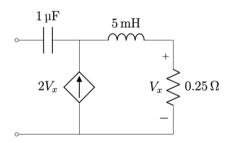
$$V_b = \frac{R_b V_S}{R_b + R_S}$$

$$I_b = \frac{V_b}{R_b} = \frac{V_S}{R_S + R_b}$$

Applying nodal

$$-gmV_b + \frac{V_0}{R_0} + \frac{V_0}{jwL} = 0$$
$$V_0 \left(\frac{1}{R_0} + \frac{1}{j\omega L}\right) = gmV_b$$

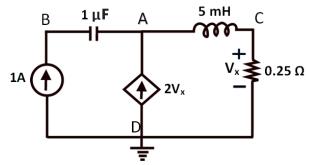
4. Determine the resonant frequency for circuit shown below.



Solution:

Calculate the Z_{eq} of the circuit and make imaginary part to be zero to calculate the resonant frequency.

To calculate the impedance, we connect a current source.



Applying KCL at node A:

$$-1 - 2V_x + \frac{V_x}{0.25} = 0$$

$$\Rightarrow -1 - 2V_x + 4V_x = 0$$

$$\Rightarrow 2V_x = 1$$

$$\Rightarrow V_x = 0.5V$$

Let say the voltage drop across the current source is V_1 .

Then applying KVL in BACDB,

$$-V_1 + \frac{1}{j\omega C} \cdot 1 + j\omega L(1 + 2V_x) + V_x = 0$$

$$\Rightarrow V_1 = \frac{1}{j\omega C} + j\omega L(1 + 2 \times 0.5) + 0.5$$

$$\Rightarrow V_1 = \frac{1}{j\omega C} + j\omega L \times 2 + 0.5$$

Hence, the impedance is

$$Z_{eq} = \frac{V_1}{1} = \frac{1}{j\omega C} + j\omega L * 2 + 0.5.$$

At resonance Im
$$(Z_{eq}) = 0$$

$$-\frac{1}{\omega_0 C} + 2\omega_0 L = 0$$

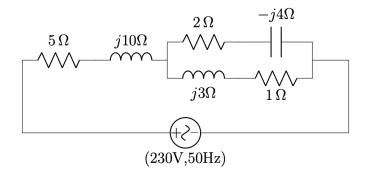
$$\Rightarrow \frac{1}{\omega_0 C} = 2\omega_0 L$$

$$\omega_0 = \frac{1}{\sqrt{2}LC} = \frac{1}{\sqrt{2} \cdot 5 \cdot 10^{-3} \cdot 10^{-6}}$$

$$\omega_0 = 10^4 \ rad/sec$$

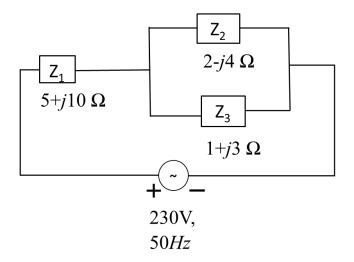
$$f_0 = \frac{\omega_0}{2\pi} = \frac{10^4}{2\pi} = 1591.5 \ Hz$$

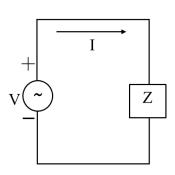
8. Find the average power and reactive power, in the network shown in figure below



Solution

The resultant circuit is





Here,

$$Z = Z_1 + (Z_2 || Z_3) = Z_1 + \frac{Z_2 Z_3}{Z_2 + Z_3}$$

$$= 5 + j10 + \frac{(2 - j4)(1 + j3)}{2 - j4 + 1 + j3}$$

$$= 5 + j10 + \frac{14 + j2}{3 - j} = 5 + 10j + \frac{(14 + 2j)(3 + j)}{10}$$

$$= 5 + 10j + \frac{1}{10}(42 + 6j + 14j - 2)$$

$$= 5 + 10j + 4 + 2j = 9 + j12 \Omega$$

& $V_{rms} = 230 \, Volts$.

Then

$$I_{rms} = \frac{V_{rms}}{Z} = \frac{230}{9 + j12} = \frac{230(9 - j12)}{225} = 9.2 - j12.27 = 15.33 \angle -53.13^{\circ} A$$

$$\Rightarrow \theta = 53.13^{\circ}$$

∴ Average Power,

$$P_{avg} = V_{rms}I_{rms}cos\theta = 230 * 15.33 * cos(53.13^{\circ})$$
 = 2115.54 W

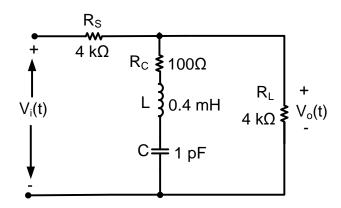
: Reactive Power,

$$P_{react} = V_{rms}I_{rms}sin\theta = 230 * 15.33 * sin(53.13^{\circ}) = 2820.72 W$$

9. A band–reject (notch) filter is shown below. Derive the expression of its transfer function H in the form

$$H(j\omega) = \frac{V_o(j\omega)}{V_i(j\omega)} = K \left[\frac{(1+ja)}{(1+jb)} \right].$$

Find out the expressions for the coefficients K, a and b. Determine the magnitudes of this transfer function at very low and very high frequencies from physical arguments. What is the resonance frequency of this circuit? What is the magnitude of the transfer function at this resonance frequency? Also calculate the level of rejection (in dB) at resonance frequency.



Connecting to phase domain, The following the following to phase domain, The following the fol

$$\Rightarrow z_1 = R_L \left[R_C + j \left(w_L - \frac{1}{w_C} \right) \right]$$

$$R_L + R_C + j \left(w_L - \frac{1}{w_C} \right)$$

Applying noltage division,

$$V_0(j\omega) = \frac{Z_1 \times V_i(j\omega)}{Z_1 + R_s}$$

$$\Rightarrow \frac{V_0(j\omega)}{V_1(j\omega)} = \frac{Z_1}{Z_1 + R_S}$$

$$\Rightarrow \frac{V_0(j\omega)}{V_i(j\omega)} = \frac{R_L\left[R_C+j\left(\omega L - \frac{1}{\omega C}\right)\right]}{R_L + R_C + j\left(\omega L - \frac{1}{\omega C}\right)}$$

$$\frac{R_{L}\left[R_{C}+j\left(\omega L-\frac{1}{\omega c}\right)\right]}{R_{L}+R_{C}+j\left(\omega L-\frac{1}{\omega c}\right)}+R_{S}$$

$$\Rightarrow \frac{V_0(j\omega)}{V_1(j\omega)} = R_L R_C + jR_L (\omega L - \frac{1}{\omega_C})$$

$$\frac{V_1(j\omega)}{V_1(j\omega)} = \frac{R_L R_C + jR_L + R_S R_C + j(\omega L - \frac{1}{\omega_C})(R_S + R_L)}{R_L R_C + R_S R_L + R_S R_C + j(\omega L - \frac{1}{\omega_C})(R_S + R_L)}$$

$$\Rightarrow \frac{V_0(j\omega)}{V_1(j\omega)} = \frac{R_L R_C \left[1 + \frac{1}{R_C} \left(\omega L - \frac{1}{\omega_C}\right)\right]}{R_L R_C + R_S R_L + R_S R_C \left[1 + \frac{1}{R_C} \left(R_L R_C + R_S R_L + R_S R_C\right)\left(\omega L - \frac{1}{\omega_C}\right)\right]}$$

$$\therefore K = \frac{R_L R_C}{R_L R_C + R_S R_L + R_S R_C}$$

$$\therefore K = \frac{R_L R_C}{R_L R_C + jR_L + R_C R_C}$$

$$K = \frac{R_L R_C}{R_L R_C + R_S R_L + R_S R_C}$$

Substituting the natures of RL, RS, Rc, K = 1/42. $a = \frac{1}{RC} \left(wL - \frac{1}{wc} \right) , b = \frac{(Rs + RL) \left(wL - \frac{1}{wc} \right)}{\left(R_L R_C + R_S R_L + R_S R_C \right)}$

For very low frequencies, $\omega \to 0$, $\chi_{\perp} \to 0$ and $\chi_{c} \to \infty$. Therefore, the ER-L-C branch is open xizcinted.

for very high frequencies, w > 00, XL - 00, Xc - 0.

Again Again, the R-L-C branch is open excented. : Hyw) w-roo = RL = 0.5

For resonance, Im[H(jw)]=0

Resonance,
$$2m \left[H(j\omega) \right]^{-1}$$

$$K \left[\frac{1+ja}{1+jb} \times \frac{1-jb}{1-jb} \right] = K \left[\frac{1-jb+ja+ab}{1+b^2} \right] = K \left[\frac{1+j(a-b)+ab}{1+b^2} \right]$$

$$\Rightarrow a - b = 0$$

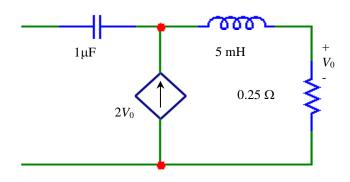
$$\Rightarrow \omega_0 = \frac{1}{\sqrt{LC}} \Rightarrow f_r = \frac{1}{2\pi\sqrt{LC}}$$

$$f_{k} = \frac{1}{2\pi \sqrt{0.4 \times 10^{3} \times 10^{12}}} + \frac{1}{2\pi \sqrt{0.4 \times 10^{3} \times 10^{12}}}$$

$$f_{k} = \frac{1}{4 \cdot 96 \text{ MHz}}$$

$$|H(j\omega)|_{\omega=2\kappa f_{k}} = \frac{1}{1 + 6^{2}} \left(\begin{array}{c} 1 + ab \\ 1 + b^{2} \end{array} \right) \left(\begin{array}{c} (a) \\ (a) \\ (a) \\ (a) \\ (b) \\ (b) \\ (a) \\ (b) \\ (b) \\ (b) \\ (a) \\ (a) \\ (a) \\ (b) \\ (b) \\ (a) \\ (a) \\ (a) \\ (b) \\ (b) \\ (a) \\ (a) \\ (b) \\ (b) \\ (b) \\ (a) \\ (a) \\ (b) \\ (b) \\ (a) \\ (b) \\ (b) \\ (b) \\ (c) \\ (c$$

10. Determine the resonant frequency of the following circuit



Solution:

$$V_0 = (i + 2V_0)^{0.25}$$

 $V_0 = 0.25i + 0.5V_0$
 $V_0 = 0.25i$
 $V_0 = 0.25i$
 $V_0 = 0.25$
 $V_0 = 0.25$
 $V_0 = 0.25$
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 $V_0 = 0.25$

Converting to prove domain.

$$J_{-j \times 0^{6}}$$
 i $J_{\omega} = J_{\omega} = J_{\omega$

at revonance,
$$X_L = X_C$$

:. $W_r = 10^4 \text{ rad/sec}$