

# ESC201: INTRODUCTION TO ELECTRONICS

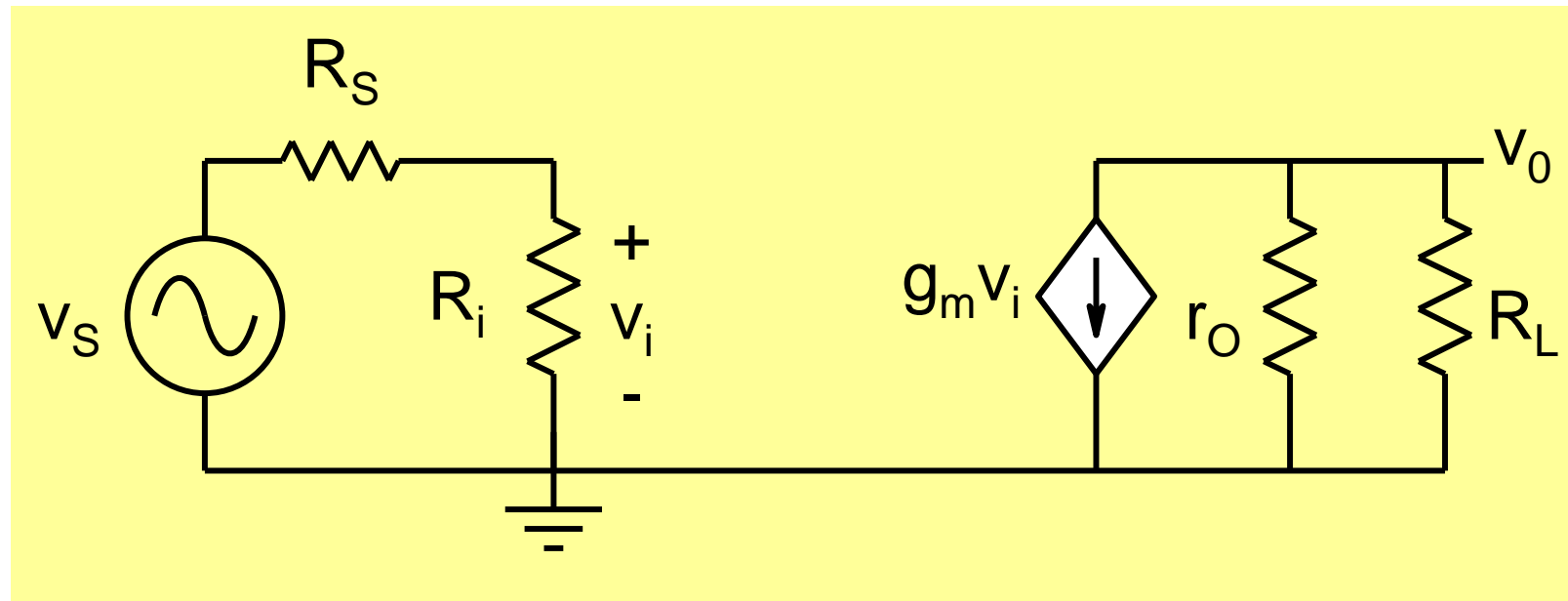
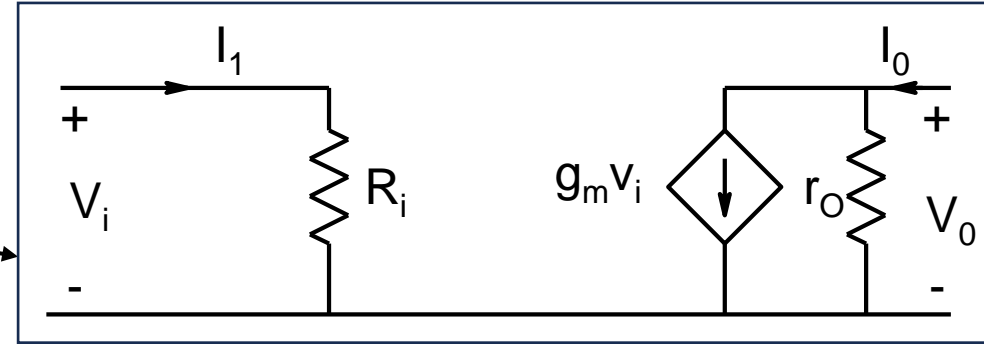
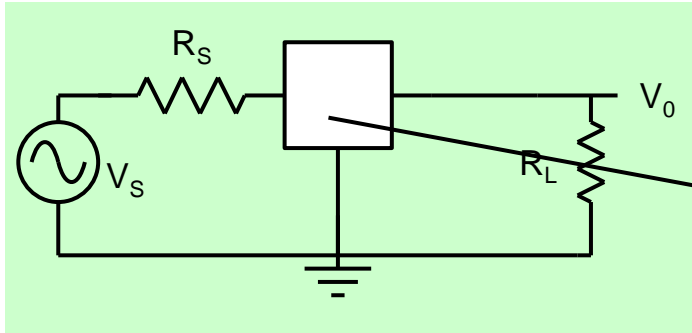
## MODULE 5: AMPLIFIERS



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Assistant Professor,  
Department of Electrical Engineering,  
IIT Kanpur



# Amplifier circuits

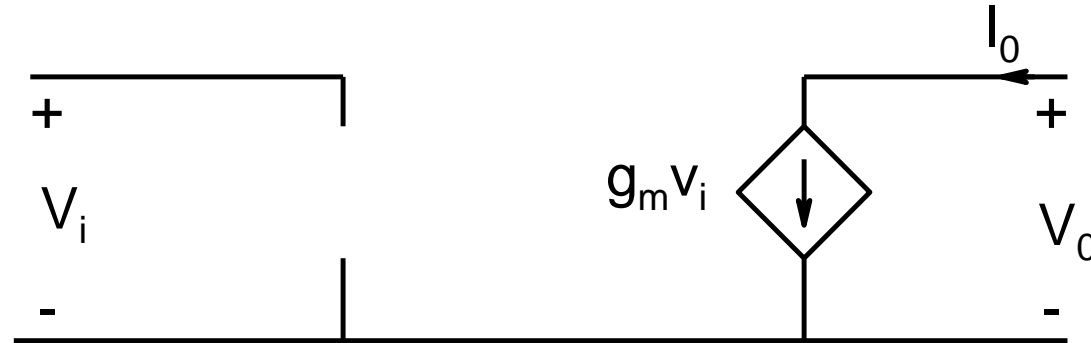


# Ideal transistor

$$A_V = \frac{V_o}{V_s} = -g_m r_o \times \frac{R_L}{r_o + R_L} \times \frac{R_i}{R_i + R_s}$$

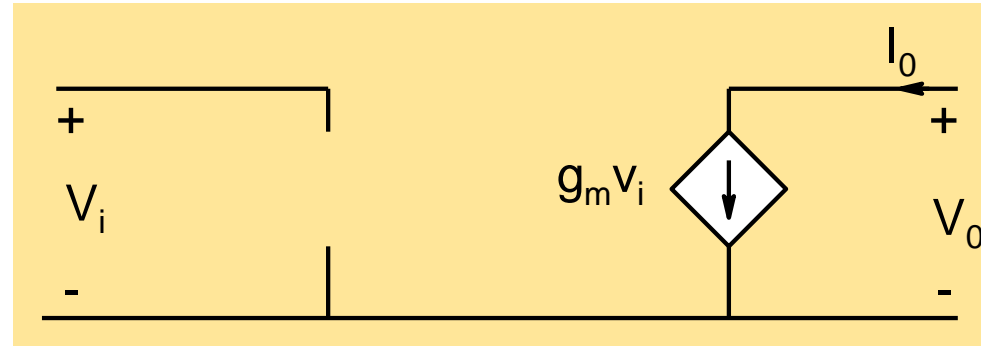
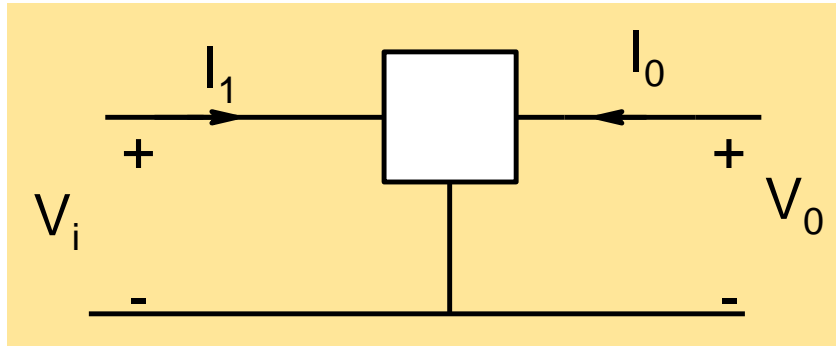
- Ideally,  $r_o$  and  $R_i$  are infinite

$$A_V = -g_m R_L$$

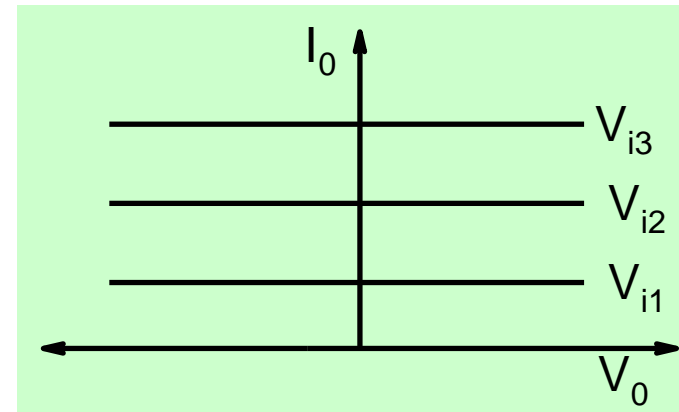
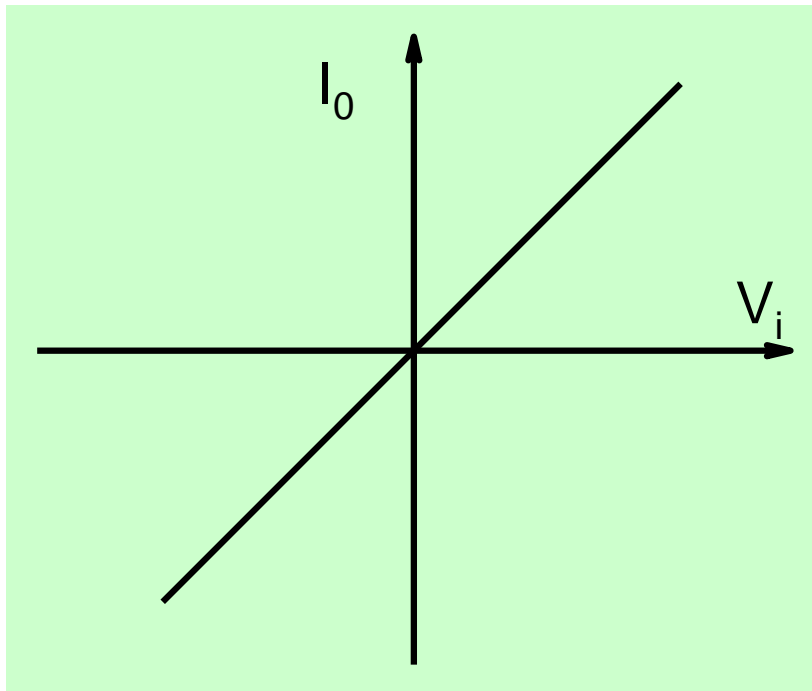


Key device needed: voltage controlled current source

# Ideal transistor characteristics

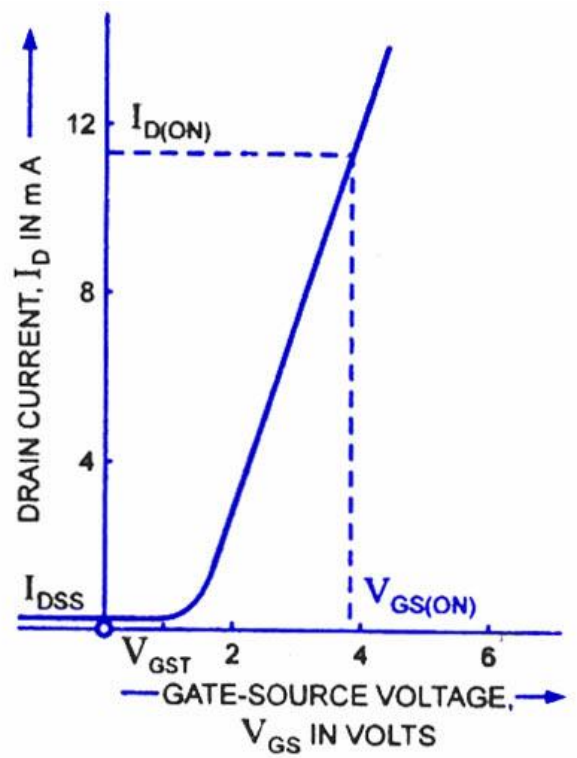
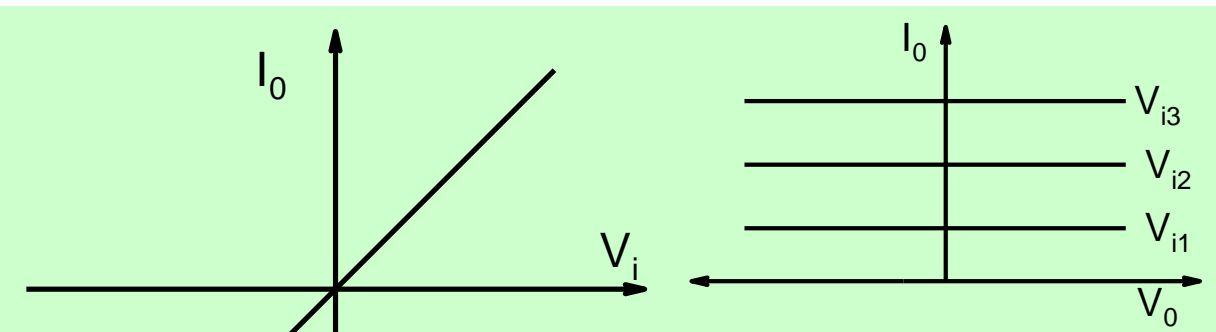


$$A_V = \frac{v_o}{v_s} = -g_m R_L$$

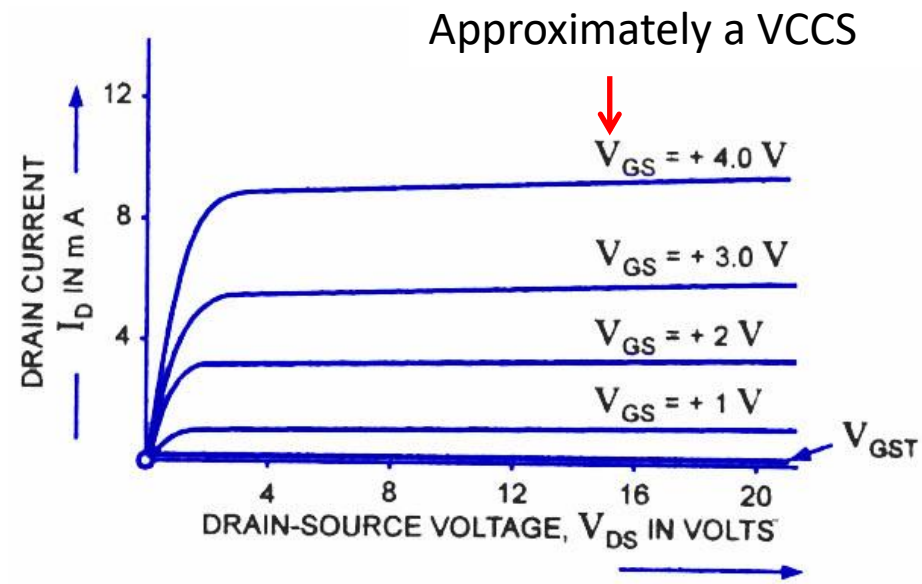


In practice there is no element which has the characteristics of ideal transistor !

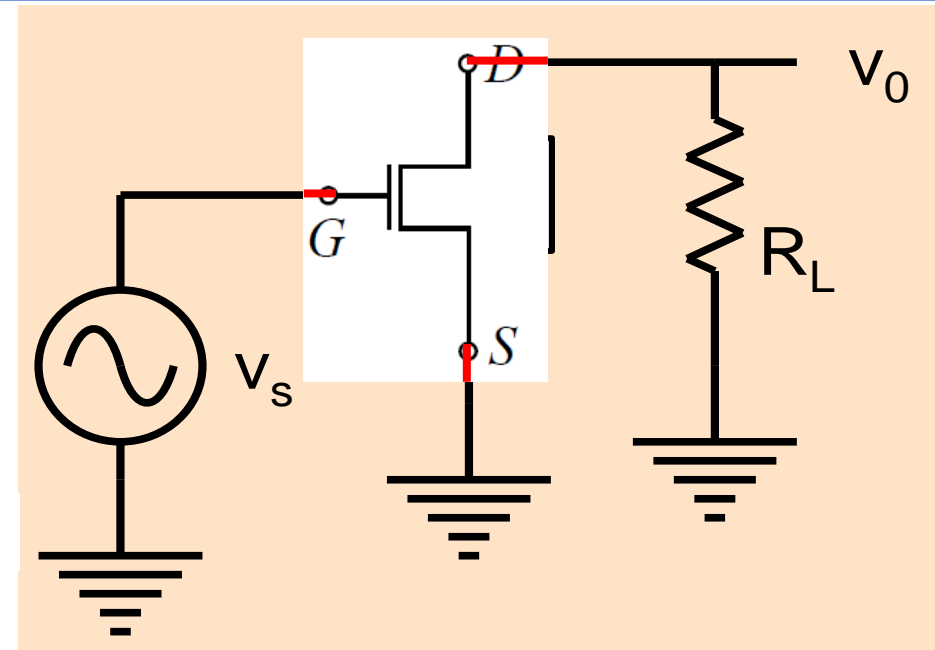
# Real transistors



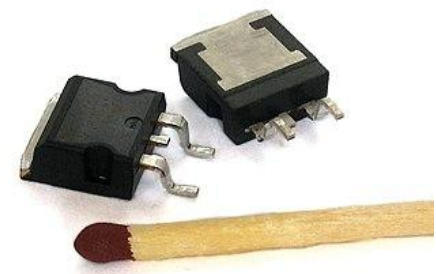
Transfer Characteristic



Drain Characteristics

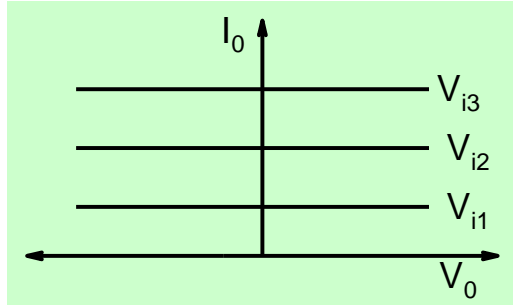
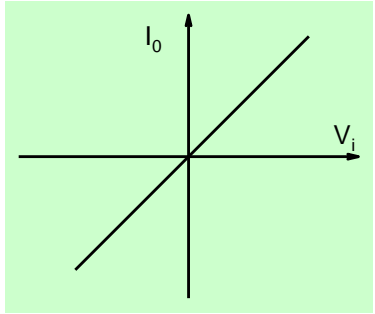


metal-oxide-semiconductor  
field-effect transistor  
MOSFET

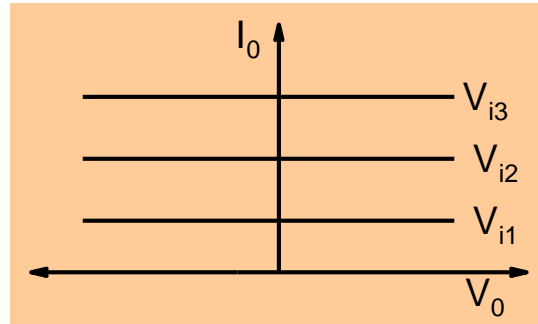
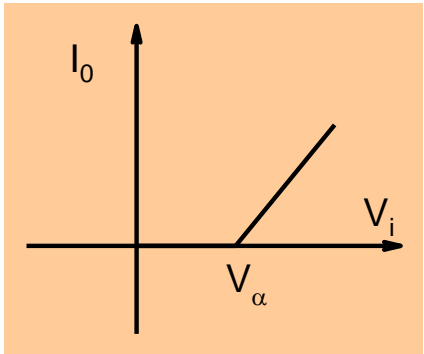


# Real Devices to Amplifiers

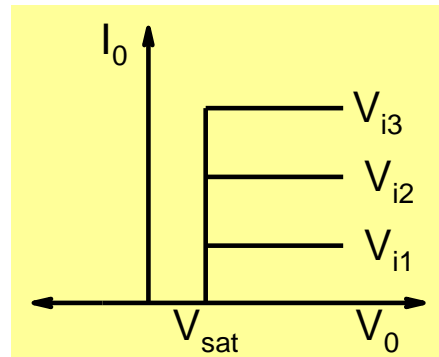
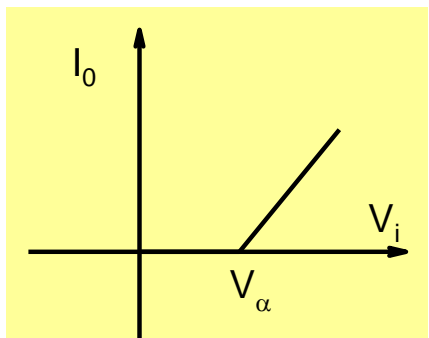
## Ideal transistor



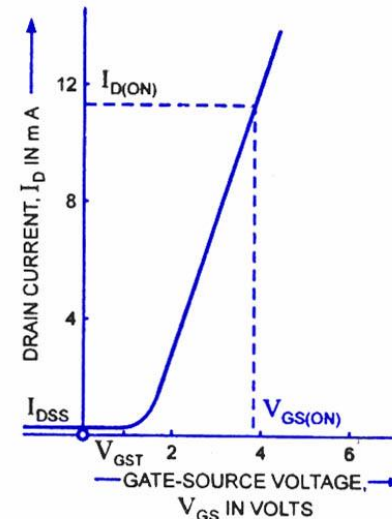
How do we use devices such as X, Y etc to make amplifiers?



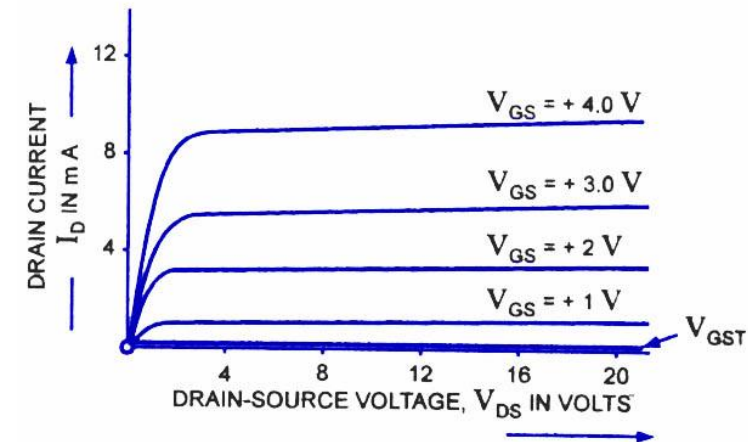
Device X



Device Y



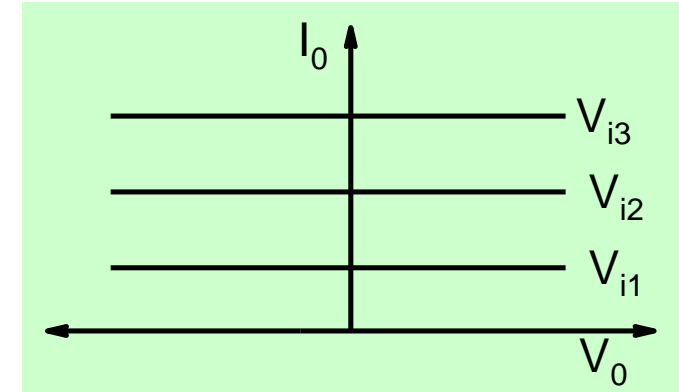
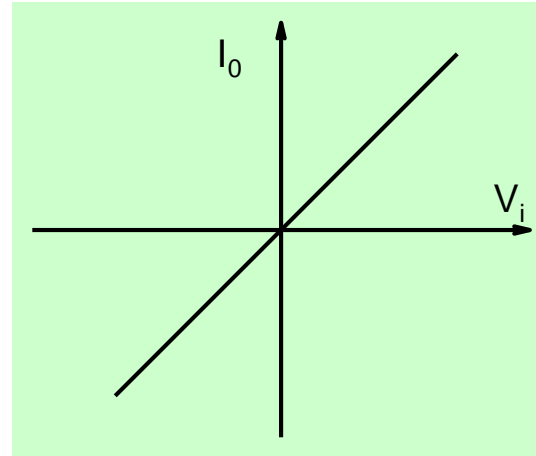
Transfer Characteristic



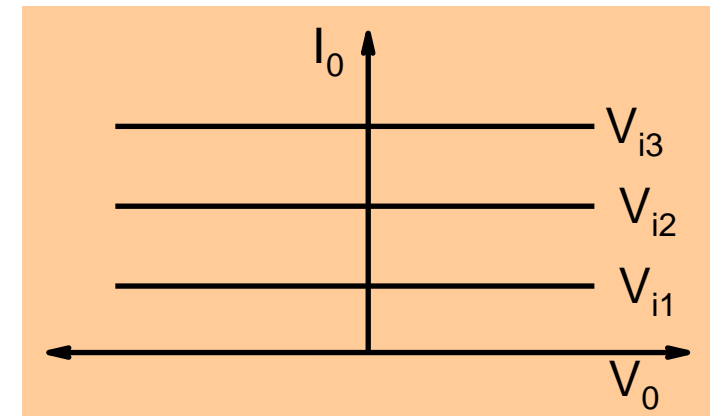
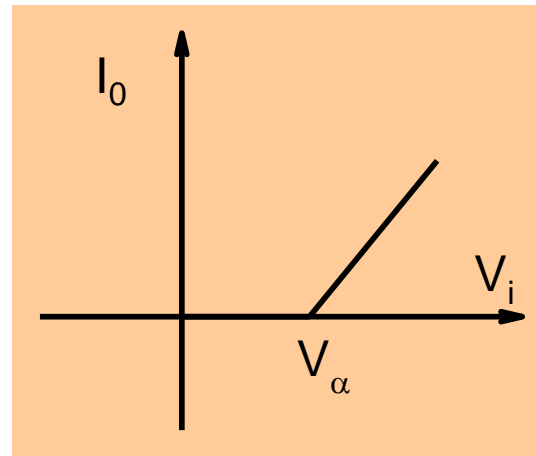
Drain Characteristics

# Simplified model X

Ideal transistor

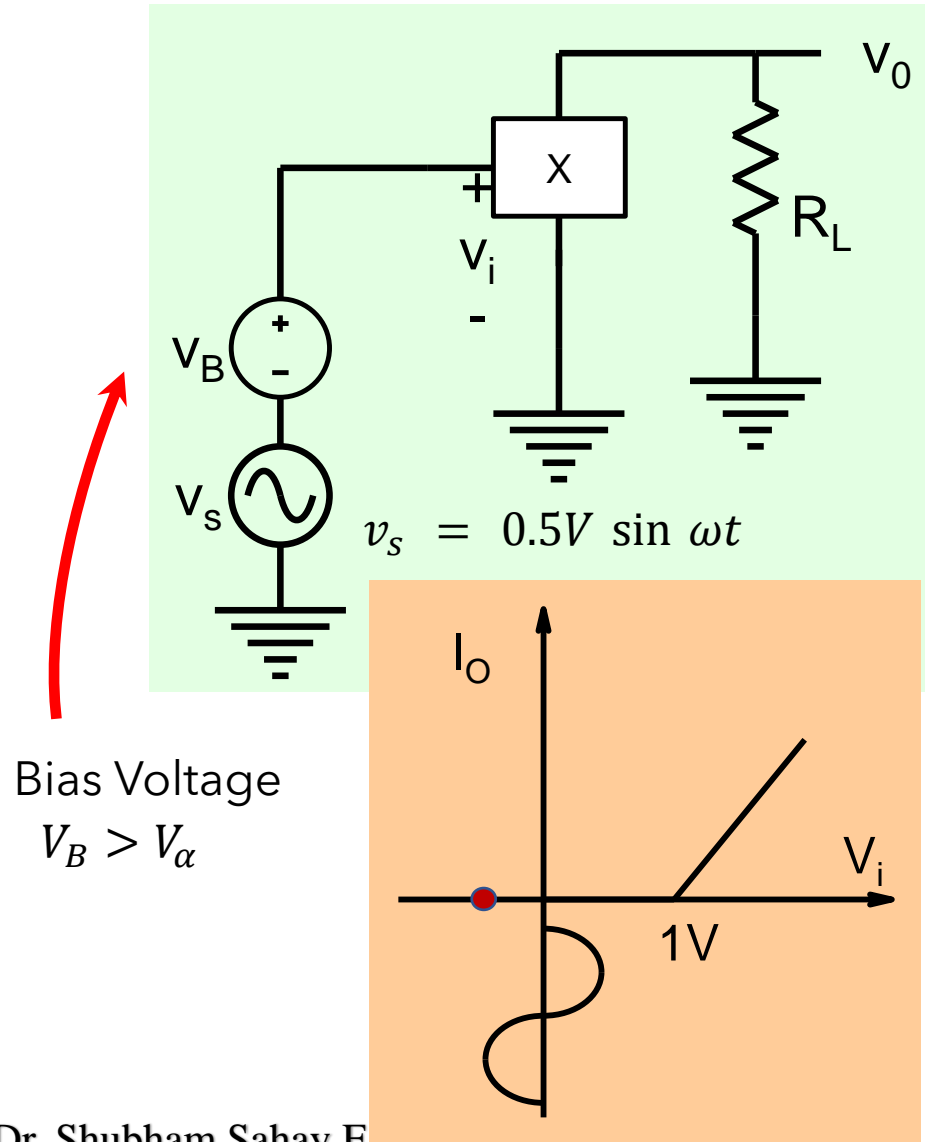


Device X (non-linear)



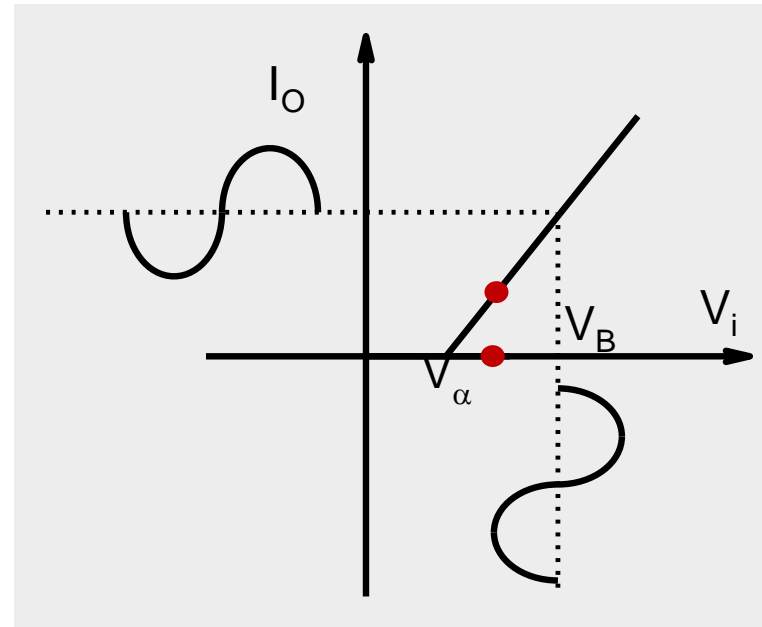
$$I_o = \begin{cases} 0 & \text{for } V_i \leq V_\alpha \\ g_m(V_i - V_\alpha) & \text{for } V_i > V_\alpha \end{cases}$$

# Amplifier with biasing



$$V_\alpha = 1V; g_m = 0.01\Omega^{-1}$$

$$R_L = 1K;$$



$$V_o = -I_o R_L$$

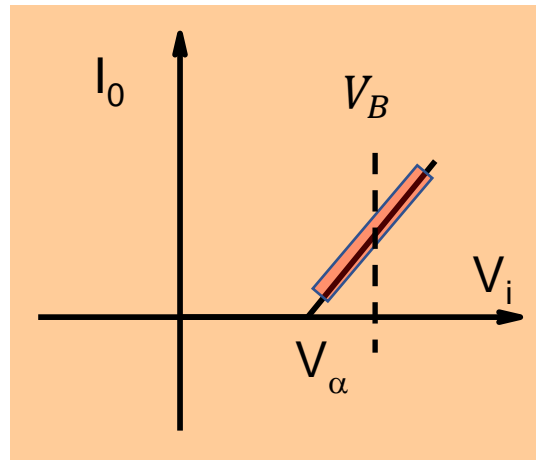
## Biasing

When only a part of device characteristics is suitable for amplification, then we need to push the device into that region by applying suitable bias voltages.



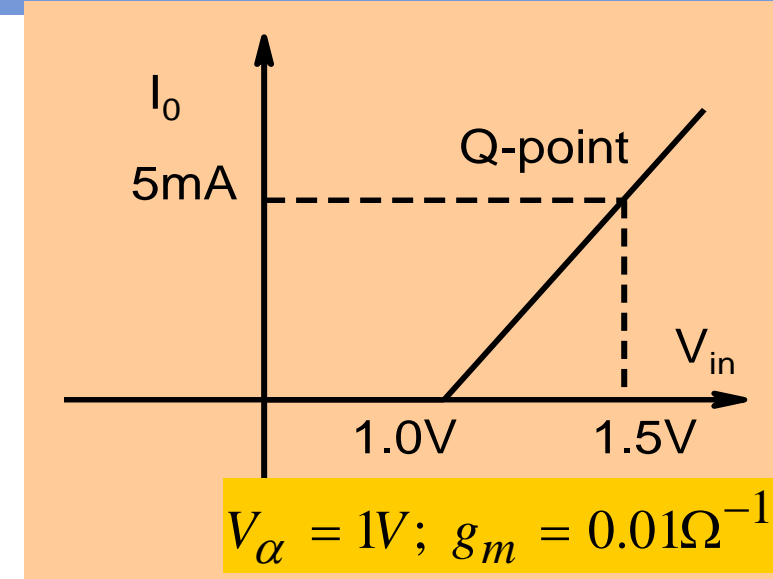
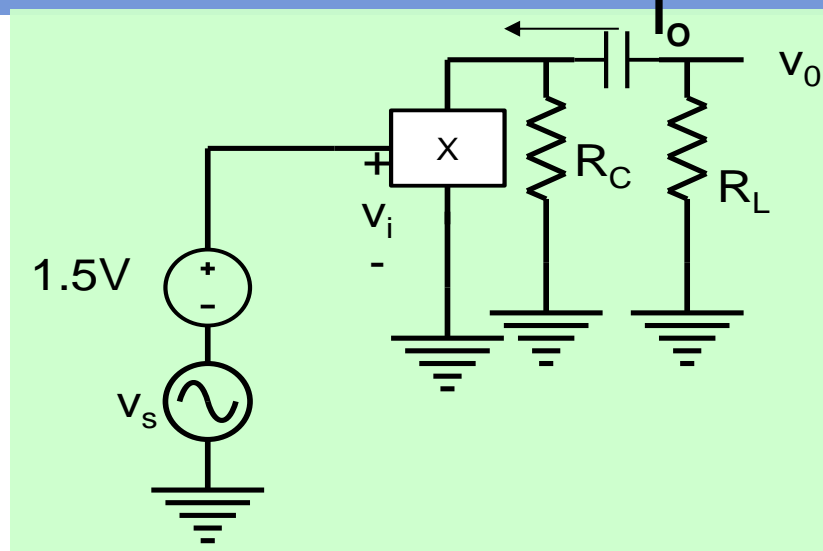
# How to choose the bias voltage $V_B$ ?

- Choose  $V_B$  as the center point of desired operating range
- Otherwise: clipping!



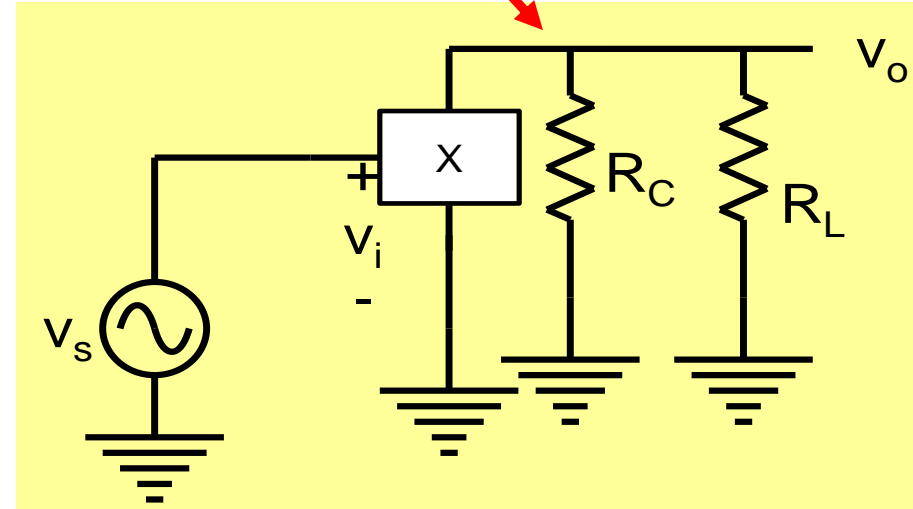
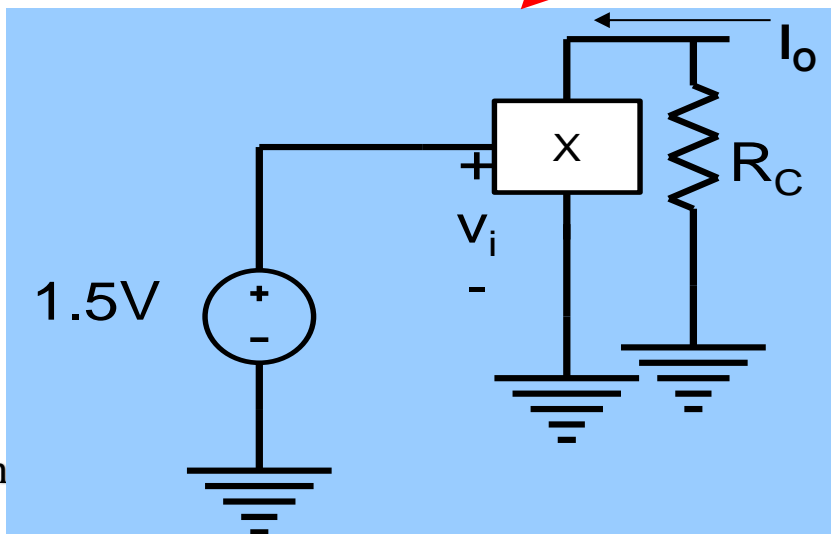
$V_B$  : Bias point or Quiescent point (Q-point)

# DC vs AC Components



dc

ac  
(signal)



Capacitor is chosen large enough so that at the signal frequency ,

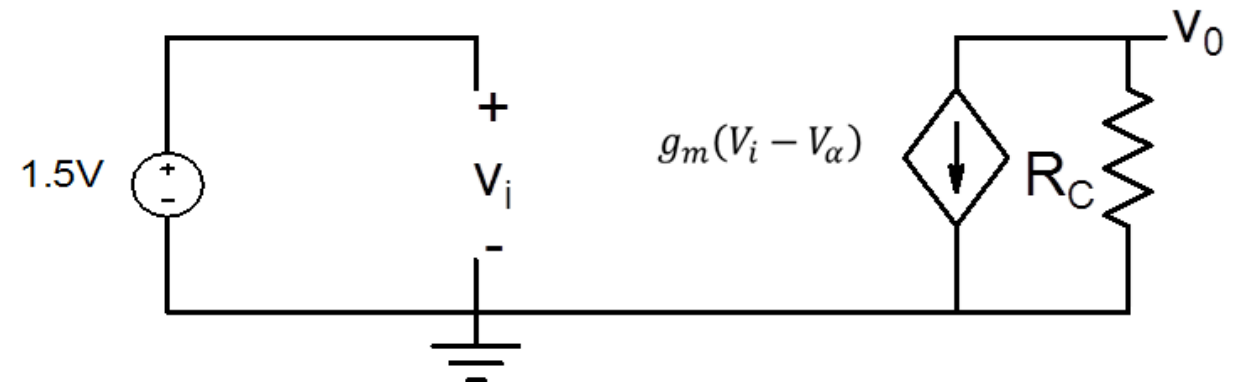
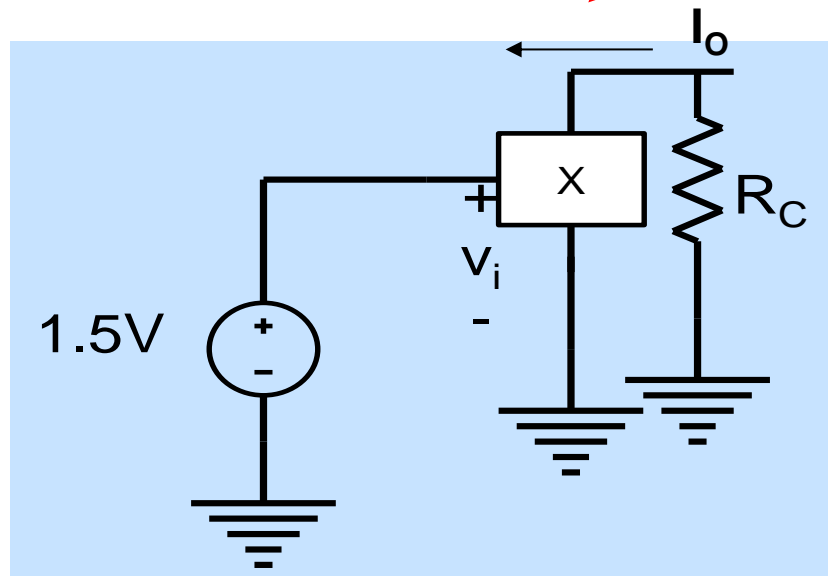
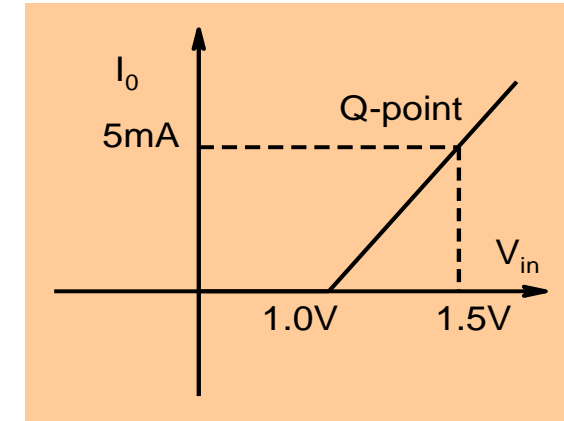
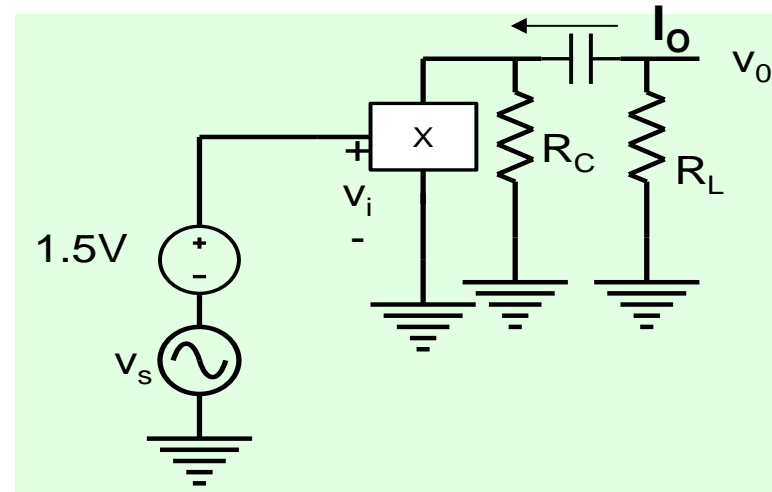
$$\frac{1}{j\omega C} \sim 0.$$

# Large signal model: non linear

$$V_{\alpha} = 1V;$$

$$g_m = 0.01\Omega^{-1}$$

Large signal model  
(aka dc model)



$$V_i = 1.5V$$

$$I_o = g_m(V_i - V_{\alpha}) = 5mA$$

Non-linear characteristics since superposition does not hold

# Small signal method

- Operate at some bias point  $V_D, I_D$
- Superimpose small signal  $v_d$  on top of  $V_D$
- Response  $i_d$  to small signal  $v_d$  is approximately linear.

- Also known as
  - Incremental model
  - Linearized model
  - AC model

$$i_D = I_D + i_d$$

signal

Bias

Additional  
small  
signal

$$v_D = V_D + v_d$$

signal

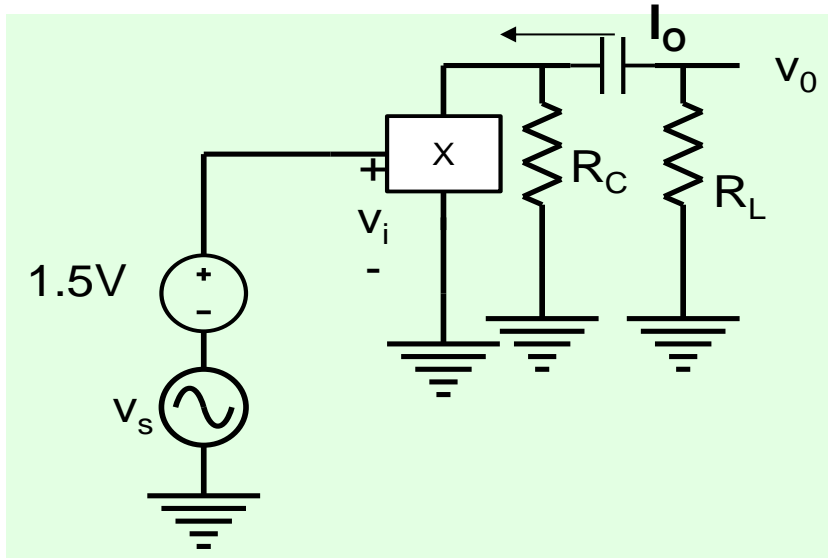
Bias

Additional  
small  
signal

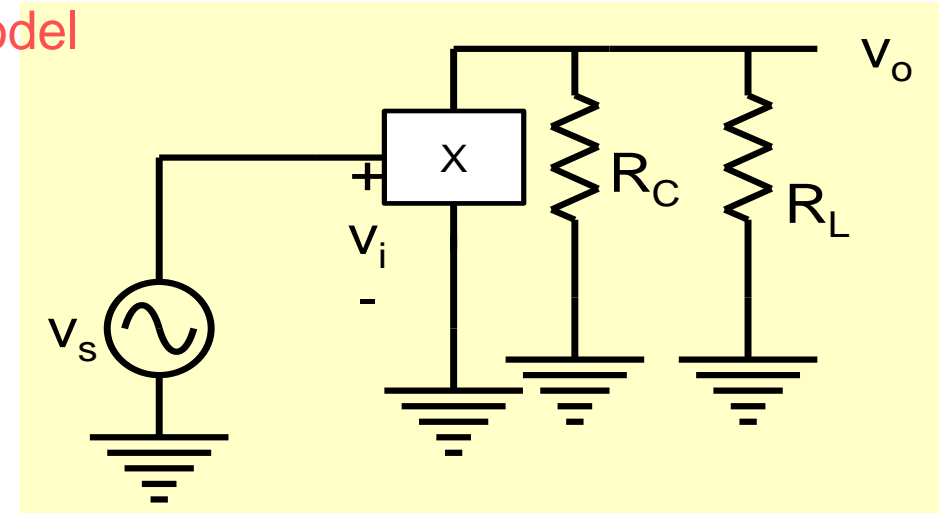
Linear

$$i_d = k v_d$$

# Small signal model: linear



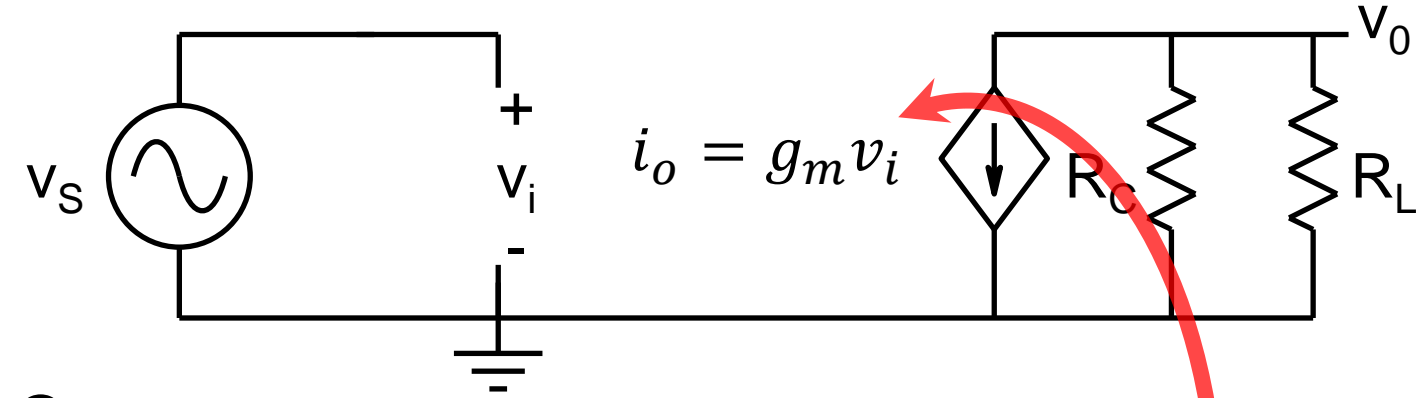
Small signal model  
aka ac model



# Small signal model

input

$$\bar{v}_i = V_i + v_i$$



Output

$$V_i \rightarrow$$

$$I_o = g_m(V_i - V_\alpha)$$

$$V_i + v_i \rightarrow$$

$$I_o + i_o = g_m(V_i + v_i - V_\alpha)$$

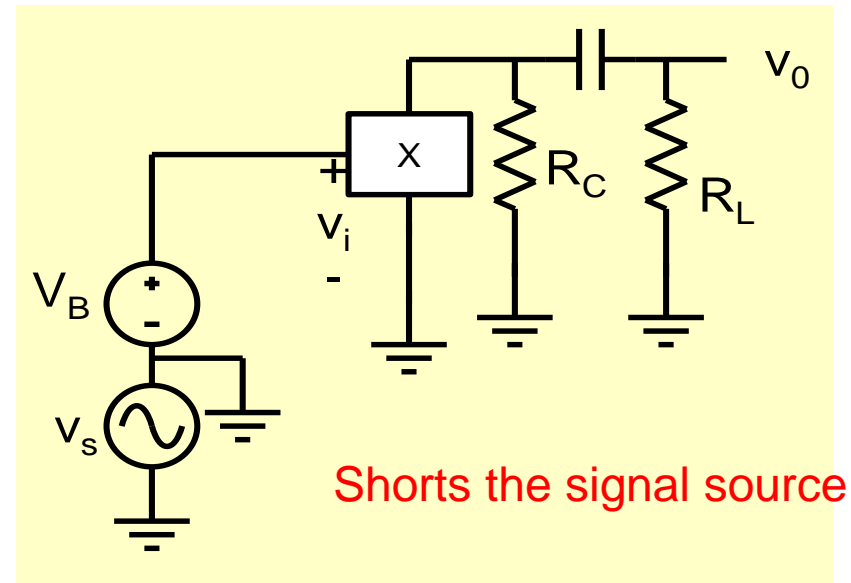
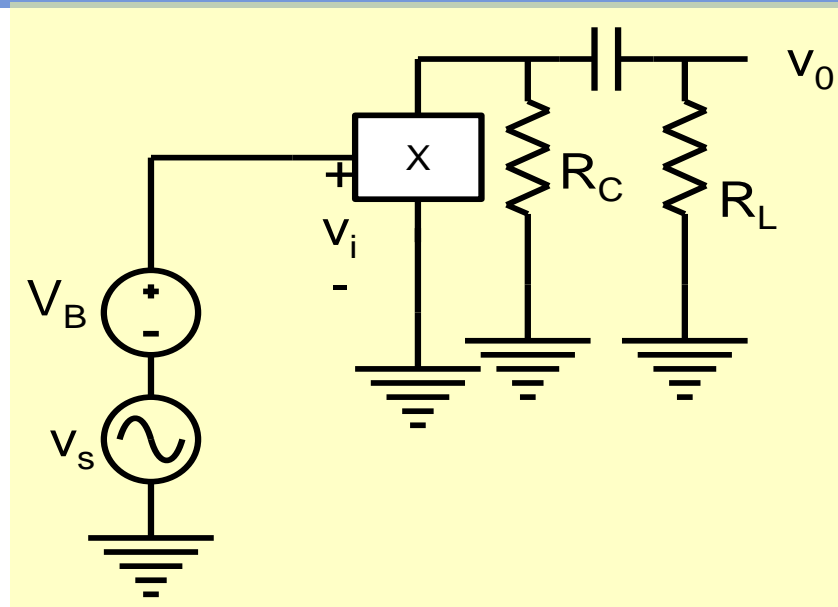
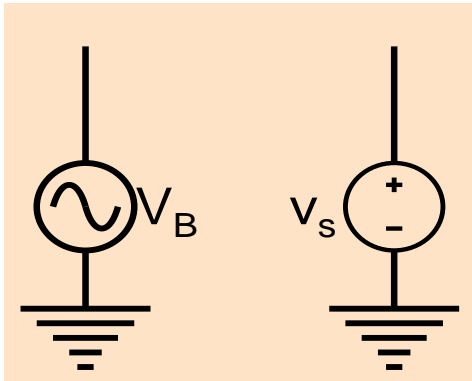
$$\text{additional } v_i \rightarrow$$

$$i_o = g_m(v_i)$$

$$v_o = -g_m v_i (R_C || R_L)$$

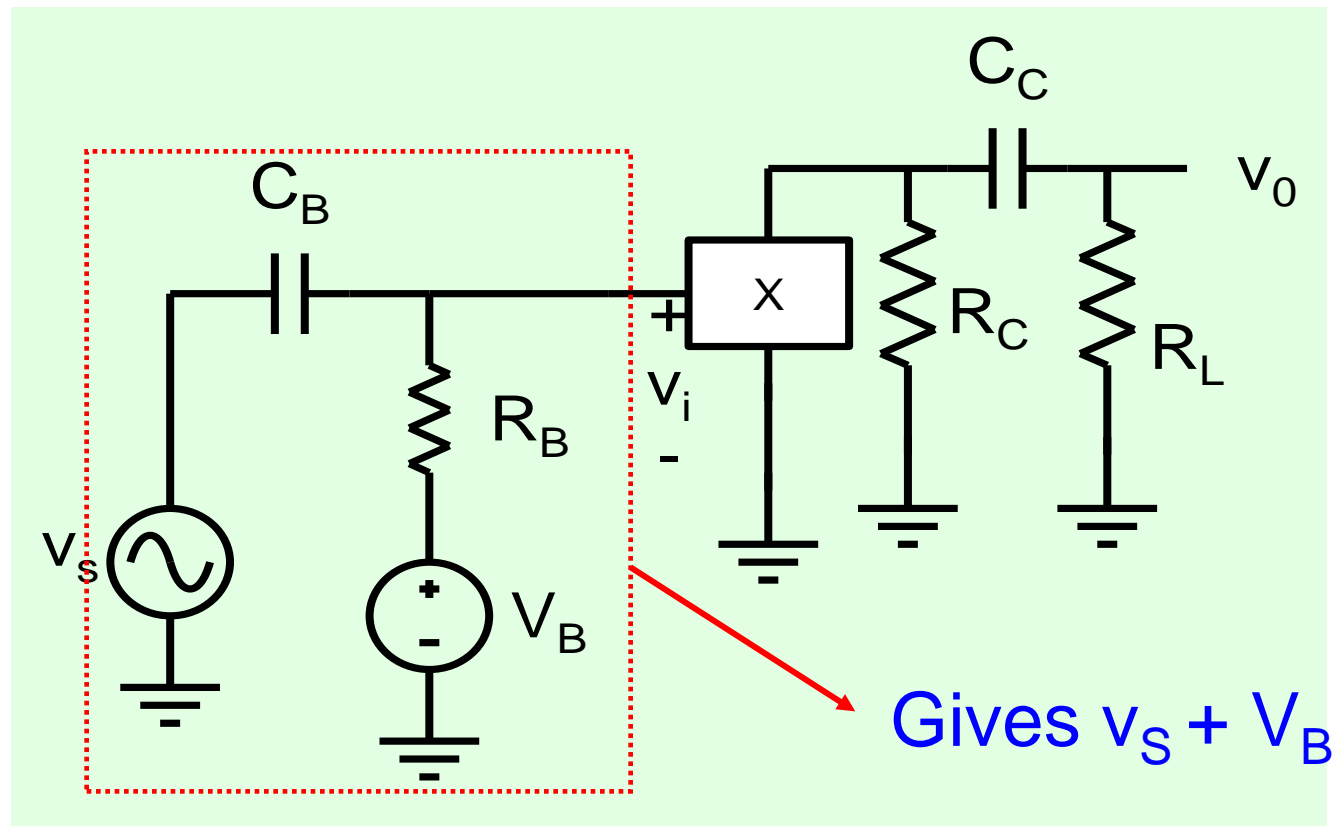
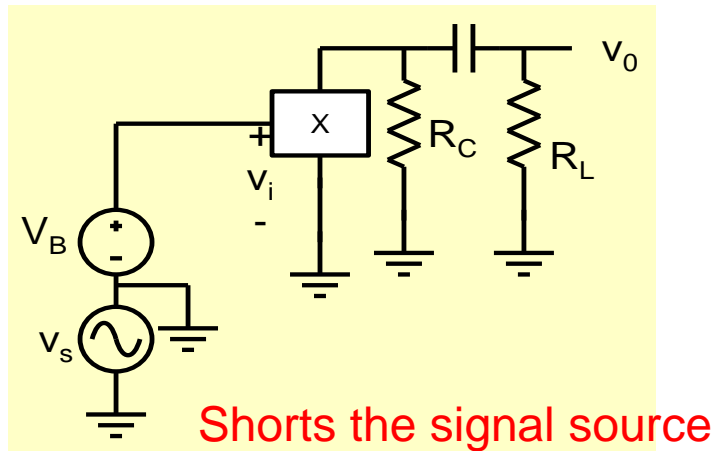
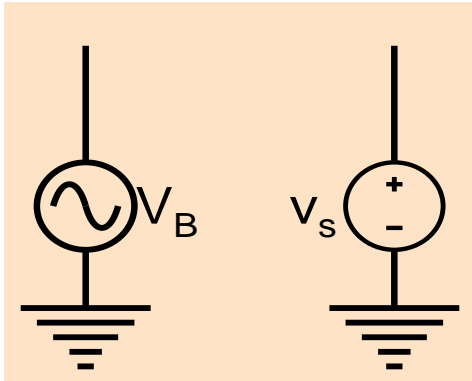
# Alternative biasing technique

What happens if both dc voltage source and signal source have one terminal as ground?



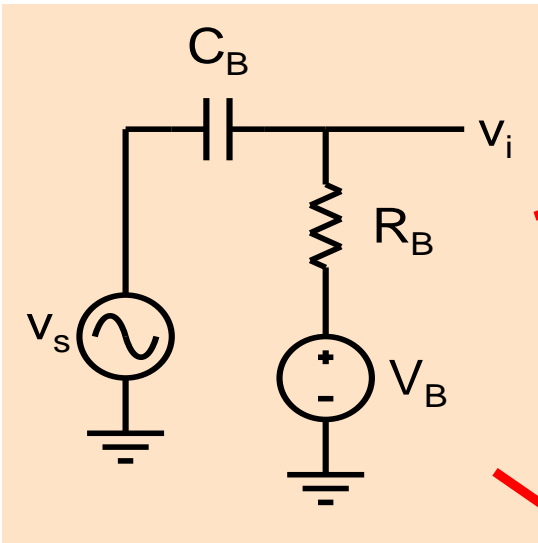
# Alternative biasing technique

What happens if both dc voltage source and signal source have one terminal as ground?

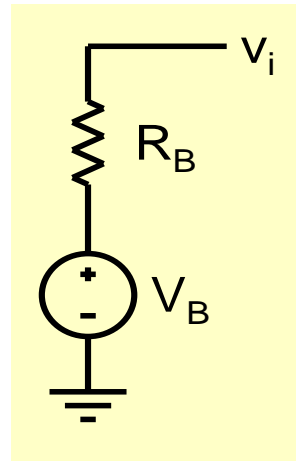




# Alternative biasing technique

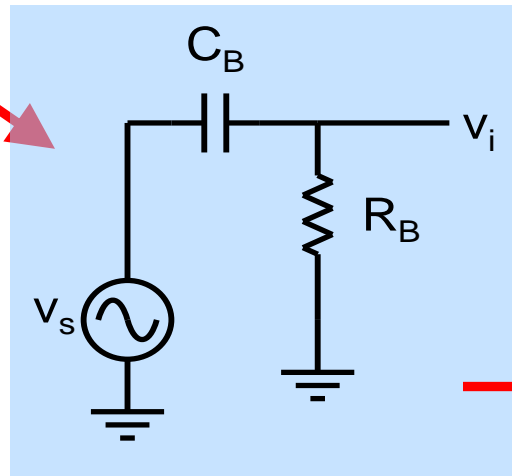


Note the role of  $R_B$



$$v_i = V_B$$

Capacitor is chosen large enough so that at the signal frequency  $1/j\omega C \sim 0$ .



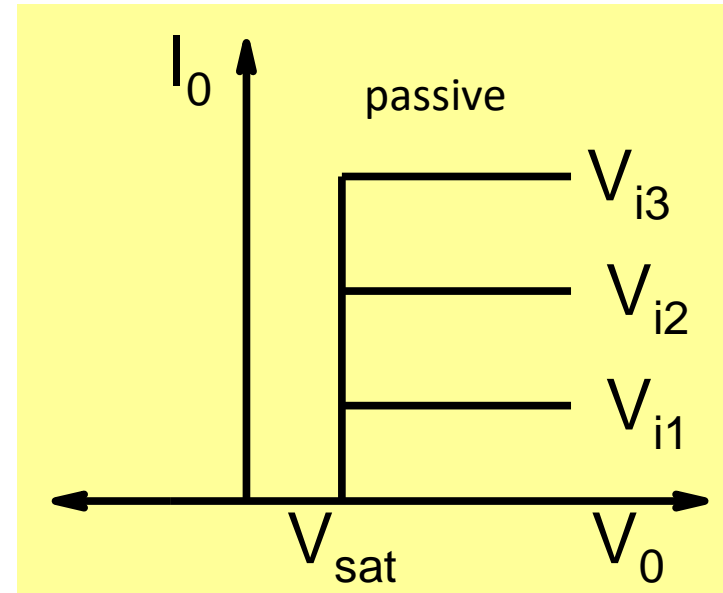
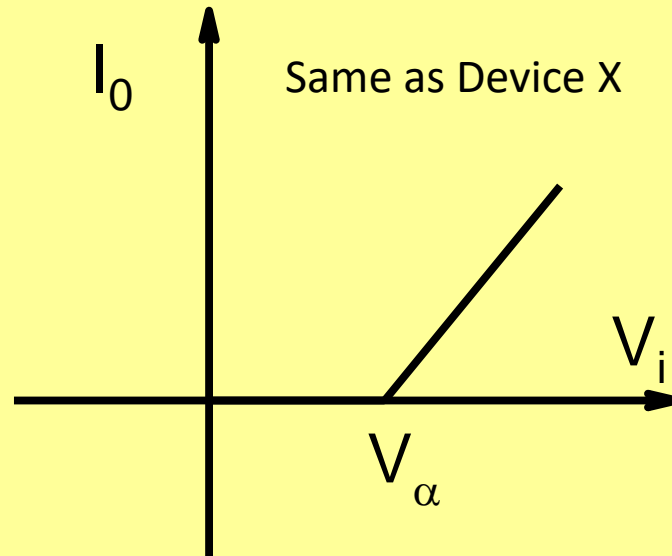
$$v_i = v_s$$

$$\bar{v}_i = v_s + V_B$$

# Simplified model Y

How do we use element Y to make amplifiers?

**Device Y**

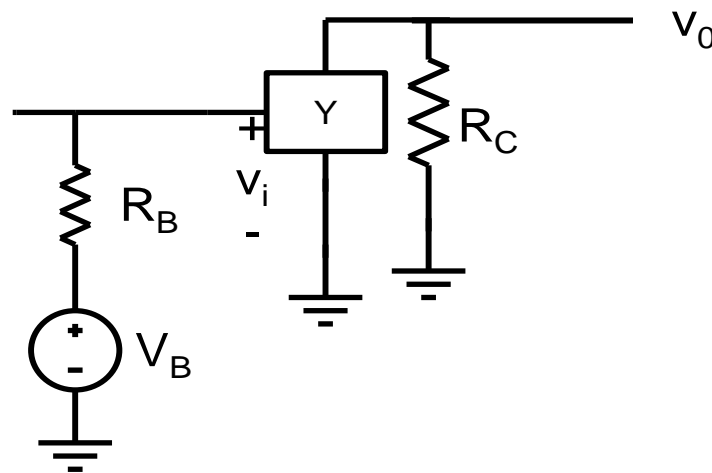
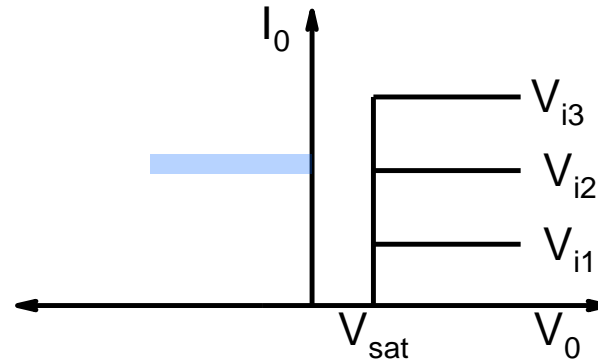
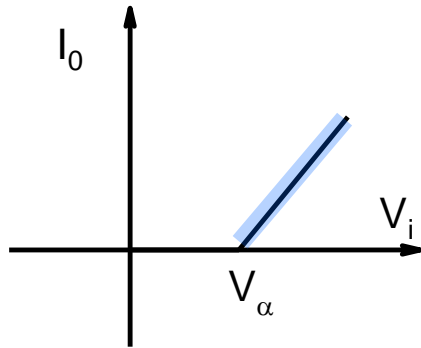


for  $V_o < V_{sat}$ :  $I_o = 0$

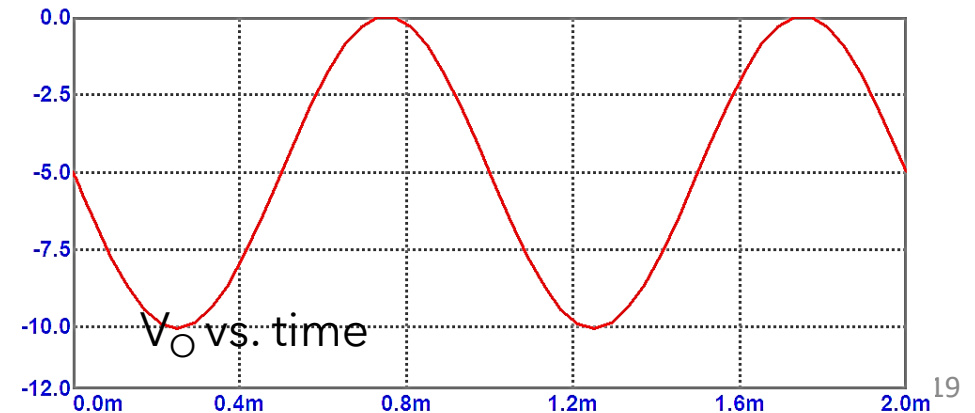
for  $V_o \geq V_{sat}$ :

$$I_o = \begin{cases} 0 & \text{for } V_i \leq V_\alpha \\ g_m \times (V_i - V_\alpha) & \text{for } V_i > V_\alpha \end{cases}$$

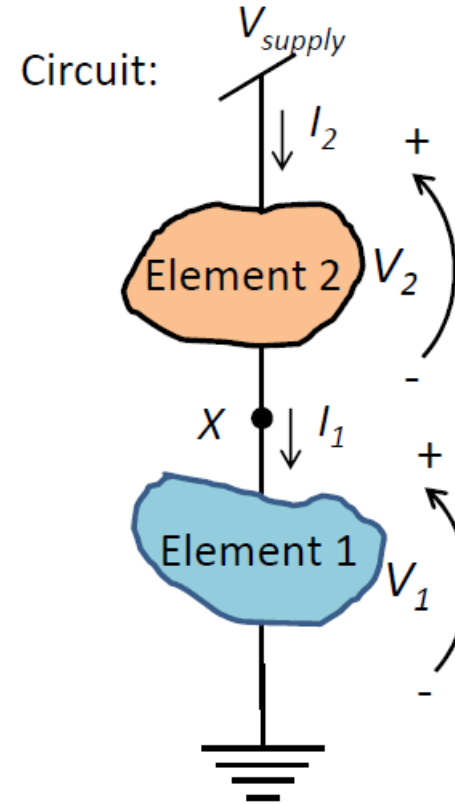
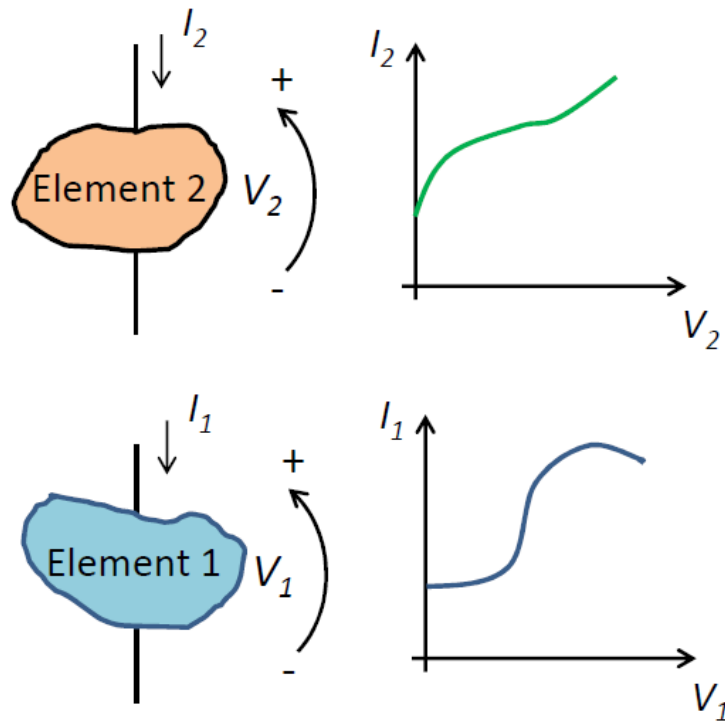
# Can we use the circuit for model X?



$V_o$  is -ve which will not produce any current in device  $Y$

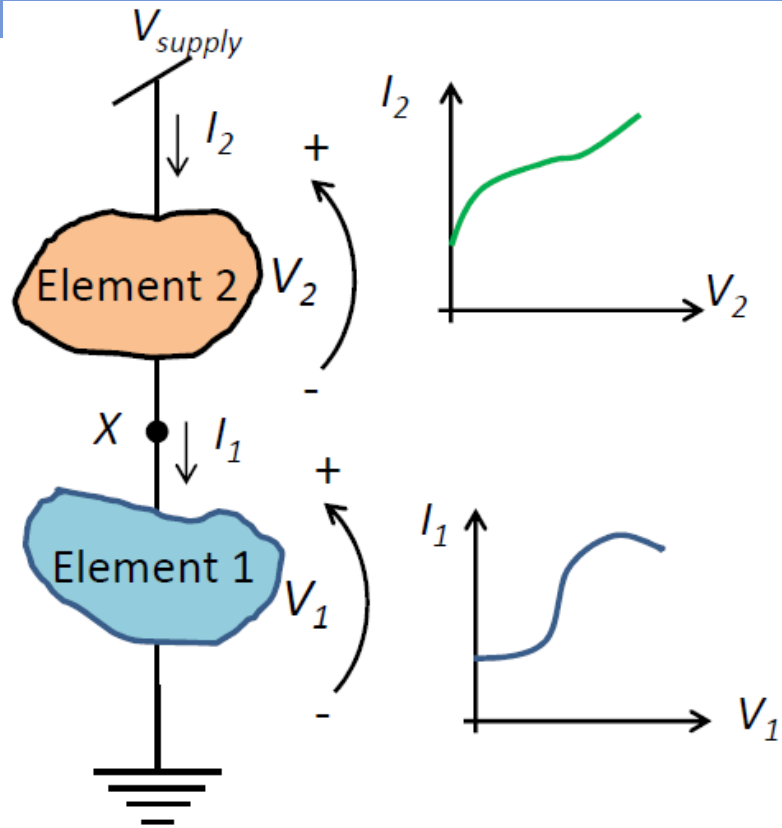


# ANALYZING TWO ELEMENT SYSTEM

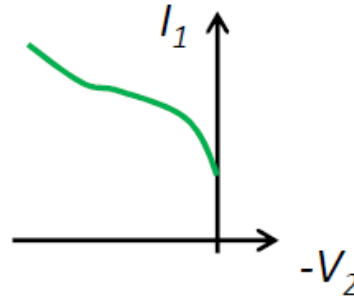


- Usually element close to the ground treated as primary element (if input given to both).
- Other element: load to primary element.
- Goal is to find the operating point of the circuit: Load line analysis.
- Represent electrical characteristics of both elements on a single plot.
- Intersection gives Operating Point.

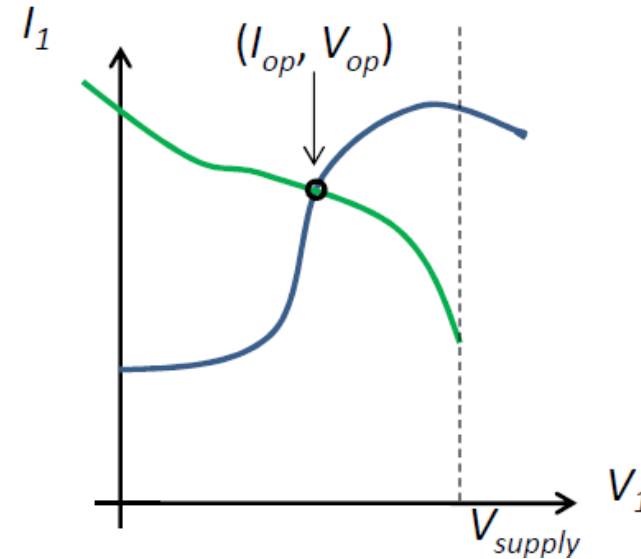
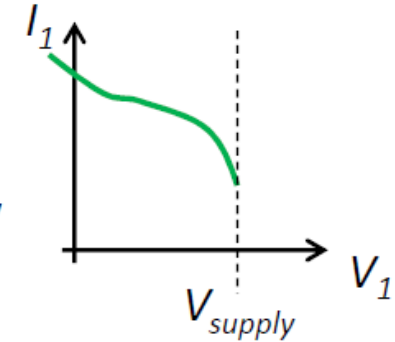
# REVISITING LOAD LINE ANALYSIS



⇒  
Reflect  
on y-axis

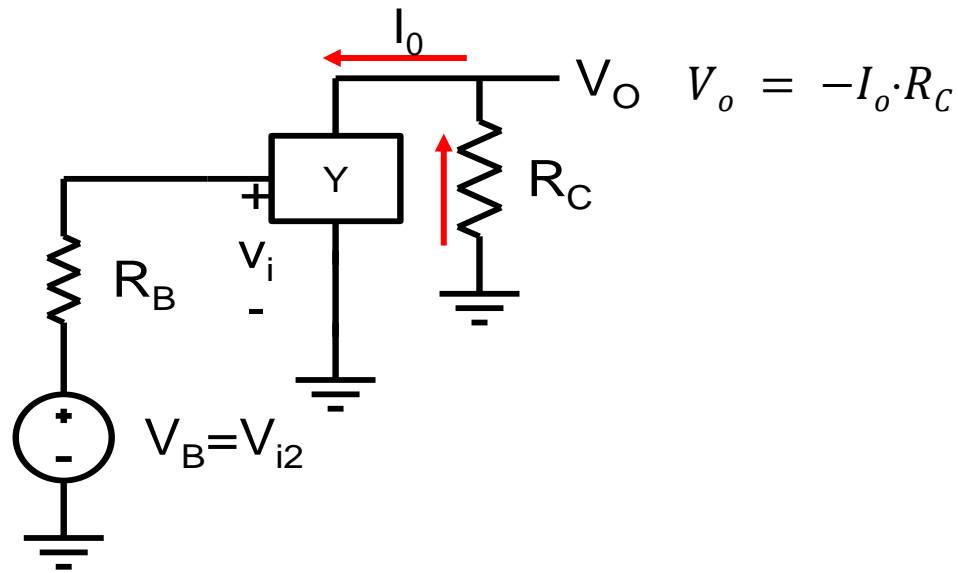


⇒  
Shift by  
 $V_{supply}$

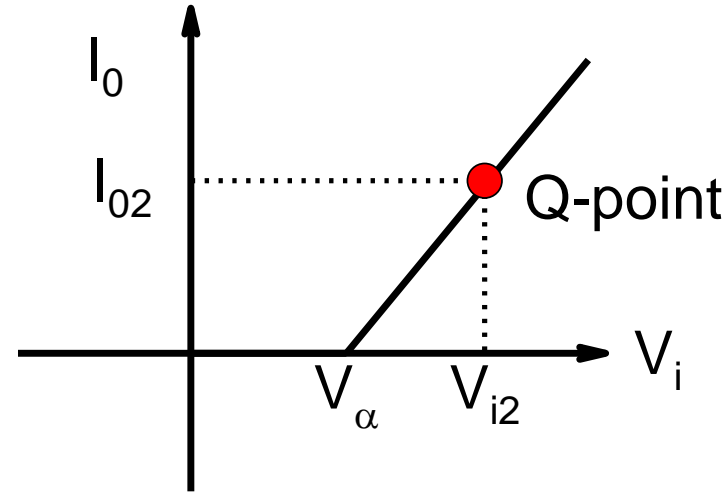


- $I_2 = I_1$  (no change in the direction);  $V_2 = V_{supply} - V_1$  i.e.  $V_1 = V_{supply} - V_2$
- Current in both Elements 1 & 2 is  $I_{op}$ .
- Voltage in node X is  $V_{op}$ .
- Voltage drop is  $V_{op}$  and  $(V_{supply} - V_{op})$  in Elements 1 & 2, respectively.

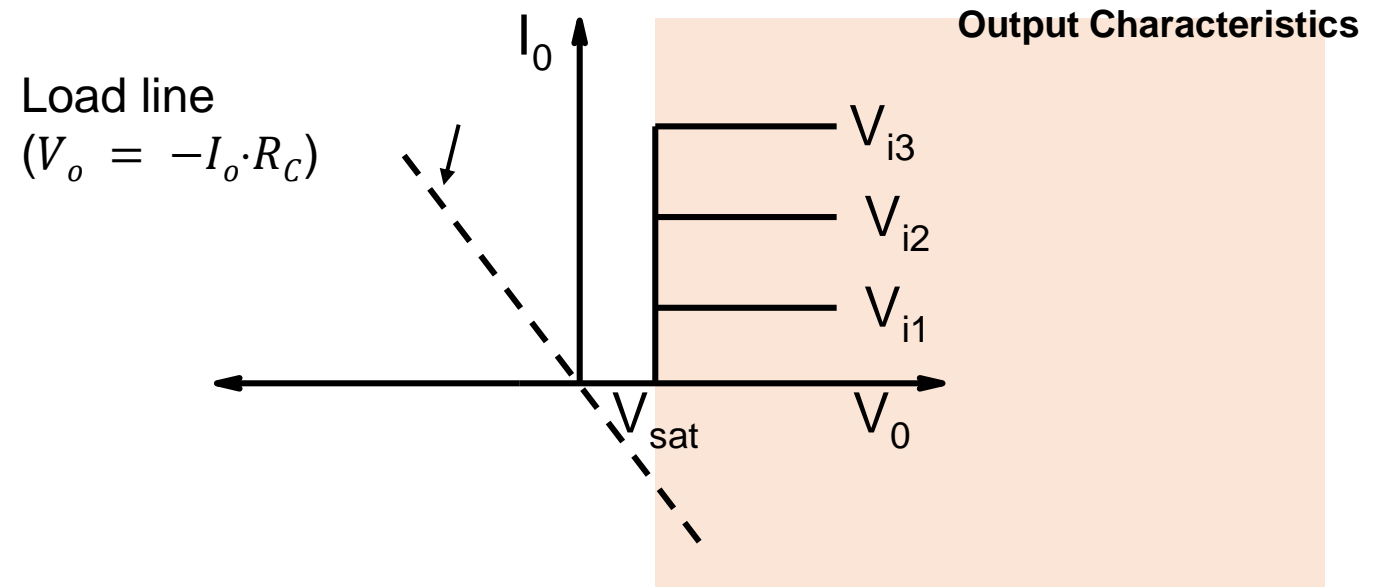
# Understanding Load Line



No solution possible  
that satisfies both load line  
and device Y

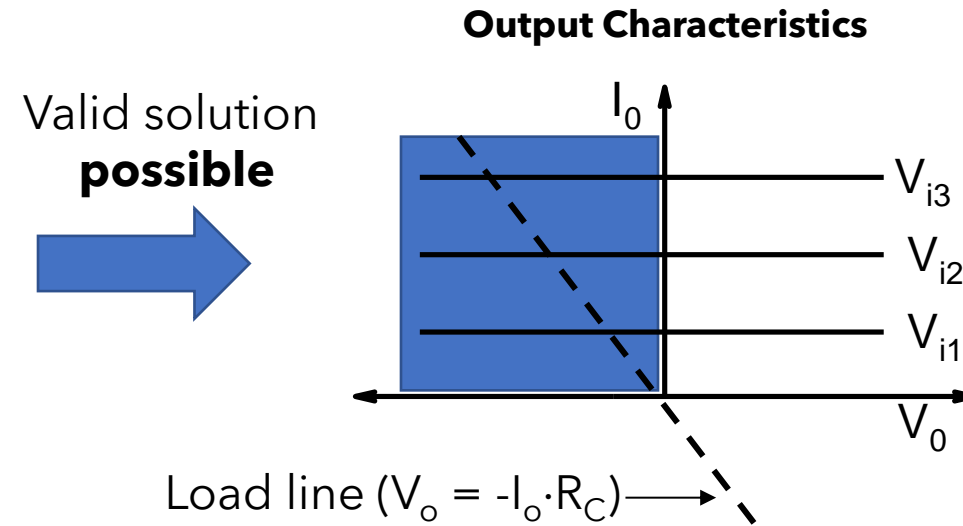


Transfer Characteristics

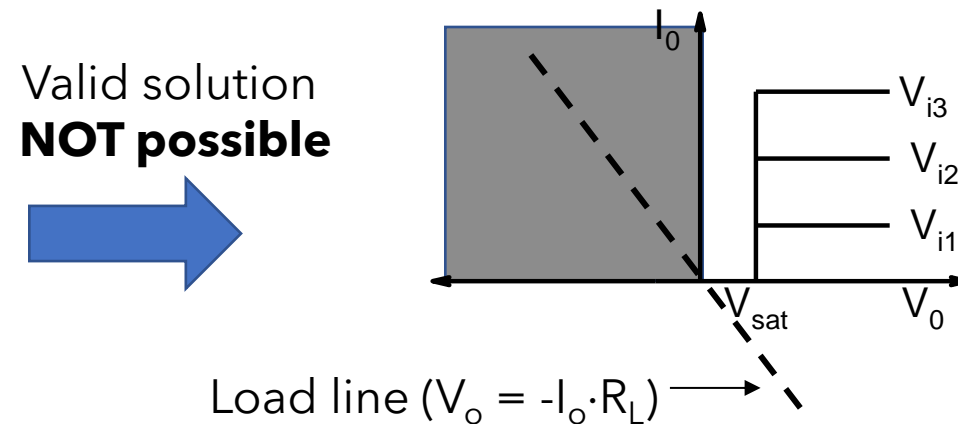


# Why is circuit working for Device X and not for Device Y?

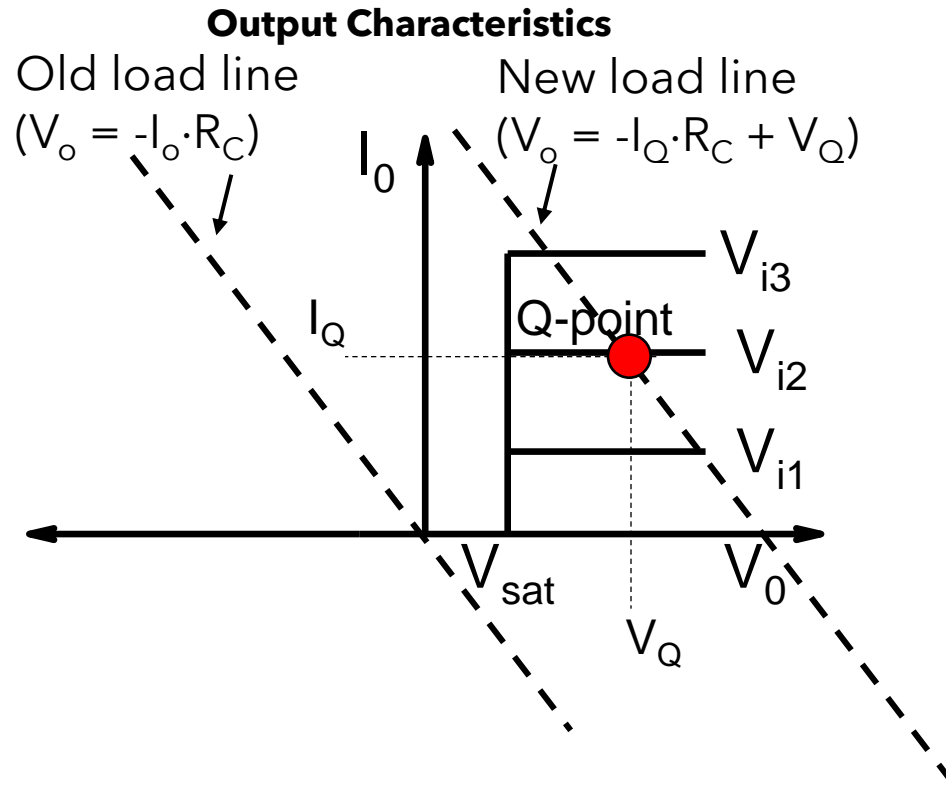
## Device X



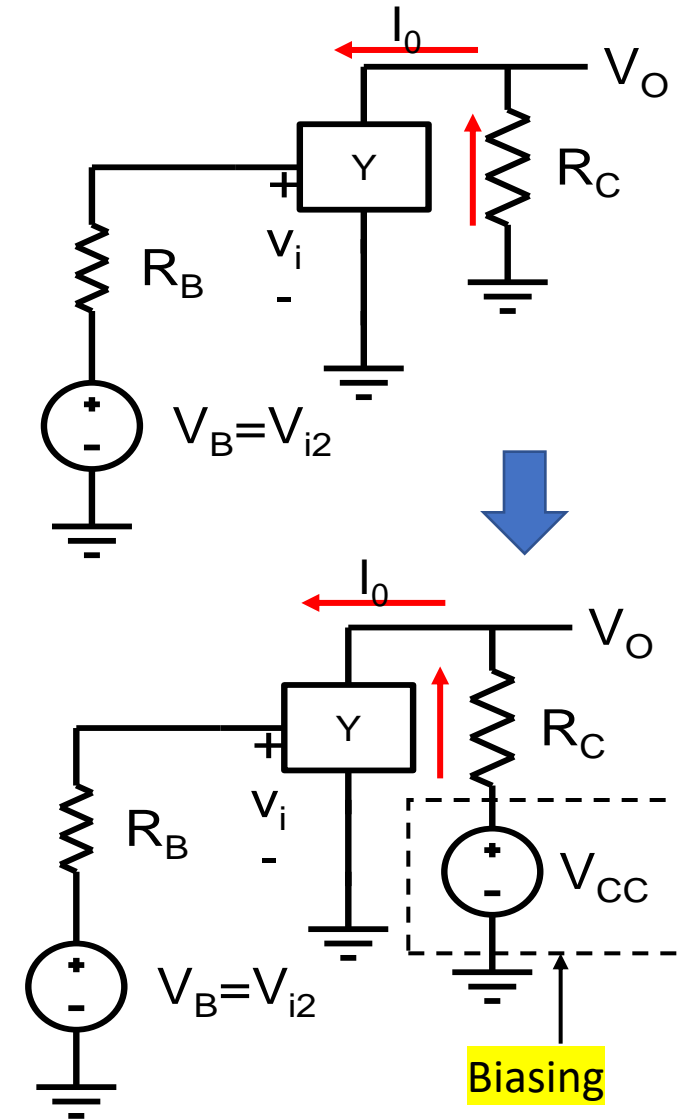
## Device Y



# Solution to get meaningful Q point

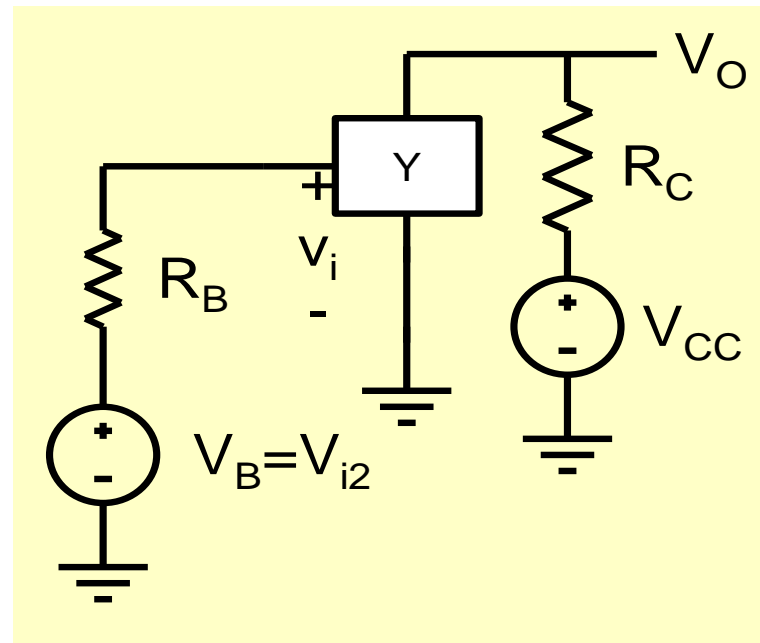
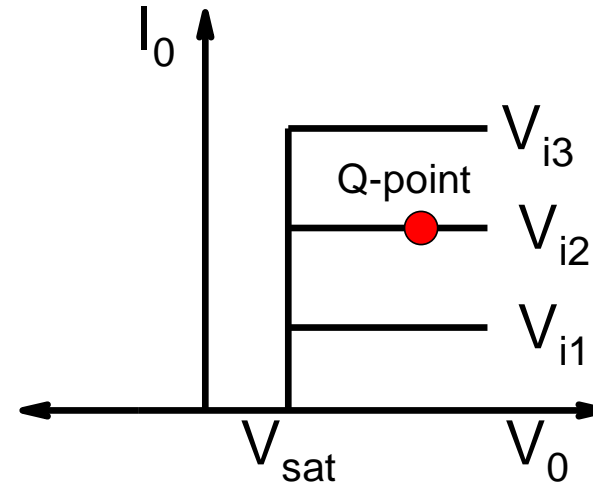
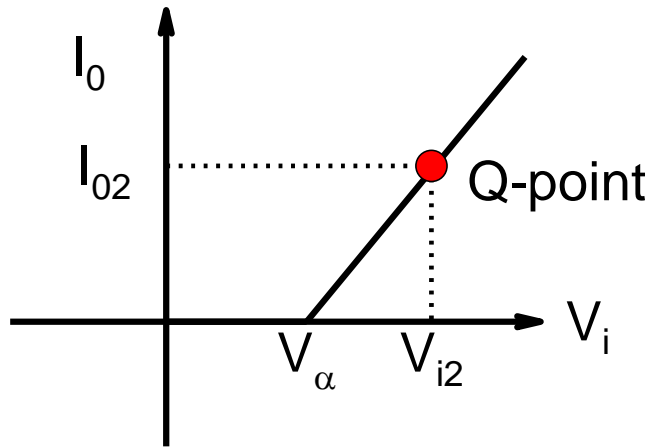


Purpose of biasing network is to operate the device in a region which resembles ideal transistor



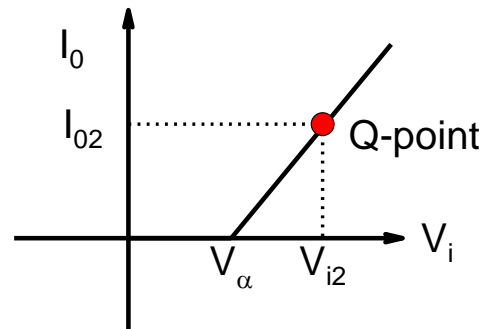


# Need bias at output

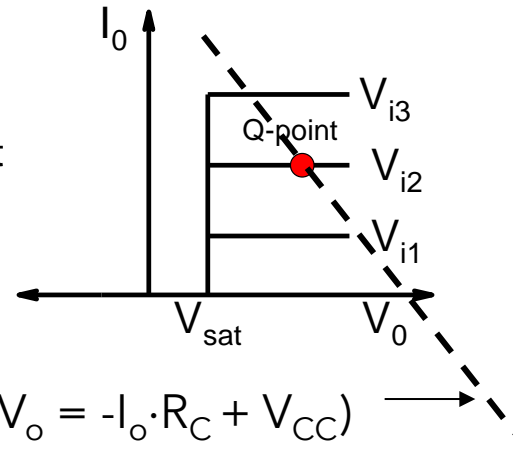


# Revised Amplifier Schematic for Device Y

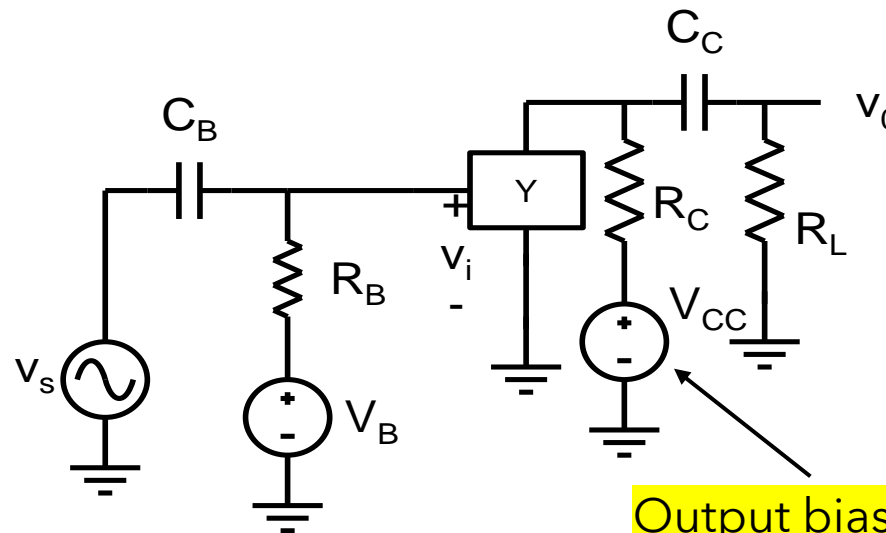
**Transfer Characteristics**



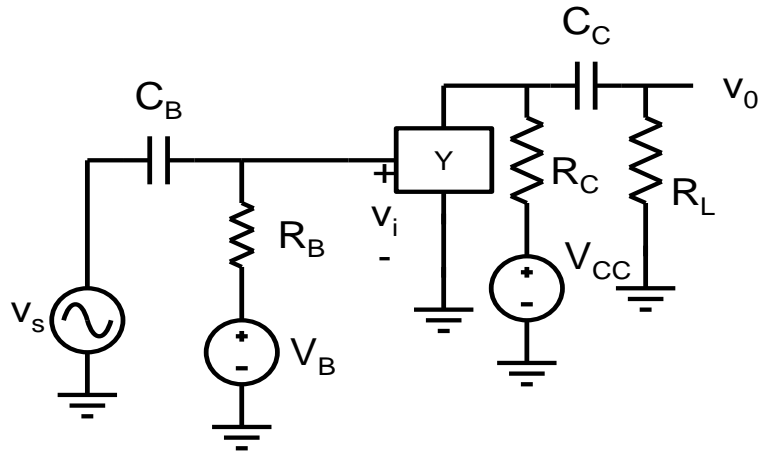
**Output Characteristics**



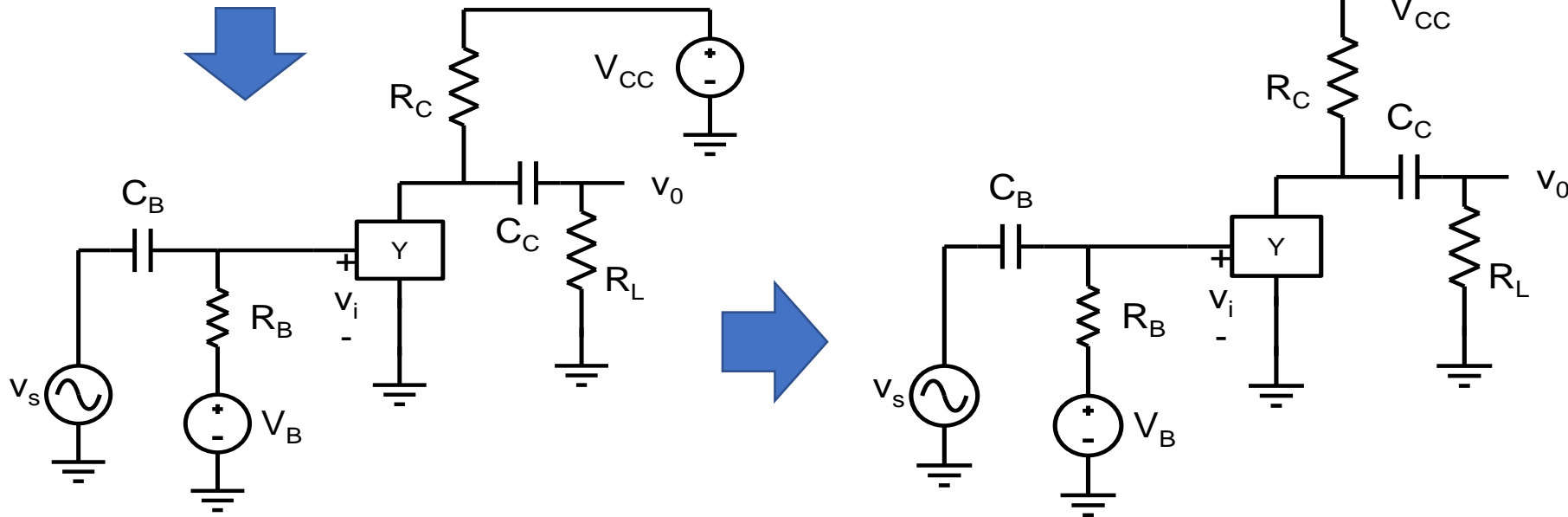
Usually  $V_{CC}$  is fixed  
 $I_o$  and  $R_C$  are varied



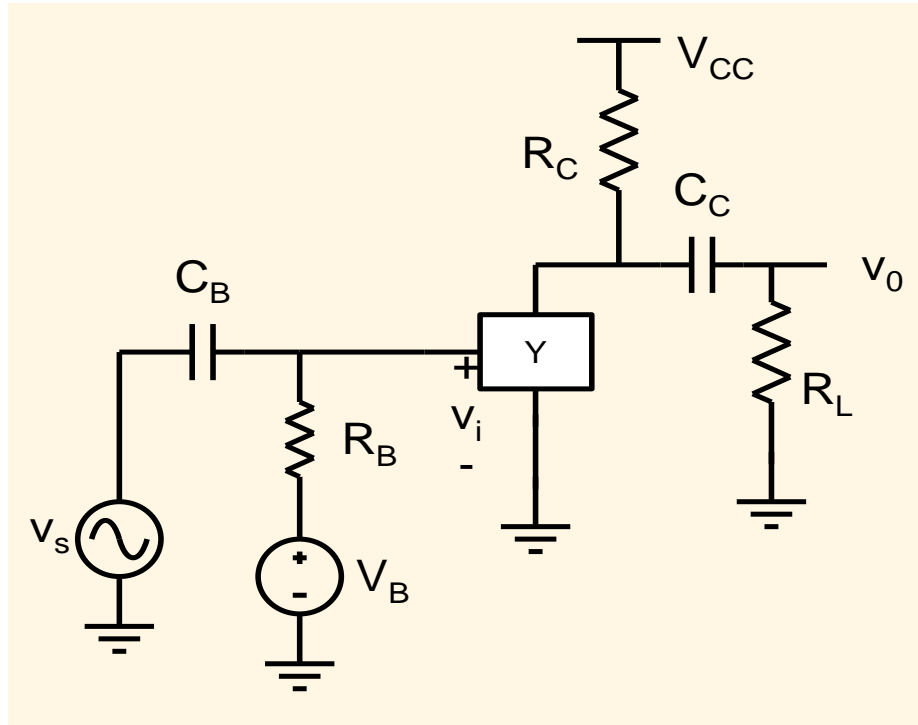
# Another representation of biasing



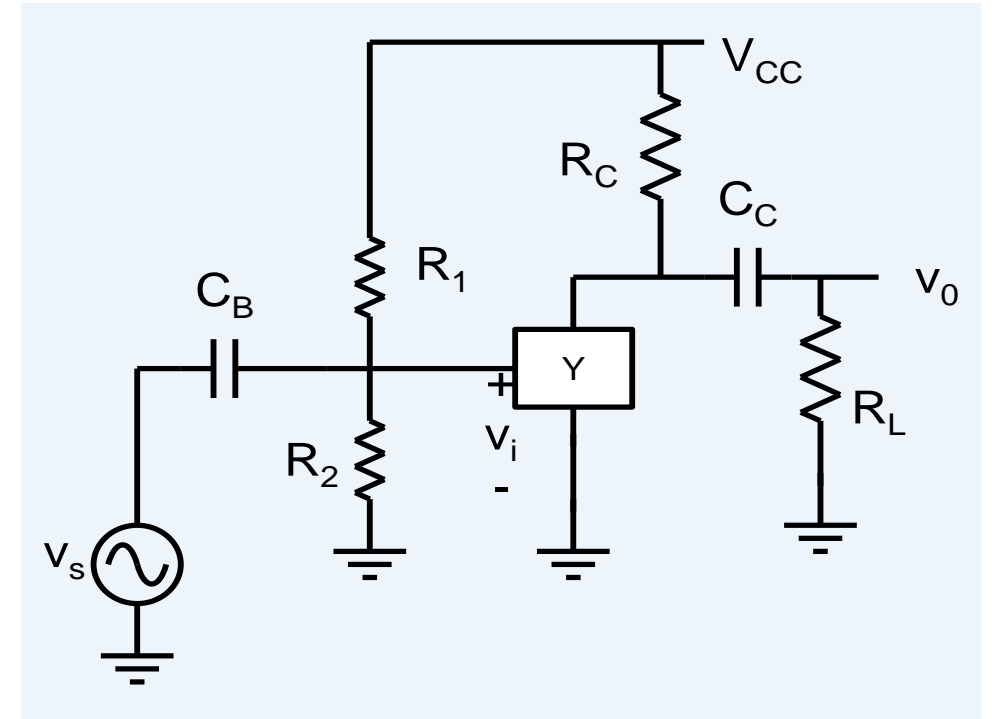
A more common representation



# Do we really need two DC power supplies?



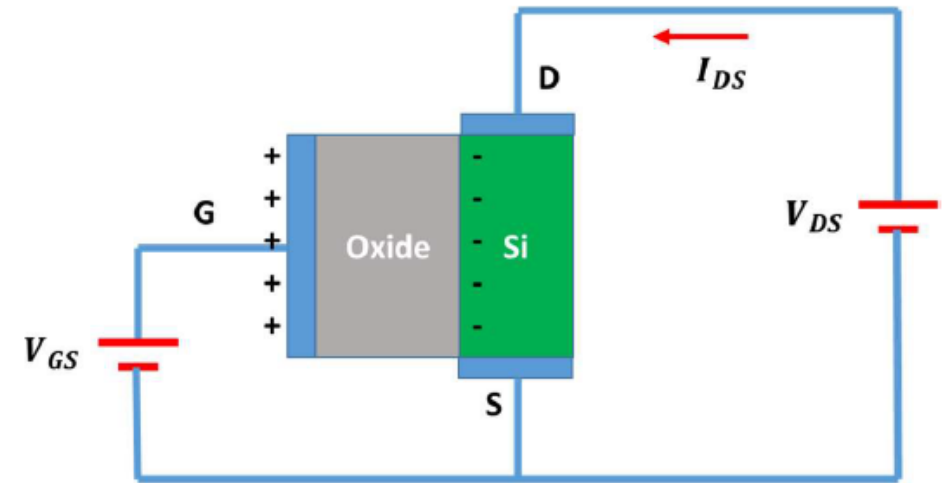
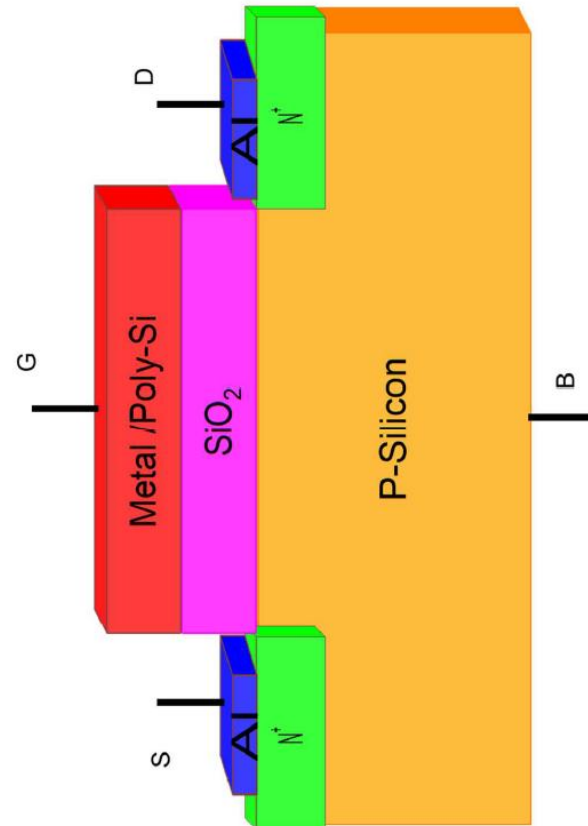
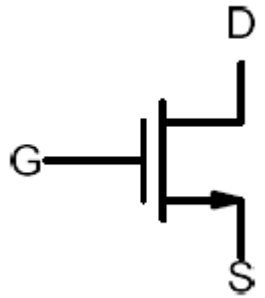
$$V_B = V_{CC} \times \frac{R_2}{R_1 + R_2}$$



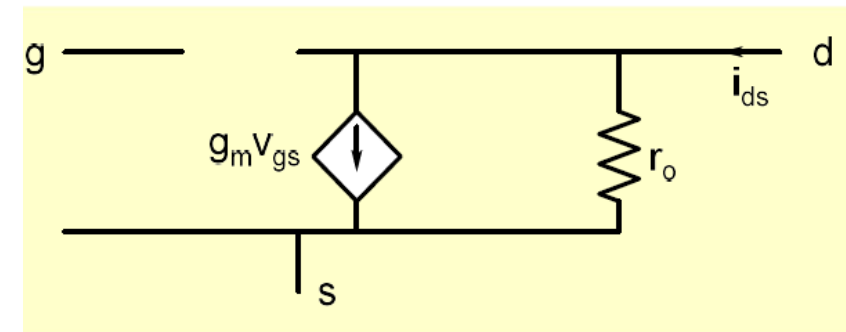
Remember: input of Y is open circuit

# MOSFETs: Workhorse of Semiconductor Industry

MOSFET : Metal Oxide Semiconductor Field effect Transistor

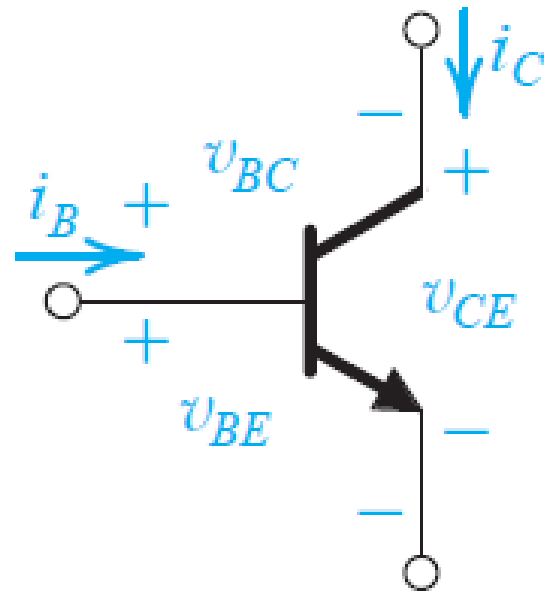


Drain current is controlled by gate voltage



Voltage controlled current source

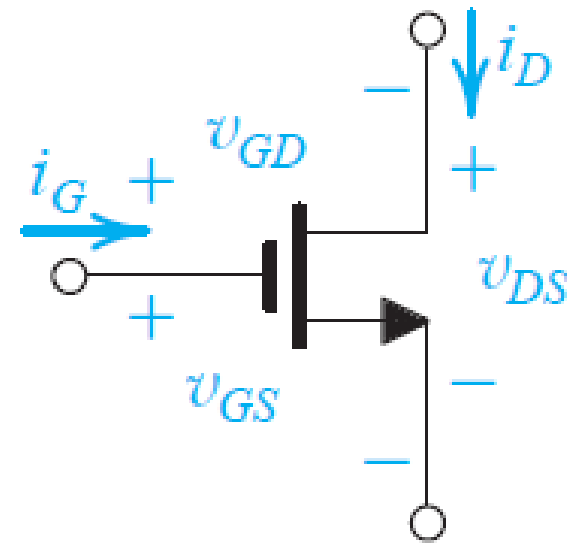
# BJT vs. MOSFET



High gain

Small caps

Static power



Low gain

Large caps

Dynamic power

# The MOSFET

