

Code No: 7HC16

Date: 30-Aug-2021(FN)

B.Tech II-Year II- Semester External Examination, Aug/Sept-2021 (Regular)
MATHEMATICS-II (Differential Calculus) - (CSE, IT and ECM)

Time: 3 Hours

Max.Marks:70

Note: a) No additional answer sheets will be provided.
b) All sub-parts of a question must be answered at one place only, otherwise it will not be valued.
c) Missing data can be assumed suitably.

ANSWER ANY 5 OUT OF 8 QUESTIONS. EACH QUESTION CARRIES 14 MARKS.

Bloom's Cognitive Levels of Learning (BCLL)

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|------------|----|---------|----|----------|----|
| Remember | L1 | Apply | L3 | Evaluate | L5 |
| Understand | L2 | Analyze | L4 | Create | L6 |

- | | BC
LL | CO(s) | Marks | | | | | | | | | | |
|--|----------|-------|-------|-----|---|---|---|---|----|---|---|----|-----|
| 1. a) Show that $u=x+y+z, v=xy+yz+zx, w=x^2+y^2+z^2$ are functionally dependent and hence find the relation between them. | L3 | CO1 | [7M] | | | | | | | | | | |
| b) A rectangular box open at the top is to have volume of 32 cubic feet. Find the dimensions of the box requiring least material for its construction. | L5 | CO1 | [7M] | | | | | | | | | | |
| 2. a) Solve $\left(1+e^{\frac{x}{y}}\right)dx + \left(1-\frac{x}{y}\right)e^{\frac{x}{y}}dy = 0$ | L4 | CO2 | [7M] | | | | | | | | | | |
| b) A body is originally at $80^\circ C$ and cools down to $60^\circ C$ in 20 minutes. If the temperature of the air is $40^\circ C$, find the temperature of the body after 40 minutes. | L4 | CO2 | [7M] | | | | | | | | | | |
| 3. a) Solve the differential equation $(D^2-5D+6)y=e^x \sin x$ | L3 | CO3 | [7M] | | | | | | | | | | |
| b) Solve $(D^2+2D+4)y=\tan 2x$ by the method of variation of parameters | L4 | CO3 | [7M] | | | | | | | | | | |
| 4. a) Find root of the equation $f(x) = e^x - 3x$ using Newton Raphson method that lies between 0 and 1. | L3 | CO4 | [7M] | | | | | | | | | | |
| b) Find the polynomial $f(x)$ by using Lagrange's formulae and hence find $f(3)$ | L3 | CO4 | [7M] | | | | | | | | | | |
| <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr> <td style="width: 10%;">x:</td> <td style="width: 10%;">0</td> <td style="width: 10%;">1</td> <td style="width: 10%;">2</td> <td style="width: 10%;">3</td> </tr> <tr> <td style="width: 10%;">y:</td> <td style="width: 10%;">2</td> <td style="width: 10%;">3</td> <td style="width: 10%;">12</td> <td style="width: 10%;">147</td> </tr> </table> | | | | x: | 0 | 1 | 2 | 3 | y: | 2 | 3 | 12 | 147 |
| x: | 0 | 1 | 2 | 3 | | | | | | | | | |
| y: | 2 | 3 | 12 | 147 | | | | | | | | | |
| 5. a) Using Taylor's series method, find an approximate value of y at x=0.2 for the differential equation $y'-2y = 3e^x$ for y (0) = 0. | L4 | CO5 | [7M] | | | | | | | | | | |
| b) Find y (0.1) using Runge- Kutta fourth order formula, given that $y' = x + x^2 y$ | L4 | CO5 | [7M] | | | | | | | | | | |

and $y(0) = 1$

6. a) Find $L^{-1}\left\{\frac{1}{s(s+2)^3}\right\}$ L3 CO6 [7M]
- b) State Convolution theorem on Laplace Transform and hence find the Inverse Laplace Transform of $\frac{1}{s(s^2+a^2)}$ L4 CO6 [7M]
7. a) If $u = \log\left(\frac{x^2+y^2}{x+y}\right)$, prove that $xu_x + yu_y = 1$ L3 CO1 [5M]
- b) Solve $x \frac{dy}{dx} + y = \log x$ L2 CO2 [5M]
- c) Solve $(D^3+1)y = \cos 2x$ L2 CO3 [4M]
8. a) If $x^3 - x - 4 = 0$, then by Bisection method find first two approximations $x_0 \wedge x_1$ L3 CO4 [5M]
- b) $\frac{dy}{dx} = x - y$, if $y(0) = 1$ find $y(0.1)$ by Euler's method. L4 CO5 [5M]
- c) Find the Laplace Transform of $\left(\frac{\sin t}{t}\right)$ L3 CO6 [4M]

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