

$$\begin{aligned}
 & 3/2^n, \quad \underline{\log \log n}, \quad \sqrt{2}^{\log n}, \quad \log n^{\log n}, \quad \sqrt{\log n}^{\log n} \\
 & \log (3/2)^n, \quad \log (\log \log n), \quad \log (2^{\frac{1}{2} \log n}), \quad \log (\log n^{\log n}), \quad \log (\log n)^{1/2} \\
 & n=2^{1024} \quad n \log (3/2), \quad \underline{\log (\log \log n)}, \quad \frac{1}{2} \log n, \quad \log n \cdot \log \log n, \quad \frac{1}{2} \underline{\log \log n} \\
 & \sqrt{2}^{1024}, \quad 3.2, \quad \underline{512}, \quad \underline{10240}, \quad \underline{5} \\
 & 2^{4096}, \quad 3.7, \quad 2048, \quad 4096 \times 12, \quad 6 \quad n=2
 \end{aligned}$$

$$\begin{aligned}
 1 \approx n^{\frac{1}{\log n}} &< \log \log n < \text{sqrt}(\log n) < \text{sqrt}(2)^{\log n} < \log n^{\log n} < 3/2^n < 2^{10} \\
 & & & & & & & 2^{11} \\
 & & & & & & & (2^{12}) \\
 1 = O(n+1)! & \checkmark \quad \log n^{\log n} = \Omega(\log \log n) \rightarrow \text{True} < (n+1)!
 \end{aligned}$$