

**Code No: 7HC16**

**Date: 04-Aug-2022 (FN)**

**B.Tech II-Year II- Semester External Examination, July/August - 2022 (Supplementary)**  
**MATHEMATICS-II (Differential Calculus) - (CSE, IT and ECM)**

**Time: 3 Hours**

**Max.Marks:70**

**Note:** a) No additional answer sheets will be provided.  
b) All sub-parts of a question must be answered at one place only, otherwise it will not be valued.  
c) Missing data can be assumed suitably.

**ANSWER ANY 5 OUT OF 8 QUESTIONS. EACH QUESTION CARRIES 14 MARKS.**

**Bloom's Cognitive Levels of Learning (BCLL)**

Remember	L1	Apply	L3	Evaluate	L5
Understand	L2	Analyze	L4	Create	L6

- |   | BC<br>LL | CO(s) | Marks  |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
|---|----------|-------|--------|------|--------|------|-----|-----|--------|-----|----|-------|-----|--------|------|--------|------|
| 1. a) If $x + y + z = u, y + z = uv, z = uvw$ , then evaluate $\frac{\partial(x,y,z)}{\partial(u,v,w)}$   | L3       | CO1   | [7M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| b) Find the maximum and minimum values of $x^3 + y^3 - 3axy$  | L5       | CO1   | [7M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| 2. a) Solve $x \frac{dy}{dx} + y = x^2 y^6$   | L5       | CO2   | [7M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| b) A body is originally at 80°C and cools down to 60°C in 20 minutes. If the temperature of the air is 40°C, find the temperature of the body after 40 minutes  | L2       | CO2   | [7M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| 3. a) Solve $(D^2 - 2D + 1)y = xe^x \sin x$   | L3       | CO3   | [7M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| b) Solve $(D^2 + a^2)y = \tan ax$ , by the method of variation of parameters  | L3       | CO3   | [7M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| 4. a) Find the real root of $x^3 - 3x - 5 = 0$ by Bisection Method  | L5       | CO4   | [7M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| b) Using Lagrange's interpolation formula find the value of y when x=10 from the following table.   | L2       | CO4   | [7M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| <table border="1" style="margin: 10px auto; border-collapse: collapse; text-align: center;"> <tr> <td style="padding: 5px;">x</td> <td style="padding: 5px;">5</td> <td style="padding: 5px;">6</td> <td style="padding: 5px;">9</td> <td style="padding: 5px;">11</td> </tr> <tr> <td style="padding: 5px;">y=f(x)</td> <td style="padding: 5px;">12</td> <td style="padding: 5px;">13</td> <td style="padding: 5px;">14</td> <td style="padding: 5px;">16</td> </tr> </table>   |          |       |        | x    | 5      | 6    | 9   | 11  | y=f(x) | 12  | 13 | 14    | 16  |        |      |        |      |
| x   | 5        | 6     | 9      | 11   |        |      |     |     |        |     |    |       |     |        |      |        |      |
| y=f(x)  | 12       | 13    | 14     | 16   |        |      |     |     |        |     |    |       |     |        |      |        |      |
| 5. a) using the Taylor's series method, solve $y' = x^2 - y, y(0) = 1$ at $x = 0.1, 0.2$ .  | L3       | CO5   | [7M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| b) Use Picard's method of approximation to find y(0.1), y(0.2) given $y' = x + y^2, y(0) = 0$ .   | L3       | CO5   | [7M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| 6. a) Find $L \left\{ \int_0^t te^{-t} \sin 2tdt \right\}$  | L5       | CO6   | [7M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| b) Using the Convolution theorem, find $L^{-1} \left\{ \frac{s}{(s^2+4)^2} \right\}$  | L3       | CO6   | [7M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| 7. a) Find first and second order partial derivatives of $x^3 + y^3 - 3axy$ and verify $\frac{\partial^2 f}{\partial x \partial y} = \frac{\partial^2 f}{\partial y \partial x}$  | L5       | CO1   | [5M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| b) The number N of bacteria grew at a rate proportional to N. The value of N was initially 100 and increased to 332 in one hour. What was the value of N after $1\frac{1}{2}$ hours?  | L2       | CO2   | [5M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| c) Solve $(D^2 - 2D + 1)y = e^{3x}$   | L2       | CO3   | [4M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| 8. a) From the following table of values of x and y, obtain $\frac{dx}{dy}$ for x=1.5   | L3       | CO4   | [5M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |
| <table border="1" style="margin: 10px auto; border-collapse: collapse; text-align: center;"> <tr> <td style="padding: 5px;">x</td> <td style="padding: 5px;">1.5</td> <td style="padding: 5px;">2.0</td> <td style="padding: 5px;">2.5</td> <td style="padding: 5px;">3.0</td> <td style="padding: 5px;">3.5</td> <td style="padding: 5px;">4.0</td> </tr> <tr> <td style="padding: 5px;">y</td> <td style="padding: 5px;">3.375</td> <td style="padding: 5px;">7.0</td> <td style="padding: 5px;">13.625</td> <td style="padding: 5px;">24.0</td> <td style="padding: 5px;">38.875</td> <td style="padding: 5px;">59.0</td> </tr> </table> |          |       |        | x    | 1.5    | 2.0  | 2.5 | 3.0 | 3.5    | 4.0 | y  | 3.375 | 7.0 | 13.625 | 24.0 | 38.875 | 59.0 |
| x   | 1.5      | 2.0   | 2.5    | 3.0  | 3.5    | 4.0  |     |     |        |     |    |       |     |        |      |        |      |
| y   | 3.375    | 7.0   | 13.625 | 24.0 | 38.875 | 59.0 |     |     |        |     |    |       |     |        |      |        |      |
| b) Using Euler's Method find y(0.2) given $y' = x + y, y(0) = 1$ taking h=0.1.  | L3       | CO5   | [5M]   |      |        |      |     |     |        |     |    |       |     |        |      |        |      |

c) Find  $L\{e^t(\cos 2t + \sinh 3t)\}$

L5 CO6 [4M]

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