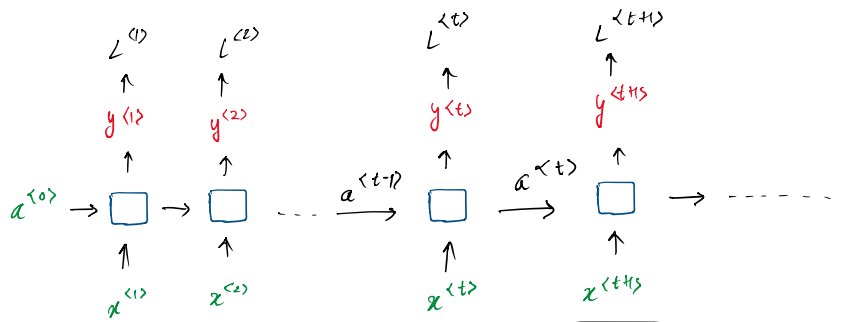


2) GRU

10 December 2025 01:51 PM



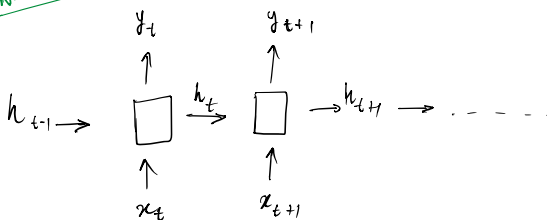
where,

$$a^{(t)} = g_1(x^{(t)} \cdot \omega_x + a^{(t-1)} \cdot \omega_a + b)$$

$$y^{(t)} = g_2(a^{(t)} \cdot \omega_y + b_y)$$

$$L(\hat{y}, y) = \sum_{i=0}^t L^{(i)}; \quad L^{(t)} = L(y^{(t)}, \hat{y})$$

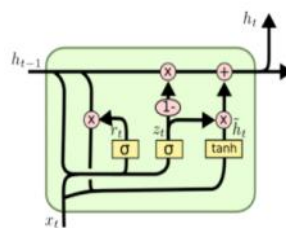
RNN's Architecture



$$h_t = \tanh(x_t \cdot \omega_x + h_{t-1} \cdot \omega_h + b_h)$$

$$y_t = h_t \cdot \omega_y + b_y$$

GRU's Architecture



$$r_t = \sigma(W_r x_t + U_r h_{t-1})$$

$$\tilde{h}_t = \tanh(W \tilde{x}_t + U(r_t \odot h_{t-1}))$$

$$z_t = \sigma(W_z x_t + U_z h_{t-1})$$

$$h_t = (1 - z_t) h_{t-1} + z_t \tilde{h}_t$$

GRU's

reset Gate \rightarrow Sigmoid function.

$$r_t = \sigma(x_t \cdot \omega_{r_x} + h_{t-1} \cdot \omega_{r_h} + b_{r_h})$$

\rightarrow matrix multiplication

Update Gate

$$z_t = \sigma(x_t \cdot \omega_{z_x} + h_{t-1} \cdot \omega_{z_h} + b_{z_h})$$

\rightarrow Decides how much of h_{t-1} to keep and how much of h_t to keep and how much to update the memory.

Candidate Activation

$$\tilde{h}_t = x_t \cdot \omega_x + (r_t \odot h_{t-1}) \cdot \omega_h + b_h$$

\rightarrow element wise multiplication

$\rightarrow \tilde{h}_t$ is just a proposal of how much of h_{t-1} is relevant to current input

final hidden state

$$h_t = h_t \odot z_t + h_{t-1} \odot (1 - z_t)$$

V

final hidden state

$$h_t = h_t * z_t + h_{t-1} * (1 - z_t)$$

→ final memory (hidden state)
to pass to next time step