

**ADVANCED CALCULUS**

Common to ECE, CSE, IT, CSE(AI&amp;ML) &amp; CSE(DS) Branches

**21MA201BS**

<b>L</b>	<b>T</b>	<b>P</b>	<b>C</b>
<b>3</b>	<b>1</b>	<b>0</b>	<b>4</b>

**Course Objectives:** To learn

- 1.Methods of solving the differential equations of First order and its applications
- 2.Methods of solving the differential equations of Higher order and its applications
- 3.Evaluation of multiple integrals and their applications
- 4.The physical quantities involved in engineering field related to vector valued functions
- 5.The basic properties of vector valued functions and their applications to line, surface and volume integrals

**Course Outcomes:** After learning the contents of this paper the student must be able to

CO 1: Identify whether the given differential equation of first order is exact or not

CO 2: Solve higher differential equation and apply the concept of differential equation to real world problems

CO 3: Evaluate the multiple integrals and apply the concept to find areas, volumes.

CO 4: Evaluate the line, surface and volume integrals and converting them from one to another

**UNIT-I: First Order Ordinary Differential Equations**

Exact, and Reducible to Exact linear and Bernoulli's Equations; Applications: Orthogonal Trajectories, Newton's law of cooling, Law of natural growth, decay and L-R Circuits.

**UNIT-II: Ordinary Differential Equations of Higher Order**

Second order linear differential equations with constant coefficients. Non-Homogeneous terms of the type  $e^{ax}$ ,  $\sin ax$ ,  $\cos ax$ , polynomials in  $x$ ,  $e^{ax}V(x)$  and  $xV(x)$ ; Method of variation of parameters; Equations reducible to linear ODE with constant coefficients; Legendre's equation, Cauchy-Euler equation, Applications to L-C-R Circuits.

**UNIT-III: Multivariable Integral Calculus**

Evaluation of Double Integrals: Cartesian and polar coordinates, change of order of integration in Cartesian form, Evaluation of Triple Integrals: Change of variables from Cartesian to Cylindrical and Spherical Coordinates.  
Applications: Areas and volumes by double and triple integrals.

**UNIT-IV: Vector Differentiation**

Vector point functions and scalar point functions. Gradient, Divergence and Curl. Directional derivatives, Tangent plane and normal line. Vector Identities (Without Proof). Scalar potential functions. Solenoidal and irrotational vectors.

**UNIT-V: Vector Integration**

Line, Surface and Volume Integrals. Theorems of Green, Gauss and Stokes (without proofs) and their applications.

**TEXTBOOKS:**

1. B.S. Grewal, Higher Engineering Mathematics, Khanna Publishers, 36<sup>th</sup> Edition, 2010.
2. Erwin kreyszig, Advanced Engineering Mathematics, 9<sup>th</sup> Edition, John Wiley & Sons, 2006.
3. G.B. Thomas and R.L. Finney, Calculus and Analytic geometry, 9<sup>th</sup> Edition, Pearson, Reprint, 2002.

**REFERENCES:**

1. Paras Ram, Engineering Mathematics, 2<sup>nd</sup> Edition, CBS Publishes.
2. S. L. Ross, Differential Equations, 3<sup>rd</sup> Ed., Wiley India, 1984.
3. Engineering Mathematics-I, by Dr. T.K.V Iyengar and others, S Chand and Co.
4. Integral Calculus by Shanthi Narayan