Problem 4

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R setup

1. Load Data

```
# NOTE: Data files must be in a 'Data' subdirectory relative to this R Markdown file
# Expected structure:
# - prob4.Rmd
# - Data/
# |- Laptop_train.csv
# |- Laptop_test.csv
setwd(dirname(rstudioapi::getSourceEditorContext()$path))
# Read CSV files using relative paths
df_train <- read_csv("Data/laptop_train.csv")</pre>
```

```
## Rows: 665 Columns: 9
## — Column specification —
## Delimiter: ","
## chr (3): Company, TypeName, GPU
## dbl (6): InventoryID, Screen, Memory, Weight, Rating, Price
##
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

```
df_test <- read_csv("Data/laptop_test.csv")</pre>
```

```
## Rows: 280 Columns: 9
## — Column specification —
## Delimiter: ","
## chr (3): Company, TypeName, GPU
## dbl (6): InventoryID, Screen, Memory, Weight, Rating, Price
##
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

2. Data Exploration

```
head(df_train)
```

```
## # A tibble: 6 x 9
   InventoryID Company TypeName GPU Screen Memory Weight Rating Price
       ## 1
        15 Asus Gaming Nvidia 17.3 16 2.73
## 2
                                                3 2050.
## 3
        17 Asus Gaming Nvidia 15.6 16 2.5
                                                4 1799
                                               10 998
## 4
        18 Asus Gaming Nvidia 17.3 16 4
         38 Asus Gaming Nvidia 15.6 8 2.3
40 Asus Gaming Nvidia 17.3 8 3
## 5
                                         2.3
                                                 6 1649
                                               9 1168
## 6
```

```
head(df_test)
```

```
## # A tibble: 6 × 9
## InventoryID Company TypeName GPU Screen Memory Weight Rating Price
        <dbl> <chr> <chr> <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
##
                   Gaming Nvidia 15.6 16 2.2
## 1
          1 Asus
                                                    8 1449
                   Gaming AMD
## 2
          29 Asus
                                  15.6
                                         8
                                             2.45
                                                    10 699
                   Gaming Nvidia 17.3 8 3
## 3
          30 Asus
                                                    7 938
                                                   5 1039
          35 Asus
                   Gaming Nvidia 17.3 8 3
## 5
         56 Asus
                   Notebook Intel 15.6 4 2.37 6 399.
                   Notebook Intel 15.6 4 2
## 6
          62 Asus
                                                    5 559
```

```
# We want to know the dimensions of our dataset.
dim(df_train) # there are 9 features and 665 observations
```

```
## [1] 665 9
```

dim(df_test) # there are 9 features and 280 observations

```
## [1] 280   9
```

str(df_train) # structure (variable types, first few entries)

```
## spc_tbl_[665 \times 9] (S3: spec_tbl_df/tbl_df/tbl/data.frame)
## $ InventoryID: num [1:665] 6 15 17 18 38 40 41 45 46 47 ...
                : chr [1:665] "Asus" "Asus" "Asus" "Asus" ...
## $ Company
               : chr [1:665] "Gaming" "Gaming" "Gaming" ...
## $ TypeName
                : chr [1:665] "Nvidia" "Nvidia" "Nvidia" "Nvidia" ...
## $ GPU
                : num [1:665] 17.3 17.3 15.6 17.3 15.6 17.3 15.6 15.6 15.6 15.6 ...
## $ Screen
## $ Memory
                : num [1:665] 16 16 16 16 8 8 8 8 8 16 ...
## $ Weight
                : num [1:665] 2.9 2.73 2.5 4 2.3 ...
## $ Rating
                : num [1:665] 1 3 4 10 6 9 4 6 8 4 ...
## $ Price
                : num [1:665] 2122 2050 1799 998 1649 ...
## - attr(*, "spec")=
##
    .. cols(
##
     .. InventoryID = col_double(),
    .. Company = col_character(),
    .. TypeName = col_character(),
##
##
    .. GPU = col_character(),
    .. Screen = col_double(),
.. Memory = col_double(),
##
##
    .. Weight = col_double(),
##
##
    .. Rating = col_double(),
##
    .. Price = col_double()
##
    .. )
## - attr(*, "problems")=<externalptr>
```

str(df_test) # structure (variable types, first few entries)

```
## spc_tbl_ [280 \times 9] (S3: spec_tbl_df/tbl_df/tbl/data.frame)
## $ InventoryID: num [1:280] 1 29 30 35 56 62 143 146 158 160 ...
## $ Company : chr [1:280] "Asus" "Asus" "Asus" "Asus" ...
               : chr [1:280] "Gaming" "Gaming" "Gaming" ...
## $ TypeName
               : chr [1:280] "Nvidia" "AMD" "Nvidia" "Nvidia" ...
## $ GPU
## $ Screen
                : num [1:280] 15.6 15.6 17.3 17.3 15.6 15.6 15.6 15.6 15.6 15.6 ...
               : num [1:280] 16 8 8 8 4 4 16 16 8 8 ...
## $ Memory
## $ Weight
               : num [1:280] 2.2 2.45 3 3 2.37 2 3.49 2.62 2.62 2.62 ...
## $ Rating
             : num [1:280] 8 10 7 5 6 5 3 1 7 4 ...
               : num [1:280] 1449 699 938 1039 399 ...
## $ Price
## - attr(*, "spec")=
##
    .. cols(
    .. InventoryID = col_double(),
##
    .. Company = col_character(),
##
    .. TypeName = col_character(),
    .. GPU = col_character(),
##
##
         Screen = col_double(),
    .. Memory = col_double(),
##
    .. Weight = col_double(),
##
    .. Rating = col_double(),
##
    .. Price = col_double()
##
    .. )
## - attr(*, "problems")=<externalptr>
```

summary(df_train) # summary statistics by column

```
GPU
##
    InventoryID
                  Company
                                    TypeName
## Min. : 2.0 Length:665
                                                   Length:665
                                  Length:665
## 1st Qu.:226.0 Class :character Class :character Class :character
##
  Median :461.0
                 Mode :character Mode :character Mode :character
   Mean :461.9
##
##
  3rd Qu.:693.0
##
  Max. :945.0
##
       Screen
                     Memory
                                    Weight
                                                  Rating
## Min. :12.50 Min. : 4.000 Min. :0.91 Min. : 1.000
##
   1st Ou.:14.00
                 1st Qu.: 4.000
                                1st Qu.:1.70
                                              1st Qu.: 3.000
##
   Median :15.60
                 Median : 8.000
                                 Median :2.06
                                              Median : 5.000
  Mean :15.21
##
                 Mean : 7.829
                                 Mean :2.09 Mean : 5.402
   3rd Qu.:15.60
                 3rd Qu.: 8.000
                                3rd Qu.:2.30 3rd Qu.: 8.000
##
   Max. :17.30 Max. :16.000 Max. :4.60 Max. :10.000
##
      Price
##
   Min. : 224
##
   1st Qu.: 589
##
  Median: 899
  Mean :1027
## 3rd Qu.:1280
## Max. :3154
```

```
summary(df_test) # summary statistics by column
```

```
InventoryID
                   Company
                                    TypeName
                                                       GPU
## Min. : 1.0
                 Length:280
                                                   Length:280
                                  Length:280
## 1st Qu.:254.0 Class :character Class :character Class :character
## Median :491.5 Mode :character Mode :character Mode :character
## Mean :499.3
##
   3rd Qu.:750.8
##
   Max. :944.0
##
     Screen
                     Memory
                                    Weight
                                                  Rating
## Min. :12.50 Min. : 4.000 Min. :0.990 Min. : 1.000
## 1st Qu.:14.00 1st Qu.: 4.000 1st Qu.:1.700 1st Qu.: 3.000
## Median :15.60 Median : 8.000
                                Median :2.040
                                              Median : 5.000
                                Mean :2.053
   Mean :15.24
                 Mean : 7.486
                                               Mean : 5.354
##
   3rd Qu.:15.60
                 3rd Qu.: 8.000
                                3rd Qu.:2.300
                                               3rd Qu.: 8.000
##
  Max. :17.30 Max. :16.000 Max. :4.600 Max. :10.000
##
      Price
## Min. : 274.9
##
   1st Qu.: 598.7
##
   Median : 897.5
## Mean : 998.5
## 3rd Qu.:1268.0
## Max. :2999.0
```

```
colSums(is.na(df_train)) # number of NAs per column
```

```
## InventoryID
                               TypeName
                                                GPU
                   Company
                                                         Screen
                                                                      Memory
            0
                         0
                                     0
##
        Weight
                    Rating
                                  Price
##
            0
                         0
                                      0
```

```
anyNA(df_train) # check if dataset has any missing values
```

```
## [1] FALSE
```

3. Create Binary Target Variable

We are creating a new binary column high for both the test and train dataframes which is 1 if the price is 500 Euros or higher, and 0 otherwise If a laptop's price is \geq 500 Euros, it gets high = 1 (expensive). If it's \leq 499.99 Euros, it gets high = 0 (not expensive).

```
# Add binary column 'high' to training and test datasets

df_train <- df_train %>%
   mutate(high = ifelse(Price >= 500, 1, 0))

df_test <- df_test %>%
   mutate(high = ifelse(Price >= 500, 1, 0))

# Check the distribution of the new binary variable in training set
table(df_train$high)
```

```
##
## 0 1
## 115 550
```

```
prop.table(table(df_train$high))
```

```
##
## 0 1
## 0.1729323 0.8270677
```

```
# Check distribution in test set
table(df_test$high)
```

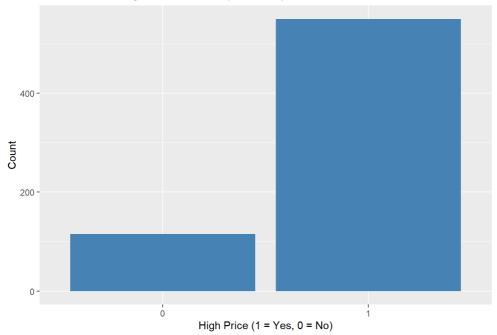
```
##
## 0 1
## 53 227
```

```
prop.table(table(df_test$high))
```

```
##
## 0 1
## 0.1892857 0.8107143
```

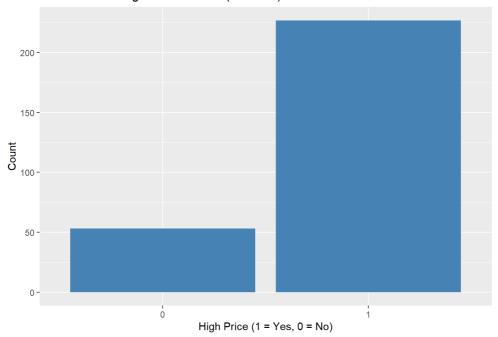
The following plot shows the count of laptops in the training set that are classified as high price (1) or low price (0). The bars are colored steel blue for better visualization.

Distribution of High vs Low Price (Train Set)



We do the same for the test set.

Distribution of High vs Low Price (Test Set)

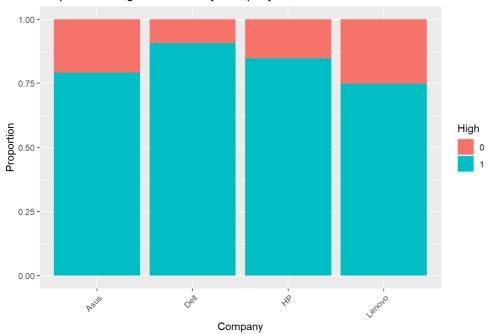


From the above plots, we can see that the classes are inbalanced, with more high price laptops (1) than low price laptops (0). The following plot shows the proportion of high price (1) and low price (0) laptops for each company in the training set. Each bar is stacked and filled by the 'high' variable: different colors for high (1) and low (0).

```
# Bar plot: Company vs High/Low Price in training set

ggplot(df_train, aes(x = Company, fill = factor(high))) +
    geom_bar(position = "fill") +
    labs(title = "Proportion of High/Low Price by Company in train set", y = "Proportion", fill = "High") +
    theme(axis.text.x = element_text(angle = 45, hjust = 1))
```

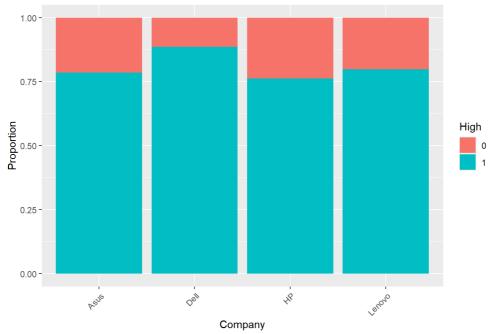
Proportion of High/Low Price by Company in train set



We are doing the same for the test set.

```
# Bar plot: Company vs High/Low in test set
ggplot(df_test, aes(x = Company, fill = factor(high))) +
geom_bar(position = "fill") +
labs(title = "Proportion of High/Low Price by Company in test set", y = "Proportion", fill = "High") +
theme(axis.text.x = element_text(angle = 45, hjust = 1))
```

Proportion of High/Low Price by Company in test set



Based on the above plots, we can see whether some manufacturers (Dell, HP, Lenovo, Asus) are more likely to sell high-priced laptops. It just gives us an intuition before we build our model.

[Optional] Make the dataset balanced

Here we will use caret package to upsample the minority class (low price laptops) in the training set to make the classes balanced. Since it is now asked, we will just present it here and continue with the original unbalanced dataset for modeling.

```
# Make copies of the original datasets
df_train_orig <- df_train</pre>
df_test_orig <- df_test</pre>
# Set seed for reproducibility
set.seed(123)
# Convert 'high' to factor for classification
 df\_train\_orig\$high <- factor(df\_train\_orig\$high, levels = c(0,1), labels = c("low","high")) 
\label{lem:df_test_orighigh} $$ df_{est_orig}$ igh, levels = c(0,1), labels = c("low","high")) $$
# Upsample the minority class (low price laptops)
df_train_orig_balanced <- upSample(x = subset(df_train_orig, select = -high),</pre>
                               y = df_train_orig$high,
                               yname = "high")
# Convert 'high' back to 0/1 for easier analysis
df_train_orig_balanced$high <- ifelse(df_train_orig_balanced$high == "high", 1, 0)</pre>
# Check the distribution of the new binary variable in balanced training set
table(df_train_orig_balanced$high)
```

```
##
## 0 1
## 550 550
```

```
prop.table(table(df_train_orig_balanced$high))
```

```
##
## 0 1
## 0.5 0.5
```

Problem 4

Question (a) Build Model

```
## Call:
## glm(formula = high ~ InventoryID + Company + TypeName + GPU +
       Screen + Memory + Weight + Rating, family = "binomial", data = df_train)
##
## Coefficients:
##
                       Estimate Std. Error z value Pr(>|z|)
                    2.647e+01 8.091e+02 0.033 0.973901
## (Intercept)
## InventoryID 5.577e-04 9.390e-04 0.594 0.552571 ## CompanyDell 1.184e+00 5.108e-01 2.318 0.020473 * ## CompanyHP 1.3090e00 5.531e-01 2.367 0.017012 *
## CompanyHP 1.309e+00 5.531e-01 2.367 0.017912 **
## CompanyLenovo -3.677e-01 6 0150 04 7
## TypeNameNotebook -1.464e+01 8.091e+02 -0.018 0.985562
## TypeNameUltrabook -1.326e+01 8.091e+02 -0.016 0.986925
                 -1.077e-01 3.544e-01 -0.304 0.761111
## GPUIntel
## GPUNvidia
                     2.031e+00 6.074e-01 3.344 0.000826 ***
## Screen
                     -1.198e+00 3.121e-01 -3.839 0.000124 ***
## Memory
                      7.337e-01 9.354e-02 7.843 4.39e-15 ***
                    1.560e+00 9.069e-01 1.720 0.085373 .
## Weight
                    -9.092e-02 4.924e-02 -1.846 0.064823 .
## Rating
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 612.47 on 664 degrees of freedom
## Residual deviance: 334.40 on 652 degrees of freedom
## AIC: 360.4
## Number of Fisher Scoring iterations: 18
```

Question (b) Which variables are significant in predicting the probability of a price's being high?

```
# Which variables are significant in predicting the probability of a
# price's being high? Variables with p-values less than 0.05 are considered
# statistically significant
significant_vars <- summary(logistic_model)$coefficients
significant_vars[significant_vars[,4] < 0.05, ]</pre>
```

```
## CompanyDell 1.1838020 0.51079418 2.317571 2.047263e-02
## CompanyHP 1.3094383 0.55310260 2.367442 1.791153e-02
## GPUNvidia 2.0311573 0.60738742 3.344089 8.255339e-04
## Screen -1.1981472 0.31212375 -3.838693 1.236912e-04
## Memory 0.7336737 0.09354129 7.843313 4.388113e-15
```

Interpretation of Results

The p-value is the probability of observing a sample with results as extreme as, or more extreme than, the observed data, assuming the null hypothesis is true. A lower p-value indicates stronger evidence against the null hypothesis. In this analysis, we use a threshold of 0.05, meaning variables with p-values below this level are considered statistically significant.

Significant predictors (p < 0.05):

- CompanyDell (p = 0.020) \rightarrow Dell laptops are more likely to be high-priced vs. Asus.
- CompanyHP (p = 0.018) \rightarrow HP laptops are also more likely to be high-priced.
- GPUNvidia (p < 0.001) → Nvidia GPUs strongly increase the likelihood of high-priced laptops.
- Screen (p < 0.001) → Larger screen size reduces the probability of being high-priced.
- Memory (p < 0.001) → More RAM strongly increases the likelihood of being high-priced.

Not significant predictors (p ≥ 0.05):

- Weight
- Rating
- InventoryID
- CompanyLenovo
- TypeName
- GPUIntel

Interpretation:

Practical factors influencing price:

- More RAM (+), Nvidia GPU (+), Dell/HP branding (+) increase odds of being expensive.
- Larger screens (-) reduce odds (perhaps because gaming/ultrabooks with smaller but more powerful components are pricey).

Baseline/reference categories:

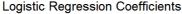
- Company baseline = Asus.
- Type baseline = Gaming.
- GPU baseline = AMD.

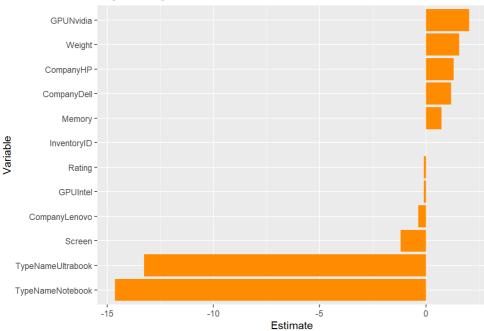
So, coefficients are relative to these baselines.

Visualize Coefficients (optional)

```
# Visualize model coefficients (excluding intercept)
# This horizontal bar plot shows the estimated coefficients from the logistic regression model (excluding the intercept).
# Each bar represents a variable, and the length and direction indicate the effect size and sign.
# Bars are colored dark orange for better visibility.
coefs_df <- as.data.frame(summary(logistic_model)$coefficients)
coefs_df$Variable <- rownames(coefs_df)
coefs_df <- coefs_df[coefs_df$Variable != "(Intercept)", ]

ggplot(coefs_df, aes(x = reorder(Variable, Estimate), y = Estimate)) +
    geom_bar(stat = "identity", fill = "darkorange") +
    coord_flip() +
    labs(title = "Logistic Regression Coefficients", x = "Variable", y = "Estimate")</pre>
```





Question (c) Comparison with the linear regression model

Logistic Regression Model

We give a short summary of the logistic regression model here: - Significant predictors (p < 0.05) included: **Company (Dell, HP), GPU (Nvidia), Screen size, and Memory**.

- Results suggest that Dell/HP branding, more RAM, and Nvidia GPUs increase the odds of a laptop being high-priced, while larger screen

sizes reduce those odds

- Baseline categories are: Asus (Company), Gaming (TypeName), AMD (GPU). Coefficients for other categories are interpreted relative to these baselines.

Linear Regression Model

The linear regression model directly predicts laptop price as a continuous outcome.

Key results:

- Screen size (-36.60, p = 0.021): Larger screens are associated with slightly lower prices.
- Memory (+90.21, p < 0.001): Each additional GB of RAM increases price on average by about €90.
- Rating (-12.82, p = 0.0067): Higher ratings are associated with slightly lower prices.
- CompanyDell (+124.91, p = 0.004) and CompanyHP (+175.31, p < 0.001): Dell and HP laptops are priced higher compared to Asus.
- TypeNameNotebook (-234.46, p < 0.001): Notebooks are significantly cheaper than Gaming laptops.
- TypeNameUltrabook (+203.68, p = 0.0019): Ultrabooks are significantly more expensive than Gaming laptops.
- GPUIntel (+163.64, p < 0.001) and GPUNvidia (+227.60, p < 0.001): Both Intel and Nvidia GPUs increase price compared to AMD GPUs.

Comparison and Insights

- Logistic regression provides a binary view (is the laptop high-priced or not), while linear regression quantifies how much each factor contributes to price in Euros.
- Both models consistently highlight Memory and GPU type as important price drivers.
- Company (Dell, HP) is significant in both models, reinforcing the strong effect of branding on price.
- · Linear regression suggests Ultrabook type is also strong price determinant, which is insignificant in the logistic model.
- The negative effect of Screen size appears in both models, reinforcing that larger screens may not always mean higher-priced laptops (likely due to mid-range notebooks with larger but less powerful builds).

Question (d) Interpretation of Significant Variables

Variable	Effect on Probability of Being High-Priced	Possible Explanation
CompanyDell	Increases \rightarrow Dell laptops are more likely to be high-priced compared to Asus.	Dell often offers premium business and gaming models at higher prices.
CompanyHP	Increases \rightarrow HP laptops are more likely to be high-priced compared to Asus.	HP has strong enterprise and premium product lines.
GPUNvidia	Increases \rightarrow Laptops with Nvidia GPUs are more likely to be high-priced compared to AMD.	Nvidia GPUs are powerful and common in high-end gaming/professional laptops.
Screen	Decreases \rightarrow Larger screen size reduces the likelihood of being high-priced.	Counterintuitive, but many premium laptops (e.g., gaming/ultrabooks) favor performance/portability over large displays.
Memory	Increases → More RAM increases the likelihood of being high-priced.	Higher RAM is directly linked to better performance.

Question (e) Comparison of coefficient signs between models

When comparing the logistic regression (high-priced vs. low-priced) with the linear regression (continuous price), most predictors show consistent directions of effect, while a few differ.

Same sign in both models:

- Memory: Positive in both → more RAM increases the likelihood of being high-priced and also raises the price level in Euros.
- GPUNvidia: Positive in both → Nvidia GPUs are associated with higher odds of being expensive and increase absolute price.
- CompanyDell / CompanyHP: Positive in both → Dell and HP branding raises both the odds of being high-priced and the absolute price compared to Asus.
- Screen: Negative in both → larger screens reduce odds of being high-priced and are associated with lower prices.

Different signs between models:

- GPUIntel: Negative in logistic regression (though not significant) but positive in linear regression → Intel GPUs are linked with slightly lower
 odds of being in the high-price group, yet contribute positively to price as a continuous outcome.
- TypeNameUltrabook: Negative in logistic regression (not significant) but strongly positive in linear regression → Ultrabooks are not clearly more likely to cross the 500 price threshold, but when they do, their absolute prices are much higher.
- TypeNameNotebook: Negative in both, but only significant in neither, so practical impact is limited.

Key takeaway

- The consistent predictors across both models are Memory, Nvidia GPUs, Weight, and Screen size, all showing the same directional
 effect.
- The main divergences are for Intel GPUs and Ultrabook type, where logistic and linear models disagree. This suggests that these
 features influence absolute pricing levels but may not cleanly separate laptops into high- vs. low-price categories.

Question (f) Predicting for a Specific Laptop

We want to predict the probability that a given laptop is **high-priced** (≥ 500 Euros).

The logistic regression model gives this probability using the logistic function:

$$P(ext{high}=1) = rac{1}{1+e^{-(eta_0+eta_1X_1+eta_2X_2+\cdots+eta_kX_k)}}$$

Given Laptop Characteristics

- InventoryID = 4096
- · Company = Lenovo
- TypeName = Ultrabook
- GPU = Intel
- Screen = 8
- Memory = 8
- Weight = 4.2
- Rating = 7

Step 1: Extract Coefficients

From the logistic regression model:

- (Intercept) = 26.47131
- InventoryID = 0.0005577
- CompanyLenovo = -0.3677
- TypeNameUltrabook = -13.25963
- GPUIntel = -0.1077
- Screen = -1.1981
- Memory = 0.7337
- Weight = 1.5602
- Rating = -0.0909

(Other coefficients are not included since they do not apply to this laptop's profile.)

Step 2: Compute the Logit (Z)

$$Z = \beta_0 + \beta_1 (ext{InventoryID}) + \beta_{Lenovo} + \beta_{Ultrabook} + \beta_{Intel} + \beta_{Screen} (ext{Screen}) + \beta_{Memory} (ext{Memory}) + \beta_{Weight} (ext{Weight}) + \beta_{Rating} (ext{Rating})$$
Substituting the values:

$$Z = 26.47131 + (0.0005577 \times 4096) - 0.3677 - 13.25963 - 0.1077 + (-1.1981 \times 8) + (0.7337 \times 8) + (1.5602 \times 4.2) + (-0.0909 \times 2 \times 22.9)$$

Step 3: Apply Logistic Function

$$P({
m high}=1)=rac{1}{1+e^{-Z}}=rac{1}{1+e^{-22.9}}pprox 1$$

Final Prediction

- Manual calculation: Probability ≈ 1.0000
- Using predict() in R: Probability ≈ 1.0000

Explanation of Implementation

- 1. Created a new observation (new_laptop) with the given laptop's features.
- 2. Extracted coefficients from the fitted logistic regression model.
- 3. Calculated the logit (Z) by plugging in the observation's values.
- 4. Applied the logistic function to transform Z into a probability.
- 5. Validated with R's predict() function, which confirmed the manual result.

The model predicts with near certainty that this Lenovo Ultrabook would be high-priced.

```
# Create a new observation
new_laptop <- data.frame(
   InventoryID = 4096,
   Company = "Lenovo",
   TypeName = "Ultrabook",
   GPU = "Intel",
   Screen = 8,
   Memory = 8,
   Weight = 4.2,
   Rating = 7
)

# Show the equation for probability:
# pr(high = 1) = 1 / (1 + exp(-(B0 + B1*InventoryID + ... + B7*Rating)))
   coefs <- coef(logistic_model)
   coefs</pre>
```

```
##
                                                                 CompanyHP
         (Intercept)
                          InventorvID
                                             CompanyDell
##
        2.647131e+01
                         5.576561e-04
                                           1.183802e+00
                                                              1.309438e+00
##
       CompanyLenovo TypeNameNotebook TypeNameUltrabook
                                                                  GPUIntel
##
       -3.677291e-01
                        -1.464189e+01
                                         -1.325963e+01
                                                             -1.077326e-01
##
           GPUNvidia
                                Screen
                                                  Memory
                                                                    Weight
        2.031157e+00
##
                         -1.198147e+00
                                           7.336737e-01
                                                              1.560218e+00
##
             Rating
##
       -9.092252e-02
```

```
# Calculate Logit (Z) manually
Z <- coefs["(Intercept)"] +
    coefs["InventoryID"] * new_laptop$InventoryID +
    coefs[paste0("Company", new_laptop$Company)] +
    coefs[paste0("TypeName", new_laptop$TypeName)] +
    coefs[paste0("GPU", new_laptop$GPU)] +
    coefs["Screen"] * new_laptop$Screen +
    coefs["Memory"] * new_laptop$Memory +
    coefs["Weight"] * new_laptop$Weight +
    coefs["Rating"] * new_laptop$Rating</pre>
# Calculate probability
prob <- 1 / (1 + exp(-Z))
print(paste("Predicted probability (manual):", round(prob, 4)))
```

```
## [1] "Predicted probability (manual): 1"

# Or use predict()
prob_predict <- predict(logistic_model, newdata = new_laptop, type = "response")
print(paste("Predicted probability (predict):", round(prob_predict, 4)))

## [1] "Predicted probability (predict): 1"</pre>
```

Question (g) Model Evaluation on Test Set

```
# Generate predictions on test set
test_predictions <- predict(logistic_model, newdata = df_test, type = "response")

# Convert probabilities to binary predictions using 0.5 cutoff
predicted_classes <- ifelse(test_predictions >= 0.5, 1, 0)

# Calculate accuracy
accuracy <- mean(predicted_classes == df_test$high)

# Create confusion matrix
conf_matrix <- table(Predicted = predicted_classes, Actual = df_test$high)

# Display results
print("Confusion Matrix:")</pre>
```

```
## [1] "Confusion Matrix:"
```

```
print(conf_matrix)
```

```
## Actual
## Predicted 0 1
## 0 29 16
## 1 24 211
```

```
print(paste("Accuracy:", round(accuracy * 100, 2), "%"))
```

```
## [1] "Accuracy: 85.71 %"
```

We applied the logistic regression model to the test dataset and evaluated performance using a 0.5 probability cutoff.

- True Negatives (TN): 29
 False Negatives (FN): 16
 False Positives (FP): 24
 True Positives (TP): 211
-

$$\begin{aligned} \text{Accuracy} &= \frac{TP + TN}{TP + TN + FP + FN} \\ \text{Accuracy} &= \frac{211 + 29}{211 + 29 + 24 + 16} = \frac{240}{280} \approx 85.71\% \end{aligned}$$

Interpretation

- The model achieves an accuracy of 85.71% on the test dataset.
- Most high-priced laptops (class = 1) were correctly identified (211 true positives), showing the model is strong at predicting expensive laptons
- Some errors occur in predicting low-priced laptops, as seen in the 24 false positives and 16 false negatives.

Visualization

The following heatmap provides a visual representation of the confusion matrix for the test set predictions.

```
# Visualize confusion matrix as heatmap
# This heatmap shows the confusion matrix for the test set predictions.
# The fill color (from sky blue to navy) indicates the number of laptops in each cell (Predicted vs Actual).
# The white text shows the count in each cell.
cm_df <- as.data.frame(conf_matrix)</pre>
colnames(cm_df) <- c("Predicted", "Actual", "Freq")</pre>
cm_df$Predicted <- factor(cm_df$Predicted, levels = c(1, 0))</pre>
cm_dfActual <- factor(cm_dfActual, levels = c(0, 1))
ggplot(cm_df, aes(x = Actual, y = Predicted, fill = Freq)) +
 geom_tile() +
  geom_text(aes(label = Freq), color = "white", size = 8) +
  scale_fill_gradient(low = "skyblue", high = "navy") +
   title = "Confusion Matrix (Test Set)",
   x = "Actual",
   y = "Predicted"
  ) +
  scale_x_discrete(position = "top") # Put Actual labels on top to match table
```

Confusion Matrix (Test Set)

