Cluster analysis: Concepts and Techniques

Chapter 10. Cluster Analysis: Basic **Concepts and Methods**

Cluster Analysis: Basic Concepts <



- Partitioning Methods
- **Hierarchical Methods**
- **Density based Methods**
- Introduction to grid based method
- Summary

What is Cluster Analysis?

- Cluster: A collection of data objects
 - similar (or related) to one another within the same group
 - dissimilar (or unrelated) to the objects in other groups

Cluster analysis

- It is the task of grouping a set of objects in such a way that objects in the same group (called a cluster) are more similar to each other and than to those in other groups(clusters)
- Known as
 - Segmentation- (as it partitioning large datasets in to groups according to their similaritis)
- Unsupervised learning: clustering do not rely on predefind classes and class labeled training examples.
- Typical applications
 - As a stand-alone tool to get insight into data distribution
 - As a preprocessing step for other algorithms

Clustering: Application Examples

- Biology: taxonomy of living things: kingdom, phylum, class, order, family, genus and species
- Information retrieval: document clustering
- Land use: Identification of areas of similar land use in an earth observation database
- Marketing: Help marketers discover distinct groups in their customer bases, and then use this knowledge to develop targeted marketing programs
- City-planning: Identifying groups of houses according to their house type, value, and geographical location
- Climate: understanding earth climate, find patterns of atmospheric and ocean

Requirements for cluster analysis and Challenges

- Scalability
 - Clustering all the data instead of only on samples
- Ability to deal with different types of attributes
 - Numerical, binary, categorical, ordinal, linked, and mixture of these
- Constraint-based clustering
 - User may give inputs on constraints
 - Use domain knowledge to determine input parameters
- Interpretability and usability
- Others
 - Requirements for domain knowledge to determine input parameters
 - Discovery of clusters with arbitrary shape
 - Ability to deal with noisy data
 - Incremental clustering and insensitivity to input order
 - High dimensionality

Considerations for Cluster Analysis

Partitioning criteria

Single level vs. hierarchical partitioning (often, multi-level hierarchical partitioning is desirable)

Separation of clusters

 Exclusive (e.g., one customer belongs to only one region) vs. nonexclusive (e.g., one document may belong to more than one class)

Similarity measure

Distance-based (e.g., Euclidian) vs. connectivity-based (e.g., density)

Clustering space

 Full space (often when low dimensional) vs. subspaces (often in high-dimensional clustering)

Major Clustering Approaches

- Partitioning approach:
 - Construct various partitions and then evaluate them by some criterion
 - Typical methods: k-means, k-medoids, CLARANS
- Hierarchical approach:
 - Create a hierarchical decomposition of the set of data (or objects)
 using some criterion
 - Typical methods: Diana, Agnes, BIRCH, CAMELEON
- Density-based approach:
 - Based on connectivity and density functions
 - Typical methods: DBSACN, OPTICS, DenClue
- Grid-based approach: DBSCAN
 - based on a multiple-level granularity structure
 - Typical methods: STING, WaveCluster, CLIQUE

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- Partitioning Methods <</p>



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Partitioning Algorithms: Basic Concept

- Partitioning method: Partitioning a database D of n objects into a set of k clusters basd on a distance functions.
- Global optimal: exhaustively enumerate all partitions
- Heuristic methods: <u>k-means</u> and <u>k-medoids</u> algorithms

The K-Means Clustering Method

- The k-means algorithm partitions the given data into k clusters.
 - Each cluster has a cluster center, called cluster centroid.
 - The centroid, usually used to represent the cluster is simply the mean of all the data points in the cluster, which gives the name to the algorithm
 e.g k-means algorithm
 - k is specified by the user

K-means algorithm

- Given k, the k-means algorithm works as follows:
 - 1)Randomly choose k data points (seeds) to be the initial centroids, cluster centers
 - 2)Assign each data point to the closest centroid
 - 3)Re-compute the centroids using the current cluster memberships.
 - 4) If a stopping criterion is not met, go to 2).

K-means algorithm — (cont ...)

```
Algorithm k-means(k, D)
    Choose k data points as the initial centroids (cluster centers)
    repeat
3
       for each data point \mathbf{x} \in D do
           compute the distance from x to each centroid;
           assign x to the closest centroid // a centroid represents a cluster
       endfor
       re-compute the centroids using the current cluster memberships
    until the stopping criterion is met
8
```

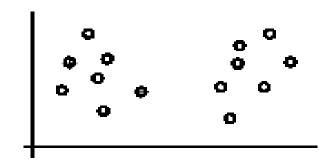
Stopping/convergence criterion

- no (or minimum) re-assignments of data points to different clusters,
- no (or minimum) change of centroids, or
- minimum decrease in the **sum of squared error** (SSE),

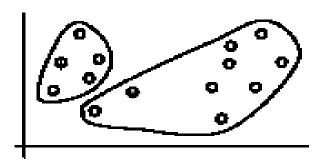
```
for(int j=1;j<=k;j++){
  for(int x: Cluster j){
    sse += distance(center of Cluster j, x)^2;
  }
}
SSE = \sum_{j=1}^{k} \sum_{\mathbf{x} \in C_{j}} dist(\mathbf{x}, \mathbf{m}_{j})^{2}
(1)
```

 C_j is the jth cluster, \mathbf{m}_j is the centroid of cluster C_j (the mean vector of all the data points in C_j), and $dist(\mathbf{x}, \mathbf{m}_j)$ is the distance between data point \mathbf{x} and centroid \mathbf{m}_j .

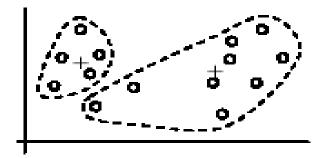
An example



(A). Random selection of k centers

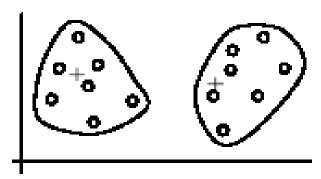


Iteration 1: (B). Cluster assignment

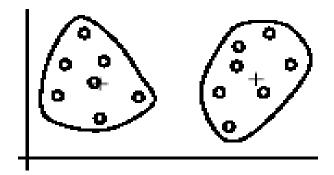


(C). Re-compute centroids

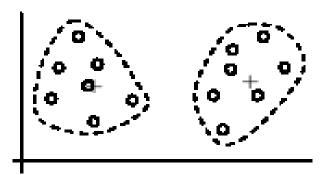
An example (cont ...)



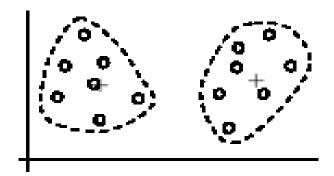
Iteration 2: (D). Cluster assignment



Iteration 3: (F). Cluster assignment



(E). Re-compute centroids



(G). Re-compute centroids

An example distance function

The k-means algorithm can be used for any application data set where the **mean** can be defined and computed. In the **Euclidean space**, the mean of a cluster is computed with:

$$\mathbf{m}_{j} = \frac{1}{|C_{j}|} \sum_{\mathbf{x}_{i} \in C_{j}} \mathbf{x}_{i} \tag{2}$$

where $|C_j|$ is the number of data points in cluster C_j . The distance from one data point \mathbf{x}_i to a mean (centroid) \mathbf{m}_i is computed with

$$dist(\mathbf{x}_{i}, \mathbf{m}_{j}) = ||\mathbf{x}_{i} - \mathbf{m}_{j}||$$

$$= |(x_{i1} - m_{j1})^{2} + (x_{i2} - m_{j2})^{2} + \dots + (x_{ir} - m_{jr})^{2}$$
(3)

Strengths of k-means

Strengths:

- Simple: easy to understand and to implement
- Efficient: Time complexity: O(tkn), where n is the number of data points, k is the number of clusters, and t is the number of iterations.
- Since both *k* and *t* are small. *k*-means is considered a linear algorithm.
- K-means is the most popular clustering algorithm.
- Note that: it terminates at a local optimum if SSE is used. The global optimum is hard to find due to complexity.

Weaknesses of k-means

- The algorithm is only applicable if the mean is defined.
 - For categorical data, k-mode the centroid is represented by most frequent values.
 - Handling categorical data: k-modes (Huang'98)
 - Replacing means of clusters with modes
 - Using new dissimilarity measures to deal with categorical objects
 - Using a frequency-based method to update modes of clusters
 - A mixture of categorical and numerical data
- The user needs to specify k.
- The algorithm is sensitive to outliers
 - Outliers are data points that are very far away from other data points.
 - Outliers could be errors in the data recording or some special data points with very different values

K-Medoids Method

- Minimize the sensitivity of k-means to outliers
- Pick actual objects to represent clusters instead of mean values
- Each remaining object is clustered with the representative object (Medoid) to which is the most similar
- The algorithm minimizes the sum of the dissimilarities between each object and its corresponding reference point

$$E = \sum_{i=1}^{k} \sum_{p \in C_i} |p - o_i|$$

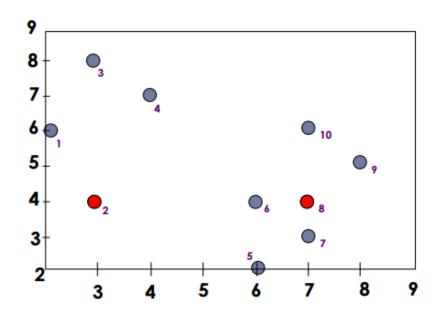
- → E: the sum of absolute error for all objects in the data set
- → P: the data point in the space representing an object
- → O_i: is the representative object of cluster C_i

K-Medoids Method

- Initial representatives are chosen randomly
- The iterative process of replacing representative objects by non representative objects continues as long as the quality of the clustering is improved
- For each representative Object O
 - For each non-representative object R, swap O and R
- Choose the configuration with the lowest cost
- Cost function is the difference in absolute error-value if a current representative object is replaced by a non-representative object

Data Objects

	\mathbf{A}_{1}	$\mathbf{A_2}$
O ₁	2	6
02	3	4
O_3	3	8
O_4	4	7
O ₅	6	2
O_6	6	4
. O ₇	7	3
√0 8	7	4
O ₉	8	5
O ₁₀	7	6



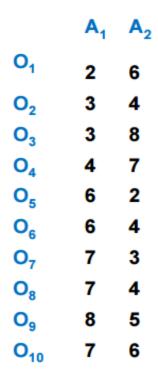
Goal: create two clusters

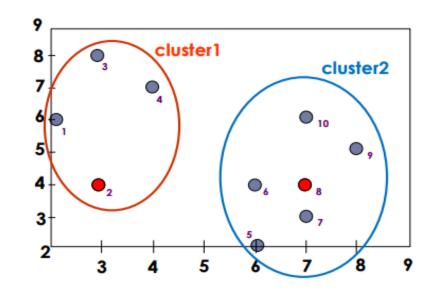
Choose randmly two medoids

$$O_2 = (3,4)$$

 $O_8 = (7,4)$

Data Objects



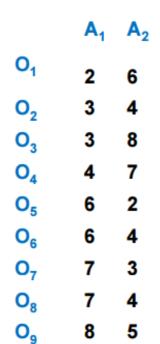


- →Assign each object to the closest representative object
- →Using L1 Metric (Manhattan), we form the following clusters

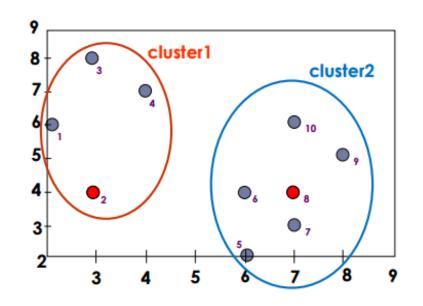
Cluster1 =
$$\{O_1, O_2, O_3, O_4\}$$

Cluster2 =
$$\{O_5, O_6, O_7, O_8, O_9, O_{10}\}$$

Data Objects



O₁₀

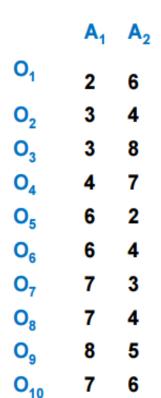


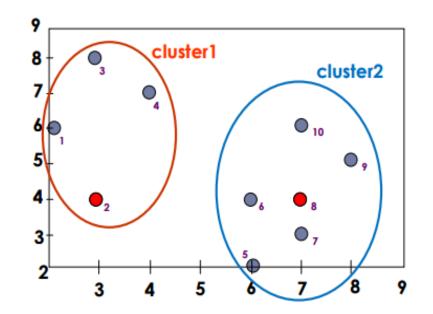
→Compute the absolute error criterion [for the set of Medoids (O2,O8)]

$$E = \sum_{i=1}^{k} \sum_{p \in C_i} p - o_i \mid = \mid o_1 - o_2 \mid + \mid o_3 - o_2 \mid + \mid o_4 - o_2 \mid$$

$$+|o_5-o_8|+|o_6-o_8|+|o_7-o_8|+|o_9-o_8|+|o_{10}-o_8|$$

Data Objects





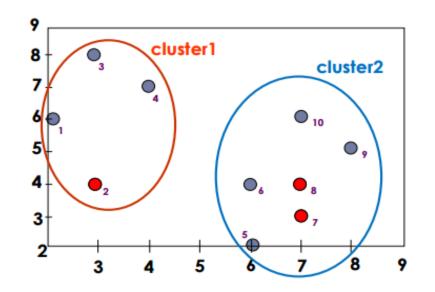
COSt

→The absolute error criterion [for the set of Medoids (O2,O8)]

$$E = (3+4+4)+(3+1+1+2+2) = 20$$

Data Objects

	\mathbf{A}_{1}	$\mathbf{A_2}$
O ₁	2	6
O ₂	3	4
O_3	3	8
O_4	4	7
O_5	6	2
O_6	6	4
O ₇	7	3
O _a	7	4



- →Choose a random object O₇
- →Swap **08** and **07**
- →Compute the absolute error criterion [for the set of Medoids (O2,O7)]

$$E = (3+4+4)+(2+2+1+3+3)=22$$

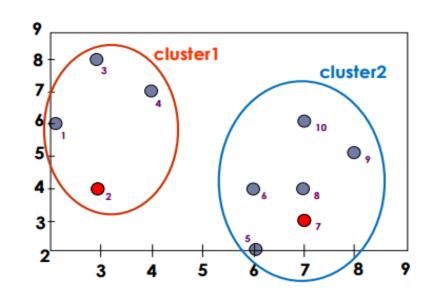




7

O₁₀

6



→Compute the cost function

Absolute error [for O_2, O_7] – Absolute error $[O_2, O_8]$

$$S = 22 - 20$$

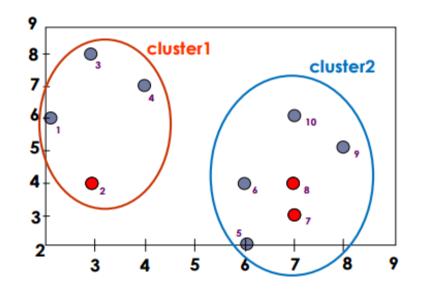
 $S>0 \Rightarrow it is a bad idea to replace <math>O_8$ by O_7

-ve value aaye S ki toh vapas calculate karo jab tak +ve value naa aa jaye

K-Medoids Method

Data Objects

	$\mathbf{A_1}$	A_2
O ₁	2	6
O ₂	3	4
O_3	3	8
O_4	4	7
O ₅	6	2
O_6	6	4
O ₇	7	3
O ₈	7	4
O ₉	8	5
O ₁₀	7	6



- In this example, changing the medoid of cluster 2 did not change the assignments of objects to clusters.
- What are the possible cases when we replace a medoid by another object?

K-Medoids Algorithm(PAM)

PAM: Partitioning Around Medoids

- Input
 - → K: the number of clusters
 - → D: a data set containing n objects
- Output: A set of k clusters
- Method:
 - (1) Arbitrary choose k objects from D as representative objects (seeds)
 - (2) Repeat
 - (3) Assign each remaining object to the cluster with the nearest representative object
 - (4) For each representative object O_i
 - (5) Randomly select a non representative object Orandom
 - (6) Compute the total cost **S** of swapping representative object Oj with O_{random}
 - (7) if S<0 then replace O_j with O_{random}
 - (8) Until no change

K-Medoids Properties(k-medoids vs.K-means)

- The complexity of each iteration is O(k(n-k)²)
- For large values of n and k, such computation becomes very costly

Advantages

 K-Medoids method is more robust than k-Means in the presence of noise and outliers

Disadvantages

- → K-Medoids is more costly that the k-Means method
- → Like k-means, k-medoids requires the user to specify k
- It does not scale well for large data sets

K-means vs k-medoids.

- What is the difference between K-means and k-medoids?
- K-means attempts to minimize the total squared error, while k-medoids minimizes the sum of dissimilarities between points labeled to be in a cluster and a point designated as the center of that cluster. In contrast to the k-means algorithm, k-medoids chooses data points as centers (medoids or exemplars).

Algorithm: k-medoids.

the minimum one

K-MEDOID	K=2	
i	x	y
×,	2	6
X 2	3	4
X3	3	8
X4	4	7
X ₅	6	2
X6	6	4
X ₂	7	3
Xs	7	4
Xq	8	5
X10	7	6

Step		į.		~ vales tative
We	Select	two	Tandom	representative
obie	ects:			
d				211)
	c. (3.)	1) .	C2 (7,9)

i	20	9	0	1	Distance / cost		C
×ı	2	6	3	4	12-31+16-4	1 -	3
×3	3	8	3	4	0 + 4	14	4
X4	4	7	3	4	1+3		4
X5	6	2	3	4	3+2		5
X6	6	4	3	4	3 + 0		3
X7	7	3	3	4	4+1		5
X9	8	5	3	4	5+1		6
×10	7	6	3	4	4+2		6
				Ole bonn a	m=(a,b) n=(c,d) la-cl+1b-d1		,

i	32	4	C	2	Distance / cost	C
XI.	2	6	7	4	12-71+16-41	7
×3	3	8	7	4	4+ 4	. 8
×4	4	7	7	4	3+5	6
×s	6	2	7	4	1+ 2	3
X6	6	4	7	4	1+0	1
׹	7	3	7	4	0+1	- 1
Xn	8	5	7	4	1+1	2
X10	7	6	7	4	0 + 2	2

Algorithm: k-medoids.

K-MEDOID EXAMPLE						
i	x	9				
×ı	2	6				
X 2	3	4				
Xa	3	8				
X4	4	7				
X ₅	6	2				
X6	6	4				
X ₂	7	3				
Xx	7	4				
Xq	8	5				
X10	7	6				

```
Step 1

we select two random representative objects:

C_1(3,4), C_2(7,4)
```

```
Step III) then cluster ove
 cluster 1: { (2,6), (3,8), (4,7), (3,4)}
cluster 2: { (7,4), (6,2), (6,4), (7,3), (8,5), (7,6) }
 Calculate total cost
T cost (2,6) = = | | | | | | |
    Total cost = { cost (3,4), (2,6), cost ((3,4), (3,8)),
                 cost ((3,4), (4,7)), cost ((7,4), (8,5)),
                 cost ((7,4), (6,2)), cost ((7,4), (6,4)),
                cost ((7,4), (7,3)), cost (17,4), (7,6) ).
            = (3+4+4)+(3+1+1+2+2)
             =20
step 3) Select one of non-medoids O'
       Let's 0'= (7,3) i.e x 7
```

Algorithm: k-medoids.

50	now	medoio	d'5 a7		3,4) 80'(7,3)	
i	×	9)'	Distance In	-
X,	2	6	7	3	(2-7) + 16-3)	-
×3	3	8	7	3	4+5	8
Xy	4	7	7	3	3+4	7
X5	6	2	7	3	1+1	7
X6	6	4	7	3	1+1	2
×8	7	4	7	3	0+1	2
×9	8	5	7	3	1+2	3
Xio	7	6	7	3	0+3	3

compare the cost of cost (ci) and cost (o') for every i & Select the minimum one

i	x	y		c,	Distance / cost	C
x,	2	6	3	4	12-31+16-4)	= 3
X3	3	8	3	4	0+4	= 4
X4	4	7	3	4	1+3	= 4
25	6	2	3	4	3 +2	= 5
X6	6	4	3	4	3+0	23
×g	7	4	3	4	4+0	= 4
Xq	8	5	3	4	5+1	= 6
XIO	7	6	3	4	4+2	=6

```
#gain cheeate the cluster

cluster 1: \( \) (3,4), (2,6), (3,8), (4,7) \( \) (105 ter 2: \( \) (7,3), (6,2), (5,4), (7,4), (8,5), (7,6) \( \) (278 cnt total cost = (3+4+4) + (2+2+1+3+3)

= 11+11

= 22

Stop 4) So cost of Swapping medoid from (2 to 0' 's

S = cwrent total cost - past total cost
```

so, moving o' would be a badidea so previous choice was

Good

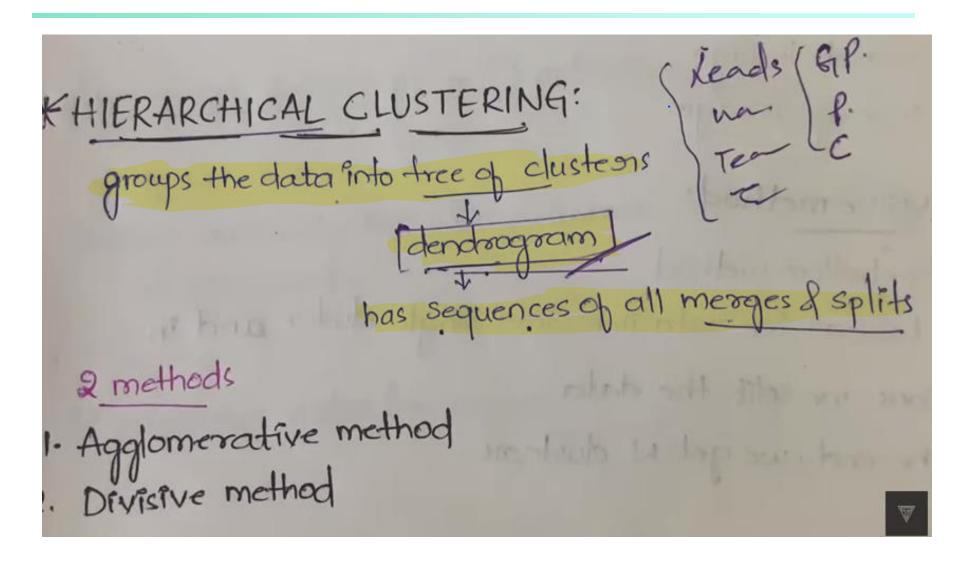
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- Partitioning Methods
- Hierarchical Methods



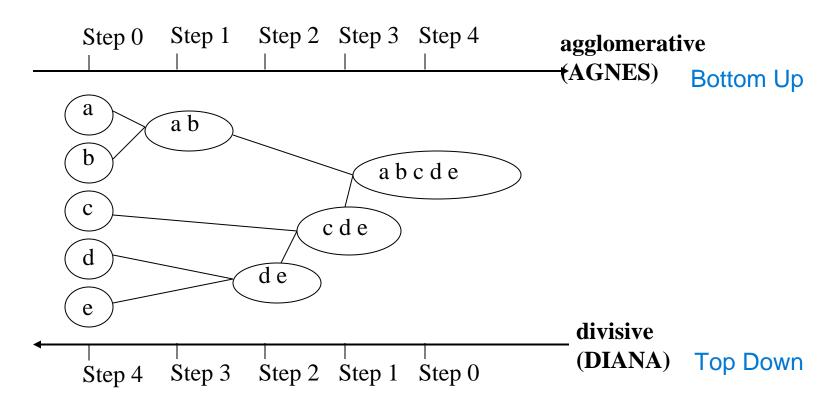
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Hierarchical Clustering

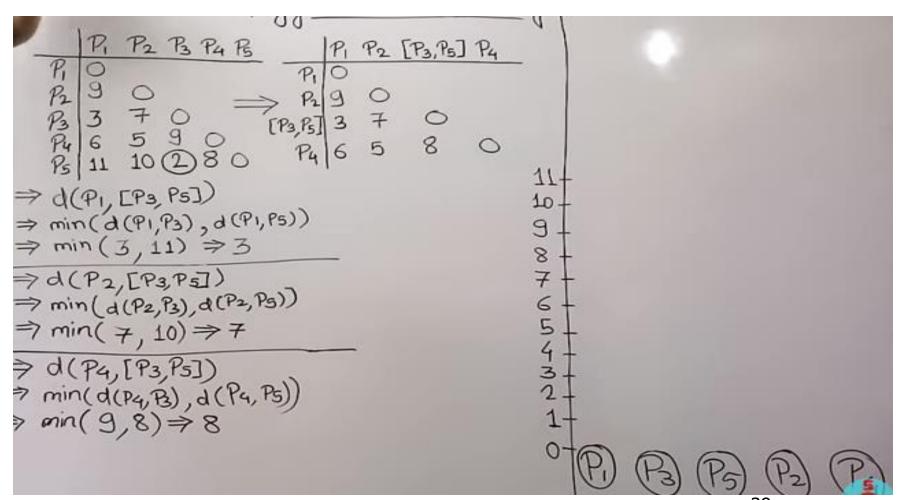


Hierarchical Clustering

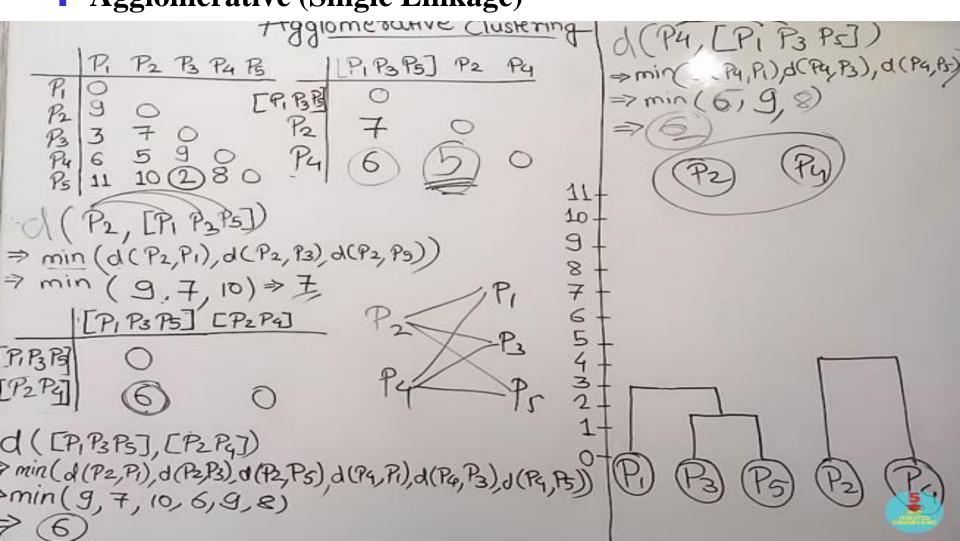
 Use distance matrix as clustering criteria. This method does not require the number of clusters k as an input, but needs a termination condition



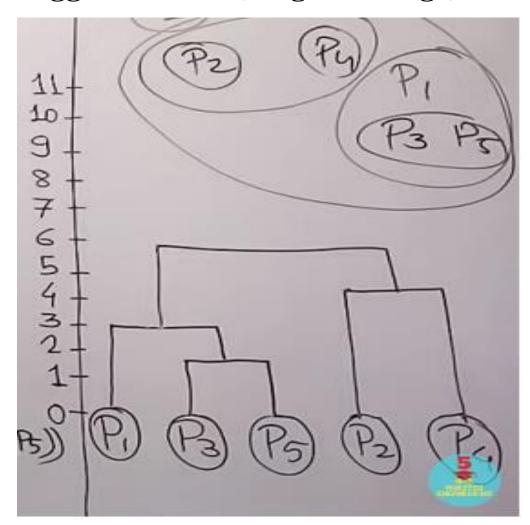
Agglomerative (Single Linkage)



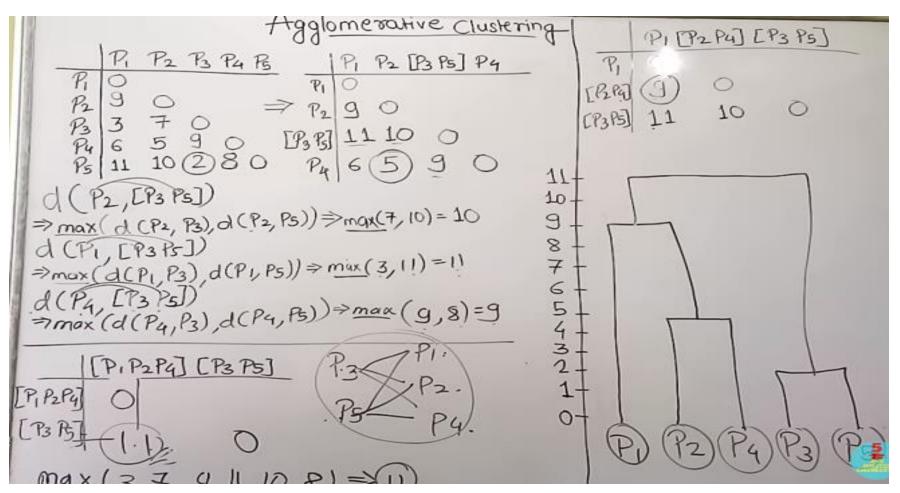
Agglomerative (Single Linkage)



Agglomerative (Single Linkage)

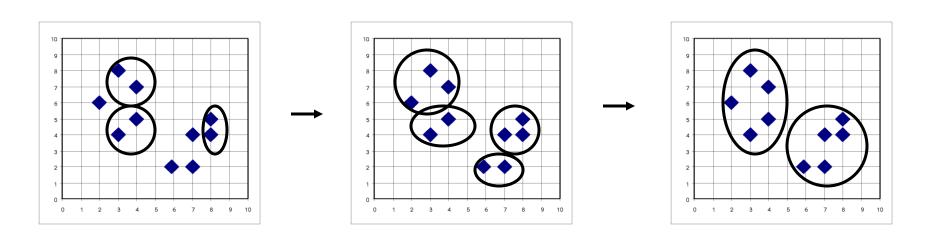


Agglomerative (Complete Linkage)

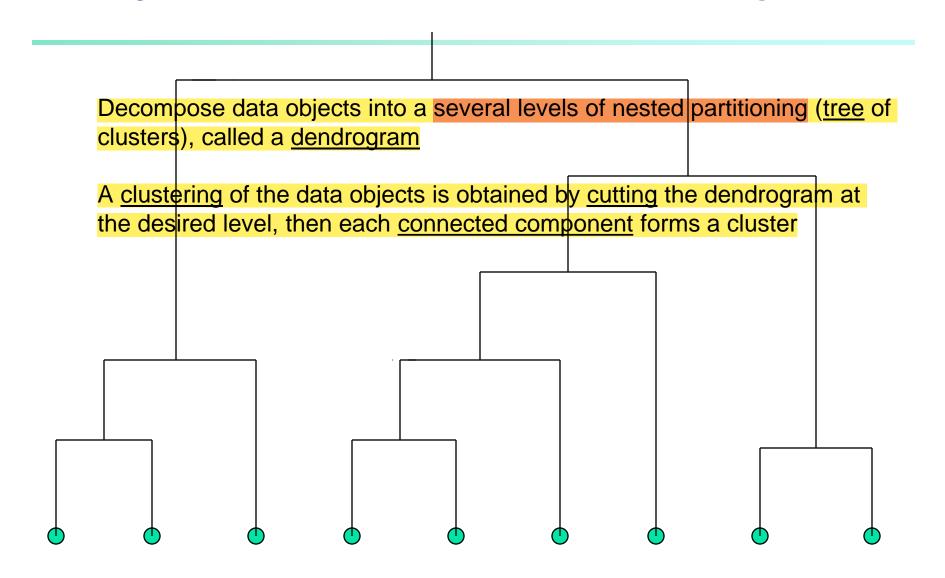


AGNES (Agglomerative Nesting)

- Introduced in Kaufmann and Rousseeuw (1990)
- Implemented in statistical packages, e.g., Splus
- Use the single-link method and the dissimilarity matrix
- Merge nodes that have the least dissimilarity
- Go on in a non-descending fashion
- Eventually all nodes belong to the same cluster

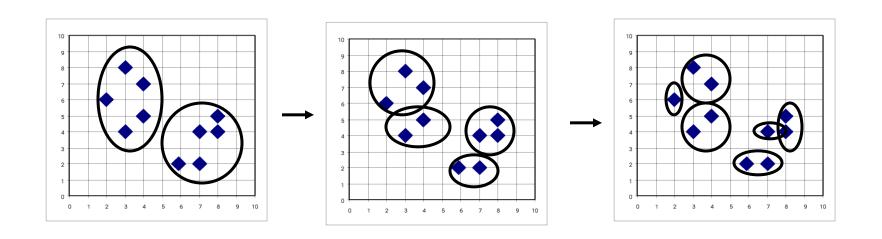


Dendrogram: Shows How Clusters are Merged



DIANA (Divisive Analysis)

- Introduced in Kaufmann and Rousseeuw (1990)
- Implemented in statistical analysis packages, e.g., Splus
- Inverse order of AGNES
- Eventually each node forms a cluster on its own

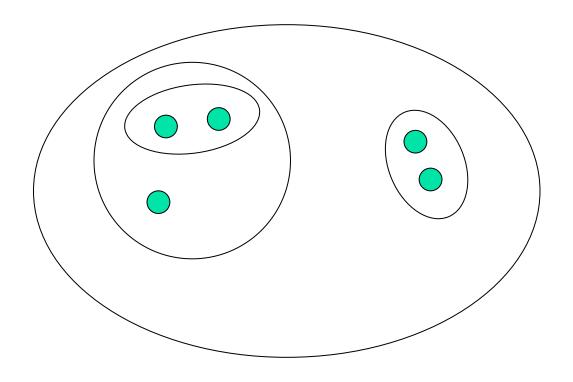


Extensions to Hierarchical Clustering

- Major weakness of agglomerative clustering methods
 - Can never undo what was done previously
 - <u>Do not scale</u> well: time complexity of at least $O(n^2)$, where n is the number of total objects
- Integration of hierarchical & distance-based clustering
 - BIRCH (1996): uses CF-tree and incrementally adjusts
 the quality of sub-clusters
 - CHAMELEON (1999): hierarchical clustering using dynamic modeling

- BIRCH: Balanced Iterative Reducing and Clustering Using Hierarchies
- Agglomerative Clustering designed for clustering a large amount of numerical data
- What Birch algorithm tries to solve?
 - Most of the existing algorithms DO NOT consider the case that datasets can be too large to fit in main memory
 - They DO NOT concentrate on minimizing the number of scans of the dataset
 - → I/O costs are very high
- The complexity of BIRCH is O(n) where n is the number of objects to be clustered.

Hierarchical clustering



Hierarchical clustering

Agnes

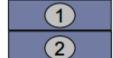
- The algorithm starts with single point clusters (every point in a database is a cluster).
- Then it groups the closest points into separate clusters, and continues, until only one cluster remains.

Clustering Feature CF

- The BIRCH algorithm builds a clustering feature tree (CF tree) while scanning the data set.
- Each entry in the CF tree represents a cluster of objects and is characterized by a triple (N, LS, SS).

Here n is the number of data points LS is the linear sum of n data points SS is the square sum of n data points

Data Objects



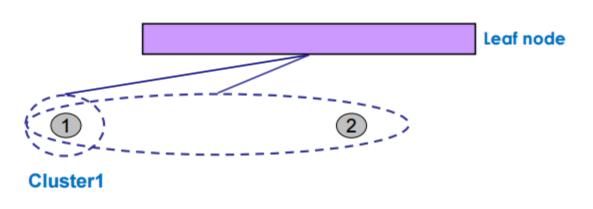
3

4

5

6

Clustering Process (build a tree)



If cluster 1 becomes too large (not compact) by adding object 2, then split the cluster

Data Objects



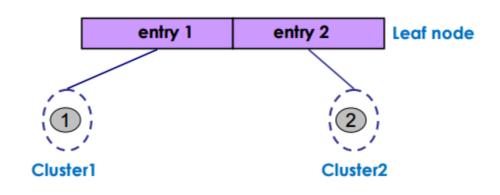
2



<u>5</u>

(6)

Clustering Process (build a tree)

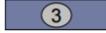


Leaf node with two entries

Data Objects



2

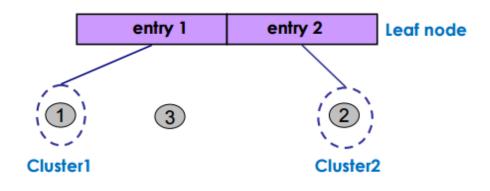


4

<u>5</u>

6

Clustering Process (build a tree)

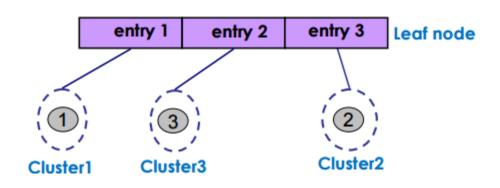


entry1 is the closest to object 3

If cluster 1 becomes too large by adding object 3, then split the cluster

Data Objects

Clustering Process (build a tree)

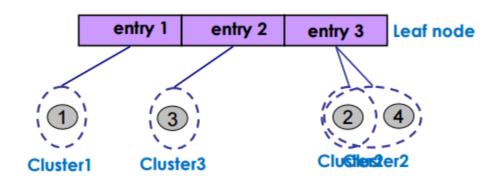


Leaf node with three entries

Data Objects

- 1
- 2
- 3
- 4
 - **5**
 - 6

Clustering Process (build a tree)



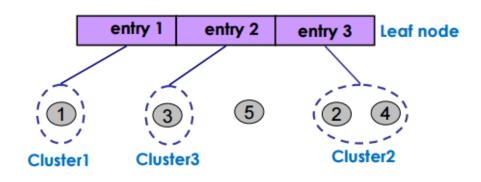
entry3 is the closest to object 4

Cluster 2 remains compact when adding object 4 then add object 4 to cluster 2

Data Objects

- 1
- 2
- 3
- 4
- 5
 - **6**

Clustering Process (build a tree)



entry2 is the closest to object 5

Cluster 3 becomes too large by adding object 5 then split cluster 3?

BUT there is a limit to the number of entries a node can have Thus, split the node

Clustering Process (build a tree) Non-Leaf node entry 1 entry 2 entry 1.1 entry 1.2 entry 2.1 entry 2.2 Leaf node (1) (3)

Cluster4

Cluster3

Cluster1

Data Objects





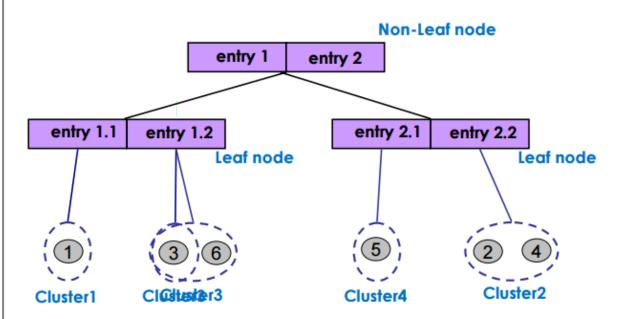
3

4

5

(6)

Clustering Process (build a tree)

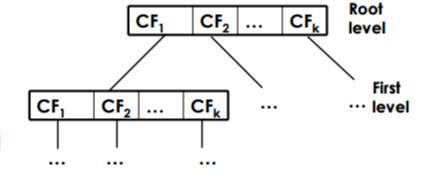


entry 1.2 is the closest to object 6

Cluster 3 remains compact when adding object 6 then add object 6 to cluster 3

CF Tree

- B = Branching Factor, maximum children in a non-leaf node
- T = Threshold for diameter or radius
 of the cluster in a leaf
- L = number of entries in a leaf



- CF entry in parent = sum of CF entries of a child of that entry
- In-memory, height-balanced tree

Clustering Feature

Clustering Feature (CF): CF = (N, LS, SS)

N: Number of data points

LS: linear sum of N points: $\sum_{i=1}^{N} X_i$

SS: square sum of N points: $\sum_{i=1}^{N} X_i^2$

CF3=CF1+CF2= $\langle 3+3, (9+35, 10+36), (29+417, 38+440) \rangle = \langle 6, (44,46), (446,478) \rangle$

$$CF_1 = \langle 3, (2+3+4, 5+2+3), (2^2+3^2+4^2, 5^2+2^2+3^2) \rangle = \langle 3, (9,10), (29,38) \rangle$$

CF Tree

- The leave contains actual clusters.
- The size of any cluster in a leaf is not larger than T.

• An example of the CF Tree

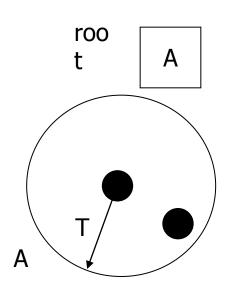
Initially, the data points in one cluster.

roo t A

Α

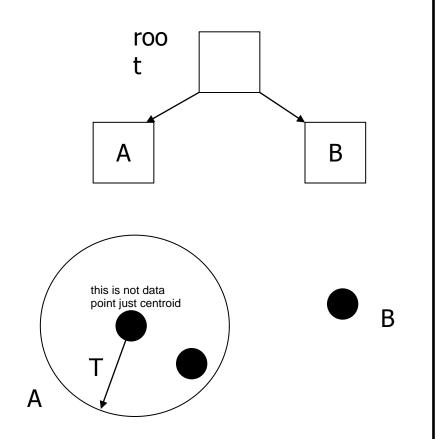
• An example of the CF Tree

The data arrives, and a check is made whether the size of the cluster does not exceed *T*.



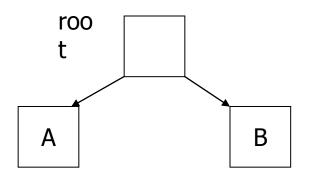
• An example of the CF Tree

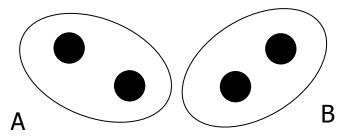
If the cluster size grows too big, the cluster is split into two clusters, and the points are redistributed.

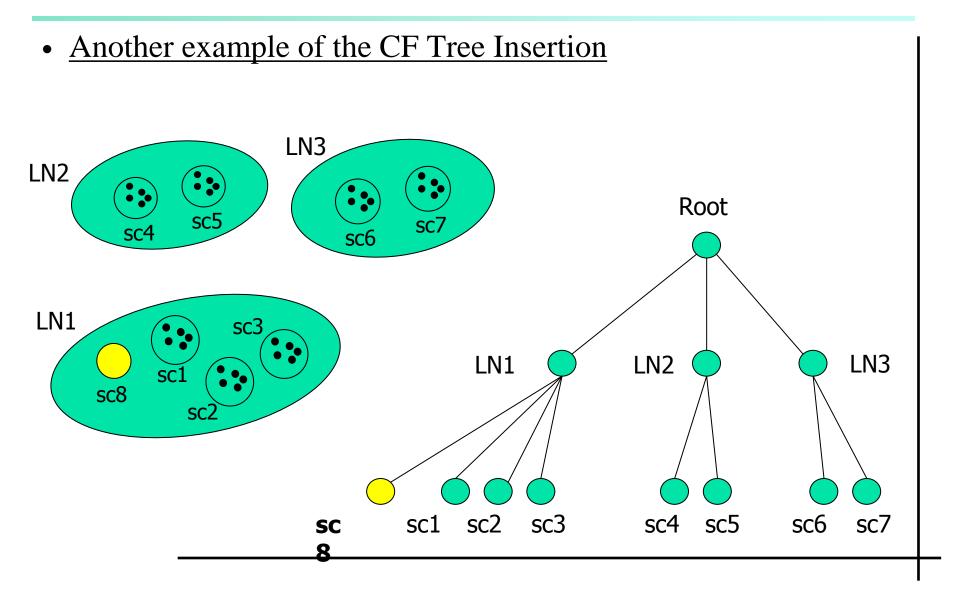


• An example of the CF Tree

At each node of the tree, the CF tree keeps information about the mean of the cluster, and the mean of the sum of squares to compute the size of the clusters efficiently.

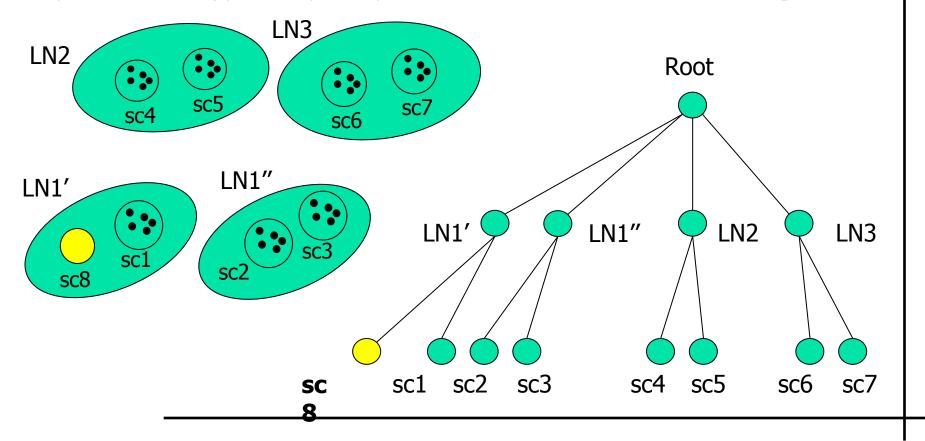


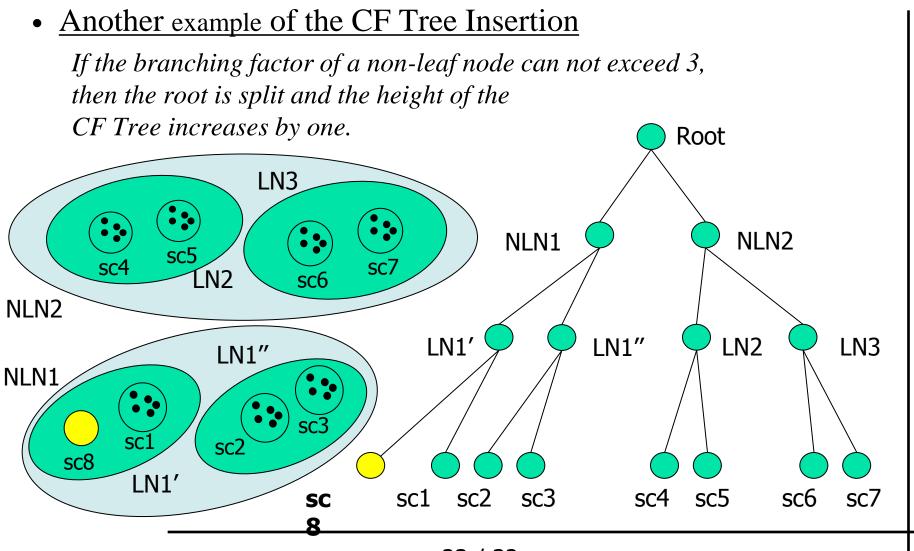




• Another example of the CF Tree Insertion

If the branching factor of a leaf node can not exceed 3, then LN1 is split.





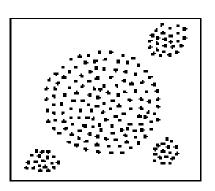
Chapter 10. Cluster Analysis: Basic **Concepts and Methods**

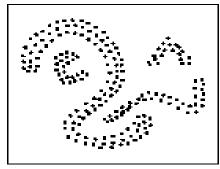
- Cluster Analysis: Basic Concepts
- Partitioning Methods
- **Hierarchical Methods**
- Density based Methods <

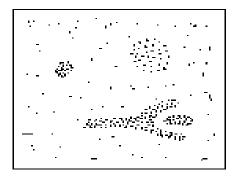


- Introduction to grid based method
- Summary

Density-based Approaches





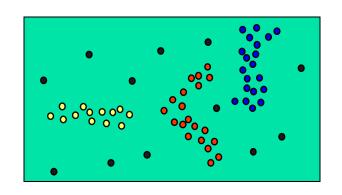


- Why Density-Based Clustering methods?
 - Discover clusters of arbitrary shape.
 - Clusters Dense regions of objects separated by regions of low density

Density-Based Clustering

• Basic Idea:

Clusters are dense regions in the data space, separated by regions of lower object density



Major features:

Discover clusters of arbitrary shape

Handle noise

One scan

Need density parameters

Several interesting studies:

DBSCAN: Ester, et al. (KDD'96)

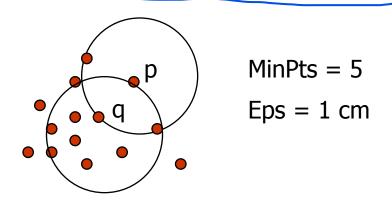
DENCLUE: Hinneburg & D. Keim (KDD'98/2006)

OPTICS: Ankerst, et al (SIGMOD'99).

<u>CLIQUE</u>: Agrawal, et al. (SIGMOD'98)

Density Concepts

- Two global parameters:
 - Eps: Maximum radius of the neighbourhood
 - MinPts: Minimum number of points in an Eps-neighbourhood of that point
- Core Object: object with at least MinPts objects within a radius 'Epsneighborhood'
- Border Object: object that on the border of a cluster

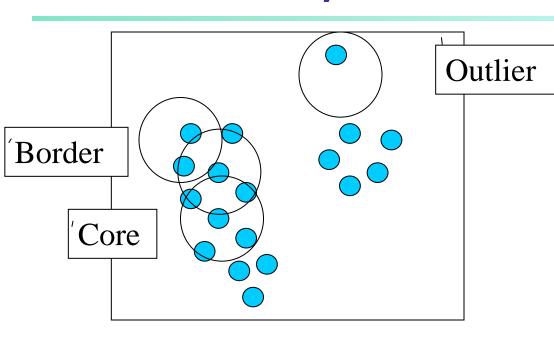


DBSCAN

(http://www2.cs.uh.edu/~ceick/7363/Papers/dbscan.pdf)

- DBSCAN is a density-based algorithm.
 - Density = number of points within a specified radius r (Eps)
 - A point is a core point if it has more than a specified number of points (MinPts) within Eps
 - These are points that are at the interior of a cluster
 - A border point has fewer than MinPts within Eps, but is in the neighborhood of a core point
 - A noise point is any point that is not a core point or a border point.

Core, Border & Outlier

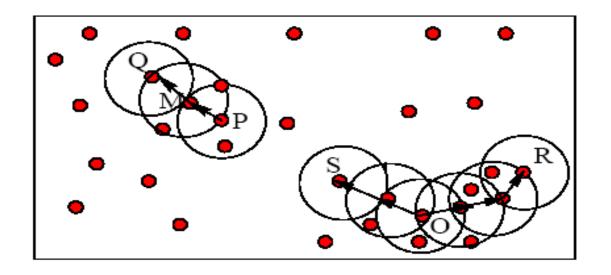


Given ε and *MinPts*, categorize the objects into three exclusive groups.

 $\varepsilon = 1$ unit, MinPts = 5

Example

 M, P, O, and R are core objects since each is in an Eps neighborhood containing at least 3 points

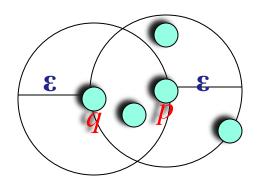


Minpts = 3
Eps=radius
of the
circles

Density-Reachability

■ Directly density-reachable

• An object q is directly density-reachable from object p if p is a core object and q is in p's ε-neighborhood.

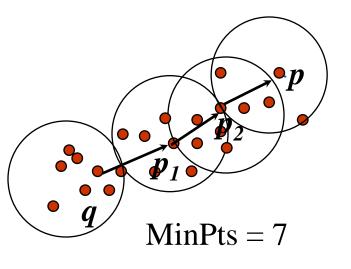


MinPts = 4

- q is directly density-reachable from p
- p is not directly density- reachable from q? No because q is not core object
- □ Density-reachability is asymmetric.

Density-reachability

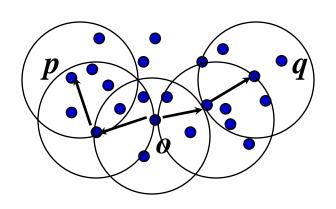
- Density-Reachable (directly and indirectly):
 - A point p is directly density-reachable from p2;
 - p2 is directly density-reachable from p1;
 - p1 is directly density-reachable from q;
 - $p\square$ $p2\square$ $p1\square$ q form a chain.



- □ p is (indirectly) density-reachable from q
- □ q is not density- reachable from p?

Density-Connectivity

- □ Density-reachable is not symmetric
 - not good enough to describe clusters
- **□ Density-Connected**
 - A pair of points p and q are density-connected if they are commonly density-reachable from a point o.

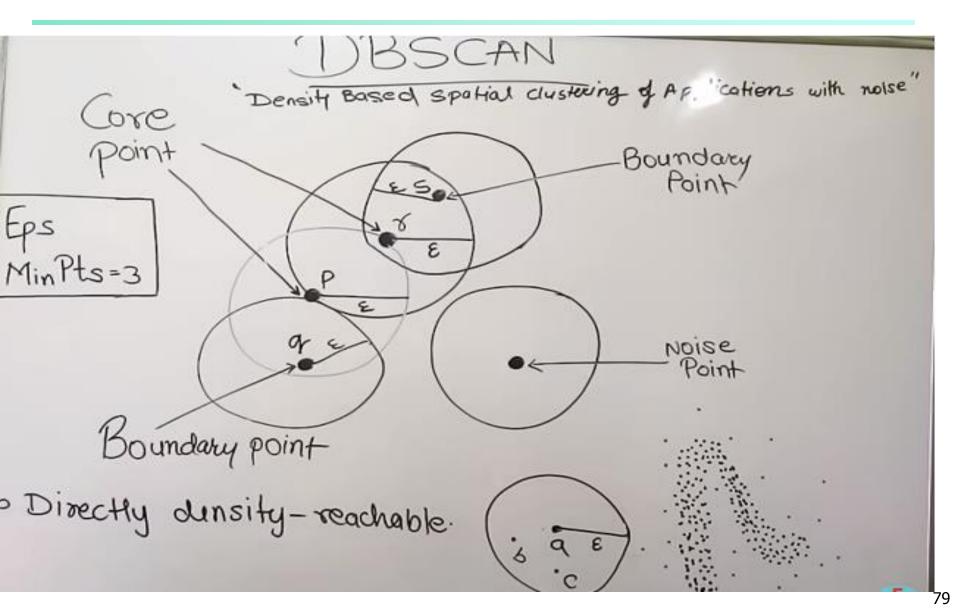


☐ Density-connectivity is symmetric

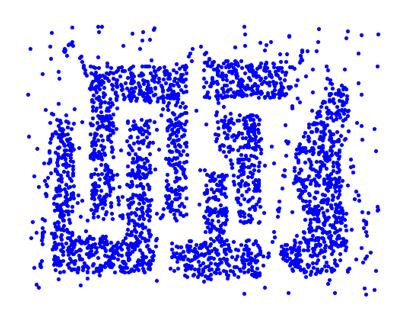
DBSCAN: The Algorithm

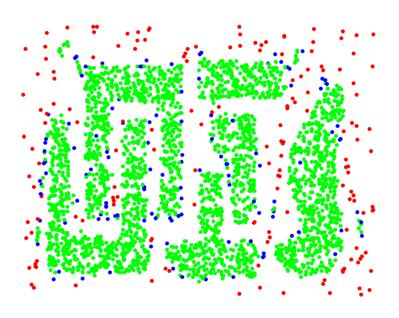
- Arbitrary select a point p
- Retrieve all points density-reachable from p wrt Eps and MinPts.
- If p is a core point, a cluster is formed.
 from ke baad core point aata hai and p is not core point
- If p is a border point, no points are density-reachable from p and DBSCAN visits the next point of the database.
- Continue the process until all of the points have been processed.

Density-Based Clustering: DBSCAN



Example



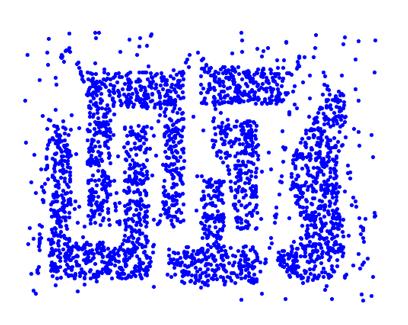


Original Points

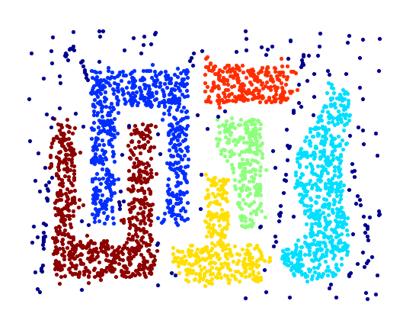
Point types: core, border and outliers

 $\varepsilon = 10$, MinPts = 4

When DBSCAN Works Well



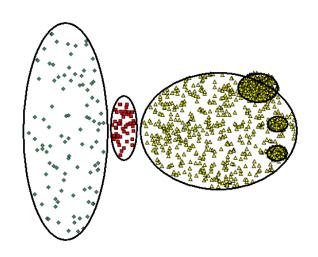
Original Points



Clusters

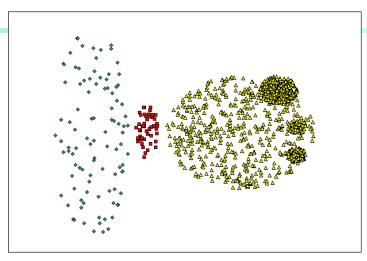
- Resistant to Noise
- Can handle clusters of different shapes and sizes

When DBSCAN Does NOT Work Well

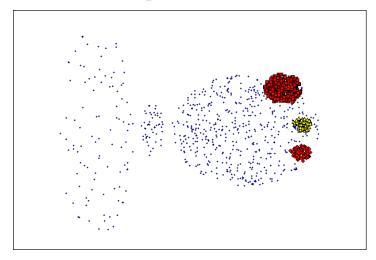


Original Points

- Cannot handle Varying densities
- sensitive to parameters



(MinPts=4, Eps=9.92).



(MinPts=4, Eps=9.75)

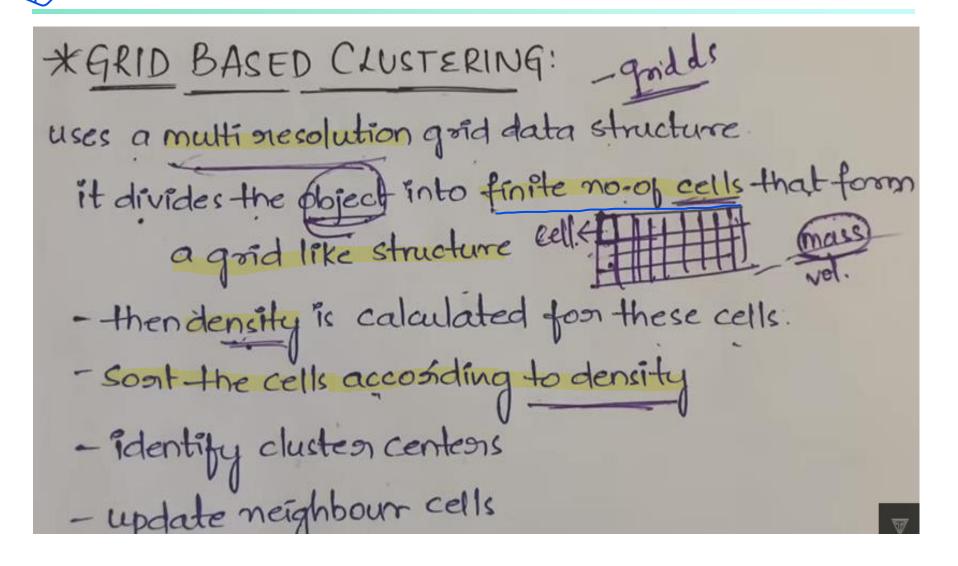
Chapter 10. Cluster Analysis: Basic **Concepts and Methods**

- Cluster Analysis: Basic Concepts
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- **Hierarchical Methods**
- **Density based Methods**
- Introduction to grid based method 🤝



Summary





Ex: STING

(Statistical Information Good clustering Algorithm)

like maps

- spatial data is divided into rectangular cells at different levels of necolution, these cells from a tree structure

cells at higher level-contains smaller cells compared
to its lower levels.

elustering - done based on parameters.

(mean, cauntimin, max, 50, type of distribution

-calculation of these parameters should start at



Chapter 10. Cluster Analysis: Basic Concepts and Methods

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Determine the Number of Clusters

- **Empirical method**
 - # of clusters: $k \approx \sqrt{n/2}$ for a dataset of n points, e.g., n = 200, k = 10
- Other methods:
 - Elbow method
 - Cross validation method

Summary

- Cluster analysis groups objects based on their similarity and has wide applications
- Clustering algorithms can be categorized into partitioning methods, hierarchical methods, density-based methods, grid-based methods, and model-based methods
- K-means and K-medoids algorithms are popular partitioning-based clustering algorithms
- Birch and Chameleon are interesting hierarchical clustering algorithms, and there are also probabilistic hierarchical clustering algorithms
- DBSCAN, OPTICS, and DENCLU are interesting density-based algorithms
- STING and CLIQUE are grid-based methods, where CLIQUE is also a subspace clustering algorithm
- Quality of clustering results can be evaluated in various ways