

*[Case Study] (9)

Ram Vs Hard Disk

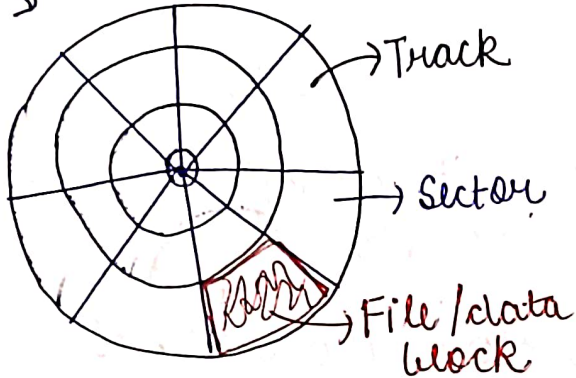
→ Temporary (Volatile)
expensive
limited ☹️

→ Hard Disk

→ Persistence
cheap

Take more time (I/O operation)

HDD →



→ Intersection of Track & Sector give us a file block.
(typically 4KB)

- Whenever we need to process any data we need to take the entire file block from Hard disk to RAM. (because C.P.U. can access data stored in RAM).

Time taken to find in 1 million Records. (Rough values)
Let say each record is an entry which takes 400 bytes.

In general
1 Block ⇒ 4KB data (can store)

$$\Rightarrow \frac{4000}{400} = 10 \text{ records/entry (1 block can store)}$$

Now 1 million records,

10^6 Records ⇒

$$\text{No. of blocks} \Rightarrow \frac{10^6}{10} = 10^5 \text{ blocks}$$

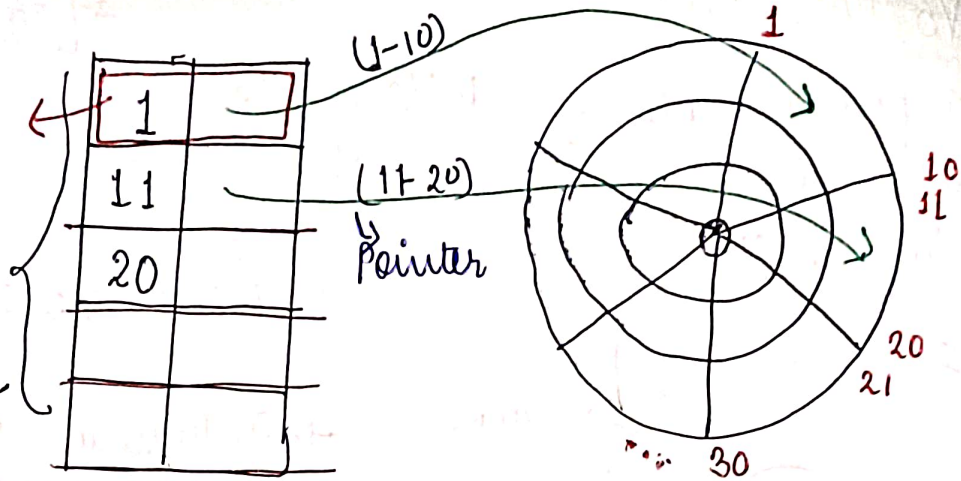
$$= 10^5 \text{ ms}$$

$$= 100 \text{ sec (Huge)}$$

(We should make it better)

[Let say any I/O operation in HDD takes 1 milli seconds.]

each entry takes 10 bytes



[INDEX TABLE]

1 block can store = 4000 Bytes

each entry takes 10 bytes

each block can store 400 entries of table.

→ 105 entries [because the table needs to store pointer to each of the data block]

How many blocks are needed to store this table?

$$\text{No. of blocks} \Rightarrow \frac{105}{400}$$

⇒ 250 blocks of disk.

And, another 1ms to read the corresponding data block (/file block).

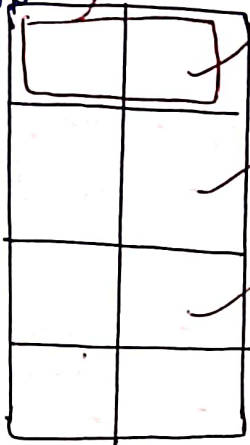
$$\Rightarrow [250\text{ms}] (0.25 \text{ seconds})$$

[Optimized]

Can we optimized More? 😊

[New]
10 bytes

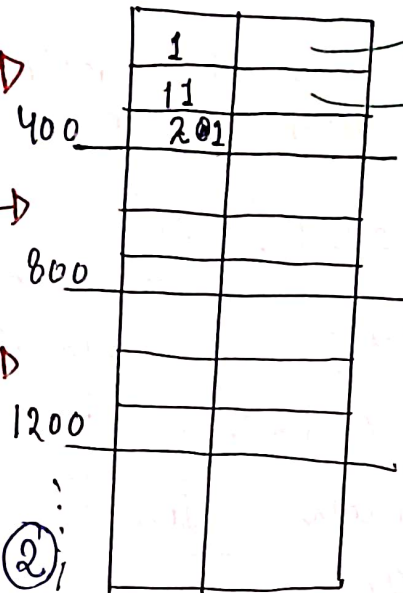
①



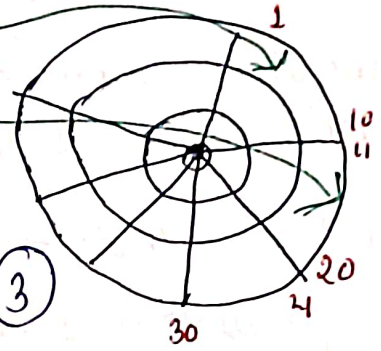
250 entries

Point to 1 Block
that store index
entries.

②

10⁵ entries

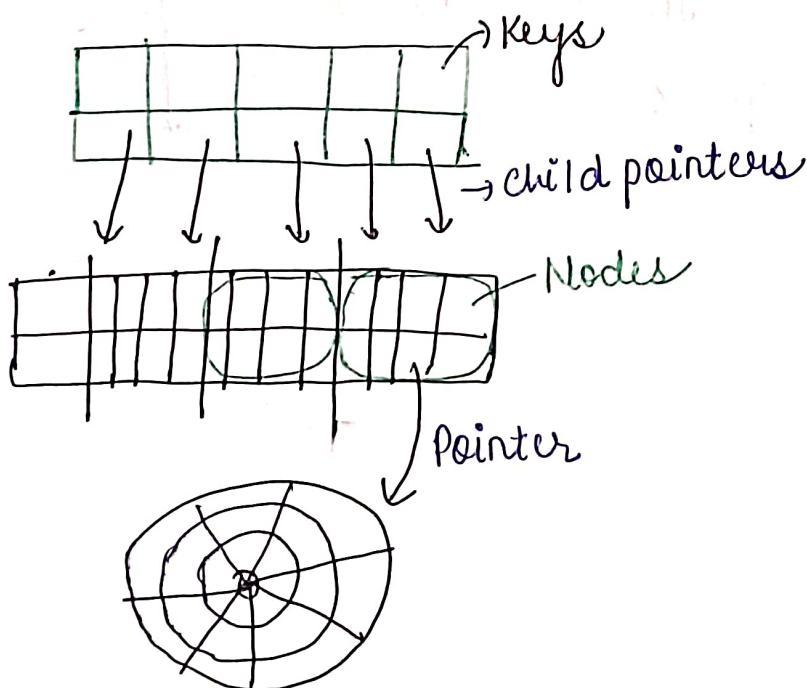
③

10⁵ blocks \Rightarrow data
250 blocks \Rightarrow Index
entries~~250 entries~~ =

$$250 \text{ entries} \times 10 \text{ bytes} = 2500 \text{ Bytes} [2.5 < 4 \text{ KB}]$$

3 I/O operation taking 3MS [0.003 seconds] (oo)

{ MULT I-LEVEL INDEXING }

This is how
the B-trees
look.

{ Search Insert

Delete / Less common DB operation

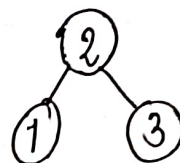
If we don't know about BTree then Balanced Tree is going to come as answer (logarithmic time to search, delete, insert).

1 million records $\Rightarrow \log_2(10^6) = 20$

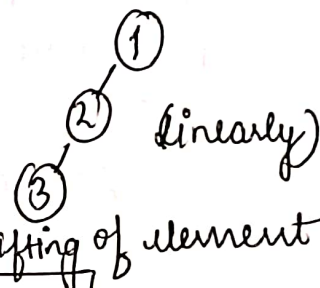
\Rightarrow 20 I/O operations with Hard disk for search, insert, delete

NOTE:- [every I/O operation is expensive.]

Database	Operations		
	Search	Insert	Delete
Balanced BST	20	20	20



	Search	Insert	Delete
Unbalanced BST	10^6	10^6	10^6



	log time Search	Insert	Delete
Sorted Array	20	10^6	10^6

Tricky! \rightarrow shifting of element

B-Tree (m-way Tree)	Search	Insert	Delete
	3	3	3

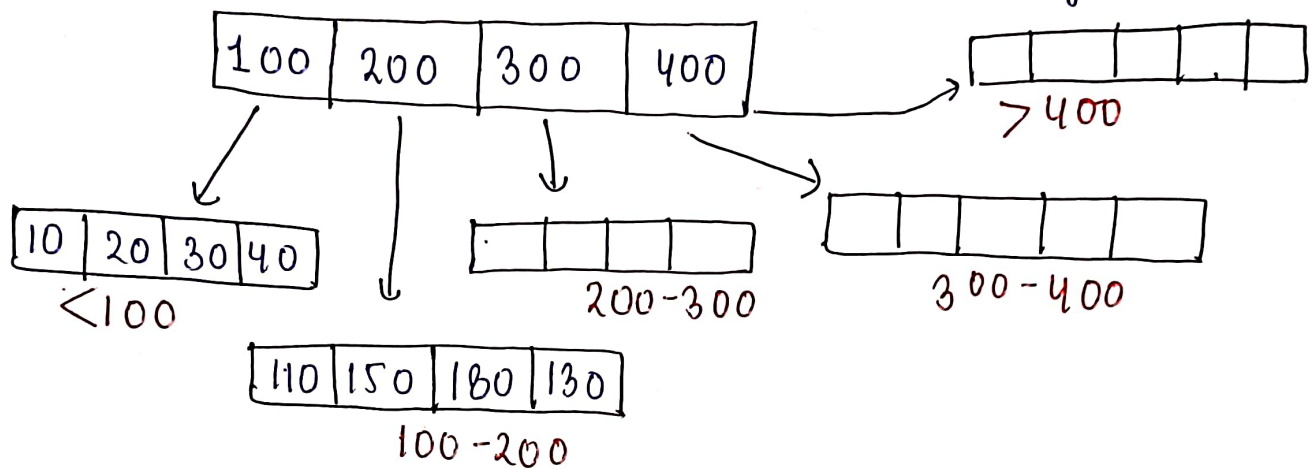
Order $\Rightarrow m$
max children $\Rightarrow m$

\Downarrow
complexity $\log_m(10^6)$
(let $m=100$)

$\Rightarrow \log_{100}(10^6) = 3$

B-Tree

↳ A node can have multiple key.



even though here we have to do more no. of comparison for every node than (BST).

But, The cost of getting a data from DISK TO RAM [which is more expensive than the no. of comparison in RAM].

↗
Main problem!

• Major characteristics of B-Tree :-

B Tree \Rightarrow order m

→ Max. no of children = m

→ Max. no of keys = $(m-1)$

→ Min. no of keys (other than root node) = $\lceil \frac{m}{2} \rceil$ integer.
 ↳ Round off to next bigger integer.
 ↳ can have min 1 key.

→ All leaves are at same level

→ $\text{Height} = \log_m n$
 ↳ n is keys

→ We grow towards root