

x_i y_i

7.6 157

7.1 174

Sample-1 Iteration-1

Step-1 :- $[7.6, 157]$, $\eta = 0.01$, $m = 1$, $c = -1$

$$\begin{aligned} 2) \quad \left. \frac{\partial E}{\partial m} \right|_{m=1} &= -(y_i^a - m x_i^a - c) \times (-x_i^a) \\ &= -(157 - 1(7.6) - (-1))(7.6) \\ &= (158 - 7.6)(7.6) \\ &= (150.4)(7.6) \\ &= 1143.04 \end{aligned}$$

$$\begin{aligned} \left. \frac{\partial E}{\partial c} \right|_{c=-1} &= -(y_i^a - m x_i^a - c) \\ &= -(157 - 1(7.6) - (-1)) \\ &= -(158 - 7.6) \\ &= -150.4 \end{aligned}$$

$$\begin{aligned} 3) \quad \Delta m &= -\eta \cdot \frac{\partial E}{\partial m} = -(0.01)(1143.04) \\ &= -11.430 \end{aligned}$$

$$\Delta c = -\eta \cdot \frac{\partial E}{\partial c} = -(0.01)(-150.4) = 1.504$$

$$m = m + \Delta m = 1 + (-11.43) = -10.43$$

$$c = c + \Delta c = -1 + 1.504 = 0.504$$

Iteration-2

$$D \quad [7.6, 157], \quad \eta = 0.01, \quad m = -10.43, \quad c = 0.504$$

$$\begin{aligned} 1) \quad \frac{\partial E}{\partial m} \Big|_{m=-10.43} &= - (157 - (-10.43)(7.6))(-0.504)(7.6) \\ &= (157 + 10.43(7.6) - 0.504)(7.6) \\ &= (156.496 + 79.268)(7.6) \\ &= (235.764)(7.6) \\ &= 1791.8 \end{aligned}$$

$$\begin{aligned} \frac{\partial E}{\partial c} \Big|_{c=0.504} &= - (157 - (-10.43)(7.6) - 0.504) \\ &= -235.764 \end{aligned}$$

$$\begin{aligned} 2) \quad \Delta m &= -\eta \cdot \frac{\partial E}{\partial m} = -(0.01)(1791.8) \\ &= -17.918 \end{aligned}$$

$$\begin{aligned} \Delta c &= -\eta \cdot \frac{\partial E}{\partial c} = -(0.01)(-235.764) \\ &= 2.357 \end{aligned}$$

$$3) \quad m = m + \Delta m = -10.43 + (-17.918) = -28.348$$

$$c = c + \Delta c = 0.504 + 2.357 = 2.861$$

sample - 2

Iteration-1

1) $[7.1, 174], \eta = 0.01, m = 1, c = -1$

$$\begin{aligned} 2) \frac{\partial E}{\partial m} \Big|_{m=1} &= -(y_i^a - mx_i^a - c)(-x_i^a) \\ &= (174 - 1(7.1) - (-1))(7.1) \\ &= (175 - 7.1)(7.1) \\ &= 167.9(7.1) = 1192.09 \end{aligned}$$

$$\begin{aligned} \frac{\partial E}{\partial c} \Big|_{c=-1} &= -(y_i^a - mx_i^a - c) \\ &= -(174 - 1(7.1) - (-1)) \\ &= -167.9 \end{aligned}$$

$$\begin{aligned} 3) \Delta m &= -\eta \cdot \frac{\partial E}{\partial m} \Big|_{m=1} = -(0.01)(1192.09) \\ &= -11.92 \end{aligned}$$

$$\begin{aligned} \Delta c &= -\eta \cdot \frac{\partial E}{\partial c} \Big|_{c=-1} = -(0.01)(-167.9) \\ &= 1.679 \end{aligned}$$

$$\begin{aligned} 4) m &= m + \Delta m = 1 + (-11.92) \\ &= -10.92 \end{aligned}$$

$$\begin{aligned} c &= c + \Delta c = -1 + 1.679 \\ &= 0.679 \end{aligned}$$

Iteration-2

$$1) [7.1, 174], \eta = 0.01, m = -10.92, c = +0.679$$

$$\begin{aligned} 2) \frac{\partial E}{\partial m} \Big|_{m=-10.92} &= - (174 - (-10.92)(7.1) - 0.679)(7.1) \\ &= (173.321 + 77.532)(7.1) \\ &= (250.853)(7.1) \\ &= 1781.056 \end{aligned}$$

$$\begin{aligned} \frac{\partial E}{\partial c} \Big|_{c=+0.679} &= - (174 - (-10.92)(7.1) - 0.679)(7.1) \\ &= -250.853 \end{aligned}$$

$$\begin{aligned} 3) \Delta m &= -\eta \cdot \frac{\partial E}{\partial m} = -(0.01)(1781.056) \\ &= -17.810 \end{aligned}$$

$$\begin{aligned} \Delta c &= -\eta \cdot \frac{\partial E}{\partial c} = -(0.01)(-250.853) \\ &= 2.508 \end{aligned}$$

$$4) m = m + \Delta m$$

$$= -10.92 - 17.81$$

$$= -28.73$$

$$c = c + \Delta c$$

$$= 0.679 + 2.508$$

$$= 3.187$$