

## Distributed Algorithms and Application of Game Theory in Cognitive Radio Networks



# Abstract

Cognitive radio (CR) technology is promising to provide high bandwidth via dynamic spectrum access techniques in various networks. Unlicensed users are allowed to utilize licensed spectrum when such usage doesn't cause harmful interferences to licensed users. This unique spectrum usage paradigm creates new problems and thus needs additional considerations. One instance is the spectrum allocation problem needs reformulation as the interference on the licensed users needs consideration. Another instance is that when clustering is needed to facilitate local cooperation, as the amount of available spectrum on unlicensed users is different, it is necessary to form nearby unlicensed users which have similar spectrum together. Routing method also needs reflecting as heterogeneous of spectrum affects whether a routing is successful or the performance of routing path.

Distributed solution is more suitable for wireless networks, because it doesn't require global information across the network, and individual unlicensed user is either agile to react to network dynamics, or only needs local information. This thesis solves a series of problem with distributed solutions. Game theory is used to analyse certain problems and help to derive solutions.

In this dissertation, we solve a series of problems residing from layer 1 to layer 3 in the OSI model [2] of CRN with distributed solutions.

- We solve the power and spectrum allocation problem in IEEE 802.22 networks. This work mainly lies in layer 1, after deciding the maximal transmission power on each secondary cellular base station, we formulate the distributed spectrum allocation problem in TV white space scenario (a special CRN where primary user is TV station which operates according to a slow and pre-decided schedule) into a canonical congestion game, then propose distributed algorithm corresponding to the behaviour of player in the game.
- When the availability of spectrum is considered to have the same probability due to licensed users' activity, and local operation is needed, i.e., for cooperative sensing, unlicensed users need to form clusters and the clusters should be robust against the primary users' activity. A distributed clustering scheme for CRN is proposed. The process of finalizing cluster membership is innovatively formulated into a congestion game, then as long as cluster head is decided, clusters which have clear membership are formed quickly by applying the light-weighted distributed scheme derived from the game. This problem can be regarded to lie in layer 2.
- In layer 3, we propose a lighted weighted routing scheme for CRN. Spectrum aware virtual coordinate is proposed, thus light weighted geographic routing can be used to decide the next hop.

Finally, using thorough simulations and numerical results, we investigate various aspects of the proposed algorithms and analyse their performance.

# Contents

<b>Abstract</b>	<b>iii</b>
<b>1 Introduction</b>	<b>1</b>
1.1 Cognitive Radio . . . . .	1
1.1.1 Spectrum Access Etiquette in Cognitive Radio Network . . . . .	2
1.1.2 Spectrum Decision . . . . .	3
1.2 Cognitive Radio Network . . . . .	3
1.2.1 Cognitive Radio Ad hoc Network . . . . .	3
1.2.2 IEEE 802.22 standards . . . . .	4
1.3 Channel Allocation in TV White Space . . . . .	4
1.3.1 Wireless Channel Allocation . . . . .	4
1.3.2 Utilize TV White Space . . . . .	5
1.4 Clustering in Cognitive Radio Network . . . . .	6
1.5 Geographic Routing in CRN . . . . .	7
<b>2 Background</b>	<b>9</b>
2.1 Centralized and Distributed Algorithms in CRN . . . . .	9
2.2 Algorithmic Game Theory . . . . .	10
2.2.1 Basics of Game Theory . . . . .	11
2.2.1.1 Strategic Game . . . . .	11
2.2.1.2 Nash Equilibrium . . . . .	11
2.2.1.3 Potential Game . . . . .	11
2.2.2 Congestion Game . . . . .	12

<b>3</b>	<b>Distributed Channel Allocation in CRN</b>	<b>13</b>
3.1	INTRODUCTION . . . . .	13
3.2	System Model . . . . .	15
3.2.1	QuasiSINR: the considered SINR on terminals . . . . .	16
3.2.2	The problem to solve in this paper . . . . .	18
3.3	Related Work . . . . .	18
3.3.1	Problem Formulation: three sequential subproblmes . . . . .	19
3.3.2	Maximal transmission power planning . . . . .	20
3.3.3	Channel allocation with fixed transmission power level . . . . .	20
3.3.4	Power allocation . . . . .	21
3.4	Decide the maximal permitted transmission power . . . . .	21
3.5	Channel Allocation with Fixed Transmission Power . . . . .	22
3.5.1	Centralized optimization programming . . . . .	22
3.5.2	Distributed White space channel allocation technology (Withe-Cat): algorithm and protocol . . . . .	23
3.5.3	Analysis in game theoretical framework . . . . .	25
3.5.3.1	Bridging the game and practical scheme . . . . .	25
3.5.3.2	Difference between equilibrium and the aimed variable	27
3.5.4	Variable transmission power after channel allocation . . . . .	27
3.5.5	Communication overhead of Dicaps in the phase of channel allocation . . . . .	28
3.6	Joint channel and power allocation . . . . .	28
3.6.1	Centralized optimization . . . . .	28
3.7	Performance Evaluation . . . . .	29
3.7.1	Performance of maximal permitted power decision and the channel allocation schemes . . . . .	31
3.7.1.1	comparison among 1. power map decisions . . . . .	31
3.7.1.2	comparison among 2.channel allocation schemes . . . . .	32
3.7.2	The performance power allocation on the basis of channel allocation	33
3.7.3	Analysis on convergence process . . . . .	34
3.7.4	Stability of SINR in the process of channel allocation . . . . .	37
3.7.5	comparison between distributed and centralized scheme . . . . .	37
3.8	Conclusion . . . . .	38

<b>A</b>	<b>Proof of Theorem 3.5.1</b>	<b>41</b>
<b>B</b>	<b>Deviation of Problem 3.7</b>	<b>43</b>
<b>4</b>	<b>Robust Clustering of Ad-hoc Cognitive Radio Networks</b>	<b>45</b>
4.1	Introduction . . . . .	45
4.2	Related Work . . . . .	47
4.3	System Model . . . . .	47
4.4	Distributed Coordination Framework: Clustering Algorithm . . . . .	49
4.4.1	Phase I - Cluster Formation . . . . .	49
4.4.1.1	Determining Cluster Heads . . . . .	50
4.4.1.2	Initial Cluster Formation . . . . .	50
4.4.1.3	Cluster Size Control in Dense CRN . . . . .	52
4.4.2	Phase II - Membership Clarification . . . . .	55
4.4.2.1	Problem Description . . . . .	55
4.4.2.2	Distributed Greedy Algorithm (DGA) . . . . .	55
4.4.2.3	Convergence of DGA . . . . .	57
4.4.2.4	Distributed Fast Algorithm (DFA) . . . . .	58
4.5	Centralized Clustering Scheme . . . . .	59
4.5.1	The Optimization Problem . . . . .	62
4.6	Performance Evaluation . . . . .	63
4.6.1	Centralized Schemes vs. Decentralized Schemes . . . . .	64
4.6.1.1	Number of Common Channels . . . . .	64
4.6.1.2	Survival Rate of Clusters with Increasing PR Users . . . . .	65
4.6.1.3	Cluster Size Control . . . . .	66
4.6.1.4	Control Signalling Overhead . . . . .	67
4.6.2	Comparison between Distributed Schemes . . . . .	69
4.6.2.1	Number of CCC per Non-singleton Clusters . . . . .	69
4.6.2.2	Survival Rate of Clusters with Increasing PR Users . . . . .	69
4.6.2.3	Cluster Size Control . . . . .	70
4.7	Conclusions and Future Work . . . . .	71

<b>5</b>	<b>Spectrum Aware Virtual Coordinates Assignment and Routing in Multihop Cognitive Radio Network</b>	<b>73</b>
5.1	Introduction . . . . .	73
5.2	RELATED WORK . . . . .	74
5.3	SYSTEM MODEL . . . . .	75
5.4	Spectrum Aware Virtual Coordinates . . . . .	76
5.4.1	Assign Spectrum Aware Virtual Coordinate . . . . .	76
5.4.2	Normalized Spectrum Availability on Secondary User . . . . .	78
5.4.2.1	Single licensed channel . . . . .	78
5.4.2.2	Multiple licensed channels . . . . .	79
5.4.3	Normalized Longest Blocking Time on Secondary Users . . . . .	80
5.4.3.1	Single licensed channel . . . . .	80
5.4.3.2	Multiple licensed channels . . . . .	81
5.5	Geographic Routing and Opportunistic Spectrum Access . . . . .	81
5.6	Performance Evaluation . . . . .	82
5.6.1	Simulation Setup . . . . .	82
5.6.1.1	Primary Users . . . . .	82
5.6.1.2	Parameter Setting . . . . .	83
5.6.2	Success Rate of Geographic Routing on Finding Path . . . . .	83
5.6.3	Routing Performance . . . . .	84
5.6.3.1	Spectrum Availability Based Virtual Coordinate . . . . .	84
5.6.3.2	Longest Blocking time Based Virtual Coordinate . . . . .	86
5.7	CONCLUSION . . . . .	88
<b>6</b>	<b>Conclusion</b>	<b>91</b>
	<b>Bibliography</b>	<b>93</b>
	<b>List of Figures</b>	<b>102</b>
	<b>List of Tables</b>	<b>105</b>



# 1

## Introduction

Wireless networks utilize radio waves instead of wires to carry information, hence seamless coverage and mobility are achievable in wireless connections. Wireless networks have experienced unprecedented growth in the past few decades and will evolve in the future. Due to the propagation characteristics of radio waves, only a small part of radio spectrum which spans from 3 kHz to 300 GHz is suitable for commercial application. In most countries, the radio spectrum is divided into different bands (also referred as channels), some of which are licensed to different types of usages and users by governments through auction, and the governments get revenue from it [27]. There are many existing wireless applications assigned with licensed spectrum. For instance, the second-generation (2G) wireless cellular network GSM (global system for mobile communications) in Europe works with GSM-900 band (from 890 MHz to 960 MHz) and GSM-1800 (1710 MHz to 1880 MHz), and the third-generation (3G) wireless cellular network works from 1.8 GHz to 2.4 GHz [81]. The assignment of frequency band rules out the unlicensed users to use the spectrum, so as to avoid interferences caused on the licensed users, and protect licensed users' commercial benefits.

The proliferation of wireless network causes significant shortage of spectrum under current spectrum allocation paradigm. Open spectrum access [72] is proposed in 1995 to cope with the scarcity of spectrum at certain places during certain time, which advocates a new spectrum usage paradigm where spectrum use does not require any license. On the other hand, there exists a large number of spectrum bands which have considerable dormant time intervals, and the spectrum is not fully utilized [16].

XXXXXX Figure of spectrum usage XXXXXX

### 1.1 Cognitive Radio

The dilemma that spectrum scarcity coexists with spectrum underutilization promotes cognitive radio (CR) as a promising technology to make full use of spectrum and accordingly solve the spectrum shortage problem. Cognitive radio is a device which is able to

sense, detect, and monitor the surrounding radio frequency environment, then based on the assessment along with the location information and certain particular operating rule, the cognitive radio tunes its radio operating parameters (e.g. center frequency, bandwidth and transmit power) on the fly so that to avoid interfering licensed users. The definition of cognitive radio evolves with the development of radio technology and regulations. We choose two representative definitions to give a formal description of cognitive radio. Cognitive radio is firstly proposed by Mitola III who defines the concept of CR in his dissertation [66] as follows:

The point in which wireless personal digital assistants (PDAs) and the related networks are sufficiently computationally intelligent about radio resources and related computer-to-computer communications to detect user communications needs as a function of use context, and to provide radio resources and wireless services most appropriate to those needs.

FCC (Federal Communications Commission in U.S.) describes CR [3] as,

a radio that can change its transmitter parameters based on interaction with the environment in which it operates. . . . This interaction may involve active negotiations with other spectrum users and/or passive sensing and decision making (smart radio) within the radio. The majority of CRs will probably be SDRs <sup>1</sup>, but a CR does not necessarily use software, nor does it need to be field programmable.

The wireless network which is composed with cognitive radio users is cognitive radio network, the acronym is CRN.

### 1.1.1 Spectrum Access Etiquette in Cognitive Radio Network

Licensed users access their allocated spectrum band whenever there is information to be transmitted, in contrary, CR users are only allowed to access licensed spectrum after validating the channel is idle or the primary user is not to be affected if they operate on the licensed spectrum. In this thesis, licensed users are referred as primary users, and CR users are denoted as secondary users.

The assessment of spectrum is a bone of contention for primary/secondary users and administration bodies. Spectrum sensing on secondary users is one common method to validate spectrum availability especially in research domain [104]. Secondary users should monitor the spectrum of interest actively and autonomously to detect primary users' appearance. Primary users can be detected by judging the primary users' signal power, spectral correlation or beacons. Spectrum sensing requires sophisticated technologies when primary users' signal is weak. Primary detection can be improved by learning technologies or cooperation among multiple secondary users [17]. Another way to protect the primary users from being affected by secondary users' operation relies on location identification and certain operating rule set. Based on the global information of primary

<sup>1</sup>software defined radio is a radio communication system which is able to receive any modulation across a large frequency spectrum, and transmit on desired spectrum band.

users' location and terrain information, centralized controller regulates that the secondary users at certain locations are restricted to operate on a few certain spectrum bands and with limited transmit power [76]. Spectrum administration bodies FCC of U.S. [7] and Electronic Communications Committee (ECC) in Europe [8] adopt the combination of spectrum sensing and location based method. Secondary users' operation is restricted on certain spectrum bands and transmit power should be below certain threshold according to their locations, and spectrum sensing ability is also required.

### 1.1.2 Spectrum Decision

After assessing RF environment or geographic location, secondary users adjust their operational parameters such as frequency, modulation schemes and transmit power, in order to support QoS aware communications, this process is referred as spectrum decision and spectrum sharing [15]. In this thesis, spectrum decision and sharing consist the major issue discussed in this thesis.

Some work in research community models the spectrum availability with stochastic or statistic model, which is helpful when deciding which channel to use. [63] proposes discrete Markov chain and adjusted duty circle models to describe the availability of licensed spectrum for GSM on 900/1800 MHz. [96] models the channel holding time with geometric and log-normal distributions. Statistics of previous sensing results is used to predict spectrum state in the future in [52]. Such models provide more complete information on the availability of the licensed channels.

The available licensed spectrum which spans a wide frequency band exhibits different characteristics [56]. Based on the requirements of interested communication, CR users need to identify the characteristics of the spectrum, which include channel quality (channel capacity, error rate, path loss, etc.) [56], channel switching delay [19], and channel holding time, i.e., the expected time duration that the primary users don't occupy the channel before any one occupies again.

## 1.2 Cognitive Radio Network

In this section, we introduce two types of cognitive radio networks, and the problems we tackle in this thesis reside in these networks.

### 1.2.1 Cognitive Radio Ad hoc Network

An ad hoc network is a decentralized paradigm of wireless network, which consists of a collection of autonomous mobile users which communicate over wireless links. Efficient distributed algorithms are needed to determine network organization, link scheduling, and routing.

Cognitive radio ad hoc network is an ad hoc network composed with cognitive radio users. Similar with ad hoc network, cognitive ad hoc radio network can also be represented as an undirected graph  $G$ . Cognitive radio users constitute the vertices, the edge between two vertices is decided not only by the distance, propagation and attenuation properties

between the two vertices, but also the spectrum availability on both vertices, i.e., , when they can decode the received signal from each other correctly, and there is common channel available between them on which communication is conducted, then an unidirectional edge is available on graph  $G$ . As to ad hoc network, the graph is constant when users are static. As to cognitive radio ad hoc network, due to primary users' activity, an edge between two vertices is decided by the fact that whether the two vertices can simultaneously access the same licensed channel. Hence, the corresponding graph is dynamic under primary users' operation, which imposes extra difficulties on network organization, routing and many other network functionalities.

## 1.2.2 IEEE 802.22 standards

Centralized spectrum decision is adopted in IEEE 802.22 [1] standard for Wireless Regional Area Networks (WRAN). IEEE 802.22 defines a cellular network paradigm for secondary equipments working on unused TV channels. Centralized database notifies the secondary users the available spectrum at their places, and is possible to decide transmission parameters for them, i.e., spectrum to be used, or transmission power. Note this database takes the functionality of spectrum sensing in addition to spectrum decision and sharing. The feasibility of this centralised paradigm is largely due to the characteristic of TV channel, as TV channel usage follows a slow and scheduled pattern.

Centralized spectrum decision doesn't work well outside the TV channel scenario. In certain scenarios, primary users are active and the channel holding time is short, thus the channel availability changes frequently. Furthermore, it is hard for CR users to obtain a full and up to date picture of the spectrum availability in the whole network. As a result, spectrum decision and sharing need reconsideration quite often, which causes a large number of control messages for network organization. As contrary, distributed schemes adapts to the varying environment quite well [106]. Distributed schemes exploit local observation, and require much less control overhead compared with centralized optimization.

The forthcoming vehicular to vehicular communication requires

## 1.3 Channel Allocation in TV White Space

### 1.3.1 Wireless Channel Allocation

xxxx what is channel allocation? xxxx

Channel allocation facilitates CRN to improve throughput [92], or cooperatively relay [107] and so on. This thesis emphasises on co-channel interference mitigation with distributed channel allocation .

Mitigating co-channel interference via channel allocation has been attracting plenty of research efforts in the past ten years, from multiple channel mesh network [80], Ad hoc network [20, 53] up to cognitive radio network [103, 47]. Channel allocation problem is converted into colouring problem thus is NP hard [80], thus centralized optimization fails to produce Authors of [20, 53] propose heuristic algorithms utilizing best response

based on the welfare on itself to assign channels among users. Simulated annealing is applied to mitigate co-channel interferences in [103]. For the same purpose, No-regret learning [47, 42] is exploit to optimize the choice on channel.

In this thesis we cope with a special channel allocation problem where symmetric interaction doesn't exist, i.e., transmission power is identical among CR users, or the propagation path loss is not symmetric. The asymmetry disables the heuristic distributed schemes provided in [20, 53], and makes channel allocation problem not to fit into the congestion game model proposed in [59] which is the first paper to discuss channel allocation from the respective of game theory. We innovatively formulate this problem in to a canonical congestion game by utilizing the centralized database in TV white space scenario, and derive efficient distributed channel selection strategy.

### 1.3.2 Utilize TV White Space

Unused TV spectrum is termed as TV White space by the Federal Communications Commission (FCC) [7], which is licensed to incumbent users such like digital TV, analog TV, and wireless microphone. As to unlicensed users, detecting incumbent users is challenging because the FCC requires the unlicensed users should be able to detect the presence of signals from TV stations or wireless microphone at a received power level of -114 dBm [89]. Thus FCC doesn't require the sensing ability on unlicensed users, but regulates the secondary usage of TV white space in a prudent manner, including the spectrum bands permitted to use based on their location, the transmission power, the distance away from TV service area and so on. Every unlicensed user should register its type and geographic location to one TV database which decides which channels can be used at its places, then unlicensed user accesses the TV database to retrieve the information about available spectrum. Some prototype applications which only rely on the TV database are proposed in cellular network [79, 35] and WiFi-like network [76] based on the FCC regulation.

Standardization activities are also ongoing on TVWS utilization, including 802.22 [1] for Wireless Regional Area Networks (WRAN), IEEE 802.11af [36] for WLAN, IEEE 802.15.4m [4] for 802.15.4 wireless networks in TVWS and 802.19.1 [5] for coexistence methods among local and Metropolitan Area Networks (MAN). IEEE 802.22 largely complies FCC regulations on the utilization of TVWS. System consists of base stations and customer premises equipments (or terminals for short), where each terminal is served by one base station. Recent standard published in Nov. 2010 suggests both sensing ability as well as database look-up to avoid affecting primary systems. As to utilization of available TVWS, IEEE 802.22 proposes centralized channel allocation in database. When two or more base stations co-exist on the same channel, TDMA like mechanism for WBSes is adopted.

Scientific research on utilization of TVWS goes on in parallel with the regulatory agency. Spectrum sharing in TVWS is formulated as optimization problem, where the guarantee that TV receivers should not be affected by the cumulative interferences form TVBD is one constraint, and the signal interference (noise) ratio becomes the other. The objective can be maximizing TVBD's downlink transmission power [54], uplink transmission power [93], or best geographic distribution of TVBDs [105].

[30, 103, 24, 85, 38] emphasise on interference mitigation among TVBDs via spectrum allocation. Vehicular networks operating with TVWS assisted by TV database and cooperative sensing is discussed in [32]. Work [33] steps further from the database paradigm and makes efforts to utilize the 'grey space', where TVDB is allowed to operate even within the TV service area.

This thesis addresses following two problems,

- Decide the maximal downlink transmission power. Both FCC regulation and 802.22 standard try to make TVBD transparent to incumbent users, but as long as TV system is not affected, i.e. certain quality of service is fulfilled, the strict restriction on unlicensed users can be relaxed so that more TVWS can be provided [54]. Abiding by the operation paradigm using data base, we investigate the maximal downlink transmission power for TVBDs by solving optimization problem where the cumulative interference on TV receivers is under a threshold.
- Distributed spectrum allocation scheme for TVBDs. According to 802.22 regulation, spectrum allocation is done centrally in TV database, this is not realistic when TVBDs belong to different economic interest groups, thus a distributed solution is needed. We propose efficient distributed scheme to allocate the TV channels in order to improve the quality of service of TVBDs. The major difference between our scheme and other spectrum allocation lies in that the downlink transmission power on different channel is different. We formulate this problem into a canonical congestion game, and derive the distributed algorithm from the best response behaviour of the player in the game.

## 1.4 Clustering in Cognitive Radio Network

Clustering is an important paving stone for the practical utilization of the unused portions of the licensed spectrum. Clustering secondary users based on geographical proximity and other relevant properties together produces following benefits. Firstly, it is more efficient to solve common control channel (CCC) problem with cluster structure. Dedicated CCC which is allocated to all nodes for the purpose of control information exchange is regarded to be under utilization. Whereas, cluster based approaches group CR nodes into clusters based on their similarity of available unlicensed channels, so that the common channels within each cluster are used to carry the control messages [55]. Secondly, cluster structure facilitates cooperative sensing and increases the sensing reliability [91]. Thirdly, cluster structure supports coordinated channel switching and simplifies routing in ad-hoc cognitive radio networks [86].

A lot of research effort has been made on distributed clustering in CRN, these work target different aspects. In [108, 21], the channel available to the largest set of one-hop neighbors is selected as common channel which yields a partition of the CRN into clusters. Schemes [60, 18] pursue high numbers of common channels within clusters, so that cluster common control channel is less likely to disappear or encounter traffic congestion. Work [101] improves spectrum sensing ability by grouping the CR users with potentially best detection performance into the same cluster. Clustering scheme [48] obtains the best cluster size which minimizes power consumption caused by communication within and among clusters.

There are three aspects need consideration when design a new clustering scheme.

- Abundance of control channels within cluster should be achieved. A large number of control channels within cluster means high robustness. When the current control channel gets occupied by primary user, cluster members can migrate to a new one and the cluster is maintained. Besides, more control channels makes multiple concurrent transmission within cluster possible. In this thesis, a distributed clustering algorithm which is especially designed to support robustness under active primary users is proposed. Related works [108, 21, 101, 48] fail to pay attention to this aspect.
- New scheme should be light weighted so that re-clustering can be quickly conducted when previous cluster is destroyed by primary user's activity. When all the common channels are occupied by primary users, cluster head selection and following procedure is conducted by the cluster members autonomously. [60] targets large number of control channels within cluster, but it intriguers high complexity.
- Efficient channel allocation scheme within and among clusters is needed, so that communication rendezvous between two clusters is quick. Communication rendezvous means the process to establish control channel between two clusters before they can communicate . [60] proposes channel allocation in round robin manner, but it causes long time on communication rendezvous.

These requirements will be fulfilled by the scheme proposed in this thesis.

## 1.5 Geographic Routing in CRN

We propose a routing paradigm in CRN. Geographic routing is applied in the CRN network which is assigned with spectrum aware virtual coordinates. The dynamic availability of spectrum leads to prevalent topology changes, which makes spectrum aware routing difficult but essential. Routing schemes are proposed in [10, 25, 84] for CRN where primary users change their operating parameters infrequently. Highly dynamic primary users impose great challenge on routing, as is discussed in [75], where the statistics of primary users' activity is utilized in routing decision. A class of packet forwarding strategies for dynamic spectrum CRN is proposed in [62, 61]. Whenever a secondary user needs to forward a packet, it chooses channel and hop jointly based on channel's statistical characteristics observed beforehand. Forwarding decision is made for each single packet, which requires complex computations, large amount of control overhead, and customized media access control mechanisms. The solution provided by Chowdhury et al.[31] improves geographic routing in multiple channel CRN by introducing circumventing mechanism, i.e., when the next hop chosen based on geographic routing metric (e. g., Euclidean distance) is affected by primary user, the routing packet chooses a neighbour of that node free from primary user's affection so as to avoid the primary user affected area. Such routing is conducted on all channels, afterwards a path merge process is undertaken and one path with alternating channel is finally formed with consideration of end to end delay.

As the decision of the next hop is largely decided by the channel availability on the time point of decision, the node chosen as next hop may not be able to work after a short while

due to primary user's reappearance. Thus, this scheme works well when the primary user's activity is infrequent, but when it goes tense, the frequent invalidity of nodes due to lack of available spectrum seriously deteriorates routing performance.

In this paper we propose SAViC, spectrum aware virtual coordinates for secondary users in multi-channel multi-hop CRN where secondary users are source limited. Virtual coordinate is independent of real geographic position, but decided by certain properties of the media among nodes, for instance, link quality or hop numbers [26]. The proposed virtual coordinate depicts the availability of licensed spectrum influenced by primary users, on top of which geographic routing decides the next hop with Euclidean distance metric, and unconsciously detours the primary affecting area, or cuts through the area with better access opportunity. This routing paradigm imposes little computation and communication cost on secondary users after assigning virtual coordinate, besides, it doesn't need real geographic location which is employed in [31, 61].

This scheme is composed with two steps,

- Design virtual coordinates so that virtual coordinates of any two secondary users reflect both geographic distance and opportunistic spectrum availability between them. We design them based on statistics of primary user's ON/OFF states which are obtained from local spectrum sensing.
- After deciding on the next hop, we adopt a lightweight heuristic method to decide which channel to transmit packet when multiple licensed channels exist in the network.

To summarize, as the Euclidean distance between two secondary users based on spectrum aware virtual coordinate reflects the availability of unlicensed channel in between from the angle of historical statistics, virtual coordinate contributes a large part to deciding on the next hop.



# 2

## Background

In this chapter, the mathematical tool which is used in thesis is introduced.

### 2.1 Centralized and Distributed Algorithms in CRN

There is a considerable line of centralized approaches proposed for problems in wireless networks, which studies the fundamental computational problems and usually produce global optimal, but centralized solution is not suitable in many real world situations. Firstly of all, there exists no central authority or controller in many wireless networks to run algorithm for certain functionality. Even there exists such centralized decision maker in wireless network, it is costly to collect necessary information from the network and later tells each user what to do. As to cognitive radio network, centralized algorithm further requires the spectrum sensing results from CR users. When the licensed users change their operation state frequently, centralized decision maker obtaining the updated sensing results from CR users imposes a great burden on the network. In some scenarios, e. g., the primary users are TV stations which work on certain channels for hours of time, centralized controller obtains spectrum availability in the network from licensed users directly. In these scenarios, it is possible that the centralized controller is only responsible to protect the licensed users from interference, and doesn't control secondary users which may belong to different business groups. Thus in wireless network and particularly cognitive radio network, each user ideally makes decision itself with local information, i.e., the information within its one or two hop neighborhood.

Distributed decision of one CR user should be carefully decided as one CR's behaviour affects neighbouring CR users which go on to prompt all the CR users in the network to act accordingly. In this thesis, the interaction between CR users will be discussed under game theoretic framework.

## 2.2 Algorithmic Game Theory

Game theory is a mathematical tool for analysing the interaction of decision makers which have conflicting objectives. Game theory has been a tool to examine and analyse the actions of economic agents since long time ago. In recent years, game theory attracts people attention into apply it in communication systems.

According to [64], there are several reasons to apply game theory in communication systems.

- Communication equipments are supposed to be manufactured and operate based on standards to fulfil certain functions, but selfish behaviour may appear on certain individual equipments to achieve advantages over their peers.

For instance, Wi-Fi equipments are manufactured complying the IEEE 802.11 standards. But it is possible that certain manufacturers or the personal who uses the Wi-Fi system (we use station in the following) manipulate certain parameters to achieve performance advantage over other stations in the network. When all the stations in one network are supposed to run distributed coordination function (DCF), i.e., the station must wait a random period of time (contention window) before accessing the media when it senses the media to be busy, a certain selfish station may not choose to wait and is keen on sensing media. The selfish behaviour causes more collisions for other stations, and possibly results in poor performance in the network. In this case, game theory facilitates the network operator to issue rules to make the selfish behaviour unprofitable, or it helps to analyse how much the impact caused by the selfish stations.

- Algorithms can be retrieved from the analysis of a problem under the game theoretical framework. In the same example of media access in IEEE 802.11 DCF mentioned in previous item, if stations are allowed to modify the length of contention window, each station will adjust its contention window to obtain the best performance. [28] shows as long as each station greedily updates its CW to maximize certain utility, after certain time it will stop to do so as the current CW is the best as to the performance. In the case, the best response becomes a algorithm for Wi-Fi systems.
- Game theory assumes the research objectives to be rational. In communication system, a device is programmed to maximize or minimize the expected utility, which is perfectly rational.
- Game theory is naturally suitable for designing distributed solutions. As discussed in section 2.1, distributed solutions doesn't rely on centralized controller, and each user in the network adopts certain action as response to the other users or environment, this falls in the scope of game theory.

As an important tool in studying, modelling, and analysing the interactions, game theory also abstracts plenty of attentions in CRN [69, 95]. In the following section, we give a brief introduction to game theory and particularly congestion game which is used in our thesis.

## 2.2.1 Basics of Game Theory

We briefly list the important concepts of algorithm game theory here, many of which are referred from [71].

### 2.2.1.1 Strategic Game

A strategic game can be represented as a tuple  $\Gamma = (\mathcal{N}, (\sum_i)_{i \in \mathcal{N}}, (u_i)_{i \in \mathcal{N}})$ , where  $\mathcal{N}$  is a finite set of players,  $\sum_i$  is player  $i$ 's finite strategies. Player  $i$  selects one strategy  $s_i \in \sum_i$  at one time to play the game.  $u_i : \prod_{i \in \mathcal{N}} \sum_i \rightarrow \mathbb{R}$  is the utility function of player  $i$ .

Some relevant common used items are introduced.  $\sum = \prod_{i \in \mathcal{N}} \sum_i$  is the set of states of the game, which denotes all the possible ways that players pick strategies.  $\sum_{-i} = \prod_{i \in \mathcal{N} \setminus \{i\}} \sum_i$  is the set of states of all the other players except for player  $i$ .  $\sigma = (s_i, \dots, s_n)$  is called one profile, which is used to denote the vector of strategies selected by the players. Strategies of opponents of player  $i$  is expressed as  $s_{-i}$ , and a profile can be shown as  $\sigma = \{s_i, s_{-i}\}$ .  $u_i(\sigma) = u_i(s_i, s_{-i})$  is the player  $i$ 's utility.

### 2.2.1.2 Nash Equilibrium

A strategy profile  $s \in S$  is a Nash Equilibrium (NE) if for any player  $i$  and each alternate strategy  $s'_i$ , there is

$$u_i(s_i, s_{-i}) \geq u_i(s'_i, s_{-i})$$

which means no unilateral deviation in strategy by any single player is profitable for that player.

There exists other equilibrium conceptions. i.e., Pareto Equilibrium (PE). Pareto Equilibrium is a subset of NE, PE is an action profile  $\bar{s}$  such that there does not exist profile  $s$  with  $u_i(s) \leq u_i(\bar{s})$  for each  $i \in N$ , and meanwhile  $u_i(s) < u_i(\bar{s})$  for at least one  $i \in N$ . PE is the necessary condition of the global optimality and accordingly is more favoured, but its application in communication system is much less than NE because it is not easy to obtain PE.

Nash equilibrium is a conceptual tool and a prediction about the rational strategic behaviour by agents in situations of conflict, hence, it carries great importance to know how much computational effort needed to compute NE. Unlucky, the computation of NE is usually a combinatorial optimization problem (chapter 2) []. but in some special cases,

### 2.2.1.3 Potential Game

A potential game is a tuple  $\lambda = (\mathcal{N}, (\sum_i)_{i \in \mathcal{N}}, (u_i)_{i \in \mathcal{N}})$ , which satisfies the following, if there exists a function  $\phi : \sum \rightarrow \mathbb{R}$ , such that for every  $i \in \mathcal{N}$ , for every  $s_{-i} \in \sum_{-i}$ , and every  $s_i, s'_i \in \sum_i$ :

$$u_i(s_i, s_{-i}) - u_i(s'_i, s_{-i}) = \phi_i(s_i, s_{-i}) - \phi_i(s'_i, s_{-i})$$

It is easy to see that the design of function  $\phi$  is the key point to form a potential game.

### 2.2.2 Congestion Game

Congestion game is a special type of potential game, which has extra conditions, but also yield favourable characteristics. Congestion game is an attractive game model which describes one kind of problem where nodes compete for limited resources in a non-cooperative manner [94]. This game formulates many problems in realistic world, e. g., minimisation of commuting time on the road for commuters, minimization of energy consumption in mobile cloud computing system [40].

Before giving the definition, we introduce an exemplary congestion game called *server matching*. Consider a couple of self-interested clients and servers. Each client should access one server. The latency of one server increases with the *number of clients* attached to it. If these clients greedily choose a permissible server because of smaller predicted latency, then after finite number of switches, no client has motivation to switch any more. More formally, a congestion game is composed of players (the self-interested clients) and resources (servers), where players are allowed to choose certain resources to use. There is cost (latency) generated on a resource for the player whenever the player uses that resource, and the cost is monotonic increasing with the number of players using it. If every player greedily searches the allowed resources to decrease its cost, the dynamics will cease a stable state called *Nash Equilibrium* (NE), where no player has motivation to adopt a new set of resources unilaterally. An important aspect of this convergence is a value called *potential* which monotonically decreases with the update of players in the convergence process.

Now we give the formal definition of congestion game.

A congestion game [82][94] can be expressed by a tuple  $\lambda = (\mathcal{N}, \mathcal{R}, (\sum_i)_{i \in \mathcal{N}}, (g_r)_{r \in \mathcal{R}})$ , where  $\mathcal{N} = \{1, \dots, N\}$  denotes the set of players (each each is labeled with a unique index number),  $\mathcal{R} = \{1, \dots, m\}$  the set of resources,  $\sum_{i \in \mathcal{N}} \subseteq 2^{\mathcal{R}}$  is the strategy space of player  $i$ . Under strategy profile  $\sigma = (\sigma_1, \sigma_2, \dots, \sigma_N)$ , player  $i$  chooses strategy  $\sigma_i \in \sum_i$ , and the total number of users using resource  $r$  is  $n_r(\sigma) = |\{i \mid r \in \sigma_i\}|$ . The cost  $g_r : \mathbb{N} \rightarrow \mathbb{Z}$  is a function of the number of users for resource  $r$ ,  $g_r^i = \sum_{r \in \sigma_i} g_r(n_r(\sigma))$ . In our paper,  $g_r^i$  is referred as *congestion* and is Monotonic.

Rosenthal's potential function  $\phi : \sigma_1 \times \sigma_2 \times \dots \times \sigma_n \rightarrow \mathbb{Z}$  is defined as:

$$\begin{aligned} G(\sigma) &= \sum_{r \in \mathcal{R}} \sum_{i=1}^{n_r(\sigma)} g_r(i) \\ &= \sum_{i \in \mathcal{N}} \sum_{r \in \sigma_i} g_r(n_r^i(\sigma)) \end{aligned} \quad (2.1)$$

$n_r^i(\sigma)$  means the number of players using resource  $r$  and *their indices are smaller than or equal to  $i$* . Note that the potential is *not* the sum of congestions experienced by every user. The change of the potential caused by one player's unilateral move from  $\sigma$  to  $\sigma'$  is equivalent to the change of gain (or loss) of that player.

$$\Delta G(\sigma_i \rightarrow \sigma'_i) = g^i(\sigma'_i, \sigma_{-i}) - g^i(\sigma_i, \sigma_{-i}) \quad (2.2)$$

$\sigma_{-i}$  is the strategy profile for all players except for  $i$ . As every congestion game is a potential game, and the total potential is finite, thus the number of improvements is upper-

bounded by  $2 \cdot \sum_{r \in \mathcal{R}} \sum_{i=1}^{n_r(\sigma)} g_r(i)$  [94].

# 3

## Distributed Channel Allocation in CRN

### 3.1 INTRODUCTION

Opportunistic utilization for secondary users working with TV broadcast spectrum (TV white space) is promising to cope with the scarcity of spectrum resources[7]. Firstly, more unused TV white frequencies become vacant than ever with the ongoing transition from analog to digital broadcasts. Secondly, the lower frequencies of TV band enable broadband access over much longer ranges compared to other bands with higher center frequencies. Nevertheless, services on TV receivers need to be protected with so called interference margin [54] which must not be exceeded jointly by all secondary users working on the the channel .

Federal Communications Commission (FCC) of U.S. and Electronic Communications Committee (ECC) in Europe have announced rules on the transmission power of white space for secondary users in US and Europe respectively[7, 8]. FCC adopts a minimum distance between secondary user and TV service area to guarantee that the interference margin is not exceeded by secondary users. The transmission power for fixed secondary users is fixed to 4 W which is a conservative setting. FCC assumes that the protection area is sufficient to protect the TV receivers, but it is not the case when there are multiple secondary equipments transmitting in the the same as is discussed in [49]. ECC's restriction requires that the secondary user adapt its transmission power in order not to violate the interference margin at exposed TV receivers. In this manner, secondary systems have to determine their maximum transmission power.

FCC issued a memorandum [7, 6] in 2010, which removed the mandatory sensing requirements and thus greatly facilitates the use of the spectrum with geolocation based channel

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<sup>2</sup>interference margin is the maximal interference caused by secondary users, which doesn't violate TV service.

<sup>3</sup>In this paper, channel and spectrum are used indiscriminately

allocation. Work [68] follows this rule to obviate spectrum sensing and only rely on the database of TV incumbents to determine the white space availability on secondary users. The authors of [68] demonstrate the feasibility of predicting the available TV spectrum accurately using suitable propagation models (Longley-Rice and terrain wherein). A central controller contains the locations of all TV stations and secondary users, then the central controller calculates the RSSI level of TV UHF signals on all secondary users and accordingly determines the available TV spectrum for them. The authors give big impetus to the database method by developing sophisticated signal propagation modelling and efficient content dissemination scheme. Enlightened by this work, it can be seen that the RSSI level caused by secondary users on TV receivers can be calculated accurately in a centralized entity if secondary users' transmission power, geo-location and appropriate propagation model are provided. Inversely, given geo-location and appropriate propagation model, secondary users' maximum transmission power can be determined by the central entity according to the interference margin (maximum RSSI level from secondary users) at TV receivers.

To guarantee the protection on TV systems from harmful interference, FCC and IEEE propose a central database to regulate the access of TV spectrum by the secondary users. The centralized database registers the location and terrain information for all secondary users in the network, and decides the available channel and maximal permitted transmission power for each secondary user. It is natural to think to utilize the central database as a controller to assign channel and power usage, but the secondary users may belong to different commercial groups and they may not content with the assigned resource. This is more truer when the considering the available channels have different quality, i.e., interference level, and permitted transmission power. Hence, the spectrum sharing of the secondary users in 802.22 network is a distributed system where each secondary user maximizes its preferred utility, and meanwhile the aggregated interference generated by them should be kept below a certain threshold on the TV system.

In this paper, the secondary users are assumed to be cellular systems consisting of base stations and associated terminals, all of which work on TV white spectrum. The corresponding secondary base stations are referred as white base stations (WBS). Some cellular networks, such as GSM or LTE network, work on Licensed spectrum, and they emphasis on providing satisfactory services to their end terminals by choosing proper transmission channel and power. As to cellular network working on TV white spectrum, they have to keep one eye on the primary users to make sure that TV service is not violated, which make the problem of channel and power selection even harder. It is possible that WBSes are owned and operated by different operators, thus completely centralized decision on the base stations' working channel and transmission power is infeasible. In this paper we will look for a distributed scheme to solve this problem.

The rest of the paper is organized as follows. we elucidate the system model in Section II, afterwards related work and problem formulation is presented in Section III. In Section IV, we discuss how to utilize the white space sufficiently by setting the transmit powers based on a convex problem formulation. We analyze the spectrum allocation problem under game theoretical framework and propose an algorithm in Section V, thereafter performance evaluation is presented in Section VI. Finally, we conclude our work and point out directions of future research in Section VII.

## 3.2 System Model

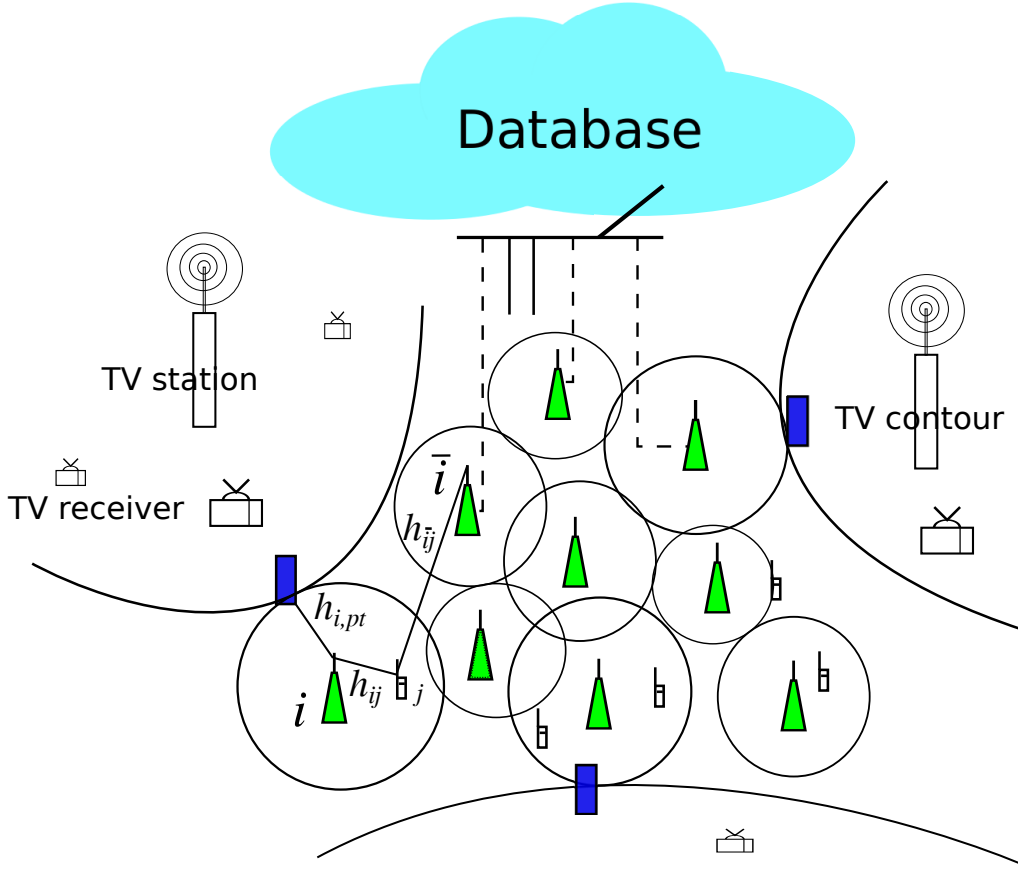
Following the IEEE 802.22 standard, the primary systems considered in this paper are digital TV (DTV) stations which use the TV spectrum legally. TV stations provide service to passive TV receivers which must not be interfered by secondary systems. The secondary systems are IEEE 802.22 Wireless Regional Area Network base stations (WBS) utilizing the TV spectrum with senseless mode [68]. WBSes serve a set of end users/terminals without interfering TV receivers significantly. Denote the set of DTV stations by  $\mathcal{K}$  and the collection of WBSs by  $\mathcal{N}$  with  $|\mathcal{N}| = N$ . Furthermore, there are  $\mathcal{C}$  channels considered in total with  $|\mathcal{C}| = C$ . These secondary systems are distributed over a certain area  $A$  and is surrounded by multiple DTV service areas, as Figure 3.1 shows. When there are two WBSes work on the same channel, co-channel interference will be caused to each other by them, while, neighbouring channel interference is not considered. Each DTV station as well as each WBS utilizes exactly one channel. We represent the usage of channel for WBS  $i$  with a binary vector  $X_i^{|\mathcal{C}| \times 1} = \{\dots, x_{ik}, \dots\} \in \{0, 1\}^{|\mathcal{C}|}$ , where  $k \in \mathcal{C}$  and binary variable  $x_{ik}$  denotes whether channel  $k$  is used by user  $i$ . As each node can only use one channel, for  $X_i$ , there is  $\sum_{k=1}^{|\mathcal{C}|} x_{ik} = 1$ . The transmission power of WBS  $i$  on channel  $c$  is  $P_i^c$ .

Let  $c(i)$  denote the channel used by a WBS  $i \in \mathcal{N}$ . The TV channels are considered to be identical. In the rest of the paper, we use the words WBS and secondary base station interchangeably. There are TV service contours deployed at the edge of the TV service area (as bold rectangles in Figure 3.1) representing the worst located TV receivers. For them a certain upper bound of interference should not be violated to guarantee the TV services, where the interference is from secondary users and noise. The deploy of contours is decided by the TV operators, which varies according to the concrete location, geographic terrain and possible deployment of secondary networks. For simplicity, we assume there is only one contour deployed for one TV area.

WBSs are interested in payload data exchange with their associated terminals with good quality of services (QoS). As to performance metric for this QoS provisioning, we choose the signal-to-noise-and-interference ratio (SINR) at the terminals. SINR is the ratio between the power of the received signal of interest and the summed power of all interference sources as experienced by the terminal. We only focus on the down-link SINR. We denote the path loss between the serving WBS  $i$  and a certain terminal  $j$  associated to it by  $h_{ij}$ , similarly, the path loss between any other secondary base station  $\bar{i} \neq i$  operating on the same channel as  $i$  and end user  $j$  is denoted as  $h_{\bar{i}j}$ . The path loss is dependent on the distance between the corresponding equipments, e.g.  $h_{ij} = K \cdot d_{ij}^{-\alpha}$ , where  $\alpha$  is the path loss exponent and  $K$  is a constant that models the reference loss over a single unit of distance. Furthermore,  $N_0$  denotes the noise power. Finally, we do consider shadowing, but do not consider fading. Hence, the sum of all disturbing RF effects (including interference) at terminal  $j$  (we assume the working channel is  $c$ ) is given by

$$f_j^c = \sum_{\bar{i}} (P_{\bar{i}}^c \cdot h_{\bar{i}j} \cdot z_{\bar{i}j}) + N_0 \quad (3.1)$$

<sup>4</sup>The assumption that one WBS only utilizes one channel is for convenience of analysis. In reality multiple channel usage (channel bonding) is requisite as one single TV channel's bandwidth is 6 MHz which is not adequate for a WBS to fulfil system requirement. We will relax this single channel usage assumption without hammering our scheme in the end of section ??.



**Figure 3.1** System model: WBS cells and DTV systems

where  $P_i^c$  denotes the transmit power of WBS  $\bar{i}$  and  $z_{ij}$  models the zero-mean log-normally distributed shadow-fading with standard deviation  $\sigma_{SH}$  between  $\bar{i}$  and  $j$ . Hence, the signal-to-interference-and-noise ratio (SINR) on end terminal  $j$  is given by:

$$\gamma_j = \frac{P_i^c \cdot h_{ij} \cdot z_{ij}}{f_j^c} \quad (3.2)$$

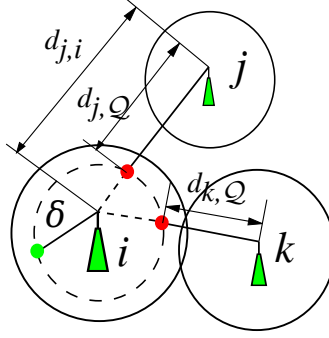
We assume all secondary systems can access the central database directly to obtain geo-location information and the channel usage situation. WBSes work on senseless mode, which can calculate the RSSI from one transmitter to an receiver with proper propagation model (e.g. Formula 3.13.2 can be calculated within database) with the geo-location and channel usage information. The geo-location information in the secondary networks is deemed to be static. We assume the secondary base stations are not under the same operators, thus there is no scheduling mechanism available among WBSes.

### 3.2.1 QuasiSINR: the considered SINR on terminals

We are interested in improving the SINR on the terminals of each cell. As the distribution of mobile terminals is varying and influenced by many factors, i.e., the type of services provided to the terminals, the type of area and mobility of terminals, it is difficult to choose one terminal whose SINR is able to represent the worst case for SINR in that cell. Thus we propose a metric *QuasiSINR* which is independent on any terminals. QuasiSINR



is defined as follows. We consider a circle around an WBS with radius  $\delta$  as is shown in Figure 3.2.



**Figure 3.2** QuasiSINR

The radius  $\delta$  is the largest distance among all associated terminals of the considered WBS. For this terminal farthest away, we now construct a worst-case SINR which factors in all interference from neighboring secondary cells as if they were closest to the considered terminal. Hence, QuasiSINR is the ratio between the weakest signal of interest and the summation of the biggest (possible) interference from other co-channel WBSs. According to this construction, the weakest strength of the signal of interest is  $P_i^c \cdot h_{iQ} \cdot z_{iQ} = P_i^c \cdot \delta^{-\alpha} \cdot z_{iQ}$  while the biggest possible interfering power from co-channel WBS  $j$  is  $P_j^c \cdot h_{jQ} \cdot z_{jQ} = P_j^c \cdot (d_{ji} - \delta)^{-\alpha} \cdot z_{jQ}$ . We denote in this context by  $Q$  the virtual worst-case terminal. Hence, as we form the SINR such a virtual 'worst-case' terminal, the co-channel interference impact is overestimated as the total received interference power is given by the sum  $\sum_{j \neq i, j \in \mathcal{N}} P_j^c \cdot h_{jQ} \cdot z_{jQ}$  where index  $j$  spans all co-channel WBSs with  $i$ . Formally, the QuasiSINR of WBS  $i$  is given by:

$$\begin{aligned} \tilde{\gamma}_i &= \frac{P_i^c \cdot h_{iQ} \cdot z_{iQ}}{\sum_{\substack{j \neq i, j \in \mathcal{N} \\ c(j)=c(i)}} (P_j^c \cdot h_{jQ} \cdot z_{jQ}) + N_0} \\ &= \frac{P_i^c \cdot \delta^{-\alpha} \cdot z_{iQ}}{\sum_{j \neq i, j \in \mathcal{N}} (P_j^c \cdot (d_{ji} - \delta)^{-\alpha} \cdot z_{jQ}) + N_0} = \frac{\tilde{P}_i^c}{\tilde{f}_i^c} \end{aligned} \quad (3.3)$$

$\tilde{P}_i^c$  represents the power of received interested signal from WBS  $i$ , which happened on any point on the  $\delta$ -circle of WBS  $i$  (green dot in Figure 3.2), and  $\tilde{f}_i^c$  denotes the sum of received co-channel interferences plus noise, where the co-channel interference happens on the intersection point (red dot in Figure 3.2) of the  $\delta$ -circle and line connecting WBS  $i$  and the interfering WBSes.

Notice regarding the QuasiSINR, that any modification of the transmit powers of co-channel interference source (i.e. other WBS working on channel  $c$ ) will have always fixed impact to the WBS concerned, so the interaction between co-channel WBSes are independent on the concrete end terminals. With QuasiSINR, the channel and power allocation problem will exclude terminals and thus simplify the problem. QuasiSINR will be validated in Section 3.7.

### 3.2.2 The problem to solve in this paper

Our goal can be illustrated in the form of an optimization problem. To ensure fairness, instead of maximizing the sum of QuasiSINR of all WBSs, we try to minimize the sum of inversed QuasiSINR.

$$\begin{aligned} & \text{Minimize} \quad \sum_{i \in \mathcal{N}} \frac{1}{\tilde{\gamma}_i} \\ & \text{subject to} \quad \sum_{k=1}^{|\mathcal{C}|} x_{ik} = 1 \end{aligned} \tag{3.4}$$

For every WBS, each channel in  $\mathcal{C}$  experiences different levels of interference from other WBSs working on it. In order to provide better service to its end users, WBS is liable to choose either the channel permitting higher transmission power or the one with less interference, or the channel compromising the two factors according to Formula 3.2. Achieving optimal white spectrum allocation in a distributed style is the goal of this work, furthermore, this distributed solution should converge fast and lead to an efficient and stable solution.

## 3.3 Related Work

Given all the other WBSes' channel/power selection in secondary network, one WBS is interested in choosing the channel experiencing the minimum interference, and utilizing the biggest possible transmit power in order to achieve better SINR at its terminals and meanwhile maximize their coverage [102, 43]. Nevertheless, high transmission power causes significant co-channel interference to other secondary cells operating on the same channel. Hence, secondary cells have to balance the own used transmit power with the interference caused on other cells as well as the interference experienced in their own cell while deciding on the channel to use (if multiple channels are available). Our goal is to find a strategy for WBSes to choose channel and power level in order to acquire good SINR on end terminals, in the same time protecting the primary users from harmful interferences. This joint power and channel allocation problem in cognitive radio scenario has drawn many attentions. The proposed solutions can be divided into two categories, centralized and distributed, which will be introduced sequentially.

As to centralized solutions, an optimization problem is always to formulated to solve the problem. In [44], the objective is to increase the number of supported terminals whose SINR is above a threshold, and the constrains are to refrain the interferences on the primary users under a certain threshold. [22] minimizes the transmission power and meanwhile makes sure the SINR of terminal is above one threshold. This work fails to consider the protection of primary users. Other schemes expect for optimization is also used to tackle this problem. [77] proposes a heuristic algorithm considering the channel availability and transmission demand of each WBS. Spectrum allocation is solved after being formulated into a colouring problem. The aforementioned two schemes don't consider varying the transmission power.

As to decentralized schemes, in order to avoid or alleviate co-channel interference between neighbouring cells, and allow arbitrary number cells to be in the 802.22 network,

[45] proposes distributed inter-network spectrum sharing scheme, where contention decisions are made in a distributed way and winner cells can use the shared channel. This work doesn't consider the role of transmission power in the co-channel interference. [43] discusses power control and channel assignment in both down-link and up-link communication in cellular network. Although the solution is distributed, Primary users are required to cooperate with secondary base station in a learning process to decide the transmission power, in addition, there is only one secondary base station considered whereas we are coping with the whole cellular network. An distributed power allocation (single channel) scheme based on learning for secondary networks is given in [37], where penalty function involving the interference threshold on primary systems is used. [102] deals with the joint channel-power selection for multiple transmission links (pairs). The authors decompose the Lagrangian dual of the problem, then propose a distributed scheme based on the dual parameters. The scheme converges to pure Nash equilibrium, but in order to facilitate this scheme, monitors are required to watch interference from secondary users, moreover, monitors have to be equipped computational ability and interact with secondary users in the whole process of convergence. Distributed joint power and channel allocation is proposed in [73], each base station chooses optimal power level and channel to optimize its utility, which involves induced and received interference along with the interference on primary users. The execution of this scheme is formulated into an exact potential game. For each base station, after several rounds of best responses in terms of channel and power level, Nash equilibrium is achieved. There are some flaws hindering the application of this scheme. First of all, the paper doesn't provide means for base stations to obtain the needed information which is needed to calculate the utility function. Secondly, as how does the base station know the interference received on the primary users, it is not clear how to calculate the punishment in the utility function, which indicates whether and how much the interference threshold on primary users is violated. Thirdly, the convergence speed of the scheme is not given, in fact, as the problem is formulated into an potential game, converge speed, or to say the number of updates before convergence is a theoretic problem which is still unsolved [x]. Last but not least, as the utility function and the potential in the game are designed as the sum of received and introduced interference, the desired signal power and the punishment, the minimization of this 'sum' does indicates meaning performance metric, i.e., SINR on terminals, or the total transmission power consumption.

[22] proposes both centralized and decentralized solutions. Two distributed schemes are proposed, joint channel and power allocation is formulated into a weighted potential game, as an alternative workaround, the problem is solved in two sequential phases.

### 3.3.1 Problem Formulation: three sequential subproblems

In the aforementioned works, the protection on primaries users is taken care during deciding the channel and power selection, but in the current 802.22 standard, there exist no communication media between the secondary network and the primary users, besides, assume such communication media is available, the communication overhead between primary users and second users is considerable. Based on this analysis, we decide the maximal transmission power for each WBS on each channel before taking care of the channel and power allocation afterwards. By doing this, the protection on the primary users from harmful interferences is excluded from the latter consideration on channel and power allocation.

In this paper we solve the channel and power allocation in downlink 802.22 network by solving three sequential subproblems: firstly, given a set of secondary WBS and their geo-location, the maximum permitted transmit power on all channel for each WBS can be determined, so that the interference margin is impossible to be broken no matter how do WBSes utility the channel and power resources. In other words, the dynamics in the secondary network is transparent to primary system. This requires to consider the joint interference that the WBS have on the TV receivers of the considered service area. Secondly, once the maximal transmit power has been determined, each WBS needs to choose its operating channel. Thirdly, transmission power is adjusted on the channel which is decided in the previous step. While for the first problem a centralized approach is of interest, the following two problems will be solved by distributed schemes.

### 3.3.2 Maximal transmission power planning

To protect the TV contours from harmful interference from secondary base stations, the aggregate interference caused by WBSs on TV contours should be lower than interference margin [54]. The sufficient condition in the context of TV white space is formulated into a centralized linear programming program (LP). Adopting centralized scheme is due to the special network structure according to IEEE 802.22 standard. The standard required a centralized database to store the available channels for each secondary base station, thus centralized scheme can be conducted there after trivial modification. The objective function is to maximize the summation of all secondary base stations' transmission power, and the constraints are built to satisfy the sufficient condition for every TV contour.

### 3.3.3 Channel allocation with fixed transmission power level

After knowing the power limit on each channel, WBSs need to decide which channel to use so as to mitigate interference among WBSs and provide better SINR to its end users. Here we assume WBSs' transmission power is the biggest permitted and fixed. Such problem lies in *channel assignment problem* which has been well investigated in many scenarios. Channel assignment problem mainly cope with mitigating co-channel interference among users, which can be converted into coloring problem thus is NP hard [80]. Authors of [20, 53] propose heuristic algorithms utilizing best response based on the welfare on itself to assign channels among users, but the assumption that transmission power is identical and path loss is symmetric renders them problematic for our problem where transmission is nonidentical and the path loss is asymmetric. Distributed algorithm based on Learning is proposed in [46] for LTE to allocate the the resource block in down link, which leads to correlated equilibrium, but large number of steps hinder its application. [70] formulates channel assignment problem in ad-hoc cognitive radio network into potential game which leads to pure NE, a learning scheme achieving slightly better performance is provided for comparison, but they assume the transmission power is identical and there is no noise in the secondary network, and the proposed random access mechanism demands a huge amount of information to be exchanged, which is a real burden for network in ad-hoc structure. [34, 99] investigates the channel allocation problem under game framework in same collision domain, the authors proposes algorithms to converge to pure Nash equilibrium (NE) and strongly dominate strategy equilibrium respectively. As to

our knowledge, there is no work dealing with channel allocation with such asymmetric interactions.

### 3.3.4 Power allocation

Working with the maximal permitted transmission power may not be the optimal in terms of power consumption and the SINR on terminals. Thus distributed power adjustment is conducted.

## 3.4 Decide the maximal permitted transmission power

We adopt the interference model and the optimization methodology from the work of [54] to plan the maximal transmission power for WBSs. In our system the WBSs locate within one area whereas TV areas locate around them. If implying linear programming to decide the maximal transmission power, the WBSs locating far from TV contours contribute more to the sum of power with the biggest permitted power, as a result the maximal transmission power on each channel obtained with LP is seriously unbalanced. To address this fairness issue, we try to maximize the summation of the logarithmic value of every WBS's value, then we formulate the problem into a series of convex optimization problems. We denote that, for WBS  $i \in \mathcal{N}$ , the maximal transmission power allowed to be used on channel  $c$  is denoted as  $P_i^c$ .  $P_i^c$  varies with respect to  $i$  and  $c$ .

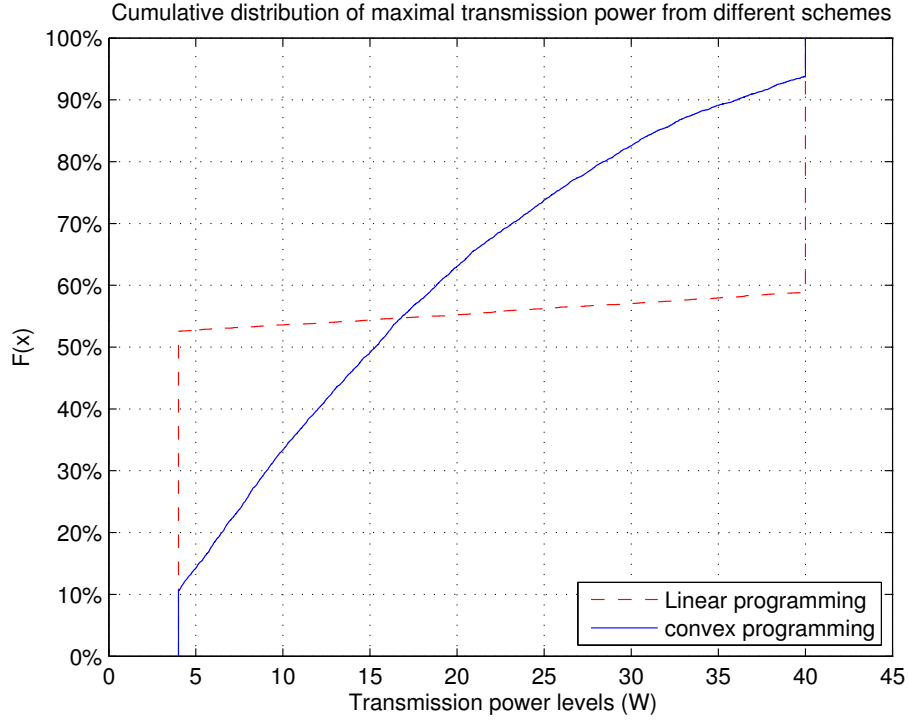
For each channel  $c \in \mathcal{C}$ , the maximal permitted transmission power on each WBS can be obtained by solving the following optimization problem,

$$\begin{aligned} & \text{Maximize} \quad \sum_{i \in \mathcal{N}} \log(P_i^c) \\ & \text{subject to} \quad \sum_{i \in \mathcal{N}} (P_i^c \cdot h_{i,pt} \cdot z) < I_{pt}^c, \end{aligned} \tag{3.5}$$

where  $I_{pt}^c$  is the interference margin for the DTV contour  $pt$  and the DTV is working on channel  $c$ .  $z$  carries the same meaning with that in 3.2. Here we only consider the interference caused by WBSs, Since their transmission power is higher and their altitude is higher[54], thus the downlink transmission contributes the main secondary interference[14], and the interference caused by white space end users is trivial and omitted. There will be multiple constraints for 3.5 if there are multiple DTV contours working on channel  $c$ . There is one optimization problem for each channel  $c \in \mathcal{C}$ , after solving the  $|\mathcal{C}|$  problems, we obtain the maximal transmission power over all channels (maximal power map) for every WBS. We solve this convex optimization problem with [41] in the centralized base station.

Figure 3.3 depicts the distribution of maximal transmission power levels obtained in 100 simulations. In each simulation the locations of TV contours are randomly decided around the WBSs. It can be seen that around half of WBSs' transmission power planned with LP is restricted to be the minimum transmission power, and the other half of WBSs' transmission power is the maximum permitted power. By applying convex programming, the planned maximal transmission power levels are distributed evenly in between the minimum

and maximum permitted power. The gain of SINR on end terminals by applying convex optimization to decide the maximal transmission power is illustrated in the simulation section.



**Figure 3.3** Distribution of maximal transmission power levels obtained from convex and linear programming respectively

Optimization problem 3.5 provides the maximal transmission power without violating the TV contour, as there are multiple channels available in the network, as long as there are WBSs which work on a different channel from others, there will be a new interference margin for TV contour, which provides tolerance space for network dynamics such as new WBS starting to work or increased interference on TV contour because of variance of broadcast path condition.

## 3.5 Channel Allocation with Fixed Transmission Power

### 3.5.1 Centralized optimization programming

In the very beginning, We formulate the channel allocation problem into a binary quadratic programming problem which can be solved in a centralized way. For two nodes  $i$  and  $j$ , there is,

$$X_i^T X_j = \sum_{k=1}^{|C|} x_{ik} \cdot x_{jk} = \begin{cases} 1 & \text{if } c_i = c_j \\ 0 & \text{if } c_i \neq c_j \end{cases} \quad (3.6)$$

The power levels across all channels are denoted by a constant vector  $P^{|C| \times 1}$ , which possibly nonidentical to all nodes because of maximal channel planning. The power used by user  $i$  is  $P_i^T X_i = \sum_{k=1}^{|C|} P_i^k \cdot x_{ik}$ .

Problem 3.4 can be modeled via general purpose nonlinear optimization:

$$\begin{aligned} \text{minimize: } & \sum_{i=1}^n \frac{\sum_{j \in \mathcal{N}, j \neq i} P_j^T X_j (X_j^T X_i) h_{ji} z + N_0}{P_i^T X_i} \\ \text{subject to } & \sum_{k=1}^{|C|} x_{ik} = 1, x_{ik} \in X_i \in \{0, 1\}^{|C|} \end{aligned} \quad (3.7)$$

$x_{ik}$  with  $i \in \mathcal{N}, k = 1, 2 \dots$  is binary variable. Problem 3.7 is a non-linear problem with binary variables, but it can be reformulated in to a quadratic programming problem as,

$$\begin{aligned} \text{minimize} & \\ \sum_{i=1}^n & \left( \sum_{j \in \mathcal{N}, j \neq i} \sum_k \frac{P_j^k}{P_i^k} \cdot h_{ji} \cdot z \cdot x_{jk} \cdot x_{ik} + \sum_k \frac{N_0}{P_{ik}} \cdot x_{ik} \right) \\ \text{subject to: } & \sum_{k=1}^{|C|} x_{ik} = 1, x_{ik} \in X_i \in \{0, 1\}^{|C|} \end{aligned} \quad (3.8)$$

The reformulation is available in Appendix B. We use LINDO[9] which is a state of art non-linear problem solver to solve the problem, which employs Branch-And-Reduce method to get the global optimal for the problem. The result will be used as a reference in the simulation section with other schemes.

### 3.5.2 Distributed White space channel allocation technology (WitheCat): algorithm and protocol

In this paper a distributed scheme for WBSs to allocate channels is proposed, which is named as white space channel allocation technology (WitheCat). WitheCat is depicted by algorithm 1 which is a best response process, where each WBS (referred as  $i$ ) greedily searches for a preferred channel based on utility function  $u_i$ , and the sum of all WBSs' utilities is minimized after finite times of updates even the interaction between WBSs are asymmetric. The utility is as follows,

$$u_i = \frac{\sum_{\substack{j \in \mathcal{N}, j \neq i, \\ c(\sigma_j) = c(\sigma_i)}} \tilde{f}_{ji}}{2 \cdot \tilde{P}_i} + \frac{1}{2} \sum_{\substack{j \in \mathcal{N}, j \neq i, \\ c(\sigma_j) = c(\sigma_i)}} \frac{\tilde{f}_{ij}}{\tilde{P}_j} + \sum_{\substack{\mathcal{S}: i, j \in \mathcal{S}, \\ c(\sigma_j) = c(\sigma_i)}} \frac{N_0}{C \cdot \tilde{P}_i} \quad (3.9)$$

where  $\tilde{f}_{ij} = P_i \cdot h_{ij} \cdot z$  and  $\tilde{f}_{ji} = P_j \cdot h_{ji} \cdot z$ . Overlooking the constant coefficient 2, the first item of  $u_i$  is one part of the inversed QuasiSINR of station  $i$ . To minimize the first item, WBS  $i$  needs to choose a channel either permits larger transmission power or experiences less interference, whereas the larger power will increase the second item

which is part of inversed QuasiSINR of other co-channel WBSs. Hence, the cost function presents a reasonable compromise between the welfare of one WBS and others. If WBS only emphasizes on its own utility (e.g. the first part of Formula 3.9), the best response process doesn't converge. We have following theorem:

**Theorem 3.5.1.** *With non-identical transmission power, if every WBS updates its channel based on algorithm 1 with utility based on its own interests, the process doesn't always converge.*

The proof is in Appendix A.

---

**Algorithm 1:** Spectrum selection for node  $i$

---

**Input:** quasi distance  $d_{ij}$  for  $\forall i, j \in \mathcal{N}$ ; path lose between  $i$  and any other WBS  $h_{ij}$ ,  $j \in \mathcal{N}$ ,  $j \neq i$ , and the fading  $z$  on it; noise  $N_0$ ; total number of secondary base stations  $N$ ; maximal transmission power  $P_j^c$ ,  $j \in \mathcal{N}$ ,  $c \in \mathcal{C}$ ;  $c(j)$ , current channel used by  $j \in \mathcal{N}$ ,  $j \neq i$ .

```

1 for  $i \in \mathcal{N}$  do
2   for  $c \in \mathcal{C}$  do
3     calculate  $u_i(c)$  based on Formula 3.9
4     if  $u_i(c) < u_i(c(i))$  then
5        $c(i) \leftarrow c$ 
6     else
7        $c(i)$  unchanged
8   Notify data base of its channel usage, which notifies the other WBSs

```

---

$c(i)$  is the current channel used by  $i \in \mathcal{N}$ . Imitating the player's behavior in the congestion game, each base station tries to find the channel  $c \in \mathcal{C}$  that brings the smallest  $u_i$  based on the other stations' decisions, every channel update will decrease the summation of utilities in the whole network and finally converges to a pure Nash equilibrium (proof is in section 3.5.3).

Some parameters needed to calculate the utility are identical for all WBSs, such as quasi distance  $e$ , the total number of WBSs  $N$ , number of channels  $C$ , attenuation factor  $\alpha$ , standard deviation  $\sigma_{WBS}$  in flat shadowing and noise  $N_0$ , albeit the following information is further needed to calculate  $u_i$ :

- $\sum_{\substack{j \in \mathcal{N}, j \neq i, \\ c(\sigma_j) = c(\sigma_i)}} \tilde{f}_{ji}^c$ ,  $c \in \mathcal{C}$ : the received interference on  $i$ ' virtual measurement point from other WBSs  $j$  working on the same channel for  $\forall c \in \mathcal{C}$ .
- $\tilde{f}_{ij}^c$ : the interference caused by  $i$  on  $j$ 's virtual measurement point when  $i$  works on channel  $\forall c \in \mathcal{C}$ .
- $P_j^c$ : transmission power of  $j$  for using  $\forall c \in \mathcal{C}$ .

Unfortunately, it is difficult to get these interferences of interested measured, for station  $i$ , it is low efficient to scan all channels and obtain the interferences  $\tilde{f}_{ji}$  on virtual measurement point for each channel, furthermore, it is impossible to split the interference  $\tilde{f}_{ij}$  from the total interference received on WBS  $j$ ' virtual measurement point.



Enlightened by the work of [68] which verifies the usage of Geo information in deciding the available channels, we let every WBS store the location information and maximal power map of all other WBSs, and it retrieves information about channel usage by other WBSs from centralized base station, after executing Algorithm 1, it reports to centralized base station for its channel update. As the location of WBSs and TV stations and the transmission channel and power of TV stations are generally static (entries of TV station change averagely once in 2 days[68]), except for the channel usage in the network, the change of the other data stored in WBS is infrequent.

We refer [70] to decide the sequence for WBSs to update their channel. [70] proposes a method like random access mechanism of CSMA/DA, where the access for broadcast medium is changed to getting access to the centralized center to retrieve the current channel usage and update its new channel. All WBS are able to access the database in one round (with random or Predetermined sequence). As WBSs are connected with database, the control messages needed to decide the sequence will not become a burden. Update of channels can happen in the boot phase, or when the quality of services (the SINR on its end users) of WBSs falls below a threshold, or a fixed time duration comes to end, or a new WBS joins in the network.

### 3.5.3 Analysis in game theoretical framework

We give an elegant proof on WhiteCat's convergence in the framework of congestion game theory. Formulating a spectrum sharing problem into a congestion game and the concept of *virtual resources* are firstly proposed in [59] which 'reversely engineer' the distributed channel allocation schemes proposed in [20, 53].

In congestion game, each player acts selfishly and aims at choosing strategy  $\sigma_i \in \Sigma_i$  to minimize their individual cost. The gain (loss) caused by any player's unilateral move is exactly the same as the gain (loss) in the potential, which may be viewed as a global objective function. For problems where the potential of the problem is the same with the summation of the cost of all users, the cost function can be used as a utility function directly. This equivalence doesn't exist in our problem, but by carefully choosing the cost function for players, we can make sure that the change of individuals' cost is in the same direction with that of the global utility.

#### 3.5.3.1 Bridging the game and practical scheme

We utilize the conception of virtual resource which is firstly introduced in [59]. In the following text, we use player and base station interchangeably.

- Player  $i$ ' strategy space is  $\Sigma_i = \{(i, j, c), j \in \mathcal{N}, j \neq i, c(\sigma_j) = c, c = 1, 2, \dots, N\}$ , and  $i$  has  $C$  admissible strategies, one strategy related with channel  $c \in \mathcal{C}$  is described by the set of virtual resources it uses:  $\sigma_i = \{(i, j, c), j \in \mathcal{N}, j \neq i, c(\sigma_j) = c\}$ , note that virtual resource  $(i, j, c) \neq (j, i, c)$ .
- Under the strategy profile  $\sigma = (\sigma_1, \sigma_2, \dots, \sigma_N)$ , player  $i$  obtains a total cost of

$$g^i(\sigma) = \sum_{\substack{j \in \mathcal{N}, j \neq i, \\ c=c(\sigma_i)=c(\sigma_j)}} (g_{(i,j,c)}(n_{(i,j,c)}(\sigma)) + g_{(j,i,c)}(n_{(j,i,c)}(\sigma))) \quad (3.10)$$

The transmission power over all channels of player  $i$  is  $\{p_{i1}, p_{i2}, \dots, p_{i|C|}\}$  and fixed. Path loss is assumed reciprocal:  $h_{ij} = h_{ji}$ , but nor is the flat fading  $z$ . To keep the formula clear in the following part, we denote  $\tilde{f}_{ij} = P_i \cdot h_{ij} \cdot z$ ,  $\tilde{f}_{ji} = P_j \cdot h_{ij} \cdot z$ ,  $\tilde{P}_i = h_{iQ}$  for  $i \in \mathcal{N}$ , where  $h_{ji} = h_{ij} = (d_{ji} - e)^{-\alpha}$ ,  $h_{ii} = h_{jj} = e^{-\alpha}$ ,  $d_{ji}$  is the distance between base station  $i$  and  $j$ , and  $\delta$  is the quasi distance introduced in section 3.2.  $N_0$  is noise which is identical for any channel and any WBS. We define the cost function for virtual recourses  $(i, j, c)$  as follows,

$$g_{(i,j,c)}(k) = \begin{cases} \frac{\tilde{f}_{ji}}{2\tilde{P}_i} + \frac{\tilde{f}_{ij}}{2\tilde{P}_j} + \frac{C \cdot N_0}{N \cdot \tilde{P}_i} & \text{if } k = 2 \\ 0 & \text{otherwise} \end{cases} \quad (3.11)$$

As resource  $(i, j, c)$  only lies in the strategy space of player  $i$  and  $j$ , based on 3.11, cost of resource  $(i, j, c)$  is only decided by the number of players(0 or 2) using it, thus this is a typical congestion game which has infinite update property [94].

Substitute Formula 3.11 to Formula 3.10, we get the total cost for user  $i$  under strategy profile  $\sigma$ .

$$\begin{aligned} g^i(\sigma) &= \sum_{\substack{j \in \mathcal{N}, j \neq i, \\ c=c(\sigma_j)=c(\sigma_i)}} (g_{(i,j,c)}(2) + g_{(j,i,c)}(2)) \\ &= \sum_{\substack{j \in \mathcal{N}, j \neq i, \\ c(\sigma_j)=c(\sigma_i)}} \left( \frac{\tilde{f}_{ji}}{\tilde{P}_i} + \frac{\tilde{f}_{ij}}{\tilde{P}_j} + \frac{C \cdot N_0}{N} \left( \frac{1}{\tilde{P}_i} + \frac{1}{\tilde{P}_j} \right) \right) \\ &= \frac{\sum_{\substack{j \in \mathcal{N}, \\ j \neq i, \\ c(\sigma_j)=c(\sigma_i)}} \tilde{f}_{ji}}{\tilde{P}_i} + \sum_{\substack{j \in \mathcal{N}, \\ j \neq i, \\ c(\sigma_j)=c(\sigma_i)}} \frac{\tilde{f}_{ij}}{\tilde{P}_j} + \frac{CN_0}{N} \sum_{\substack{j \in \mathcal{N}, \\ j \neq i, \\ c(\sigma_j)=c(\sigma_i)}} \left( \frac{1}{\tilde{P}_i} + \frac{1}{\tilde{P}_j} \right) \\ &= \frac{\sum_{\substack{j \in \mathcal{N}, j \neq i, \\ c(\sigma_j)=c(\sigma_i)}} \tilde{f}_{ji}}{\tilde{P}_i} + \sum_{\substack{j \in \mathcal{N}, j \neq i, \\ c(\sigma_j)=c(\sigma_i)}} \frac{\tilde{f}_{ij}}{\tilde{P}_j} + \frac{2CN_0}{N} \sum_{\substack{i \in \mathcal{S} \subset \mathcal{N}, \\ \mathcal{S}: \forall i \in \mathcal{S} \\ c(\sigma_i)=c}} \frac{1}{\tilde{P}_i} \end{aligned} \quad (3.12)$$

Let  $\mathcal{S}$  denote the set of WBSs which work on the same channel. Now we try to get the potential over all WBSs, note that the summation of one WBS's congestion is related to its index. For any two WBS  $i, j \in \mathcal{S}$  with  $i < j$ , the potential brought in by  $i$  is 0, while, that caused by  $j$  is in the form of  $g_{(i,j,c)}(2) + g_{(j,i,c)}(2)$ . In other words, for each interfering pair of WBSs, only the WBS with bigger index contributes to the potential. The total potential is,

$$\begin{aligned} G(\sigma) &= \sum_{r \in \mathcal{R}} \sum_{i=1}^{n_r(\sigma)} g_r(i) = \sum_{i \in \mathcal{N}} \sum_{r \in \sigma_i} g_r(n_r^i(\sigma)) \\ &= \sum_{i \in \mathcal{N}} \frac{\sum_{\substack{j \in \mathcal{N}, j \neq i, \\ c(\sigma_j)=c(\sigma_i)}} \tilde{f}_{ji}}{\tilde{P}_i} + \frac{CN_0}{N} \sum_{\substack{\mathcal{S} \subset \mathcal{N}, \\ \forall i \in \mathcal{S}, c(\sigma_i)=c}} |\mathcal{S}| \sum_{i \in \mathcal{S}} \frac{1}{\tilde{P}_i} \end{aligned} \quad (3.13)$$

Question:

When power is variable, is it still a congestion game, or potential game?

When players minimize their utilities (cost or potential) illustrated by Formula 3.12, the total congestion in the secondary network given by Formula 3.13 decreases monotonically before reaching one Nash equilibrium. Players' greedy update in the game to minimize its cost Function 3.12, which ceases finally in pure Nash Equilibrium. The strategy and cost function of players in the game is transplanted as Algorithm 1 and utility Function 3.9 respectively.

### 3.5.3.2 Difference between equilibrium and the aimed variable

Here rises a question, is the final value obtained by Algorithm 1 exactly the same as the expression 3.13 representing a Nash equilibrium? The answer is that there is very little difference if interference is considered. Recall the target objective we want to minimize in Problem 3.4 is,

$$\begin{aligned} \sum_{i \in \mathcal{N}} \frac{\tilde{f}_i}{\tilde{P}_i} &= \sum_{i \in \mathcal{N}} \frac{\sum_{\substack{j \in \mathcal{N}, j \neq i, \\ c(\sigma_j) = c(\sigma_i)}} \tilde{f}_{ji} + N_0}{\tilde{P}_i} \\ &= \sum_{i \in \mathcal{N}} \frac{\sum_{\substack{j \in \mathcal{N}, j \neq i, \\ c(\sigma_j) = c(\sigma_i)}} \tilde{f}_{ji}}{\tilde{P}_i} + \sum_{i \in \mathcal{N}} \left( \frac{N_0}{\tilde{P}_i} \right) \end{aligned} \quad (3.14)$$

Compare Formula 3.14 and 3.13, we find that the difference between the objective value and the final value promised by congestion game is the difference between the last items in Formula 3.14 and 3.13. When channels are evenly distributed, there is  $C/N^* \mid \mathcal{S} \mid \approx 1$ , thus Formula 3.14 and 3.13 are approximately the same, but monotonicity on the decrease of expression 3.14 is not perceived whereas convergence to NE is still guaranteed. When  $N_0 = 0$ , the potential is exactly the same with the object we want to minimize.

From above analysis, we can see the assumption that each WBS only occupies one channel can be easily removed, for example, each WBS can access multiple channels, and we can regard that WBS consists of multiple WBSs (have the same location) and each of which works on one channel. Then the proof on convergence of WhiteCat can be applied directly to this case.

Note that the convergence of the game is independent on the the concrete form of the cost function. The reason we use function 3.12 is the total potential of the game is approximately the same with the total utility of all WBSs in the network, if the the goal of a problem varies and the total utility is different, a distinctive utility for each WBS should be accordingly proposed. Hence, we say that WhiteCat scheme provides a prototype for the problems where the interaction among users are asymmetric: based on a suitable utility involves the welfare of itself and its neighborhood community, the best response approach can converge in a decentralized style.

### 3.5.4 Variable transmission power after channel allocation

After deciding on the working channel, WBSes operate with the maximal permitted transmission power. As the utility defined in Section 3.11 is division of linear function of transmission power and received interference, it is natural to assume that there could exist a

vector of transmission power  $\{p_1, p_2, \dots, p_N\}$  where  $p_i < P_{max}^c, \forall i \in \mathcal{N}$ , and the metric doesn't diverge much from the already achieved metric. But by using the metric as utility, there is no WBS has the motivation to diverge from the power level being used (the maximal permitted power) with other WBSes keep their transmission power the same.

We adopt the function form of utility proposed in [88].

$$u = \frac{E \cdot R}{p} (1 - e^{-0.5 \cdot \gamma})^L$$

This new utility is function of both its own transmission power and quasiSINR, thus one WBS doesn't need relevant information from other WBSes. This function has several attracting properties. It is a monotonically increasing function of  $\gamma$  for a fixed transmission power  $p$ , and it approaches to 0 when  $\gamma$  increases to infinity, and it is a monotonically decreasing of the transmission power  $p$  for a fixed  $\gamma$ . This function goes to 0 when  $p$  goes to either 0 or infinity. The WBSes keeps on minimizing this utility and finally result in NE.

### 3.5.5 Communication overhead of Dicaps in the phase of channel allocation

Channel allocation with different transmission power is NP hard, this is one reason for us to propose distributed algorithm. Dicaps is a distributed scheme but certain information of other WBSes is needed. The centralized base station is piggybacked to provided the needed information. As to a WBS, the number of such inquiries is the number of steps before convergence. The upper bound of total update steps is  $2n^2$ , thus averagely, the upper bound of update steps for each WBS is  $2n$ . We give the proof of this upper bound.

xxxxxx

## 3.6 Joint channel and power allocation

In the section 3.5, the problem is decomposed into sub problems which are solved sequentially, one is solved by linear/convex programming in the data center, the others are solved with distributed schemes. The decomposition of the original problem along with the distributed scheme may yield a result away from the optimal, so in this chapter, we propose centralized scheme which looking for the global optimal results in order to examine the performance of DiCAPS.

### 3.6.1 Centralized optimization

When we consider to optimize the transmission power and channel in the same time, the optimization problem 3.8 is not quadratic any more and becomes mixed integer non-linear problem, for which there is no efficient solution. We reformulate problem 3.8 into a mixed binary quadratic optimization problem with some auxiliary variables created, i.e., binary number  $\alpha$ , real number  $\beta$  and  $q$ , where

$$x_{jk} \cdot x_{ik} = \alpha_{ij}^k \quad (3.15)$$

$$\beta_{ij}^k = p_j^k \cdot \alpha_{ij}^k \quad (3.16)$$

$$\frac{1}{p_i^k} = q_i^k \quad (3.17)$$

Then the optimization problem can be stated as:

$$\begin{aligned} & \text{minimize} \\ & \sum_{i=1}^n \left( \sum_{j \in \mathcal{N}, j \neq i} \sum_k q_i^k \cdot \beta_{ij}^k \cdot h_{ji} \cdot z + \sum_k N_0 \cdot q_i^k \cdot x_{ik} \right) \\ & \text{subject to:} \\ & x_{jk} + x_{ik} - \alpha_{ij}^k \leq 1 \\ & -x_{jk} - x_{ik} + 2 \cdot \alpha_{ij}^k \leq 0 \\ & \beta_{ij}^k - p_j^{k,max} \cdot \alpha_{ij}^k \leq 0 \\ & -\beta_{ij}^k + p_j^{k,min} \cdot \alpha_{ij}^k \leq 0 \\ & \beta_{ij}^k - p_j^k - p_j^{k,min} \cdot \alpha_{ij}^k \leq -p_j^{k,min} \\ & -\beta_{ij}^k + p_j^k + p_j^{k,max} \cdot \alpha_{ij}^k \leq p_j^{k,max} \\ & \sum_{k=1}^{|\mathcal{C}|} x_{ik} = 1, x_{ik} \in \{0, 1\}^{|\mathcal{C}|} \\ & q_i \cdot p_i = 1 \end{aligned} \quad (3.18)$$

The objective function is quadratic, and all the constraints except for the last one are linear. The first two constraints realizes Formula 3.15, the following four constraints realizes Formula 3.16. Due to the quadratic equability constraint  $q_i \cdot p_i = 1$ , the optimization problem is non-convex and only a few solvers are able to solve it by using global searching. One workaround to avoid global searching is to linearise the equality constraint. After linearising constraint  $q_i \cdot p_i = 1$ , the problem becomes mixed integer quadratic problem, and can be solved with Gurobi.

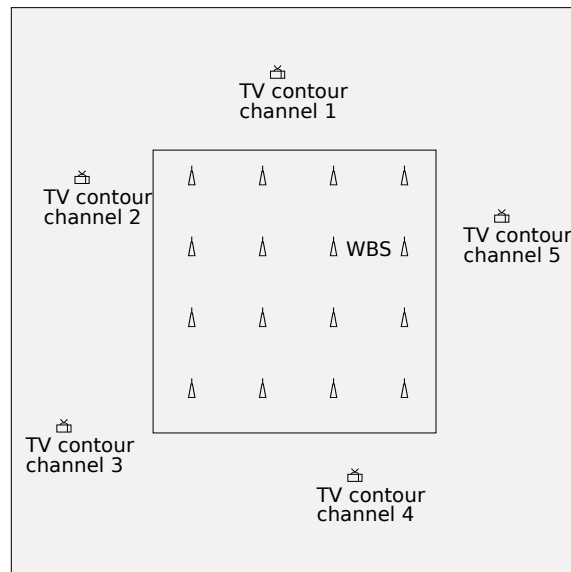
result is not ready.

## 3.7 Performance Evaluation

We compare the performance of WhiteCat, with another two distributed heuristic schemes (Whitespace channel allocation selfish) WhiteCase and no-regret learning, besides, the centralized optimization and a random allocation are used for reference.

- *WhiteCase*: Each WBS selfishly updates its channel to achieve the best (in this paper means the smallest) possible utility based on Formula A.1.
- *No-regret learning*: Each WBS maps the probability of choosing each strategy to a certain proportion of the regret which the WBS may have if it doesn't choose that strategy, and the WBS choose the strategy with the biggest probability. WBSs update such mapping dynamically and this approach converges to correlated equilibrium. Please refer the original paper [42] for details.

A square area which is 60KM x 60KM is divided into 16 minor square blocks evenly, for each block there is one WBS locating in the middle of it. Same amount of end terminals distributed in each minor block, however, they don't necessarily belong the WBS in that minor block, they choose the WBS to join, which caused the strongest received signal strength indicator (RSSI) on it. There is a rim area with width of 30Km around the square area, where TV contours are randomly located. The TV station which protected by TV contour working only on one channel. The location of WBSs and TV contours are illustrated in Figure ???. The other parameters are listed in the table 3.1.



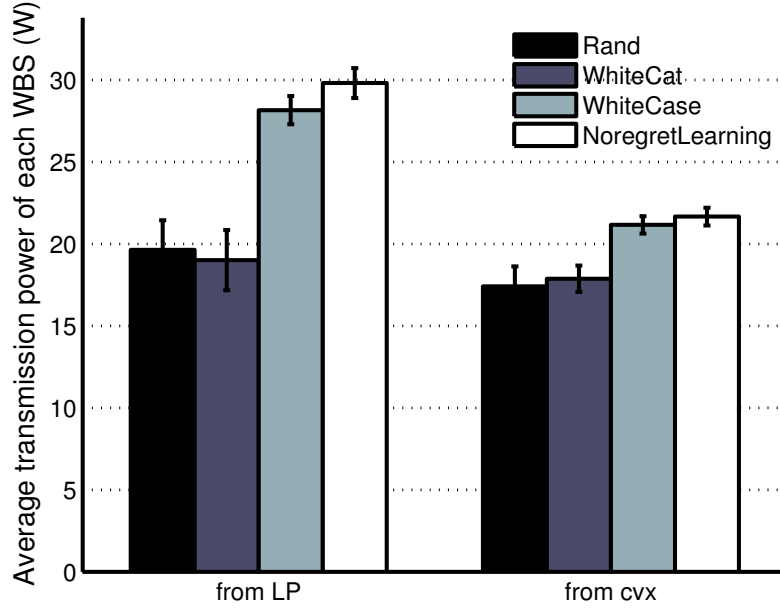
**Figure 3.4** Layout of WBSs and TV contours

Number of channels	5
Number of WBSs	16
Noise	$10^{-12}W$
length of the square to locate WBSs	60Km
Distance between quasai terminal and WBS	7KM
Interference threshold on TV contour	$10^{-7}W$
Path loss factor	2
Standard deviation in flat shadowing	8
Minimal WBS transmission power	4W
Maximal WBS transmission power	40W
Number of end terminals in network	800

**Table 3.1**

### 3.7.1 Performance of maximal permitted power decision and the channel allocation schemes

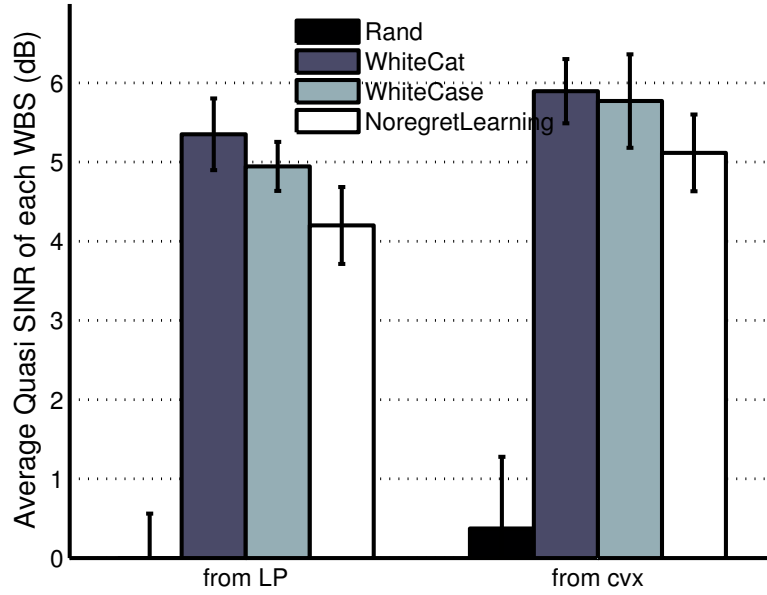
Respectively with the power map obtained from linear programming and convex programming, we execute channel allocation problems. Note that in each run, all the 5 schemes compared here run with the exact the same simulating parameters. add the performance from LP. this is comparison among 1. power map decisions, 2.channel allocation schemes



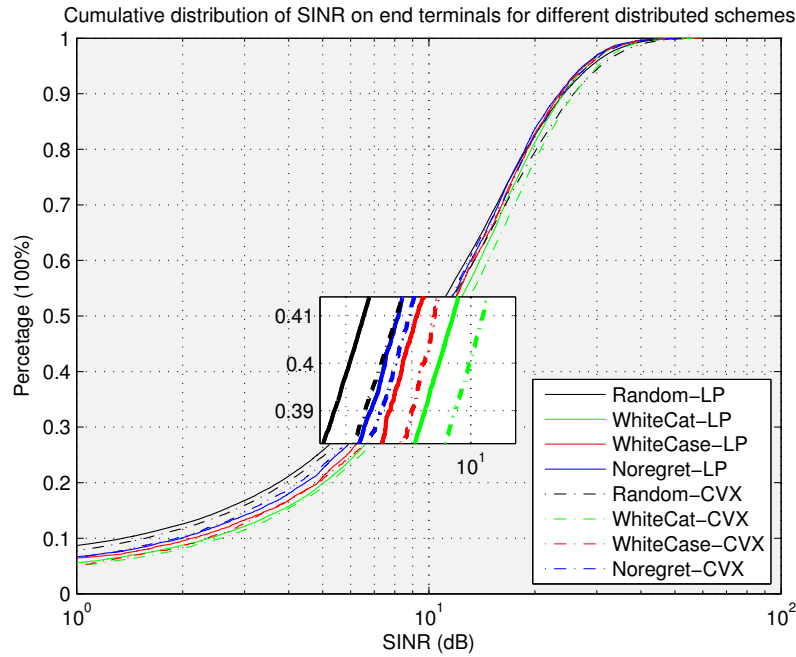
**Figure 3.5** Power consumed by different distributed spectrum allocation schemes under different ways deciding the maximal transmission power map

#### 3.7.1.1 comparison among 1. power map decisions

We simulate the 4 distributed spectrum allocation schemes with the maximal permitted transmission power map obtained from convex programming and linear programming respectively, and then tell which maximal power map generation outperforms based on the performances of the 4 spectrum allocation schemes. We run simulations for 100 times, the WBSs' location is fixed in each run whereas the location of TV contours, end terminals and the sequence for WBS to update are randomly decided. Figure 3.5 and 3.6 show that all the four distributed spectrum allocation schemes consume less transmission power consumption by 15% to 30% and achieve better QuasiSINR when convex programming is applied to decide the maximal power map. The cumulative distribution function curve of SINR on end terminals is drawn in Figure 3.7, where the x axis represents SINR level, and the y axis shows the cumulative proportion of end terminals whose SINR equals or smaller than that level. The curves show that except for the random method, all three other distributed schemes perform better in low SINR area ( $\text{SINR} < 10\text{dB}$ ) with convex programming, while worse in the high SINR area. Hence we adopt convex programming to decide the maximal transmission power in the following simulation.



**Figure 3.6** QuasiSINR achieved by different distributed spectrum allocation schemes under different ways deciding the maximal transmission power map

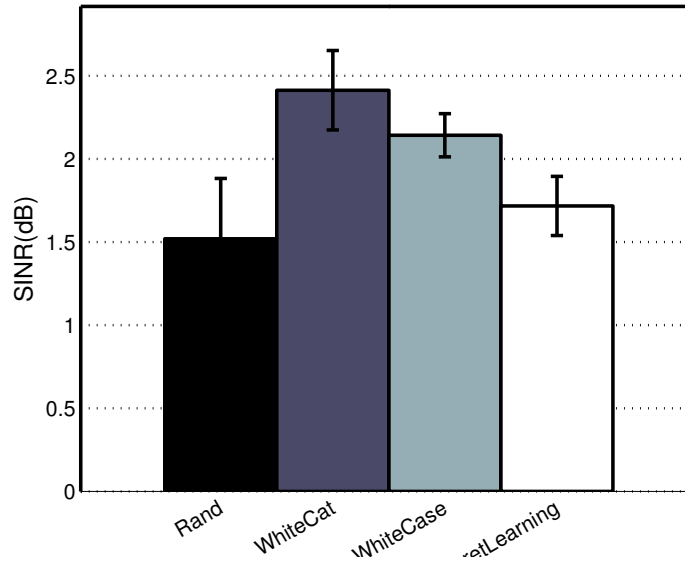


**Figure 3.7** CDF of SINR on end users obtained by different CA schemes under different methods to decide the maximal transmission power map

### 3.7.1.2 comparison among 2.channel allocation schemes

After deciding the maximal permitted transmission power on each channel for each WBS, the data center distributes this maximal power map to all WBSes, and trigger the procedure of distributed channel allocation.





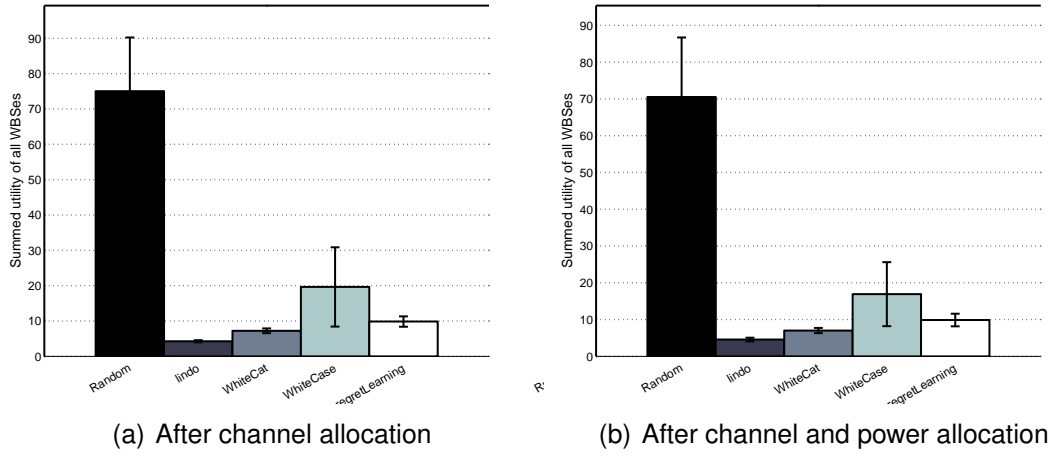
**Figure 3.8** The average SINR of the 20% worst end terminals

The performance of the four spectrum allocation approaches working with the maximal power map calculated from convex programming is elucidated in the right part of both Figure 3.5 and 3.6. We can see that WhiteCat consumes 12% less transmission power than WhiteCase and No-regret learning schemes, whereas better QuasiSINR is obtained. The cumulative distribution function curve of SINR on end terminals with convex programming is presented in Figure 3.7 with dash lines, we can see that for any cumulative proportion under 90%, the corresponding SINR level from Whitecat on end terminals is slightly (around 0.5-1 dB) but stably higher than that obtained by WhiteCase and No-regret schemes, and 3 dB higher than that in random scheme.

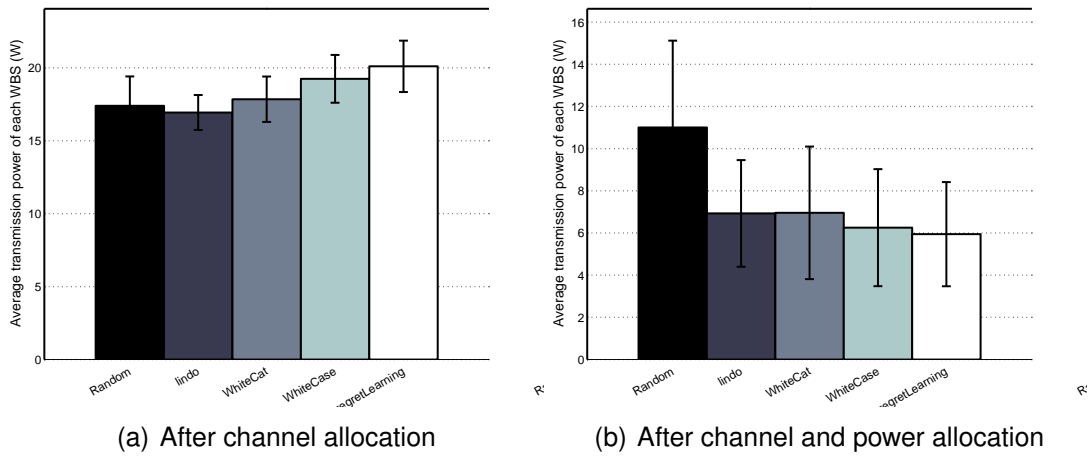
In each run of simulation, average value of the 20 % end terminals with the worst SINR is recorded, and the averaged such value over 100 simulations is illustrated in Figure 3.8 which shows WhiteCat achieves better performance for the worst suffered end terminals than WhiteCase and No-regret approaches.

### 3.7.2 The performance power allocation on the basis of channel allocation

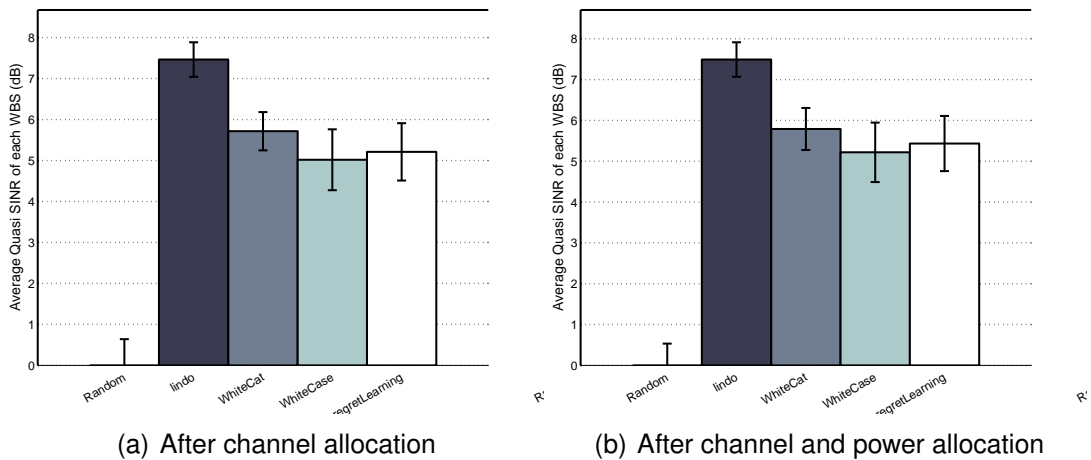
Power adjustment is conducted after channel allocation is completed. Distributed channel allocation schemes, along with the power adjustment, are compared with two other schemes. One is centralized optimization shown in section ??, which is used as upper bound. The other is the scheme proposed in xxx which is introduced in section ??, which is distributed joint power and channel allocation scheme. As we have discussed, this scheme doesn't aim to improve the SINR on end terminals, but on the sum of produced and received interferences. The performance evaluation is shown in the first subfigure in Figure 3.9, 3.10 and 3.11. Figure 3.9(a) shows the gap of utility between the centralized optimization (lindo) with other decentralized schemes. Figure 3.10(a) shows whiteCat and centralized scheme consume the least power.



**Figure 3.9** summed utility of all WBSes, which is the objective in problem  $P_1$

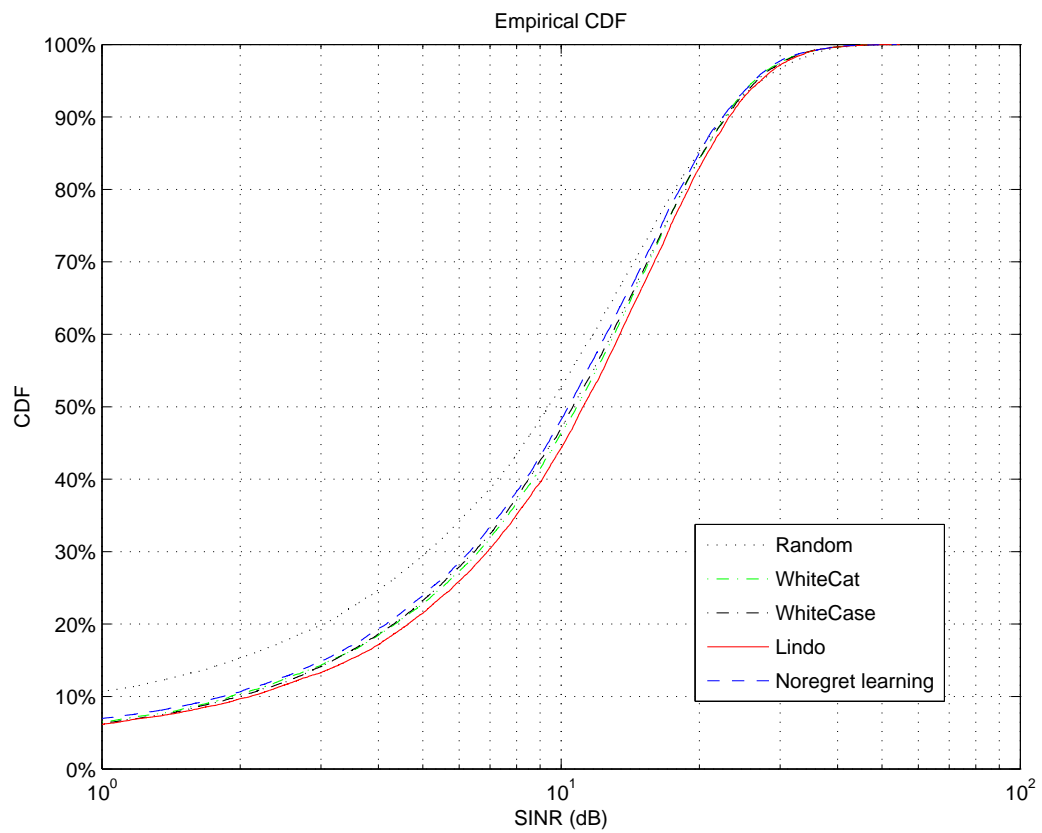
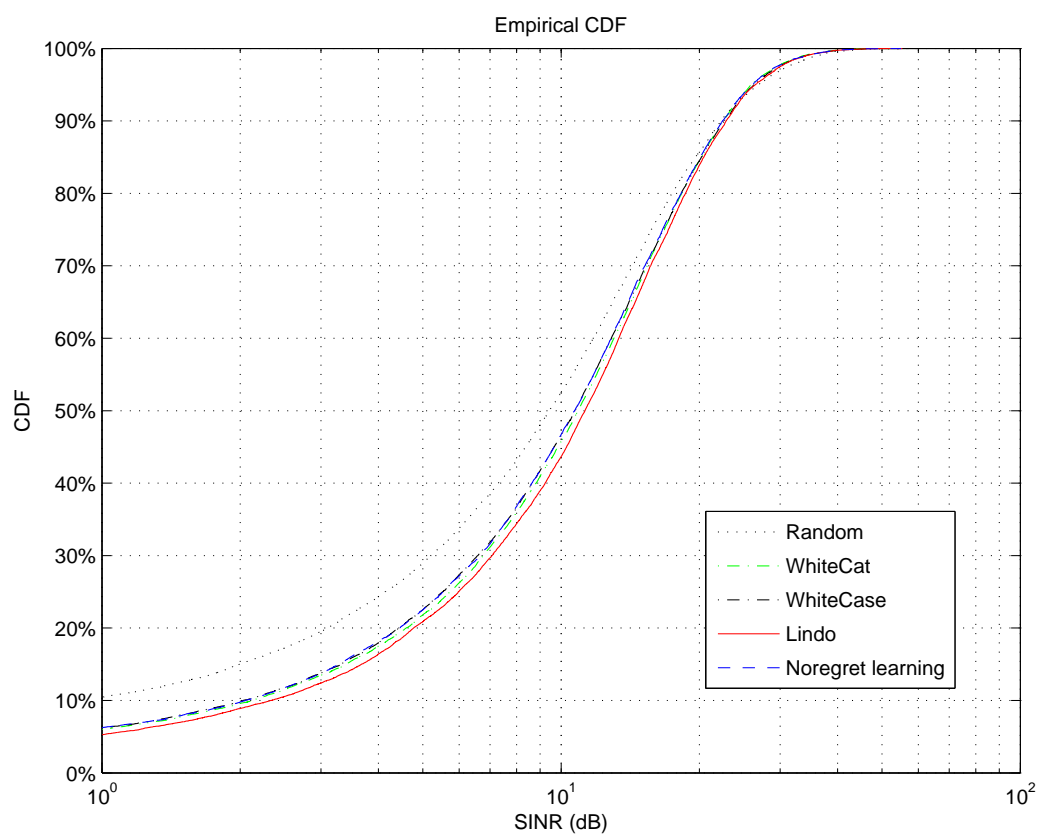


**Figure 3.10** Average transmission power of one WBSes



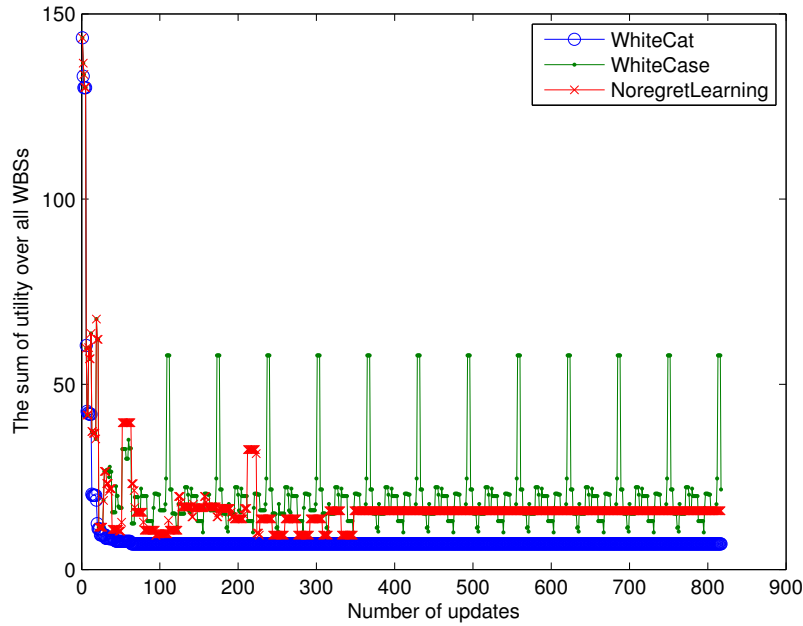
**Figure 3.11** quasiSINR: SINR at the reference point

Compare the two figures in Figure 3.9, 3.10, 3.11, we can see that transmission power is reduced by 50% to 70% for all schemes except for the random selection scheme, and the utility and quasiSINR are almost the same.

**Figure 3.12** SINR on end users after channel allocation**Figure 3.13** SINR on end users after channel and power allocation

### 3.7.3 Analysis on convergence process

In the congestion game, each player has at most  $(n - 1) * |\mathcal{C}|$  resources available for usage, so there is no polynomial steps converging to NE, while, simulation shows the algorithm can quickly converge to NE when the number of WBS is up to 100. Figure 3.14 depicts one instance of simulation, where WhiteCat converges quickly, No-regret produces oscillation but converges finally, while WhiteCase can not converge thus has to be enforced stop after 16000 updates.



**Figure 3.14** Convergence with three different schemes in one simulation instance

We also compare the convergence speed between WhiteCat with no-regret scheme. We fix 16 WBSs' location working with 4 channels, whereas the location of TV contours and end terminals are randomly decided. We account each WBS accessing the base station (refer to 3.5.2) as *one step*. We record the number steps before convergence. Table 3.2 illustrated the average number of steps needed for convergence in 100 runs of simulations. As there is no guarantee for WhiteCase to converge, we stop the channel allocation process after 16000 steps (1000 rounds). We can see WhiteCat is 20 times faster than no-regret, and the relatively small confidence interval shows that WhiteCat's convergence is not affected obviously by different network conditions, which is reasonable as more knowledge of the network is known by users executing Whitecat. As to average running time for each convergence with Matlab, Whitecat is much smaller than the other two schemes, as the nonlinear solver LINDO to be discussed in next subsection, the running time is about 40 minutes. Figure 3.14 reflects one instance of the convergence of three schemes in one run of simulation. Notice that there is a slight rise when the value on the X-axis is 35, which comes from the difference between 3.14 and 3.13.

Scheme	average #steps	95% CI	average time
Whitecat	58	5.6	2s
Whitecase	4587	2742	50s
No-regret	1916	1541	144s

**Table 3.2**

### 3.7.4 Stability of SINR in the process of channel allocation

WBS provides service to end users in the process of channel allocation. A certain SINR corresponds to certain transmission configurations like modulation type and data rate. Oscillation of SINR may cause reconfiguration, reduced throughput or delay variance, thus is not preferred. We propose a metric *Cost of Oscillation* (COS) to represent the stability of SINR in the converging process. We assume each update step takes the same amount of time which is 1 time unit, the variance of SINR on end user  $i$  at time point  $t + 1$  compared with that at time  $t$  is  $\Delta\gamma_i(t + 1) = \left| \frac{\gamma_i(t+1) - \gamma_i(t)}{\gamma_i(t)} \right|$ . The COS value for one network applied with a certain channel allocation scheme is,

$$COS = \sum_{t=1}^T \sum_{i \in \mathcal{N}} \Delta\gamma_i(t) \quad (3.19)$$

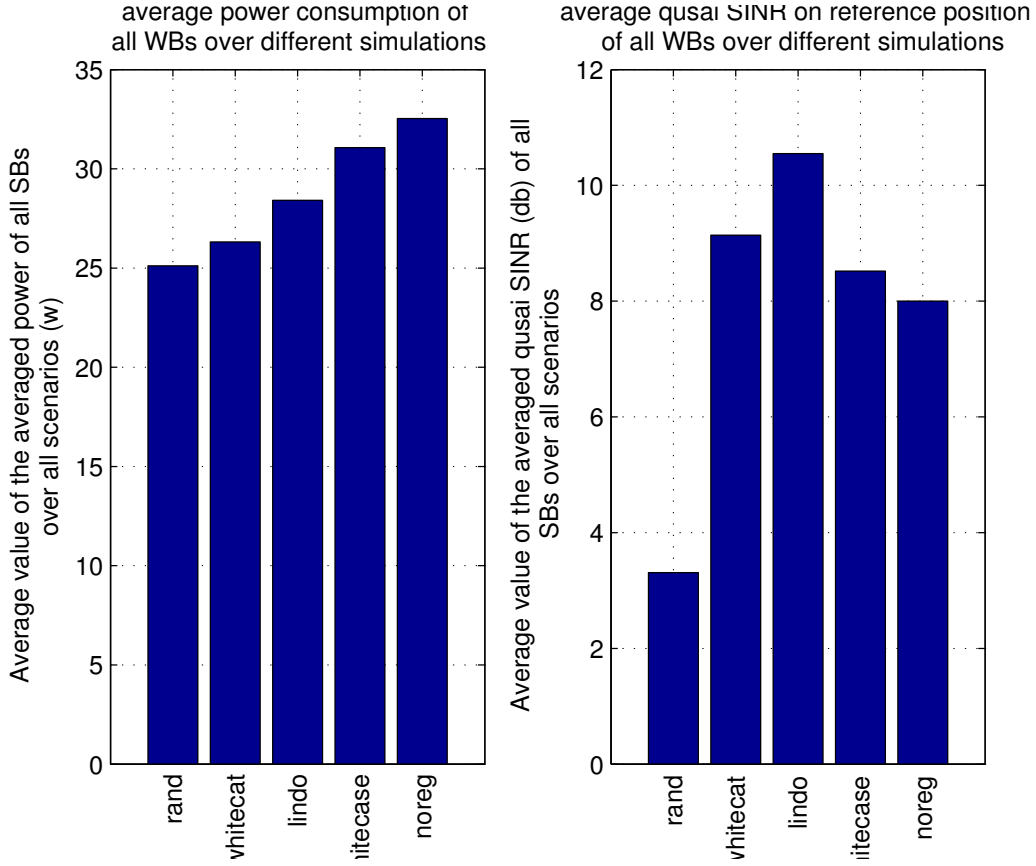
$\gamma_i(0)$  is the SINR for  $i$  before starting channel allocation. The variance of SINR in channel allocation process is shown in table 3.3 from which we can see WhiteCat achieves only 6% of oscillation on SINR compared with No-regret approach.

Scheme	COS	95% Confidence interval
Whitecat	8850	2984
Whitecase	246790	168050
No-regret	145460	1541

**Table 3.3**

### 3.7.5 comparison between distributed and centralized scheme

After comparing the performances of WhiteCat with the other two heuristic solutions, we have a look at the difference between these distributed approaches with the centralized optimization method. For these heuristic schemes, the sequence to update influences the final performance, while, it is very difficult to find out the optimal sequence which achieve the best performance, for our simulation configuration, the number of different sequence for 16 WBSs is  $16!$  which has order of magnitude of 14. For demonstration purpose, we choose 100 different update sequences randomly for 100 times of simulation. In each simulation the sequence of WBS to update their channels is randomly decided be identical for all the 4 schemes. As solution of optimization has nothing to do with sequence, we only solve the optimization problem for once. We fixed the location of WBSs and PU contours, only leave the end terminals randomly scattered in the inner square area in each simulation.



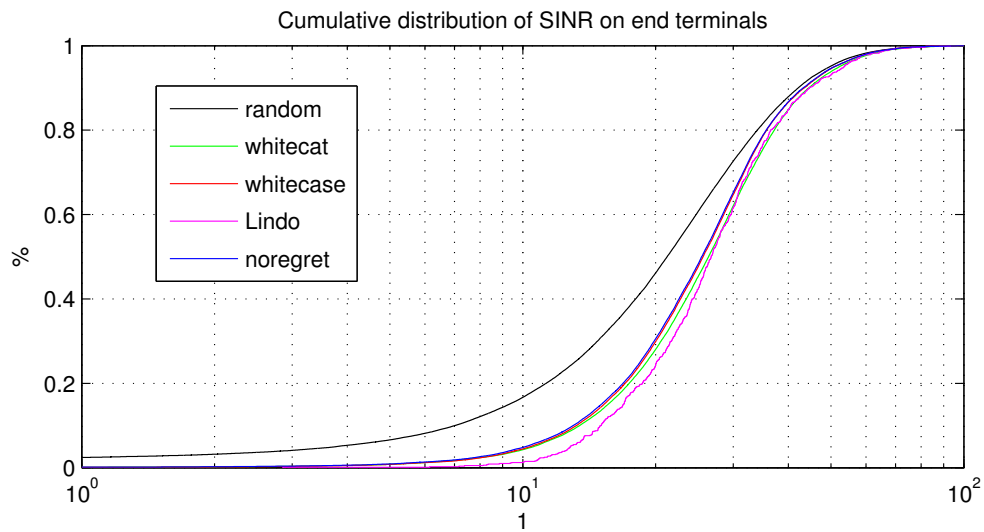
**Figure 3.15** Average Power consumption and QuasiSINR

Figure 3.15 shows the average power consumption and average QuasiSINR over all WBSs and rounds of simulations. WhiteCat consumes the least of power except for the random scheme. while, Lindo outperform others

Figure 3.16 demonstrates the cumulative distribution of SINR on all end terminals, where the centralized optimization achieves 3 dB better SINR on end terminals than distributed schemes, which means there is still big space to improve the performance of decentralized approaches.

### 3.8 Conclusion

We propose a method to assign maximum transmission power to secondary users to make full use of the white TV spectrum. The second contribution of the paper is the design of a distributed channel assignment scheme called WhiteCat which is designed for secondary users to decide which chunk of spectrum should be used in order to improve cell performance in the down-link transmission direction. WhiteCat provides end terminals better SINR with less transmission power, and converges to one pure Nash equilibrium in a faster speed compared with two other schemes (greedy best response as well as a no-regret learning scheme). WhiteCat is formulated into a standard congestion game which proves the convergence of the scheme. WhiteCat requires a central data base containing information about the previously allocated channels to secondary users as well as their positions and propagation information among the base stations. Compared to previous work that suggests the use of a central data base for base station registration and channel



**Figure 3.16** Cumulative distribution of SINR on all end terminals when applying different schemes

validation, this is a minor overhead to be introduced. For future work we will address the problem of allowing base stations to set the transmit power arbitrarily within the maximum transmit power limit.





# A

## Proof of Theorem 3.5.1

For selfish best response approach, the utility function is set as follows,

$$u_i = \frac{\sum_{c(i)=c(i)} \tilde{f}_{ji} + N_0}{P_i \cdot h_{ii}} \quad (\text{A.1})$$

*Proof.* In order to simplify the proof, we assume  $N_0 = 0$ . Consider one WBS  $i$  executing algorithm 1 with utility A.1, and updates its channel from  $c_i$  to  $c'_i$ , we denote  $u'_k, k \in \mathcal{N}$  as the utility of WBS  $k$  when  $i$  chooses channel  $c'_i$ , accordingly, the summation of utilities of all WBSs after  $i$  changing to  $c'_i$  is  $U' = \sum_{\forall k \in \mathcal{N}, c(i)=c'_i} u'_k$ .

$$\begin{aligned} U' &= u'_i + \sum_{j \in \mathcal{N}, j \neq i} u'_j \\ &= u'_i + \sum_{j \in \mathcal{N}, j \neq i} (u_j + (u'_j - u_j)) \\ &= u'_i + \sum_{j \in \mathcal{N}, j \neq i} u_j + \sum_{j \in \mathcal{N}, j \neq i} (u'_j - u_j) \\ &= u'_i + \sum_{j \in \mathcal{N}, j \neq i} u_j + \sum_{\substack{j \in \mathcal{N}, \\ j \neq i, \\ c(j)=c'_i}} (u'_j - u_j) + \sum_{\substack{j \in \mathcal{N}, \\ j \neq i, \\ c(j)=c_i}} (u'_j - u_j) \\ &\quad + \sum_{\substack{j \in \mathcal{N}, j \neq i, \\ c(j) \neq c'_i, c(j) \neq c_i}} (u'_j - u_j) \\ &= u'_i + \sum_{j \in \mathcal{N}, j \neq i} u_j + \sum_{\substack{j \in \mathcal{N}, \\ j \neq i, \\ c(j)=c'_i}} \left( \frac{\tilde{f}_{ij}}{\tilde{P}_j} \right) - \sum_{\substack{j \in \mathcal{N}, \\ j \neq i, \\ c(j)=c_i}} \left( \frac{\tilde{f}_{ij}}{\tilde{P}_j} \right) \end{aligned} \quad (\text{A.2})$$

where,

$$\begin{aligned} u'_i &= u_i + \Delta u_i(c_i \rightarrow c'_i) \\ &= u_i + \sum_{\substack{j \in \mathcal{N}, \\ j \neq i, \\ c(j)=c'_i}} \left( \frac{\tilde{f}_{ji}}{\tilde{P}_i} \right) - \sum_{\substack{j \in \mathcal{N}, \\ j \neq i, \\ c(j)=c_i}} \left( \frac{\tilde{f}_{ji}}{\tilde{P}_i} \right) \end{aligned} \quad (\text{A.3})$$

bring A.3 into A.2, we get,

$$\begin{aligned} U' &= U + \sum_{\substack{j \in \mathcal{N}, \\ j \neq i, \\ c(j)=c'_i}} \left( \frac{\tilde{f}_{ji}}{\tilde{P}_i} \right) - \sum_{\substack{j \in \mathcal{N}, \\ j \neq i, \\ c(j)=c_i}} \left( \frac{\tilde{f}_{ji}}{\tilde{P}_i} \right) \\ &\quad + \sum_{\substack{j \in \mathcal{N}, \\ j \neq i, \\ c(j)=c'_i}} \left( \frac{\tilde{f}_{ij}}{\tilde{P}_j} \right) - \sum_{\substack{j \in \mathcal{N}, \\ j \neq i, \\ c(j)=c_i}} \left( \frac{\tilde{f}_{ij}}{\tilde{P}_j} \right) \end{aligned} \quad (\text{A.4})$$

According to algorithm 1, the summation of second and third items, which is the variance of  $i$ ' utility, is negative. If we can confirm the summation of fourth of the last four items is negative, the whole utility of the network decreases with  $i$ ' each update. For simplification, we assume that the channel is symmetric, which means,  $h_{ij} = h_{ji}$ , and  $z$  is identical among all WBSs. Then, the problem we want to confirm is equivalent to the following: Given the in-equation with  $n, m$  are natural numbers

$$\sum_{i=1}^m \alpha_i < \sum_{i=1}^n \beta_i, \quad (\text{A.5})$$

Prove the following in-equation is correct or not,

$$\sum_{i=1}^m \left( \alpha_i + \frac{1}{\alpha_i} \right) < \sum_{i=1}^n \left( \beta_i + \frac{1}{\beta_i} \right), \quad (\text{A.6})$$

We propose a small contradiction to prove A.6 is not true. When  $m = 2, n = 1$ , and  $\alpha_1 = 1, \alpha_2 = 0.5, \beta = 2.1$ , we can see that although  $\sum_{i=1}^m \alpha_i = 1.5 < \sum_{i=1}^n \beta_i = 2.1$ , there is  $\sum_{i=1}^m \left( \alpha_i + \frac{1}{\alpha_i} \right) = 4.5 > \sum_{i=1}^n \left( \beta_i + \frac{1}{\beta_i} \right) = 2.58$ . hence, with WBS's update, it is possible that  $U' > U$ , thus there is no monotonically convergence by utilizing A.1.  $\square$

Notice that the last four items in A.4 is exactly the change of summation of utilities of all WBSs after  $i$ ' update if WhiteCat is executed, hence the monotonic convergence of WhiteCat is proved here analytically if noise is considered to be zero. If noise is considered, we can follow the conclusion in the end of 3.5.3.1 that WhiteCat converges without monotonicity.

# B

## Deviation of Problem 3.7

We reformulate the objective problem 3.7 which is a binary non-linear programming to binary quadratic programming as follows,

$$\begin{aligned}
 & \sum_{i=1}^n \frac{\sum_{j \in \mathcal{N}, j \neq i} P^T X_j (X_j^T X_i) h_{ji} z + N_0}{P^T X_i} \\
 &= \sum_{i=1}^n \left( \frac{\sum_{j \in \mathcal{N}, j \neq i} \sum_k (P_{jk} \cdot x_{jk} \cdot x_{ik} \cdot h_{ji} \cdot z) + \sum_k N_0 \cdot x_{ik}}{P^T X_i} \right) \\
 &= \sum_{i=1}^n \left( \frac{\sum_{j \in \mathcal{N}, j \neq i} \sum_k (P_{jk} \cdot x_{jk} \cdot x_{ik} \cdot h_{ji} \cdot z)}{P^T X_i} + \frac{\sum_k N_0 \cdot x_{ik}}{P^T X_i} \right) \\
 &= \sum_{i=1}^n \left( \sum_{j \in \mathcal{N}, j \neq i} \sum_k \frac{(P_{jk} \cdot x_{jk} \cdot x_{ik} \cdot h_{ji} \cdot z)}{P^T X_i} + \sum_k \frac{N_0 \cdot x_{ik}}{P^T X_i} \right)
 \end{aligned} \tag{B.1}$$

we now simplify the first item in the parenthesis. If we assume secondary base station  $i$  is working on channel  $m$ , then there is  $x_{im} = 1$ , then

$$\begin{aligned}
 \frac{P_{jk} \cdot x_{jk} \cdot x_{ik} \cdot h_{ji} \cdot z}{P^T X_i} &= \frac{P_{jk} \cdot x_{jk} \cdot x_{im} \cdot h_{ji} \cdot z}{P_{im} \cdot x_{im}} \\
 &= \frac{P_{jk} \cdot x_{jk} \cdot h_{ji} \cdot z}{P_{im}}
 \end{aligned} \tag{B.2}$$

other wise, formula B.2 equals to 0.

Similarly, for the second item in the bracket,

$$\frac{N_0 \cdot x_{ik}}{P^T X_i} = \frac{N_0}{P_{ik}} \cdot x_{ik} \tag{B.3}$$

then, formula B.1 becomes,

$$\sum_{i=1}^n \left( \sum_{j \in \mathcal{N}, j \neq i} \sum_k \frac{P_{jk}}{P_{ik}} \cdot h_{ji} \cdot z \cdot x_{jk} \cdot x_{ik} + \sum_k \frac{N_0}{P_{ik}} \cdot x_{ik} \right) \quad (\text{B.4})$$

which is a binary quadratic programming problem.

# 4

## Robust Clustering of Ad-hoc Cognitive Radio Networks

### 4.1 Introduction

Cognitive radio (CR) is a promising technology to solve the spectrum scarcity problem [65]. In CR systems, primary users access their allocated spectrum band whenever there is information to be transmitted. In contrast, CR users (forming cognitive radio networks, abbreviated as CRN) can only access primary channels after validating the channel is idle. This refers to the process of sensing a particular channel and verifying (with a previously specified probability of error) that it is not used by a primary user currently. This form of spectrum sharing is also referred to as opportunistic spectrum access.

Clustering algorithms have been proposed in the literature for ad-hoc network [50, 58, 23] and sensor networks [11]. In ad-hoc networks, the major focus of clustering is to preserve connectivity (under static channel conditions) or to improve routing. In the context of sensor networks, the emphasis of clustering has been on longevity and coverage.

In cognitive radio network, due to attenuation of signal propagation, primary users can only be detected by CR users when they locate closely to CR users. As a result, CR nodes which locate closely with each other are possibly affected by the same group of primary users, so that the availability of licensed spectrum is similar to them, i.e., certain channels are available on each of them. The similarity of available spectrum on a group of neighbouring CR nodes, along with the benefit of collaborative decision among multiple nodes, leads to clustering as a effective approach for many applications.

For instance, clustering is regarded as an effective method used in cooperative spectrum sensing [91, 108]. Collaborative sensing relies on the consensus of CR users within certain area, and decreases considerably the false sensing reports caused by fading and shadowing of reporting channel. Clustering is also efficient to let all CR users<sup>1</sup> within the

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<sup>1</sup>User and node are used interchangeably in this paper

same cluster stop payload transmission on the operating channel and initiate the sensing process, so that the all the CR nodes within the one cluster are able to vacate the channel swiftly when primary users are detected by at least one CR node residing in the cluster [97]. With cluster structure, the possibility that one CR node interferes neighbouring clusters after vacating the channel due to primary node appearance is reduced [78], as it can be notified by cluster head or other cluster members about the possible collision. Clustering algorithm has also proposed to support routing in cognitive ad-hoc networks [11].

Except for the advantages brought in by clustering, there is a issue on clustering structure itself in cognitive radio network. As the activity of primary users is controlled by licensed operators and generally not known to CR users, the connectivity between CR nodes in a CRN is not guaranteed. For a pair of communicating CR nodes, whenever a primary user is detected to be operating on the working channel, CR nodes have to retreat that working channel. The affected CR nodes switch to one other idle channel if there are available idle channels, if not, the communication is cut down. When coexisting with primary users, the ability for one pair of CR nodes to maintain communication with licensed channels is totally decided by primary users' activity. Thus robustness of connection with licensed channels demonstrates to be objective from the perspective of secondary users. To maintain one cluster operating with licensed channels, at least one common channel is available for all members in that cluster. Thus the number of available common channels in the cluster indicates robustness of it when facing uncontrolled influence from primary users. It is not difficult to see that forming clusters with different neighbours leads to different amount of common channels in the cluster. As a result, how to form the clusters takes an important role on the robustness of clusters in CRN.

To solely pursue connectivity robustness against the primary users' activity, i.e., to maintain more common channels within clusters, the best clustering strategy is ironically that each node constitutes one single node clusters. Apparently this contradicts our motivation of proposing cluster in cognitive radio network. Hence, expected cluster size should be required for the formed clusters. In this thesis, our goal is to propose a clustering approach which produces clusters with more common channels, and meanwhile they satisfy the requirement on cluster size.

In this chapter, we propose ROSS, a distributed clustering algorithm which integrates most CR nodes into clusters and produces robust clusters against primary users' activity, besides, cluster size control is also given consideration. Compared to previous work, ROSS involves much less control messages, and the generated clusters are significantly more robust. In ROSS, cluster head is selected through coordination within its neighborhood, and then cluster membership is decided locally and its convergence is proved under game theoretic framework. On the basis of ROSS, we propose ROSS-DFA which is a light weighted version of ROSS, which requires exchanging less overheads. Throughout this chapter, we refer both ROSS-DGA and ROSS-DFA, along with these added size control feature, as *variants of ROSS*.

The rest of paper is organized as follows. After reviewing related work in section 4.2, we present our system model in Section 4.3. Then we introduce our clustering scheme ROSS and its variants in section 4.4. Centralized scheme is given discussion in section 4.5. Performance evaluation is in section 4.6. Finally, we conclude our work and point out direction future research in section 4.7.

## 4.2 Related Work

Prior to the emergence of open spectrum access, clustering is proposed in ad hoc network or mesh network [11]. Overhead generated by clustering in ad hoc network is analysed in [90, 100].

As to cognitive radio network, there are some clustering strategies aiming at different purposes proposed. [48] proposes clustering strategy in cognitive radio network, which looks into the relationship between cluster size and power consumption and accordingly controlling the cluster size to decrease power consumption. [98] targets on the QoS poisoning and energy efficiency. This approach first decides on the relay nodes which minimize transmission power consumption, then the chosen nodes become cluster heads and clusters are formed in a dynamic coalition process. These two schemes emphasis on power efficiency and don't take into account the channel availability and the issue of robustness of the formed clusters. Cogmesh is proposed in [29] to construct clusters by the neighbour nodes which share local common channels, and by interacting with neighbour clusters, a mesh network in the context of open spectrum sharing is formed. Robustness issue is not considered by this clustering approach. In [108], the channel available to the largest set of one-hop neighbours is selected as common channel which yields a partition of the CRN into clusters. This approach minimizes the set of distinct frequency bands (and hence, the set of clusters) used as common channels within the CRN. However, bigger cluster sizes generally lead to less options within one cluster to switch to if the common channel is reclaimed by a primary node. Hence, this scheme does not provide robustness to formed clusters. Scheme SOC proposed in [55] forms clusters by focusing on strengthening robustness of clusters. The authors consider the balance between the number of idle common channels within cluster and cluster size and propose an algorithm that increases the number of common channels within clusters. One drawback of this scheme is, in order to increase the number of common channels within clusters, the scheme excludes certain CR nodes from the formed clusters, so that isolated nodes have to form clusters themselves. This leads to a high variance on the size of clusters.

## 4.3 System Model

Let us consider an area in which a certain licensed spectrum band is shared by primary and CR users. One control channel<sup>2</sup> is available for the CR nodes to exchange control messages in the process of cluster formation. The licensed spectrum is divided into  $|P|$  non-overlapping spectrum bands (we call them channels). When licensed channels are available to use between two CR nodes in the same time, payload communication can be conducted on one or multiple licensed channels. There are  $|J|$  primary users in the area and  $|I|$  CR users. While primary users are assumed to be fixed, CR users can be mobile. Spectrum sharing is implemented by the opportunistic access paradigm. Hence, primary users access their allocated channels whenever they need without any explicit notification to CR users. We assume that primary users have a relatively low variation in activity (periods of activity and inactivity in the range of seconds or minutes). In contrast, CR users are only allowed to access channels after validating these to be unoccupied by

<sup>2</sup>for example, ISM band or other reserved channels which are exclusively used for transmitting control messages

primary users. Validation refers to the process of ensuring that no primary transmission is actually taking place on the respective channel. This is achieved by spectrum sensing by which the CR users validate channels with a certain probability of detection as well as with a certain periodicity, i.e., every  $T_{\text{sense}}$  time the currently used channels need to be validated again. Denote the spectrum sensing result of each CR user  $i$  by  $V_i = \{v_1, v_2, \dots, v_{p_i}\}$  with  $p_i = |V_i| \leq P$  indicating the total number of available channels for CR user  $i$ . If active, primary and CR users both have a certain transmission range. Any user outside this transmission range can not receive data from the transmitter (i.e., any CR user outside this range can not detect the primary user that transmits). Therefore, different CR users have different views on the occupancy of the spectrum (apart from the fact that there might be false negatives in the sensing process), i.e.,  $V_i \neq V_j$ , for  $i \neq j$ . In the following, we do not consider the primary users further and focus on the operation of cognitive radio network (CRN). All  $|I|$  CR users form an Ad-hoc network in which data is to be transmitted potentially from any node to any other node. Communication on licensed channels is possible only when nodes  $i, j$  is both located in each other's transmission range and both share a validated licensed channel.

Due to the assumed 0/1 nature of connectivity and primary user interference, the CRN working solely with licensed channels can be represented by a connectivity graph  $\mathcal{G}(I, \mathcal{E})$ , where  $\mathcal{E} = \{(i, j, v) | i, j \in I \wedge v \in V_i \wedge v \in V_j\}$  is wireless link between any CR node  $i$  and its neighbour  $j$  with licensed channel  $v$ . Due to relatively low primary user dynamics, time index is omitted here.

For CR node  $i$  in CRN, its neighborhood  $Nb_i$  consists of all the CR nodes locating within its transmission range (links are assumed to be reciprocal) and have at least one common channel with node  $i$  each, i.e.  $j \in Nb_i \Rightarrow V_i \cap V_j \neq \emptyset$ . CR nodes exchange their spectrum sensing results  $V_i$  over the control channel, and neighborhood establishment and maintenance are done with the control channel and according to a neighborhood discovery protocol which is out of scope of our work. In the rest of the paper, the word *channel* only refers to the licensed spectrum.

A cluster  $C$  is composed with cluster head and cluster members, which satisfies the following conditions:

- Cluster head  $H_C$  is able to communicate with any cluster member directly, i.e., for any cluster member  $i \in C$ , there is  $i \in Nb_{H_C}$
- There exist at least one common channel for the cluster, i.e.,  $\cap_{i \in C} V_i \neq \emptyset$

Cluster head coordinates the activities of cluster members, i.e., notifies all the members to evade a channel when the channel is sensed by one cluster member to be occupied by primary users, or notify the members to use a different channel for payload communication. Cluster is denoted as  $C_i$  when its cluster head is  $i$ . We refer to the common channels within a cluster  $C$  by the term *inner common channels* (ICC) and denote this set of channels by set  $K_C$ .  $K_C = \cap_{i \in C} V_i$ , and  $k_C = |K_C|$  is the number of common channels for cluster  $C$ . As the CR users are potentially mobile, clustering is performed with some periodicity, but obviously not more often than spectrum sensing.



Symbol	Description
$N, J$	set of CR and primary nodes in the scenario
$P$	set of non-overlapping channels in the scenario
$Nb_i$	node $i$ 's neighborhood
$C$	a cluster
$V_i$	set of available channels on CR node $i$
$V_C$	set of available channels for cluster $C$
$\phi_i$	the number of available channels for cluster $i$ note it is different than $ V_i $
$C_i$	a cluster whose cluster head is $i$
$H_C$	cluster head of a cluster $C$
$\delta$	desired cluster size
$S_i$	set of claiming clusters, each of which includes debatable node $i$ after phase I
$K_{C_i}$	set of common channels within cluster $C_i$
$k_{C_i}$	number of common channels of cluster $C_i$

**Table 4.1** Notations

## 4.4 Distributed Coordination Framework: Clustering Algorithm

Despite this fact, as some features brought by clustering structure are valued as said in introduction section, the clustering scheme which groups certain CR nodes together and meanwhile produces robust connectivity will be proposed.

In this section, we present the new clustering scheme named ROSS (RObust Spectrum Sharing). It is based on the local sensing results  $V_i$  of all CR users  $i$  and utilizes local similarity of the available channels to form clusters. ROSS consists of two phases: *cluster formation* and *membership clarification*. We will describe both phases individually.

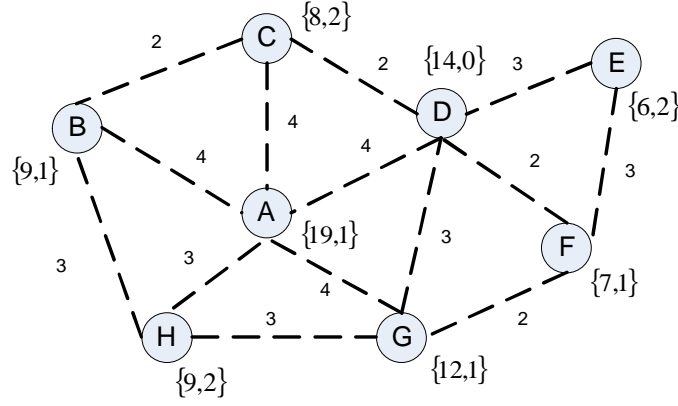
### 4.4.1 Phase I - Cluster Formation

Via spectrum sensing and communication with neighbours, every CR node is aware of the channel availabilities on itself and all its neighbours. We use two metrics for each CR node to characterize the robustness of channel availability between it and its neighborhood.

*Individual Connection Degree  $D_i$* :  $D_i = \sum_{j \in Nb_i} |V_i \cap V_j|$ , which denotes the sum of the pairwise common channels of node  $i$ , and is an indicator of node  $i$ 's adhesive property to the CRN.

*Social Connection Degree  $G_i$* :  $G_i = |\bigcap_{j \in Nb_i} V_j|$ , which is the number of common channels in  $Nb_i$ .  $G_i$  represents the ability of a neighborhood to form a robust cluster. Figure 4.1 illustrates an example CRN where the corresponding *Spectrum/Social Connection Degree* are specified for each node.

The algorithm of phase I can be sketched like this: cluster heads are determined first, then clusters are formed second.



**Figure 4.1** Connectivity graph and the connectivity vector  $\{D_i, G_i\}$  on each node. The available channels sensed by each CR node are:  $V_A = \{1, 2, 3, 4, 5, 6, 10\}$ ,  $V_B = \{1, 2, 3, 5, 7\}$ ,  $V_C = \{1, 3, 4, 10\}$ ,  $V_D = \{1, 2, 3, 5\}$ ,  $V_E = \{2, 3, 5, 7\}$ ,  $V_F = \{2, 4, 5, 6, 7\}$ ,  $V_G = \{1, 2, 3, 4, 8\}$ ,  $V_H = \{1, 2, 5, 8\}$ . Dashed lines indicates two end nodes are within transmission range of each other. Each edge is labeled by the number of common channels between the two ends.

#### 4.4.1.1 Determining Cluster Heads

In this phase, each CR node decides whether it is cluster head by comparing relevant metrics with its neighbours. This judgement is conducted periodically, and phase I ends after every node is certain that it is cluster head or not. Briefly states, the CR node which has the smallest *Individual Connection Degree* in its neighbourhood cluster head, i.e., , CR node  $i$  is cluster head, if  $D_i < D_k, \forall k \in Nb_i \setminus CHs$  ( $CHs$  donate the cluster heads existing in  $Nb_i$ ). If there is another CR node  $j$  in its neighborhood has the same *Individual Connection Degree*, i.e.,  $D_j = D_i$ , furthermore  $D_j < D_k, \forall k \in Nb_j \setminus \{CHs \cup i\}$ , then the node with higher *Social Connective Degree* becomes cluster head, and the other one becomes member of it. If  $G_i = G_j$  as well, node ID is used to break the tie, i.e., the one with smaller node ID takes precedence and becomes cluster head. This algorithm is contradictory to intuition by choosing the node with smallest  $D_i$  as cluster head. The reason is that, by deciding cluster head in this way, the CR node with bigger  $D_i$  will locate at the edge of clusters, and as they have higher *Individual Connection Degree*, they are more likely to be integrated into one certain cluster, thus less singleton clusters are formed.

The pseudo code of cluster head determination algorithm in Phase I is in Algorithm 2.

#### 4.4.1.2 Initial Cluster Formation

After deciding itself being cluster head, CR node broadcasts to notify its neighbours, meanwhile,  $i$ 's initial cluster is formed immediately, which is  $i$ 's neighborhood except for those nodes which have become cluster heads, i.e.,  $C_i = (Nb_i \setminus CHs) \cup i$ . It is possible that the formed cluster has no common channel for its members, this can be handled in the following way. As smaller cluster size increases the number of common channels within the cluster, certain nodes are eliminated until there is at least one common channel. The elimination of nodes is performed according to an ascending list of nodes sorted by their number of common channels with the cluster head. If there are nodes having the

**Algorithm 2:** Cluster head determined and cluster formation

**Input:** Unclustered CR node  $i$  which is aware of  $D_j$  and  $G_j$ ,  $j \in Nb_i$ , and the ID of CRs which have be decided to be cluster heads,  $ID_{CH}$ ,  $CH \in Nb_i$ .

Empty sets  $\tau_1, \tau_2, \tau_3, \tau_4, \tau_5$

**Result:** Whether or not  $i$  is cluster head

```

1  for CR node  $j \in Nb_i \setminus CHs$  do
2      if  $D_i == D_j$  then
3           $\tau_1 \leftarrow j$ 
4      else
5          if  $D_j < D_i$  then
6               $\tau_2 \leftarrow j$ 
7          end
8      end
9  end
10 if  $\tau_2 \neq \emptyset$  then
11      $i$  is not CH; break;
12 else if  $\tau_1$  is  $\emptyset$  then
13      $i$  is CH; break;
14 else
15     for  $\forall k \in \tau_1$  do
16         if  $\nexists m \in Nb_k \setminus CHs$ , such that  $D_m < D_k$  then
17              $\tau_3 \leftarrow k$ 
18         end
19     end
20     if  $\tau_3$  is  $\emptyset$  then
21          $i$  is CH; break;
22     else
23         for  $\forall n \in \tau_3$  do
24             if  $G_n > G_i$  then
25                  $\tau_4 \leftarrow n$ 
26             else
27                 if  $G_n == G_i$  then
28                      $\tau_5 \leftarrow n$ 
29                 end
30             end
31         end
32         if  $\tau_4 \neq \emptyset$  then
33              $i$  is not CH; break;
34         else if  $\tau_4$  is  $\emptyset$  and  $\tau_5 \neq \emptyset$  then
35             if  $ID_i < ID_r, \forall r \in \tau_5$  then
36                  $i$  is CH; break;
37             end
38         else
39              $i$  is CH; break;
40         end
41     end
42 end
43 if  $i$  is cluster head then
44      $D_j, j \in Nb_i \setminus CHs$  is changed as a big positive value  $M$ ;
45 end

```

*/\*  $\tau_1 \neq \emptyset, \tau_1 == \emptyset$  \*/*

*/\*  $\tau_4$  and  $\tau_5$  are  $\emptyset$  \*/*

same number of common channels with cluster head, the node whose elimination brings in more common channels will be chosen and excluded. If this criterion meet a tie, then the tie will be broken by deleting the node with smaller ID. At the end of this procedure every formed cluster has at least one common channel. For the nodes eliminated in this procedure, they can possibly become cluster heads or get included by other clusters later on. The pseudo code for cluster head to make sure at least one common channel is shown in Algorithm 3.

Figure 4.1 depicts an example how CR nodes decide cluster heads. Node  $B$  and  $H$  have same individual connection degree,  $D_B = D_H$ , but as  $G_H = 2 > G_B = 1$ , node  $H$  becomes cluster head. In Figure 4.1, the cluster  $C_H$  is  $\{H, B, A, G\}$ .

After receiving the notification from a cluster head, one CR node is aware that it is one member in a cluster, then the individual connection degree of that CR user is changed to a big positive value  $M$  (can be regarded as a positive infinite value), which is bigger than all the possible individual connectivity degrees happened in the CR network. Then this CR user broadcasts this new individual connection degree to all its neighbours. If a CR node  $i$  is associated to multiple clusters,  $D_i$  is still set to  $M$ . The purpose of manipulation on individual connection degree is to make the CR nodes out side this cluster possible to become cluster heads, so that every CR node either becomes cluster head or a member of at least one cluster. This is stated in the following theorem.

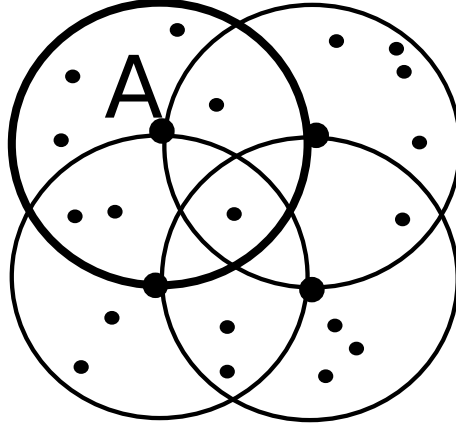
**Lemma 1.** *Every node in CRN will be included into at least one cluster in phase I in finite steps.*

*Proof.* To see this, assume there are some nodes not assigned to any cluster and node  $\alpha$  is one of them. As node  $\alpha$  is not contained in any cluster, there must be at least one node  $\beta \in Nb_\alpha$ , with  $D_\beta < D_\alpha$ . Thus, node  $\beta$  has at least one neighbouring node  $\gamma$  with  $D_\gamma < D_\beta$ , and this series of nodes with monotonically decreasing  $D_i$  might continue but finally ceases because the total number of nodes is limited. Now we find the last node  $\omega$  in this series, because  $\omega$  is the end node and does not have neighbouring nodes with smaller connectivity degree  $D$ , so  $\omega$  will become a cluster head and embrace all its one-hop neighbours, including the node before it in the node series (here we assume that every new formed cluster has common channels). After that, the node recruited into cluster will set its connectivity degree  $D$  to  $M$ , which enables the node further down in the list to become a cluster head. In this way, all the nodes in the series are included in at least one cluster in an inverse sequence. This clearly contradicts the initial assumption and proves the claim stated above. The proof implicitly shows that, within  $|I|$  steps, all nodes will become a part of certain clusters and so phase I converges.  $\square$

#### 4.4.1.3 Cluster Size Control in Dense CRN

Assume CR nodes are evenly distributed and cluster head locates in the middle of each cluster, the initial cluster formed is the neighborhood of cluster head, which is decided by the transmission range and network density. In extreme situation of dense network, when one cluster is formed, based on the rule for cluster head selection, the nearest another cluster head generated could at most locate just outside the neighborhood or equally speaking, just slightly away from the previous cluster head's transmission range. Then,

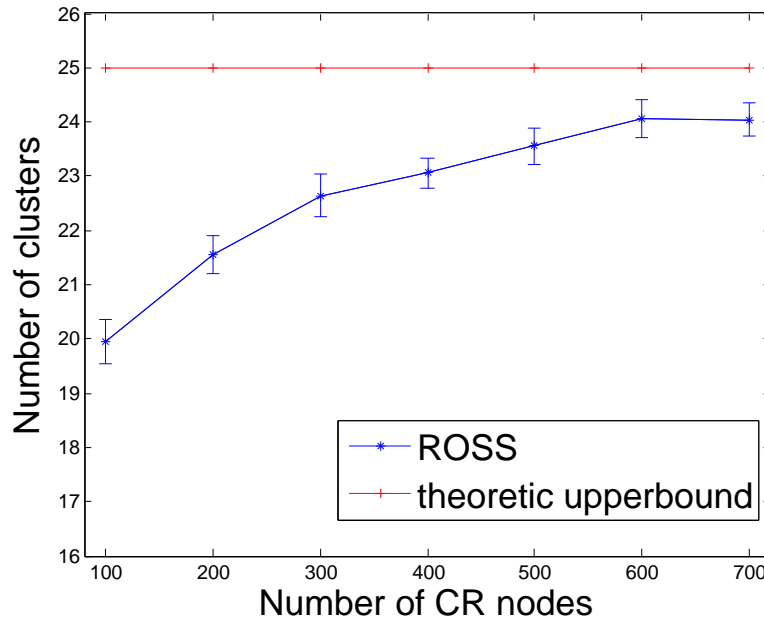
the distance between two neighbouring cluster heads is just slightly greater than the transmission range, as Figure 4.2 shows. Bigger black dots in the middle of clusters are cluster



**Figure 4.2** Possible clusters in dense CRN

ters heads, and smaller dots are cluster members. Circles mean the transmission range of cluster head, within which CR nodes are absorbed in cluster. We now have a look at how does the network density affect the cluster size when the transmission range is constant.

Assume all the CRs are evenly put in a square plane, and  $l$  is the length of side of simulation plan square, and  $r$  is CR's transmission radius. Then the maximum number of clusters is  $l^2/r^2$ .



**Figure 4.3** Number of clusters formed

Assume  $r = 10, l = 50$ , the theoretical upper bound is 25. We scatter the CR nodes in network of size  $l \times l$  randomly, and run simulations for 50 times with different network scale under certain influence from PRs, in order to obtain the number of formed initial clusters. As Figure 4.3 shows, the number of clusters increases with network density, but is upper bounded by 25. The confidence rate is 95% in the figure.

In case of dense network, the cluster size is big, which brings heavy burden on cluster head. Thus in dense network which limited resources are available on cluster heads, or the

inner communication doesn't support big clusters [xxxxx], certain measures are needed to reduce the network size. This task falls on cluster head. Cluster heads prune their cluster members if sizes are greater than the desired size  $\delta$ . Given desired size as  $\delta$ , cluster head excludes members sequentially, whose absence leads to the maximum increase on the number of common channels within the cluster. This process ends when the size of resultant cluster is at most  $\delta + 1$  and at least one CCC is available. This procedure is similar with that guarantees at least one CCC available in the cluster, and the algorithm is also given in Algorithm 3.

---

**Algorithm 3:** available CCC guarantee, or cluster size control conducted by cluster head

---

**Input:** Initial cluster formed, empty sets  $\mathcal{T}_1, \mathcal{T}_1$

**Output:** cluster has at least CCC, and satisfies the requirement on cluster size

/\* When available CCC is to be guaranteed, execute line 1,  
when cluster size control is conducted, execute line 2 \*/

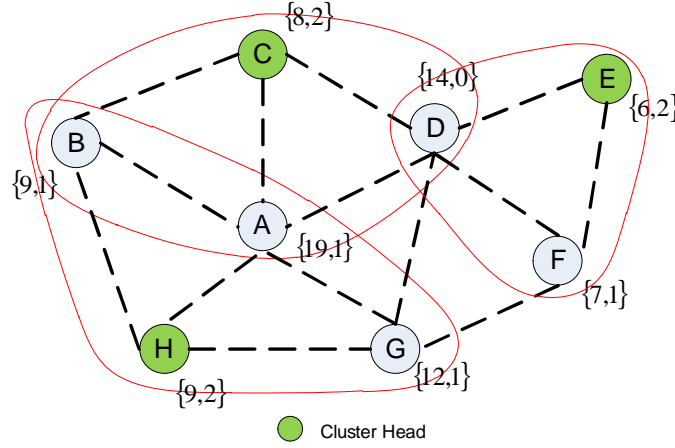
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1 while  $V_C = \emptyset$  do
2 while  $|C| > \delta + 1$  do
3   calculate  $\lambda = \min_{i \in C, i \neq H_C} (|K_{H_C} \cap K_i|)$ ;
4   for each  $i \in C \setminus H_C$  do
5     if  $|V_{H_C} \cap V_i| == \lambda$  then
6        $\mathcal{T}_1 \leftarrow i$ 
7     end
8   end
9   if  $|\mathcal{T}_1| == 1$  then
10    delete node  $i$  from  $C$ ;
11    break;
12  else
13    calculate  $\mu = \text{Max}_{i \in \mathcal{T}_1} (|\cap_{j \in C \setminus i} V_j| - |\cap_{j \in C} V_j|)$ ;
14    for each  $i \in \mathcal{T}_1$  do
15      if  $|\cap_{j \in C \setminus i} V_j| - |\cap_{j \in C} V_j| == \mu$  then
16         $\mathcal{T}_2 \leftarrow i$ 
17      end
18    end
19    if  $|\mathcal{T}_2| == 1$  then
20      delete node  $i$  from  $C$ ;
21      break;
22    else
23      delete  $i \in \mathcal{T}_2$ , which has the highest ID;
24    end
25  end
26 end

```

---

Figure 4.4 shows the clusters formed in the example in Figure 4.1 when the desired cluster size is 3.



**Figure 4.4** Clusters formation after the first phase of ROSS. Some nodes remain debatable nodes after the first phase.

## 4.4.2 Phase II - Membership Clarification

### 4.4.2.1 Problem Description

Notice in Figure 4.4, there are several nodes, like  $A$ ,  $B$ ,  $D$ , are included by more than one cluster. We refer to these nodes as *debatable nodes* as their cluster affiliations are not clear, and the clusters which include debatable node  $i$  are named as *claiming clusters* and represented as  $S_i$ . The set of available channels of one cluster are known by the debatable nodes which locate in that cluster. Debatable nodes need to be uniquely associated to one cluster and removed from the other claiming clusters, which is called as cluster membership clarification.

### 4.4.2.2 Distributed Greedy Algorithm (DGA)

After Phase I, each debatable node is member of at least one cluster, thus a debatable node  $i$  needs to decide which cluster  $C \in S_i$  to stay, and leaves the others. The principle for debatable node  $i$  to choose one claiming cluster to stay is to result in the greatest increase of common channels in all its claiming clusters. Node  $i$  communicates with each claiming cluster head in  $S_i$  to obtain the vector of available channels, then calculate the number of increased common channels in that cluster if it leaves that cluster. If among these claiming clusters exists one cluster  $C$  which gets the least increased common channels than any other claiming clusters, then  $i$  chooses to stay in cluster  $C$ . When there are multiple claiming clusters experiencing the same less increased common channels, then  $i$  chooses the claiming cluster whose cluster head shares more common channels with  $i$ . IDs of relevant cluster heads will be used to break tie if the previous rule doesn't work.

Algorithm for debatable node  $i$  to decide on which claiming cluster to stay in shown in Algorithm 4:

Debatable node  $i$  can either execute this algorithm periodically or triggered by the change of membership of  $C \in S_i$ . Notice that, as to debatable node  $i \in C$  and cluster  $C \in S_i$  could have more than one debatable node except  $i$ , the choices of those debatable nodes of cluster  $C$  change  $C$ 's membership and potentially further trigger node  $i$  to alter its previous decision. Thus, a question arises that whether the process converges if ROSS-DGA is

**Algorithm 4:** Debatable node  $i$  decides its affiliation**Input:** all claiming clusters  $C \in S_i$ **Output:** one cluster  $C$ 

```

1 calculate  $\lambda = \text{Max}_{C \in S_i} (|K_{C \setminus i}| - |K_C|)$ ;
2 define set  $\mathcal{C}_1$ ;
3 for each  $C \in S_i$  do
4   if  $|K_{C \setminus i}| - |K_C| == \lambda$  then
5      $\mathcal{C}_1 \leftarrow C$ 
6   end
7   /* metric is the increase of CCCs due to  $i'$  departing */
7 end
8 if  $|\mathcal{C}_1| == 1$  then
9   choose cluster  $C$ ;
10  break;
11 else
12  calculate  $\mu = \text{Max}_{C \in \mathcal{C}_1} (V_{H_C} \cap V_i)$ ;
13  define set  $\mathcal{C}_2$ ;
14  for each  $C \in \mathcal{C}_1$  do
15    if  $V_{H_C} \cap V_i == \mu$  then
16       $\mathcal{C}_2 \leftarrow C$ 
17    end
18    /* metric is the number of common channels between  $i$ 
19    and cluster head of demanding cluster */
18  end
19  if  $|\mathcal{C}_2| == 1$  then
20    choose cluster  $C$ ;
21    break;
22  else
23    calculate  $\nu = \min_{C \in \mathcal{C}_2} |C|$ ;
24    define set  $\mathcal{C}_3$ ;
25    for each  $C \in \mathcal{C}_2$  do
26      if  $|C| == \nu$  then
27         $\mathcal{C}_3 \leftarrow C$ 
28      end
29      /* metric is cluster size */
29    end
30    if  $|\mathcal{C}_3| == 1$  then
31      choose cluster  $C$ ;
32      break;
33    else
34      choose the  $C \in \mathcal{C}_3$ , which has the highest ID;
35    end
36  end
37 end
38 Node  $i$  notifies  $H_C$  which is cluster head of  $C$  of its affiliation decision, cluster  $C$ 
then accepts it.

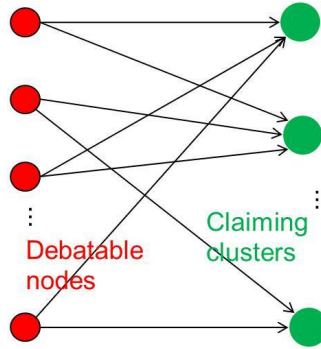
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implemented. In the following we show that the process of membership clarification can be converted to a congestion game, where a stable state is reached by the greedy procedure after a finite number of updates.

#### 4.4.2.3 Convergence of DGA

To formulate the problem of membership clarification for the debatable nodes in the context of a game, we look at the problem from a different perspective. In the new perspective, the debatable nodes are regarded as isolated and don't belong to any cluster, which means the clusters they used to belong to become their neighbouring clusters. Then as to each debatable node, the previous problem to decide which clusters to leave becomes a new problem that which cluster to join. In this new problem, debatable node  $i$  (note now  $i \notin S_i$ ) chooses one cluster  $C$  out of  $S_i$  to join if the decrement of common channels in cluster  $C$  is the smallest in  $S_i$ , and the decrement of number of ICC in cluster  $C$  is  $\sum_{C \in S_i} \Delta |K_C| = \sum_{C \in S_i} (|K_C| - |K_{C \cup i}|)$ . The relation between debatable nodes and claiming clusters is shown in Figure 4.5.



**Figure 4.5** debatable nodes and claiming clusters

In the following, the debatable nodes constitute the players, and we show that the decision of debatable nodes to clarify their membership can be mapped to the behaviour of the players in a *player-specific singleton congestion game* when proper cost function is given.

The game to be constructed can be represented by a 4-tuple  $\Gamma = (\mathcal{P}, \mathcal{R}, (\sum_i)_{i \in \mathcal{N}}, \Delta |K_C^i|)$ , where elements in  $\Gamma$  are given as below,

- $\mathcal{P}$ , the set of players of the game, which are the debatable nodes after phase I in our clustering problem.
- $\mathcal{R} = \cup S_i, i \in \mathcal{P}$ , denotes the set of resources for players to choose,  $S_i$  is the set of claiming clusters of node  $i$ .  $\mathcal{R}$  is the set of claiming clusters after phase I in our clustering problem.
- As to the strategy space  $\sum_i$  of player  $i \in \mathcal{N}$ , there is  $\sum_i \subseteq 2^{[S_i]}$ . As one debatable node is supposed to choose one claiming cluster in our problem, thus only one resource is allocated for  $i$ , accordingly this congestion game is a singleton game.

- The utility (cost) function  $f(C)$  of resource  $C \in R$ , (or to say  $f(r)$  of resource  $r \in R$ ) is  $\Delta|K_C^i|$  which represents the decrement of ICCs in cluster  $C$  caused by debatable node  $i$  joining in it. As to cluster  $C \in S_i$ , the decrement of ICCs caused by enrolment of debatable nodes is  $\sum_{i: C \in S_i, i \rightarrow C} \Delta|K_C^i|$ .  $i \rightarrow C$  means  $i$  joins in cluster  $C$ . Obviously this function is non-decreasing with respect to the number of nodes joining in cluster  $C$ .

The utility function is not purely decided by the number of players (debatable nodes) as that in a canonical congestion game, as in this game the channel availability on debatable nodes is different. Given two same sized groups of debatable nodes, when the nodes are not completely the same (neither are the channel availabilities on these nodes), the cost happened on one claiming cluster could be different if the two groups of debatable nodes join in that cluster respectively. Hence, this game is called player specific. In this game, every player greedily updates its strategy (choosing one claiming cluster to join) if joining in a different claiming cluster minimizes the decrement of ICCs  $\sum_{i: C \in S_i} \Delta|K_C^i|$ , player's strategy in the game is exactly the same with the behaviour of debatable node in membership clarification phase, which is described by Algorithm 4.

As to singleton congestion game, there exists pure equilibria which can be reached with greedy update [13].

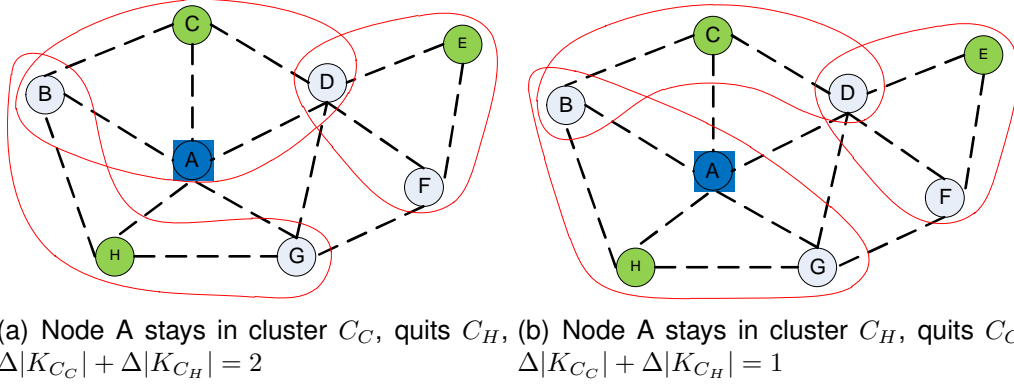
Based on above model and analysis, phase II converges is Algorithm 4 is run by debatable nodes.

The number of steps, or the upper bound of steps in convergence needs a formal proof

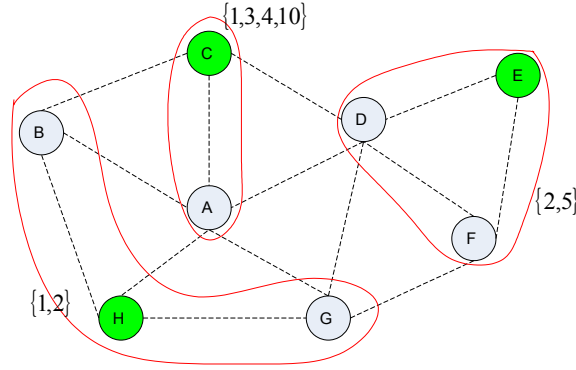
#### 4.4.2.4 Distributed Fast Algorithm (DFA)

The complexity of DGA is quite large recalling that the formation of clusters takes at most  $|I|$ . Here we propose a faster algorithm DFA which is especially suitable for CRN where channel availability might change dynamically and re-clustering is possible. In DFA, each debatable node executes only one iteration of Algorithm 4 (by setting 'the current value' in Line 14 to zero). Every cluster includes all its debatable nodes, thus the membership is static and debatable nodes can make decisions simultaneously without considering the change of membership of its claiming clusters. For example, for node  $A$  in Figure 4.4, the membership of cluster  $C_C, C_H \in S_A$  are  $\{A, B, C, D\}$  and  $\{A, B, H, G\}$  respectively.

The two possible strategies of node  $A$ 's clarification is illustrated in Figure 4.6. In Figure 4.6(a), node  $A$  staying in  $C_C$  and leaving  $C_H$  brings 2 more ICC in  $S_A$ , as it is more than that brought by another strategy showed in 4.6(b),  $A$ 's membership is clear. After the decisions made similarly by the other debatable nodes  $B$  and  $D$ , the final clusters formed are shown in Figure 4.7.



**Figure 4.6** Membership clarification: possible cluster formations decided by node A's different choices



**Figure 4.7** Final formation of clusters, common channels for each cluster is shown.

## 4.5 Centralized Clustering Scheme

The centralized clustering scheme aims to form clusters with certain sizes, meanwhile the total number of common channels of all clusters is maximized. In the following, we refer this problem as *centralized clustering* for short, and the problem definition is as follows,

**Definition 1.** *Centralized clustering in CRN.*

Given a cognitive radio network  $\mathcal{N}$  where nodes are indexed from 1 to  $N$  sequentially. Based on certain correlation, some CR nodes constitute one cluster  $C$ .  $1 \leq |C| \leq k$  where  $k$  is positive integer. We name the collection of such clusters as  $\mathcal{S} = \{C_1, C_2, \dots, C_l\}$  (the subscript  $i$  is the unique index of cluster in  $\mathcal{S}$ , not the ID of cluster head of relevant cluster),  $\mathcal{S}$  has following properties:  $\bigcup_{1 \leq i \leq l} C_i = N$  and  $V_{C_i} \neq \emptyset$  for any  $i$  which satisfies  $1 \leq i \leq l$ .

Following condition distinguish the centralized clustering problem discussed in this thesis. The number of common channels is denoted as  $f$  which is  $|V_C|$  if  $|V_C| > 1$ , and  $f = 0$  if  $|V_C| = 1$ . The question of this problem is to find a subcollection  $\mathcal{S}' \subseteq \mathcal{S}$ , so that  $\bigcup_{C_j \in \mathcal{S}'} C_j = N$ , and  $C'_j \cap C_j = \emptyset$  for  $C'_j, C_j \in \mathcal{S}'$ , so that  $\sum_{C \in \mathcal{S}'} f$  is maximized. The decision version of centralized clustering in CRN is to ask whether exist  $\mathcal{S}' \subseteq \mathcal{S}$ , so that  $\sum_{C \in \mathcal{S}'} f \geq \lambda$  where  $\lambda$  is a real number.

In the following part of this section, we will discuss the complexity of centralized clustering problem and provide solution for it. We put the definition of weighted k-set packing problem here as it will be used in the analysis on the complexity of our problem.

**Definition 2.** *Weighted  $k$ -set packing.*

Given a set  $\mathcal{G}$  which contains finite number of positive integers, and a collection of set  $\mathcal{Q} = \{s_1, s_2, \dots, s_m\}$ , where for each element  $s_r, 1 \leq r \leq m$ , there is  $s_r \subseteq \mathcal{G}$ ,  $1 \leq |s_r| \leq k$ , and  $s_r$  has an associated weight which is positive real number. The question is whether exists a collection  $S \subseteq \mathcal{Q}$ , where  $S$  contains only disjoint sets and the total weight of sets in  $S$  is greater than  $\lambda$ . Weighted  $k$ -set packing is NP-hard when  $k \geq 3$ . [39]

**Theorem 4.5.1.** *CRN clustering problem is NP-hard, when the maximum size of clusters  $k \geq 3$ .*

*Proof.* To see centralized clustering problem is NP-hard, we reduce the NP-hard problem *weighted  $k$ -set packing* to it.

To complete the reduction, we need to conduct following two steps:

- step 1: Show there exists a polynomial algorithm  $\sigma$ , by which any instance (e. g.,  $\mathcal{S}$ ) of a weighted  $k$ -set packing can be transformed to instance  $\sigma(\mathcal{S})$  for centralized clustering.
- step 2: Show that  $\mathcal{S}$  is a yes instance of weighted  $k$ -set packing if and only if  $\sigma(\mathcal{S})$  is an yes instance for CRN clustering problem.

We continue using the notation introduced in problem definition. Let set  $\mathcal{G}$  contains  $N$  positive integer numbers which are indexed from 1 to  $N$  sequentially. Assume one instance  $\mathcal{S}$  of weighted  $k$ -set packing is a collection of disjoint sets  $\mathcal{Q} = \{s_1, s_2, \dots, s_m\}$ , each set is composed by certain amount of elements in  $\mathcal{G}$ .  $\omega$  indicates the weight for each set  $s$ ,  $\omega : \mathcal{S} \rightarrow \mathbb{Z}^+$ .

The polynomial algorithm  $\sigma$  consists of three transformations.

- In the first transformation, for each set  $s_i$  of instance  $\mathcal{S}$ , the elements are duplicated, for instance, given  $s_i = \{1, 4, 6\}$ , the dummy set  $s'_i$  is  $\{1, 1, 4, 4, 6, 6\}$ . By doing this, we obtain the dummy sets and constitute the dummy instance  $\mathcal{S}'$  based on  $\mathcal{S}$ . The purpose of this transformation is to eliminate the single element set in  $\mathcal{S}$ . The weight of set is unchanged after this transformation, i.e.,  $\omega(s_i) = \omega(s'_i)$ . After this transformation, there is no set with only one element. This transformation requires  $\sum_{s_i \in \mathcal{S}} |s_i|$  steps.
- In the immediate following second transformation, we transform the dummy instance  $\mathcal{S}'$  to an instance for CRN clustering problem. Given an instance  $\mathcal{S}'$ , we retrieve all the elements which appear in it, and map each of those elements into one CR node, i.e., each integer corresponds to one CR node, particularly, that integer becomes the CR node's ID. As to duplicated elements, we also map them into a CR node, thus there exist CR nodes with the same ID. As a result, these CR nodes constitute a collection of CR nodes, but note that they have not constituted one CRN yet as there are not connections drawn among them. Connections in CRN under this context is decided by physical conditions, which says the corresponding CR nodes have common channels and close enough to communicate with each other. This transformation requires  $2 \cdot \sum_{s_i \in \mathcal{S}} |s_i|$  steps.

- Mere isolated nodes don't constitute network, thus we add connections in CRN based on the sets in  $\mathcal{S}'$  sequentially. For each set  $s' \in \mathcal{S}'$ , we add connection between two CR nodes if their IDs are in  $s'$ . There is also connection between the CR node and its dummy node. The number of common channels of the CR nodes equals to the weight of set  $s'$ . No connection exists between two CR nodes if their IDs don't appear in one set in  $\mathcal{Q}$ . Afterwards, the CR node whose ID doesn't appear in any set in  $\mathcal{S}'$  becomes single node clusters, according to the definition of clustering problem in CRN, the number of common channels is 0. This procedure requires  $\sum_{s'_i \in \mathcal{S}'} |s_i|$  steps to map sets in  $\mathcal{S}'$  into CRN and connections, and at most  $N$  steps to complement the single node clusters in CRN.

The number of common channels of cluster  $f$  is non-decreasing function of cluster size, while, the weight of set in weighted k-set packing problem doesn't have this property. In weighted k-set packing, the weight of a set with smaller size could be larger than a set with more elements. But this difference doesn't hinder the transformation and we use an example to explain. Assume two sets in  $\mathcal{S}$  are  $s_1 = \{1, 2\}$  and  $s_2 = \{1, 2, 3, 4\}$ , their weights are 3 and 5 respectively. Their dummy sets are  $s'_1 = \{1, 1, 2, 2\}$  and  $s'_2 = \{1, 1, 2, 2, 3, 3, 4, 4\}$  and their new weights are 3 and 5 as before. The connections mapped to CRN are contradictory to reality, as the number of common channels of CR node group  $\{1, 1, 2, 2\}$  can only be smaller than that of  $\{1, 1, 2, 2, 3, 3, 4, 4\}$ . We let this contradiction in the process of mapping happen because it will be eliminated later: no matter one instance  $\mathcal{S}$  for weighted k-set packing results in *yes* or *no*, at most only one set of  $s'_1$  and  $s'_2$  is chosen, then we can safely delete the connections based on the deleted set from the CRN, and the contradiction is eliminated.

We have crossed the hurdle of finding one polynomial algorithm  $\sigma$  to transform instance of weighted k-set packing to an instance for clustering in CRN. Now we look into the step 2 in reduction.

When the instance  $\mathcal{S}$  for weighted k-set packing contains one solution, i.e., there is a group of sets in  $\mathcal{S}$ , whose sum weights is greater than  $\lambda$ , then in the CRN which is mapped from  $\mathcal{S}'$ , the sum number of common channels of the clusters which correspond to the selected sets in  $\mathcal{S}$  and  $\mathcal{S}'$ , is greater than  $\lambda$ .

When there is no solution out of set  $\mathcal{G}$  for weighted k-set packing, let's assume the maximum sum of weights of all instances is  $\sum_{s_i \in \mathcal{S}} \omega(s_i) = \delta < \lambda$ . The dummy set of each  $s_i \in \mathcal{S}$  is mapped to cluster of CR nodes. Definition of CRN clustering regulates that the number of common channels is 0 when the cluster has only one node. As to  $|s_i| = 1$ , the mapped cluster has two nodes, with one of them is the dummy CR node. Then number of common channels is on longer 0 but equals to the weight of corresponding set  $s_i$ . Then the sum number of common channels of the clusters in CRN is  $\delta < \lambda$ , thus, there is no clustering solution for the mapped CRN.

After proving weighted k-set packing can be reduced to centralized clustering in CRN, we can say the latter problem is NP-hard.  $\square$

### 4.5.1 The Optimization Problem

As there is no efficient algorithm to solve clustering problem in CRN, we adopt binary linear programming to solve the problem. Note that binary linear programming is in NP-complete.

Given a CRN  $N$  and desired cluster size  $\delta$ , we get a collection of clusters  $G$ , where clusters satisfy the conditions of clusters in Section 4.3, and the sizes of clusters are  $1, 2, \dots, \delta$ . Note that the legitimate clusters include the singleton ones, which guarantees the partition of any network is feasible. With  $n = |N|$ ,  $g = |G|$ , we construct a  $g \times n$  matrix  $Q_{g \times n}$ . Each element  $q_{ij} = |k_{C_i}|$  if  $j \in C_i$ , and  $q_{ij} = 0$  if  $j \notin C_i$ . In other words, Each non-zero element  $q_{ij}$  denotes the number of common channel of the cluster  $i$  where node  $j$  resides.

$$Q = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & \cdots & n-1 & n \end{matrix} \\ \begin{matrix} C_1 \\ C_2 \\ \vdots \\ C_i \\ \vdots \\ C_{i'} \\ \vdots \end{matrix} & \begin{pmatrix} k_{C_1} & k_{C_1} & 0 & \cdots & 0 & 0 \\ k_{C_2} & 0 & k_{C_2} & \cdots & 0 & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & k_{C_i} & 0 & \cdots & k_{C_i} & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\ k_{C_{i'}} & 0 & 0 & \cdots & k_{C_{i'}} & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \end{pmatrix} \end{matrix}$$

**Figure 4.8** Matrix Q

We also have one  $G \times N$  binary matrix  $X$ , the element of the matrix is binary variable  $x_{ij}$ ,  $i = 1, \dots, G$ ,  $j = 1, \dots, N$ .  $x_{ij} = 1$  denotes cluster  $i$  is one partition chosen by the clustering scheme,  $x_{ij} = 0$  means this partition is not adopted.

$$\text{minimize} \quad \sum_{j=1}^g \sum_{i=1}^n (-x_{ij}q_{ij} + w_i * \text{cost}(\delta)) \quad (4.1)$$

$$\text{subject to} \quad \sum_{i=1}^g x_{ij} = 1, j = 1, \dots, n \quad (4.2)$$

$$\sum_{j=1}^n x_{ij} = \delta * (1 - w_i), j = 1, \dots, g \quad (4.3)$$

$x_{ij}$  and  $w_j$  are binary variables.

As the resultant clusters are with certain desired sizes, we try to maximize the sum of products of cluster size and number of common channels in the objective function. The second item of objective function denotes the *punishment* for choosing the cluster whose size is not  $\delta$ . We design  $\text{cost}(\delta)$  as follows,

$$\text{cost}(\delta) = \begin{cases} 0 & \text{if } |C_i| = \delta \\ \alpha_1 & \text{if } |C_i| = \delta - 1 \\ \alpha_2 & \text{if } |C_i| = \delta - 2 \\ \dots & \end{cases}$$

where  $\alpha_i > 0$  and increases with  $i$  getting larger. Choice of  $\alpha_i$  affects the resultant clusters.

Constraint 3.2 restricts that node  $j$  resides in exactly one cluster. In constraint 3.3,  $w_j$  is an auxiliary binary variable,  $w_j = 0$  denotes cluster  $j$  is chosen in the solution. When

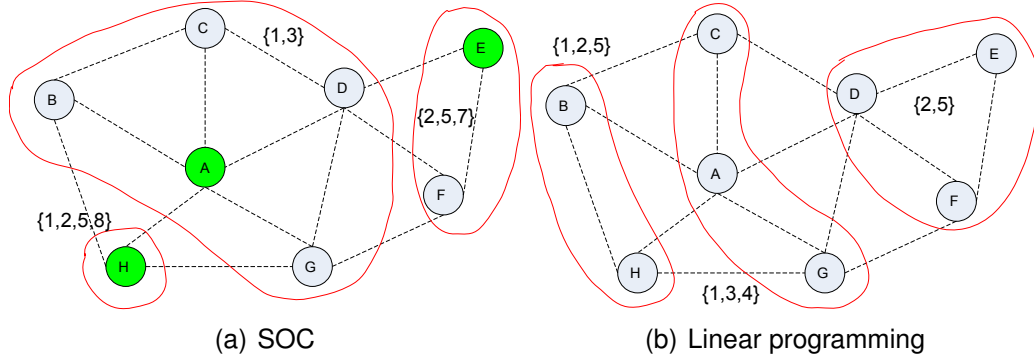
$w_i = 1$ ,  $i$ th cluster is not chosen according to constrain 3.3, then the objective function suffers certain *loss*.

This is a linear binary optimization problem, which is solved by function *bintprog* provided in MATLAB.

Take CRN in Figure 4.1 for example. As  $|N| = 8$ , we let the cluster size  $\delta$  to be either 2 or 3 so that the partition of network is possible. A collection of clusters  $G$  is built, where the clusters satisfy the conditions for cluster in Section 4.3 and the sizes of clusters are 1, 2 and 3.  $G = \{\{A\}, \{B\}, \dots, \{B, C\}, \{B, A\}, \{B, H\}, \dots, \{B, A, C\}, \{B, H, C\}, \{A, D, C\}, \dots\}$ , and  $|G| = 38$ .

The clustering result of binary linear programming is  $\{\{D, E, F\}, \{A, C, G\}, \{H, G\}\}$ , the number of common channels is  $\{2, 3, 3\}$ . The solution from ROSS is  $\{\{B, H, G\}, \{C, A\}, \{D, E, F\}\}$ , the number of common channels is  $\{2, 4, 2\}$ . By applying SOC, the clustering result is  $\{A, B, C, D, G\}, \{E, F\}, \{H\}$ .

The final clusterings of the example CRN by SOC and linear programming are as follows,



**Figure 4.9** Final clustering of the example CRN

As to the average number of common channel, the results of ROSS, LP and SOC are 2.66, 2.66, and 3 respectively. Note there is one singleton cluster  $C_H$  generated. When the singleton cluster  $\{E\}$  is excluded, the average number of common channels of SOC drops to 2.5.

## 4.6 Performance Evaluation

In this section, we evaluate the performances of the two variants of ROSS, i.e., ROSS-DGA and ROSS-DFA, besides, the cluster size control scheme is also evaluated when the desired cluster size is smaller than the average neighbourhood size. We choose SOC as comparison scheme. To the best of our knowledge, SOC [55] is the only work emphasizing on the robustness of clustering structure from all previous work on clustering in CRN. The authors of [55] compared SOC with other schemes based on the average number of common channels within each cluster, on which SOC outperforms other schemes by 50%-100%. This is because the schemes except for SOC are designed either for ad hoc network without consideration of channel availability [23], or for CRN but just considering basic connection among CR nodes [108]. Hence, we only compare the two versions

of our scheme ROSS-DGA and ROSS-DFA with SOC to show the merits of ROSS, and also compare with the centralized scheme to see the gap with the global optima. We will investigate the following metrics:

- Average number of common channels per un-singleton cluster.
  - SOC adopts the average number of common channel over all clusters, i.e., including the singleton clusters. As we try to look into the robustness of clusters of CRs, we exclude those singleton clusters.
- Number of unclustered CRs with moderate and vigorous intensity of PRs' activities.
  - This is the straight forward metric on robustness of clusters. We investigate how many clusters survives when we increase the intensity of PRs' activity.
- Cluster sizes
  - Homogeneous clusters size is pursued.
- Amount of control messages involved.

The simulation is done by implementing random graph structures in C++. There are two parts of simulation, in the first part, we investigate the gap between the distributed schemes with the centralized scheme. As there is no polynomial time solution available to solve the centralized problem, we adopt a small network to compare the performances of the ROSS, SOC and the centralized solution. In the second part, we increase the network scale and change network density to thoroughly compare the two distributed schemes.

## 4.6.1 Centralized Schemes vs. Decentralized Schemes

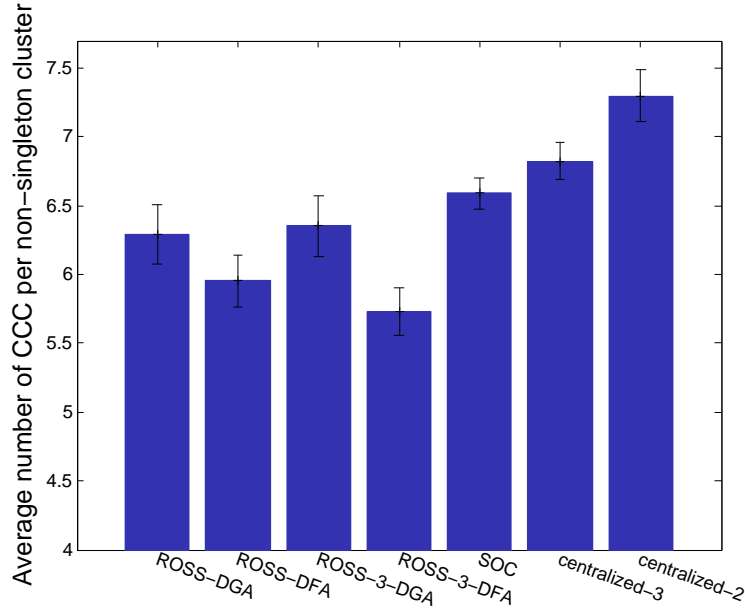
Coinciding with the system model in Section 4.3, 10 primary users and 20 CR users are dropped randomly (with uniform distribution) within some area of size  $A^2$ , where we set the transmission ranges of primary and CR users to  $A/3$ . There are  $P = 10$  available channels. With this setting, the average number of neighbours of one CR user is around 5. Each primary user randomly occupies one channel, and CR users are assumed to be able to sense the existence of primary users and identify available channels. When clustering scheme is executed, around 7 channels are available on each CR node. All primary and CR users are assumed to be static during the process of clustering. Performance results are averaged over 50 randomly generated topologies with equal parameters. The desired cluster size is 3. The confidence interval shown in figure corresponds to 95% confidence level.

### 4.6.1.1 Number of Common Channels

We first have a look at the average number of common channels per cluster, which is used in [60] as the sole criterion for clustering robustness. Figure 4.10 shows the average number of common channel of non-singleton clusters, as the singleton clusters (in other words unclustered nodes) don't execute any functionalities of clusters, which are described in



Section 4.1. As to schemes, centralized schemes outperform distributed schemes on number of common channels. SOC achieves the most number of CCC than variants of ROSS. SOC is liable to group the neighbouring CRs which share the most abundant spectrum together, no matter how many of them are, thus the number of CCC of the formed clusters is higher, but this method leaves considerable number of CRs which have less spectrum not in any clusters. As to variants of ROSS, the procedure of debatable nodes greedily looking for better affiliation improves the number of CCC, thus ROSS-DGA with and without size control outperform ROSS-DFA and its size control version respectively. We also notice that, the size control feature doesn't affect the number of CCC for both ROSS-DGA and ROSS-DFA.



**Figure 4.10** Number of common channels for non-singleton clusters, the numbers in the names of schemes annotate the desired cluster size.

#### 4.6.1.2 Survival Rate of Clusters with Increasing PR Users

We investigate the robustness of the formed clusters when they co-exist with varying intensity of PRs' activities. After the clusters are formed under the influence of the initial 10 PRs, extra 100 PRs are sequentially added into the network. The transmission range and channel occupancy of the new PR is the same with the previous ones, i.e., transmission range is  $A/3$ , and one channel out of 10 is randomly chosen to operate. As to one cluster, if there is no common channels available for all members because of the new added PRs, the cluster destroyed, and the former cluster member CRs become unclustered CRs.

Figure 4.11 shows the number of unclustered CRs with the increase of PRs, which indicates the vulnerability of clusters under varying surrounding of licensed spectrum.

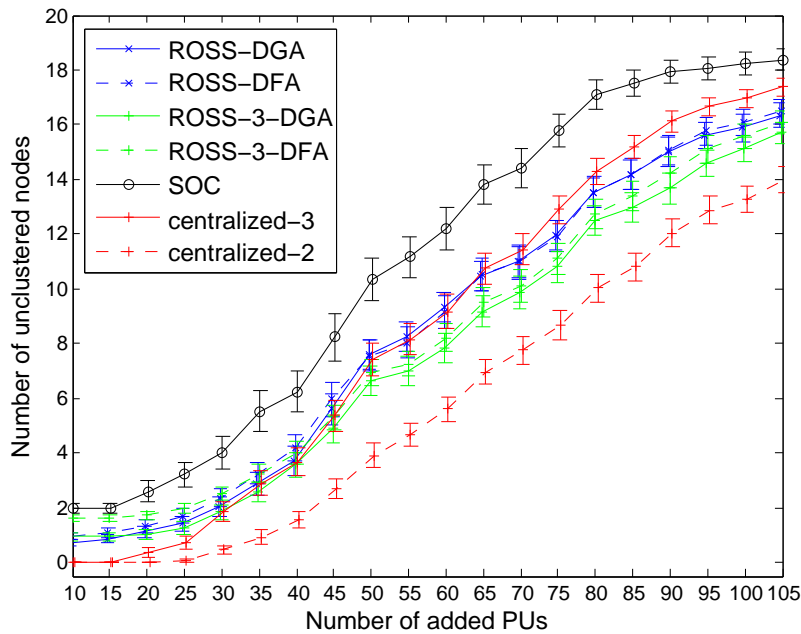
We obtain three conclusions corresponding to three comparisons shown in this figure,

- Centralized scheme with cluster size of 2 produces the most robust clusters, and SOC results in the most vulnerable clusters. Centralized scheme with cluster size of 3 achieves less unclustered CRs than variants of ROSS when the number of PRs

is 10~30, when number of PUs is 30~60, same amount of unclustered CRs are generated with variants of ROSS. When there are 75 and more new PRs, centralized scheme with cluster size of 3 results in more unclustered CR nodes than variants of ROSS. Size control feature makes both ROSS-DGA and ROSS-DFA outperform themselves without size control when number of new PRs is greater than 50.

The reason that centralized scheme with cluster size of 3 does not completely excel variants of ROSS is due to the favourable achievement of it: the uniformly sized clusters. As distributed schemes, variants of ROSS generate considerable amount of smaller clusters which are more likely to survive when PRs' activities become intense. The comparison on cluster sizes will be given in details in 4.6.1.3.

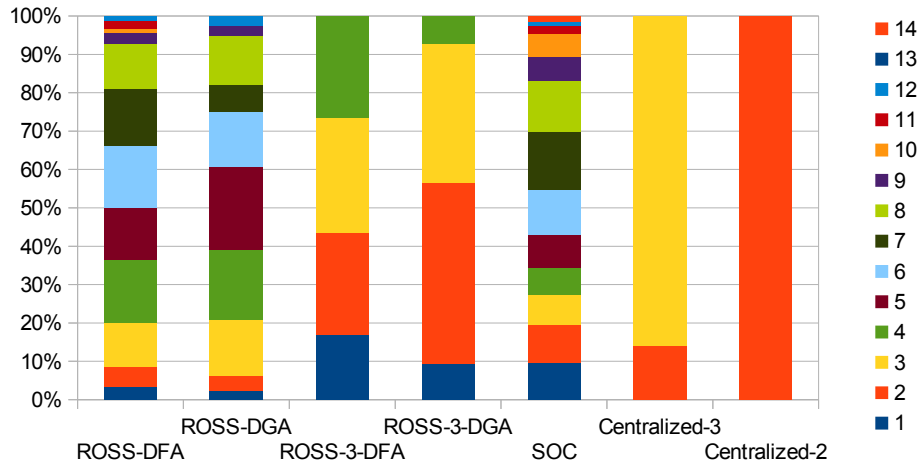
- ROSS with size control is better than the other two distributed schemes. The size control decreases the clusters size and makes the clusters more robust when under PRs' activity.
- Greedy algorithm improves survival rate. ROSS-DGA improves the survival rate of ROSS-DFA, so does ROSS-DGA with size control against ROSS-DFA with size control. This comply with the observation on number of CCC in section 4.6.1.1. As the debatable CRs greedily update their affiliation with demanding clusters, and the metric for updating is the maximum increase of CCCs of the demanding clusters, the average number of common channels is improved (shown in Figure 4.10), then the robustness of clusters is enhanced. Meanwhile, sizes of more clusters become smaller also contributes more robustness.



**Figure 4.11** Number of CRs which are not included in any clusters

#### 4.6.1.3 Cluster Size Control

Figure 4.12 shows the number of CRs residing in certain sized clusters. The centralized schemes are able to form clusters which strictly satisfy the requirement on cluster sizes.



**Figure 4.12** Distribution of CRs residing in Clusters with different sizes, as to ROSS with size control feature, the desired cluster size is 3.

When the desired size is 2, each generated cluster has two members. When the desired size is 3, in average only 3 CRs are formed into 2 node clusters. When ROSS-3-DFA is applied, most number of CRs are in 3 node clusters, nevertheless, slightly less nodes are found in 2 node and 4 node clusters, there are also considerable number of singleton clusters. ROSS-3-DGA decreases the clusters sizes and results in more 2 node clusters, the second most CRs are found in 3 node clusters. ROSS-DGA and ROSS-DFA generate rather even distribution of nodes with different sizes, whereas SOC results in more CRs unclustered or clusters of large sizes. Figure 4.12 shows distributed clustering schemes are not able to control cluster sizes perfectly, but ROSS-DGA and ROSS-DFA eliminate the clusters whose size diverges largely with the desired one, i.e., single node clusters and clusters with size of 13 and 14. Particularly, size control enable both ROSS-DGA and ROSS-DFA to achieve clusters whose sizes demonstrate certain homogeneity, i.e., cluster sizes vary from 1 to 4. But there are considerable number of single node clusters, which is due to the cluster pruning discussed in section 4.4.1.3.

#### 4.6.1.4 Control Signalling Overhead

As to any variants of ROSS, there are two phases, in the first phase, clusters are formed, in the second phase, cluster membership is decided so that each node only resides in one cluster. Control message exchanges between CR nodes are involved in both phases.

In this section we compare the amount of control messages involved for clustering in different schemes, e. g., centralized scheme, ROC, ROSS-DGA, ROSS-DFA and those with size control feature. In order to highlight the amount of control signalling only for clustering, we omit the control messages used for neighbourhood discovery, which are regarded the same for all schemes, and only compare the number of control messages brought in by the features of the schemes. The control message here refers both broadcast and unicast.

As to variants of ROSS, in the first phase, after each node broadcasts their new knowledge on spectrum robustness, cluster is automatically formed by cluster head which is decided from consensus by comparing the spectrum robustness with neighbours, then the cluster head broadcasts message containing its ID and the available channels in its cluster. As to ROSS with size control feature, there are same amount of cluster heads with ROSS without enabling size control feature, and the cluster head broadcasts the available channels

of the pruned cluster. Afterwards in the second phase, membership clarification of debatable nodes is conducted. Debatable node informs the cluster which it going to stay and the cluster head broadcasts message about its new cluster. As to SOC, each node needs to maintain one cluster, the final clusters are formed after three rounds of comparisons and cluster mergers, while as to ROSS, only debatable nodes need to communicate with cluster heads to clarify their membership.

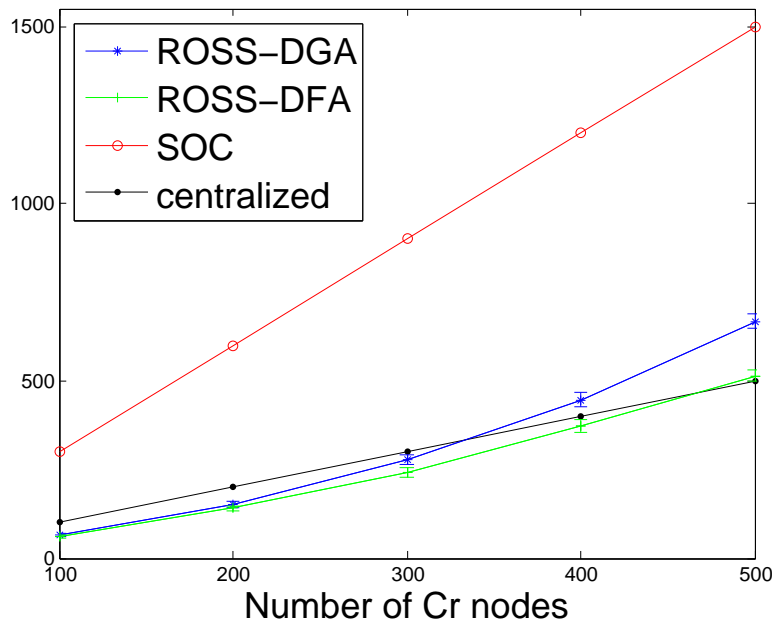
Worst case protocol complexities. We assume that the protocols execute synchronously. We compare the Time Complexity (TC), defined as the number of steps required to perform a protocol operation, and the Communication Complexity (CC), defined as the number of broadcast in performing the operation.

The complexity parameters are the number of nodes  $n$  in network, number of clusters  $h$ .

The quantitative analysis of amount of control overhead and the size of messages are illustrated in Table 4.2,

Scheme	Number of broadcast	Content of message
ROSS-DGA, ROSS-x-DGA	$h+2*m^2c$ (upper bound)	$ID_{H_C}$ and $V_C$ for $h + m^2c$ times, notification to join in one cluster for $m^2c$ times
ROSS-DFA, ROSS-x-DFA	$h + 2m$ (upper bound)	$ID_{H_C}$ and $V_C$ for $h + m$ times, notification to join in one cluster for $m$ times
SOC	$3 * n$	$\{V_i\}, i \in M \subseteq Nb_i$
Centralized	$n$	$\{C\}$

**Table 4.2** Singalling overhead. Notations:  $n$ -number of CR nodes in CRN,  $h$ -number of cluster heads,  $m$ -number of debatable nodes,  $c$ -number of demanding clusters,  $\delta$ -desired cluster size

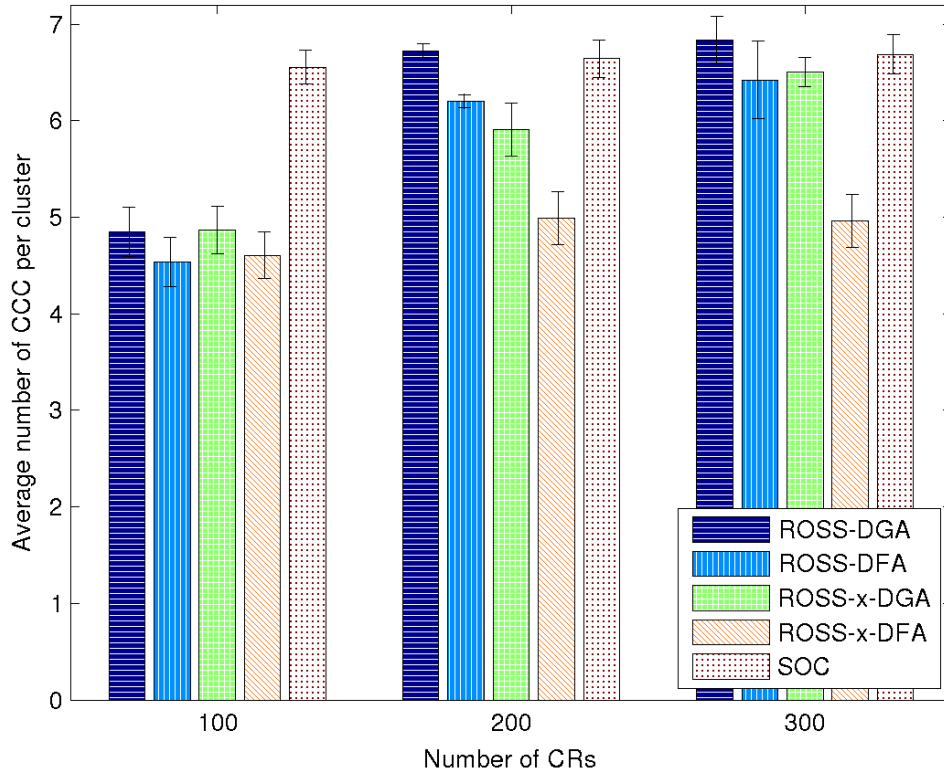


**Figure 4.13** Number of control messages

## 4.6.2 Comparison between Distributed Schemes

In this part we investigate the performances of distributed schemes in CRN with different network scales and densities. The transmission range for CR is  $A/10$  whereas  $A/5$  for PR. The number of PR is 30, we investigate the CRN where number of CR is 100, 200 and 300.

### 4.6.2.1 Number of CCC per Non-singleton Clusters



**Figure 4.14** Number of common channels for non-singleton clusters. As to ROSS with size control feature,  $x = 2$  when  $N = 100$  and  $200$ ,  $x = 3$  when  $N = 300$ .

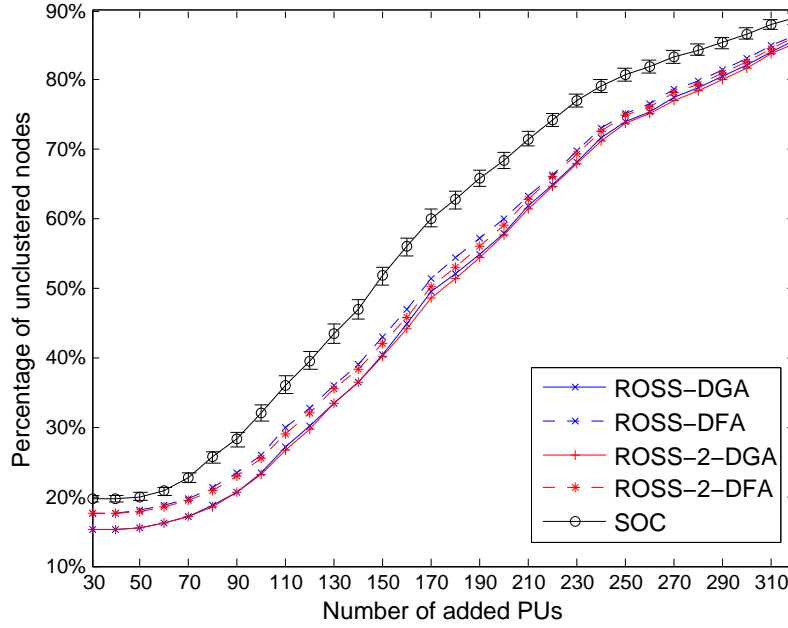
Figure 4.14 shows the Figure 4.14 illustrates the average number of CCC of the non-singleton clusters. It shows when  $N = 100$ , variants of ROSS have 30% less CCC than SOC, but this gap is decreased when  $N$  is 200 and 300. This means SOC performs better on average number of CCC per non-singleton clusters when network density is small, which is already observed in section 4.6.1.1. When the network becomes more dense, ROSS-DGA achieves even more CCC than SOC, and ROSS-DFA and ROSS-x-DGA visibly increase their performances on CCC.

### 4.6.2.2 Survival Rate of Clusters with Increasing PR Users

With the increase of PRs in the network, clusters become broken as no CCC available within the clusters. In this part of simulation, we add 290 more PRs randomly in CRN

with interval of 10 to evaluate the robustness of clusters. Figure 4.15 shows the increasing trend of the number of singleton clusters with the increase of PRs. SOC generates around 10 more singleton clusters than the variants of ROSS, which accounts for 10% of the whole network. The confidence intervals of the variants of ROSS are not shown in the figure as they overlap, and we only show the average values. It can be seen that greedy algorithms result in slightly less singleton clusters than their counterparts.

Figure 4.16 shows a more dense CRN where  $N = 300$ . SOC noticeably causes more singleton clusters than ROSS variants, except for ROSS-3-DFA when PRs are few. The reason is ROSS-3-DFA only conduct cluster membership once, which leaves large number of singleton clusters, while, in ROSS-3-DGA increase the size of smaller clusters through debatable nodes' repeated updates.



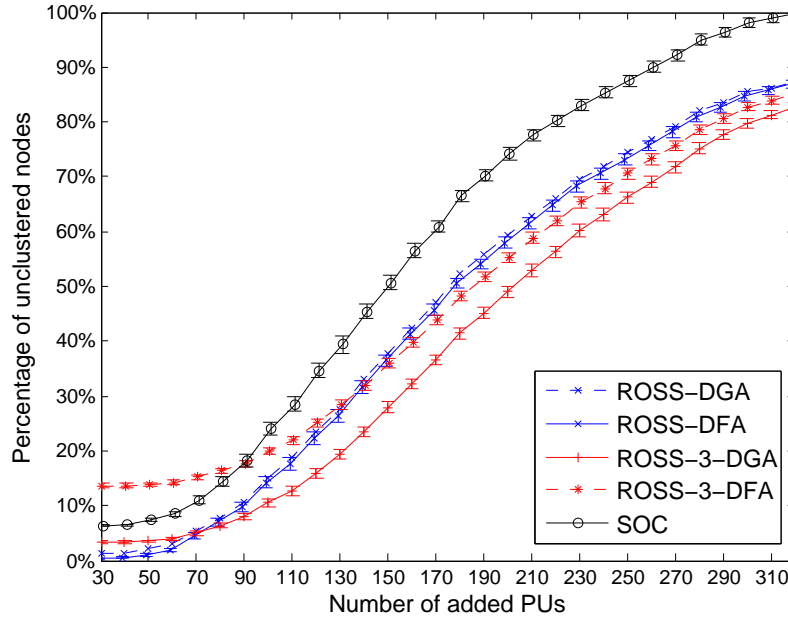
**Figure 4.15** Number of CRs which are not included in any clusters,  $N = 100$

From the Figure 4.15 and 4.16, we can see greedy versions of ROSS is more robust than their counterpart variant of ROSS. When the network is more dense, the improvement on cluster sizes and robustness by the greedy search is more obvious.

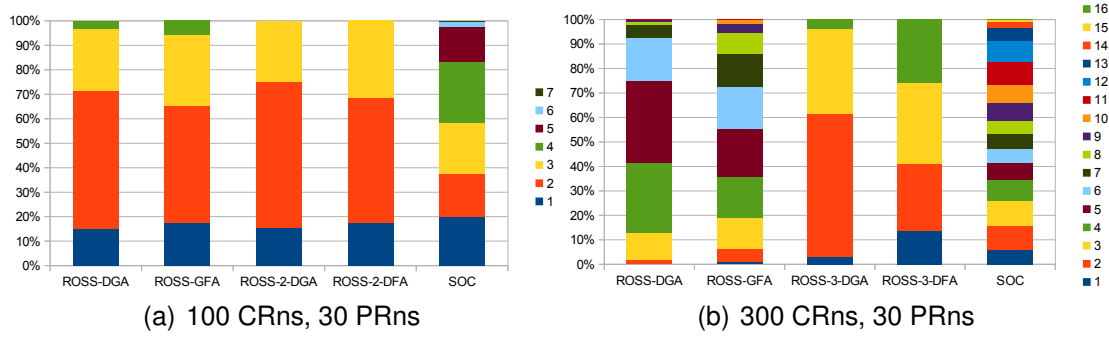
#### 4.6.2.3 Cluster Size Control

Cluster size analysis is made when the number of PRs is 30.

We see in Figure 4.17(a), when variants of ROSS are applied, most CRs are included into clusters with size of 2, thereinto, ROSS-2-DGA achieves the some homogeneous result, i.e., , there is no cluster whose size is greater than 3, and the number of CRs in 2 node cluster is greater than that resulted from ROSS-2-DFA. This is due to in the phase that debatable nodes clarify their membership, greedy search not only increases the number of CCC of relevant clusters, but also lets debatable nodes stay in smaller cluster, as shown in algorithm 4. SOC doesn't have size control feature thus the cluster sizes diverge greatly. In a more dense network with 300 CRs, where desired size is 3, 94% of CRs are integrated into 2 or 3 node clusters by ROSS-3-DGA, as to ROSS-3-DFA, 13%



**Figure 4.16** Number of CRs which are not included in any clusters,  $N = 300$



**Figure 4.17** Distribution of CRs in clusters with different sizes

CRs constitute singleton clusters, and 27% CRs are within 4 node clusters. Cluster size spans over a large range for schemes which don't have cluster size control mechanism. As to ROSS-DGA, ROSS-DFA and SOC, 95% of CRs stay in clusters whose sizes are smaller than 8, 9 and 14 respectively.

## 4.7 Conclusions and Future Work

We investigate extensively the robust clustering problem in CRN, which is important to form clusters which maintains unbroken to the greatest extent possible under primary users' activity. We prove the NP hardness of the problem and one distributed and light weighted clustering scheme ROSS-DGA is proposed. The clusters resulted from ROSS-DGA and its faster version ROSS-DFA are less vulnerable compared with other distributed clustering schemes, and demonstrates similar survival rate with centralized scheme under primary users' influence. An light weighted cluster size control mechanism is contained in both ROSS-DGA and ROSS-DFA, which is advantageous for coopera-

tive sensing and network operation with clusters. Furthermore, considerable less control messages are generated when compared with other clustering schemes.



# 5

## **Spectrum Aware Virtual Coordinates Assignment and Routing in Multihop Cognitive Radio Network**

### **5.1 Introduction**

Cognitive radio technology is promising to solve the significant shortage of spectrum, which is due to proliferation of wireless devices. According to the definition of FCC (Federal Communications Commission in U.S.), cognitive radio is a device which is able to sense, measure, or learn its environment and accordingly tune its radio operating parameters (like center frequency, bandwidth and transmit power) on the fly, i.e. during operation. In this paper cognitive radio equipment is also called secondary user. Together with these features secondary user is allowed to reuse licensed spectrum of so called licensed user.<sup>1</sup> The cognitive radio devices are capable of vacating a spectrum band if the primary user reappears in order not to cause harmful interference to licensed users.

Since primary user's activity demonstrates different patterns [51], the availability of licensed spectrum exhibits different dynamics accordingly. In certain scenarios the licensed spectrum occupancy stays available for fairly long time, e. g., TV white space [68]. In that case the licensed spectrum occupancy can be seen as static during a long period of time. In other scenarios primary user's state changes frequently, but measurements [96, ?] show that the percentage of time that licensed spectrum is occupied at a specific location or during a certain period of time doesn't change, i.e. in city down town during the work time, the duty circle of spectrum occupancy by cellular network is stable.

To fully exploit the potential of the secondary spectrum, it is crucial to investigate routing in dynamic spectrum environment. The dynamic availability of spectrum causes frequent

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<sup>1</sup>Terms licensed and primary, user and node, as well as spectrum band and channel are used indistinguishably in the following paper.

break down of links between secondary users, and leads to prevalent topology changes, which makes spectrum aware routing difficult but essential.

Recent measurement in [?] shows the spectrum occupancy doesn't have significant spatial correlations between different locations. It follows that licensed spectrum is used by primary users heavily in some areas, whereas in the rest area licensed spectrum is available over longer time spans for secondary to use. It is obvious to see that a routing path is better to go through the areas where primary users occupation is lower, as this alleviates or avoids the burden to cope with changing or totally occupied spectrum when forwarding packets potentially with latency requirements. Geographic routing is a natural choice to realize this geography sensitive routing path. Geographic routing is light weight regarding the determination of next hop, and achieves high scalability in various wireless networks [12]. Merely knowing the geographic locations of its neighbours and the destination, a node is able to locally choose the next hop which has the smallest distance to the destination. However, in CRN dynamic link state renders geographic routing unsuccessful since packets are forwarded to the destination through the shortest path rather than avoiding areas heavily influenced by primary users.

To enable geographic routing in CRN, in this paper we propose SAViC, spectrum aware virtual coordinates for secondary users in multi-channel multi-hop CRN. The virtual coordinate is independent of real geographic position, and has been proposed to represent for example properties of the media instead like, link quality [?] or hop numbers [26]. Following this line of thought, our proposed virtual coordinates in this paper represent the spectrum occupancy of primary users. On top of this, we propose that the geographic routing scheme then decides the next hop with Euclidean distance metric, and detours the area affected by primary users, or cuts through the area with lower spectrum occupancy. With SAViC, geographic routing imposes little computation on deciding the next hop, and requires less communication cost transmitting packet to the next hop. As to our knowledge, this is the first work integrating the spectrum usage by primary users into network coordinates in order to support geographic routing in CRN, which carries meanings especially for those resource restricted devices which want to work with licensed frequency band. The remainder of the paper is organized as follows, after reviewing related work in Section II, system model is introduced in Section III. Assignment of SAViC is explained in Section IV, followed by opportunistic access during transmission in Section V. Section VI gives performance evaluation, concluding remarks are given in the last Section.

## 5.2 RELATED WORK

When secondary users are static and primary users' operation activity is known, i.e., primary users occupy a certain channel for long time, or they occupy a channel with fixed probability, then centralized routing schemes for CRN can be designed[74]. But as centralized scheme requires sensing result from each secondary user in the network, thus suffers from any changes of channel state of secondary users [10], besides, one centralized controller is needed to calculate the routing path on the basis of collected information from the network [74, 75]. Considerable amount of distributed schemes are proposed to cope with routing in CRN where spectrum state is usually considered to be rapid changing. [25] proposes CAODV (Cognitive Ad-hoc On-demand Distance Vector) and let each CR node explore all channels and stores route for each available channel. CAODV requires frequent messages exchange between secondary users to maintain the up to date

connections on each channel due to PU's activities, which is a burden for secondary user when primary users' activity is intense. [84] improving the DSR scheme (Dynamic Source Routing) by letting RREQ messages record spectrum availability, link quality and congestion possibility along routing paths, but it also suffers from frequently changing channel state.

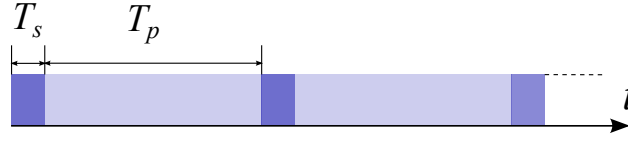
To cope with the rapid change of channel state, some routing schemes abandon routing table and let the transmitter decide the next hop for each single packet based on spectrum state between transmitter and neighbours. When there is packet to send, secondary user evaluates channel availability based on the statistics of sensing history [62], or the prediction on channel availability in the forthcoming time slot [61], then secondary user chooses the favoured channel and next hop node to send out the packet. Distance to the destination is also a consideration for choosing next hop. Such per-packet forwarding paradigm reacts swiftly on the fast changing channel state, but it requires more powerful computation power on secondary users. Firstly, that scheme produces high computation complexity on determining the channel and next hop node, secondly, specifically designed MAC mechanism and large amount of control messages are needed to coordinate the communication between the sender and the potential next hop nodes, these aspects make it uneconomic for many networks, e.g. wireless sensor network operating with licensed spectrum [87]. Furthermore, as this kind of routing paradigm emphasizes on finding the maximal transmission opportunity of secondary spectrum, the selection on preferred channel decreases the scope of next hop neighbours, thus it may yield route which does not reach the destination [51, 83].

Chowdhury et al. [31] proposes *SEARCH* which is a valuable attempt to avoid the primary users' influences on routing path on the basis of geographic routing. In *SEARCH*, the source node launches geographic routing on each channel, and every routing path bypasses the nodes where corresponding channel is unavailable. Paths on different channels will merge on the nodes where path circumvent happens, in case such change of path and switch of channel lead to shorter time needed to send packets to destination. After receiving the routing message on each channel, the destination decides the shortest path and sends back notifications along the chosen path. The routing path is blocked when one primary user locating along it changes its state from OFF to ON, thus source node needs to periodically launch route request to update the routing path which may have been invalid. *SEARCH* adopts routing table and doesn't involve frequent overhead exchanges and risk of failing to reach the destination.

### 5.3 SYSTEM MODEL

We consider a CRN composed with secondary users which are randomly and statically deployed in a plane. There are orthogonal licensed channels denoted by set  $C$ , and secondary user is allowed to use any of them if no primary user is detected on that channel by the secondary user. One common control channel (CCC) in license-exempt band is available for all secondary users to exchange control messages. Only one licensed channel is used for payload transmission. Primary users are static, and they occupancy spectrum in a constant manner, e. g., the percentage of time that they access a certain channel is static in any period of time.

Proactive spectrum sensing is conducted locally and periodically as Figure 5.1 shows.



**Figure 5.1** Sensing duration  $T_s$  and sensing period  $T_p$

The sensing duration  $T_s$  includes both detection time in physical layer and the decision synchronisation time. Sensing period  $T_p$  is the time between two successive sensing durations. If the channel is sensed as busy<sup>2</sup> in sensing duration, which means at least one primary user in the vicinity is in ON state, we say the state of primary user is labelled as ON in the following sensing period  $T_p$ . If not a single primary user is sensed, primary users in vicinity in the following sensing period is said to be in state OFF. Secondary user senses each licensed channel for time  $T_{access}$  with round robin scheduling, and records statistics of ON/OFF states of that channel at its place.

## 5.4 Spectrum Aware Virtual Coordinates

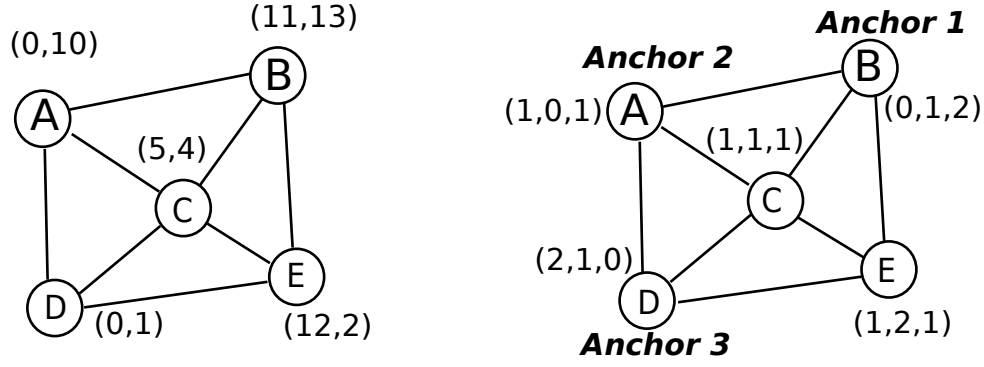
Virtual coordinate has been proposed in sensor or ad hoc network [26, ?]. In the left part of Figure 5.2, nodes are labelled with physical positions. The right hand side part shows the same network assigned with triplet virtual coordinate for each node according to VCap [26], where each coordinate denotes the minimal number of hops away from corresponding anchor. This kind of virtual ordinate is obtained based on anchors which locate at the edge of network, which belongs to tree based virtual coordinates. Anchor messages are broadcasted from anchor, which contain one counter recording the number of hops travelled, the minimum counter of the arriving anchor messages becomes the virtual coordinate of the arrival node. Except for the hope numbers away from certain anchor node, virtual coordinate can also be composed with link quality [?] in wireless sensor network. The hop based virtual coordinate is independent on actual physical position, but as the supports greedy geographic routing successfully [26, ?]. For example, when the source-destination is B and D, the greedy geographic routing based on euclidean distance calculated with virtual coordinate in both networks obtains the same routing path:  $B \rightarrow C \rightarrow D$  which is one the the shortest paths.

In this paper, we propose licensed spectrum aware virtual coordinate in CRN, which enables geographic routing to find the path with better available spectrum. Figure 5.3 shows one CRN where secondary users are assigned one virtual coordinate according to anchor 1. When nodes locating within primary users' transmission range, e. g., node A and C, their transmission opportunity is decreased due to sporadic spectrum, which increases the cost for packet transmission, e. g., transmission delay and energy consumption. We integrate this obstacle on transmission caused by spectrum scarcity into virtual coordinate.

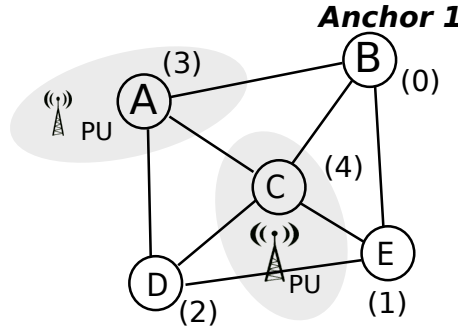
### 5.4.1 Assign Spectrum Aware Virtual Coordinate

As to SAViC, each anchor initiates anchor messages which flood over the network, and results in the corresponding virtual coordinate. Several anchors are needed to assign unique

<sup>2</sup>Concrete sensing techniques is not discussed in this paper.



**Figure 5.2** Left: nodes with physical locations, Right: nodes with doublet virtual coordinate, each virtual coordinate is the number of hops away from corresponding anchor. Connecting lines denote the communication is possible.



**Figure 5.3** A network under primary users' influence assigned with SAViC, only anchor 1 is involved. Flooding of anchor messages is not shown.

virtual coordinate for each secondary user. How to select anchors is out of the scope of this paper. In the following, we introduce how is one virtual coordinate is decided on each node with respect to one anchor.

Initially, the virtual coordinate on each node is set as a big positive value. An anchor message is generated on the anchor, which contains a counters *counter* and set as 0. The anchor message is broadcasted on control channel. The influence of primary users on a secondary user is quantified as spectrum availability  $\lambda$  on that secondary user. The bigger value indicates heavier spectrum occupation by primary users.  $\lambda$  will be discussed in section 5.4.2 and 5.4.3.

When a node  $i$  receives one anchor message,  $i$  compares its current virtual coordinate with the sum of the  $\lambda$  and *counter*1 in the arriving anchor message. If the sum is greater than its current virtual coordinate, which indicates that the path traversed by anchor message exposes to more tense activity of primary users, node  $i$  drops the anchor message. If the sum is smaller than its current virtual coordinate, the node set its virtual coordinate as the sum and updates *counter*1 contained in the anchor message before forwarding. This process is presented as Algorithm 5. This phase ends after a period of time to make sure each node obtains its virtual coordinate. Secondary user obtains virtual coordinate after each anchor nodes sequentially flood the anchor messages.

In the following, we introduce the normalized spectrum availabilities  $\lambda$  on secondary user, and the two resultant virtual coordinates, duty circle based virtual coordinate and blocking time based virtual coordinate.

---

**Algorithm 5:** Secondary user  $i$  obtains  $vc_i$  with respect to an anchor

---

**Input:**  $vc_i = M$ ,  $M$  is one big positive number

---

```

2 if  $i$  is anchor then
4    $vc_i = 0$ ;
6   set  $counter1 = \lambda_i$  in anchor message;
8   broadcast anchor message;
9 end
11 if receive anchor message then
13   if  $counter + \lambda_i \geq vc_i$  then
15     drop anchor message;
16   else
18      $vc_i = counter + \lambda_i$ ;
20     set  $counter = vc_i$  in anchor message;
22     broadcast anchor message;
23   end
24 end

```

---

## 5.4.2 Normalized Spectrum Availability on Secondary User

Based on the statistics of primary user's ON/OFF states in time duration  $T_{assessment}$  which contains multiple  $T_s$ , secondary user  $i$  characterizes the likelihood that one licensed channel, say  $k$ , is available at its own position with *duty circle*, which is

$$\gamma_i^k = \frac{\Delta_{OFF}}{\Delta_{OFF} + \Delta_{ON}}, \quad (5.1)$$

where  $\Delta_{OFF}$  is the number of sensing periods when channel  $k$  is sensed as OFF in  $T_{assessment}$ . To implement SAViC whose resultant Euclidean distance between two nodes reflects both influence from primary users and distance in terms of hops, we need to design a normalized quantified spectrum availability  $\lambda_i$ .

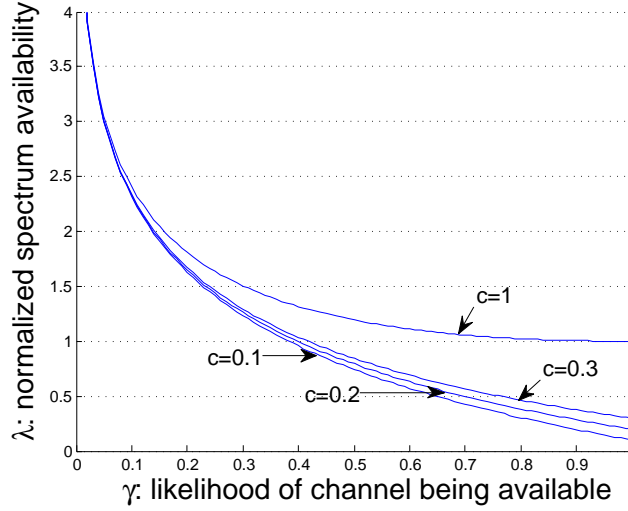
### 5.4.2.1 Single licensed channel

When there is only one licensed channel in CRN (the superscript of channel  $\lambda$  is omitted), the normalized spectrum availability on node  $i$  is proposed as,

$$\lambda_i = -\ln \gamma_i + c \cdot \gamma_i \quad (5.2)$$

The reason to choose this form is as follows. When one anchor message which originates from anchor  $X$  is forwarded from node  $a$  to  $b$  without being dropped, with function 5.2, the distance based on virtual coordinate reflects both the spectrum availability and geographic distance in terms of hops between the two nodes. Based on Algorithm 5 and Formula 5.2, the distance on dimension  $X$  is,

$$\begin{aligned}
 |x_b - x_a| &= \sum_{i \in P_{(a,b)}} (-\ln \gamma_i + c \cdot \gamma_i) \\
 &= -\ln \left( \prod_{i \in P_{(a,b)}} \gamma_i \right) + c \cdot \sum_{i \in P_{(a,b)}} \gamma_i
 \end{aligned} \quad (5.3)$$



**Figure 5.4** Normalized spectrum availability with respect to the likelihood of spectrum being available one a node

where  $P_{(a,b]} = (\dots, b)$  denotes the list of nodes after  $a$  and till  $b$ , which forward the same anchor message. The first item is logarithmic product of the likelihood of spectrum availability on nodes in  $P_{(a,b]}$ . The product is the likelihood that one message travels from node  $a$  to  $b$  without hampered by primary users. The second item denotes number of hops, which can be seen clearly when  $\gamma_i = 0$  for node  $i \in P_{(a,b]}$ .

$\lambda_i$  needs to be monotonically decreasing with respect to  $\gamma_i$ , so that the less spectrum availability results in bigger cost for communication, thus there should be

$$\frac{\partial \lambda_i}{\partial \gamma_i} = c - \frac{1}{\gamma_i} < 0 \quad (5.4)$$

hence the tuning parameter  $c$  should be smaller than 1. In the simulation part, we choose  $c = 0.2$  so that  $\lambda$  visibly reflects the changes of  $\gamma$  when  $\gamma$  is not too small, as Figure 5.4 shows.

#### 5.4.2.2 Multiple licensed channels

When multiple licensed channels is allowed to use without interfering primary users, one node can switch to an another channel which is at present available to send or forward packet, then the normalized channel availability is,

$$\gamma_i = 1 - \prod_{k=1}^{|C|} (1 - \gamma_i^k) \quad (5.5)$$

Similar with Formula 5.2, the normalized spectrum availability on node  $i$  when multiple secondary channels are available is,

$$\begin{aligned} \lambda_i &= -\ln \gamma_i + c \cdot \gamma_i \\ &= -\ln(1 - \prod_{k=1}^{|C|} (1 - \gamma_i^k)) + c \cdot (1 - \prod_{k=1}^{|C|} (1 - \gamma_i^k)) \end{aligned} \quad (5.6)$$

### 5.4.3 Normalized Longest Blocking Time on Secondary Users

Channel utility introduced in previous subsection characterizes the likelihood that secondary user is allowed to forward packets, but it fails to reflect the availability of spectrum in a finer granularity of time. For instance, in the period of time  $T_{access}$  to access the spectrum availability, one channel which frequently changes between state ON and OFF due to primary users' violent operation may have the same likelihood of available spectrum with the channel where primary user sojourns on state ON for long time. This difference has direct consequence on delay when the likelihood of spectrum availability on PU affected secondary nodes is homogeneous.

Let  $T_{ON}^k$  be the length of time period that channel  $k$  is not available, there is  $T_{ON}^k = n \cdot (T_s + T_p)$ , where  $n$  is the number of consecutive sensing duration that channel  $k$  is sensed as busy.  $T_{ON}^k$  is recorded within  $T_{access}$ , and we use  $\tau^k = \overline{T_{ON}^k}$  to denote the average value of the time duration that channel  $k$  is occupied by primary user, which is the maximum time period that secondary user is blocked from sending/forwarding.

#### 5.4.3.1 Single licensed channel

In single licensed channel scenario, the normalized maximum blocking time on node  $i$  is (superscript  $k$  is omitted),

$$\lambda_i = f(\tau_i) = \gamma_i \cdot \tau_i + b \cdot e^{-\gamma_i \cdot \tau_i} \quad (5.7)$$

The first item is the product of blocking time and likelihood of spectrum availability, not that the latter is identical for any PU affected secondary user and thus can be regarded as constant. The second item denotes hop, when PU affected secondary users are out of any primary user's transmission range.

Same with the analysis in section 5.4.2, when one anchor message travels through path  $P_{(a,b)}$ , the distance on the corresponding coordinate dimension is the sum of the normalized longest blocking time, which is the function of the sum of maximum blocking time on the cascaded nodes on the trajectory of anchor message,

$$\begin{aligned} |x_b - x_a| &= \sum_{i \in P_{(a,b)}} (\gamma_i \cdot \tau_i + b \cdot e^{-\gamma_i \cdot \tau_i}) \\ &= \gamma_i \cdot \sum_{i \in P_{(a,b)}} \tau_i + b \cdot e^{-\gamma_i \cdot \sum_{i \in P_{(a,b)}} \tau_i} \end{aligned} \quad (5.8)$$

Normalized longest blocking time  $\lambda$  is monotonically increasing with  $\tau_i$ , which requires

$$\begin{aligned} \frac{\partial \lambda_i}{\partial \tau_i} &= \gamma_i - \gamma_i \cdot b \cdot e^{-\tau_i \cdot \gamma_i} > 0 \\ b &< e^{\gamma_i \cdot \tau_i} \end{aligned} \quad (5.9)$$

then we set the tuning parameter  $b$  as 1.



### 5.4.3.2 Multiple licensed channels

In multiple licensed channel scenario,  $\tau_i$  equals to the smallest maximum blocking time over all secondary channels on node  $i$ ,

$$\tau_i = \min \tau_i^x, x \in C \quad (5.10)$$

The normalized maximum blocking time on node  $i$  is as Formula 5.7 shows.

In following part of this paper, the virtual coordinate based on normalized spectrum utility is referred as *spectrum availability based VC*, and The virtual coordinate based on normalized maximum blocking time is denoted as *blocking time based VC* out of convenience.

When  $\lambda$  on secondary nodes is identical, the resultant SAViC appears to be similar with hop based virtual coordinate. In reality, as the measurement shows in [?], heterogeneity of spectrum usage by primary users is very normal, besides, the two kinds of virtual coordinates make it easier to find out such heterogeneity. [?] also shows within certain frequency band, primary users' activity is stable for hours, e. g., cellular network. When primary user's operation pattern changes, e. g., occupy spectrum with increased duty circle, then SAViC needs to be reimplemented.

## 5.5 Geographic Routing and Opportunistic Spectrum Access

Although spectrum aware virtual coordinate is the main concern of this paper, we also introduce the geographic routing to be used as it affects the routing result directly. With geographic routing, packet sender/forwarder chooses the neighbour which has smaller Euclidean distance to the destination. The distance between node  $i$  and destination  $d$  is  $\sqrt{(x_d - x_i)^2 + (y_d - y_i)^2 + (z_d - z_i)^2}$ , when virtual coordinate can be denoted as  $\{x, y, z\}$ . An trivial improvement on greedy geographic routing is implemented in network layer to mitigate the dead end problem. When routing protocol reaches dead end node  $u$  which is closest to destination,  $u$  adds its ID to the packet as taboo before forwarding the packet to  $v$  which is closest to the destination in its neighborhood. The packet will not be sent to the nodes whose IDs appear to be taboos.

Buffer is implemented on each node, where packets stay temporally when no unoccupied licensed spectrum is available. Secondary user resend buffered packet every period of time, and drop it if there is still no available channel after trying for 10 times.

In multiple channel CRN, after one node deciding on the next hop via geographic routing, which channel to use needs to be answered. This problem involves considerations from many aspects, such as minimizing channel switch cost [83], mitigating co-channel interferences [57] etc.. We adopt a lightweight heuristic method in this paper. When there is packet to send and the next hop is decided, packet sender chooses the channel in descending sequence with channel's metric, i.e., likelihood of channel availability, or blocking time. The sender chooses the channel with the best metric, then conducts spectrum sensing in the immediately following sensing duration to determine the channel's usability. If the channel is sensed as free to use, sender transmits *request\_channel\_x* to the next

hop on the control channel, when it receives the answering message *channel\_x\_available* from that node, it starts communication on channel  $x$  in the following sensing period. If the channel is sensed to be busy before or among the transmission, or it receives *channel\_x\_unavailable* message from next hop node, the sender moves to the channel with the second best metric, and conduct the same procedure as described above.

## 5.6 Performance Evaluation

In this section, we will present the performance of geographic routing together with SAViC. Both metrics of spectrum availability and blocking time. Prior to that, we introduce the set-up of simulation.

### 5.6.1 Simulation Setup

In this section, we introduce the deployment of the primary users to generate various spectrum availability in the network, then introduce the important parameters in simulation. Different from [26] where simulation is conducted without considering any activities in MAC and physical layer, simulation in this paper deploys a wireless environment which is close to reality, e. g.,interferences and channel shadowing are involved.

#### 5.6.1.1 Primary Users

In simulation, primary user alternates state between ON and OFF as a two-state discrete time Markov chain (2DTMC) [67]. The probability that it changes from one state to the other, or stays in the same state is called transition probability. Transition probability further decides the stationary probability of 2DTMC, which represents the percentage of time that primary user is in state ON or OFF in a long run. The relationship between stationary probability  $\Pi = \{\pi_{\text{ON}}, \pi_{\text{OFF}}\}$  and duty circle  $\gamma$  is,

$$\lim_{T_{\text{assessment}} \rightarrow \infty} \gamma = \pi_{\text{OFF}} \quad (5.11)$$

Transition probability also decides the continuous sojourning time of primary user on a certain state, which affects the longest blocking time sensed by secondary users. Hence, by adjusting transition probability, we can let primary user operate with desired intensity, i.e. stationary probability for being in state OFF, or continuous sojourning time of being on state ON. We denote stationary probability of state OFF as  $P_{\text{OFF}}$ , and the maximal blocking time as  $T$ . In the following, we only use  $P_{\text{OFF}}$  and  $T$  to define primary user's dynamics, and omit mentioning the transition probability. The time unite of the DTMC for primary user to follow is 0.1s.

As spectrum availability based and longest blocking time based virtual coordinates are designed for CRN which is influence by certain primary user activity, we design two primary user distributions. As a result, we design two categories of primary user settings to evaluate the routing performance assisted by the two categories of virtual coordinate respectively.

- As to spectrum availability based virtual coordinate, two primary users are located in the CRN which can not affect all the nodes in CRN, as shown in Figure 5.6(a).
- For blocking time based virtual coordinate, network is evenly covered by primary users which have the same duty circle, but some primary users have different blocking time with the others, as Figure 5.9 shows.

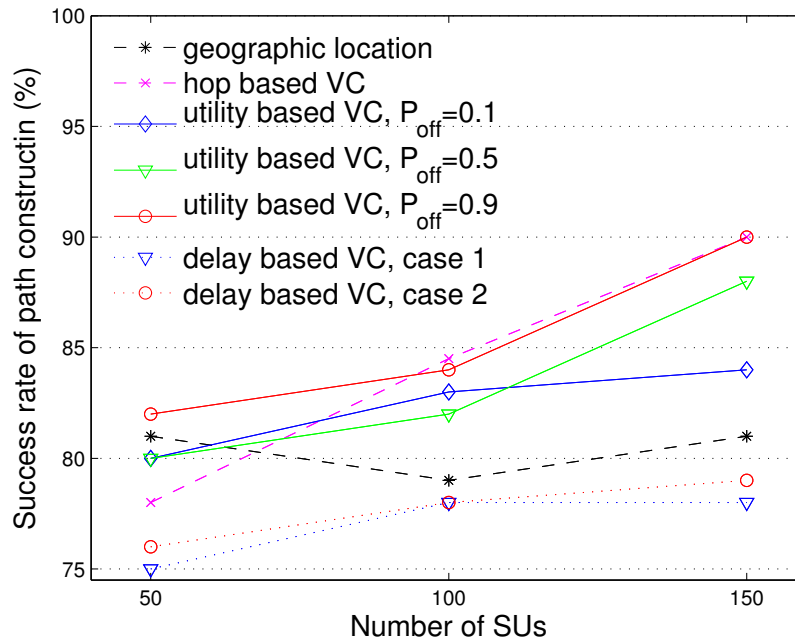
When multiple channel scenario is to be investigated, existing primary users simply start to work with current and additional channels, and there is no new primary users appear.

### 5.6.1.2 Parameter Setting

Simulation is conducted with INET framework provided by OMNeT++ simulator [?], which comprises both generation of SAViC and following geographic routing. Secondary users are randomly distributed in a square area and 6 nodes which locate at the edge are deployed as anchors.

### 5.6.2 Success Rate of Geographic Routing on Finding Path

We evaluate SAViC's reachability, i.e. given the virtual coordinate of destination, geographic routing forwards packet from source to the the node with the desired virtual coordinate. The comparisons are real geographic location, and hop based virtual coordinate according to VCap [26]. We deploy 6 anchors and the there is no duplicated virtual coordinate among the resultant virtual coordinates.



**Figure 5.5** Reachability of different virtual coordinates, the average number of neighbors is 6, 12, and 14

In order to evaluate the effectiveness of coordinates to support geographic routing, we design different configurations of primary users. As to duty circle based VC, two primary

users are randomly deployed in the network. As to delay based VC, we configure 9 primary users to evenly cover the network, among of them, 4 primary users have different maximal blocking time with the rest. Under one configuration of primary users, 1000 random CRN is generated and in each CRN one far departed pair of source and destination is chosen to test.

Figure 5.5 shows, spectrum availability based virtual coordinate supports geographic routing to achieve similar reachability with hop based virtual coordinate<sup>3</sup>, which is better than that with real geographic location. Blocking time based virtual coordinate performs a little bit worse than other coordinates. In summary, after integrating the primary user's influence, SAViC supports geographic routing to achieve comparable success rate of path construction with conventional virtual coordinate and real geographic location.

### 5.6.3 Routing Performance

We sequentially present the routing performance of SAViC based on spectrum availability and blocking time respectively. In more details, spectrum availability SAViC is compared with hop based virtual coordinate VCap and *SEARCH*. The reason to choose *SEARCH* [31] is it is on the basis of geographic routing and utilizes routing table in the interval of updates, thus it requires less computation ability and overhead exchanges. The time interval for *SEARCH* to update routing tables of the nodes on routing path is 5s. Both single and multiple licensed channel scenarios are investigated for the three solutions.

#### 5.6.3.1 Spectrum Availability Based Virtual Coordinate

We start by looking into the performance of SAViC in single channel scenario.

We start with a case study, two primary users locate at the centers of dashed circles as shown in Figure 5.6(a). VC based on spectrum availability and VCap (hop is its metric) are assigned to secondary users separately. The red dashed path in Figure 5.6(a) is formed by geographic routing with VCap, which cuts across the primary users' affecting area and thus suffers great packet loss. The black dash and blue solid paths are formed with spectrum availability based virtual coordinate, the two paths are formed when primary user's working intensities  $P_{\text{OFF}}$  is 0.1 and 0.9 respectively. These two paths vividly illustrate that utility based virtual coordinate successfully integrates the spectrum scarcity in CRN network, and decomposes a large part of routing decision. The paths of *SEARCH* is not drawn here as the routing path is possible to change after path update. We keep the primary users in the middle of the network, for each activity intensity, 50 CRNs where secondary users are randomly located are generated. Figure 5.6(b) shows the PDR of spectrum availability based virtual coordinate is high except for a minor decline when  $P_{\text{OFF}}$  is between 0.5 and 0.8, which is contradictory to the monotonically increasing trend of hop based virtual coordinate. This can be explained by the path snapshot in Figure 5.6(a). When channel is sensed to be scarce (primary users access channel intensively),

<sup>3</sup>The numerical result of hop based virtual coordinate coincides with the simulation result presented in [26] under the same network density

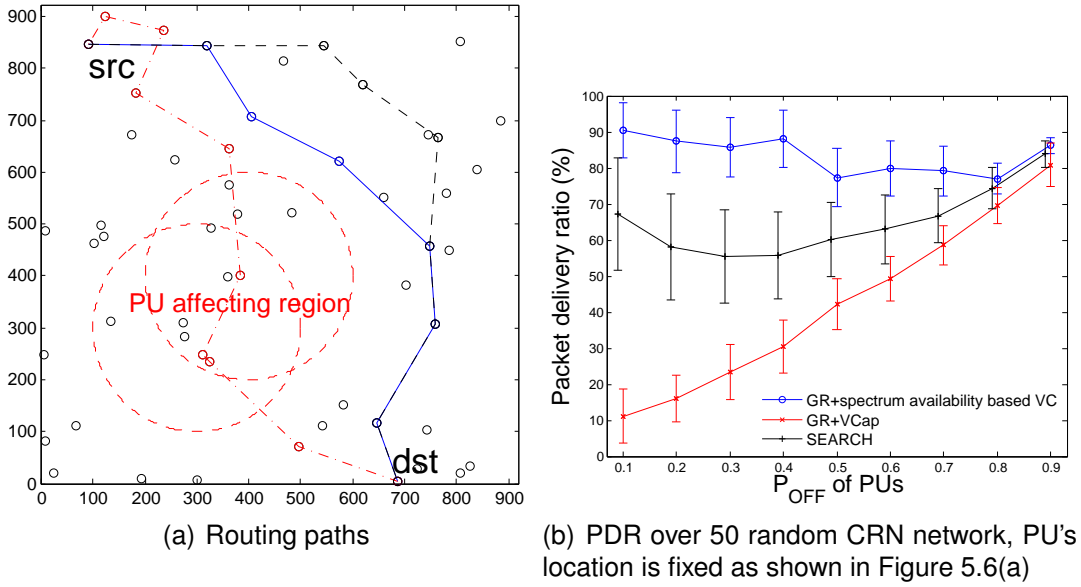


Figure 5.6 Routing paths and corresponding PDR

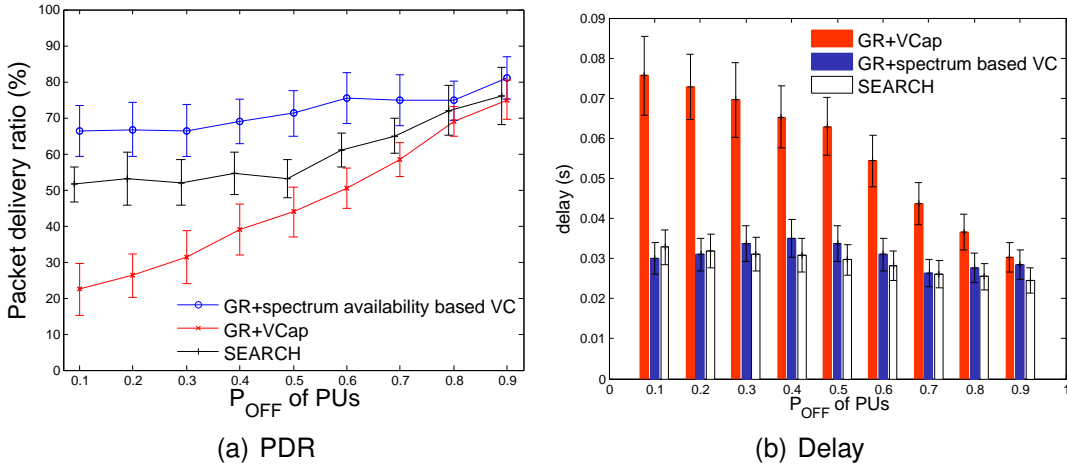


Figure 5.7 Packet delivery ratio with single secondary channel, over 50 randomly located CR nodes and PUs

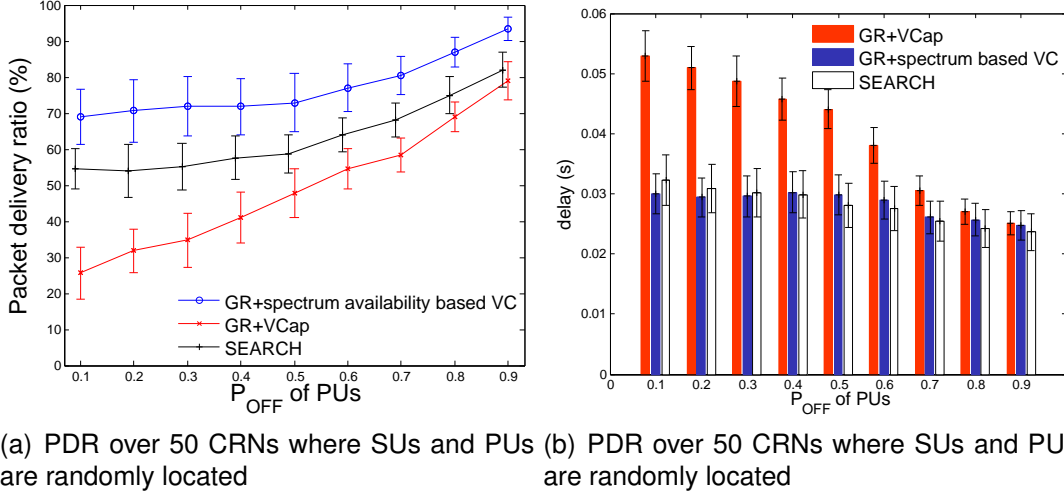
path generated is far away from the affected area and circumvents completely. When primary users become less intensive, routing path moves closer to that area. In other words, the weaker dynamics of primary users attracts path and result in packet drop. When  $P_{OFF}$  approaches to 1, spectrum availability based virtual coordinate becomes actual hop based virtual coordinate as the link metric in formula 5.2 becomes zero.

The paradox of more licensed spectrum leads to worse PDR also happens to *SEARCH*, which declines first and increases later on. When channel is heavily utilized by primary users, the routing request is more likely to encounter operating primary user, then a node out of the primary user affecting area is chosen as next hop, so that the path experiences less packet loss (with the price of more hops). When primary users become less intense, routing request is more likely to traverse the affected areas, as a result, the routing path experiences packet loss due to the primary users in that area before next route update.

Figure 5.7(a) shows the PDR when both primary and secondary users' locations are random. SAViC's performance deteriorates because the source and destination may be in-

fluenced by primary users, so that a path completely detour the primary users' area is impossible. where geographic routing has no means to detour the affected areas. In figure 5.7(b), SAViC and SEARCH achieve lower delay although forwarding more packets, which means SAViC is effective to facilitate geographic routing to avoid PU affecting areas.

Now we introduce the routing performance in multiple channel scenario, where two licensed channels available, but only one is allowed for payload transmission.



**Figure 5.8** Packet delivery ratio with multiple secondary channel scenario

In this part of simulation, we follow the setting of single channel scenario, except that secondary users have at most two licensed channels.

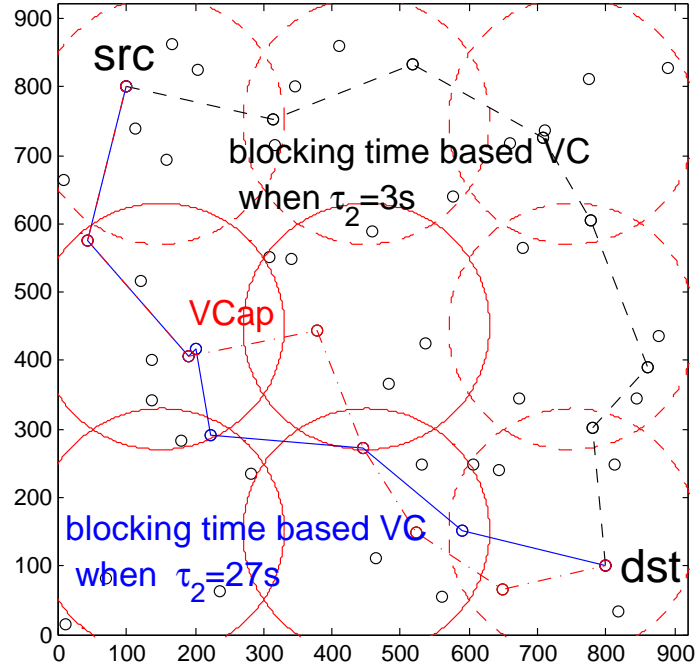
Thanks to the second channel, the packet delivery ratio is increased as shown in Figure 5.8(a), and delay is decreased as depicted in Figure 5.6(a). SAViC still outperform the other schemes especially in the aspect of PDR.

### 5.6.3.2 Longest Blocking time Based Virtual Coordinate

As discussed in section 5.4.3, spectrum availability based virtual coordinate doesn't reflect the sparsity or abundance of spectrum well when the the likelihood of spectrum availability is homogeneous in CRN. A CRN working with single licensed channel in Figure 5.9 is used to show the fail of spectrum availability based virtual coordinate. Two items are used in the following to make the analysis tidy.

$T_1$	Maximal blocking time of primary users whose transmission ranges are solid circles in Figure 5.9
$T_2$	Maximal blocking time of the other primary users

In the network, 9 primary users evenly distributed,  $P_{OFF} = 0.5$  for each of them. For the primary users denoted by the solid circles, maximal blocking time  $T_1 = 3s$ , and  $T_2 = 1s$  and  $3s$  for the other primary users. When  $T_2 < T_1$ , the resultant routing path is in black



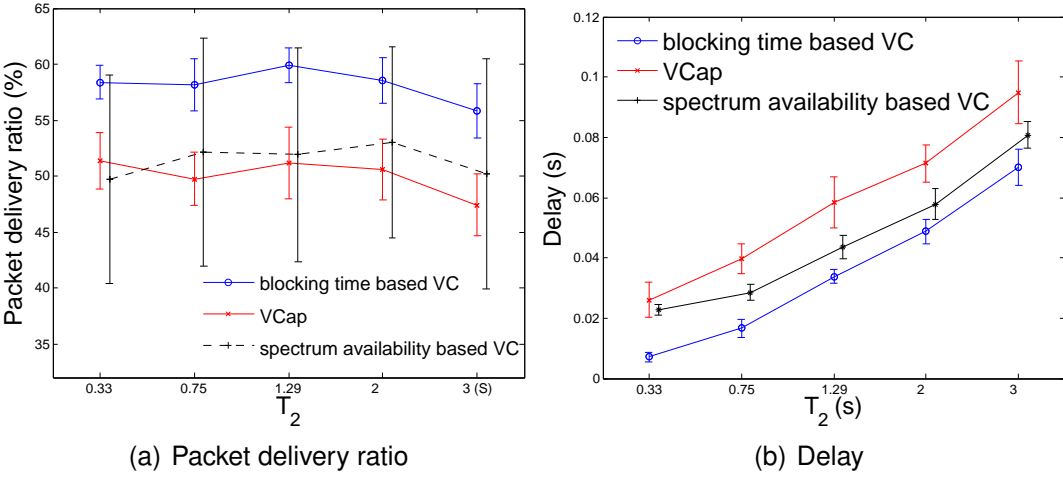
**Figure 5.9** Routing paths in one network,  $T_1 = 3s$ . Circles denote the transmission range of primary users.

and dashed, which goes through area where primary users have shorter maximal blocking time. When  $T_2 = T_1$ , the resultant routing path largely converges with the path with VCap.

The ineffectiveness of spectrum availability based virtual coordinate in case of identical  $P_{\text{OFF}}$  is observed in Figure 5.9. In this case a different characteristic, i.e., the longest blocking time, which shows the geographically diverse characteristics of spectrum can be used. In our simulation,  $P_{\text{OFF}} = 0.9$  for all primary users, but they are diverse on sojourn time, i.e.  $T_1$  of primary user is 3s, and  $T_2$  is shorter. We randomize the location of secondary users in 50 networks, and present the performance of blocking time based virtual coordinate to show its superiority on decreased end to end delay and PDR. In this part of simulation, we don't show the result of *SEARCH*, as it performs as bad as geographic routing with hop based virtual coordinate. The reason is the widespread primary users seriously hamper the routing requests to arrive at destination, consequentially most paths for forwarding the packets can not be constructed successfully.

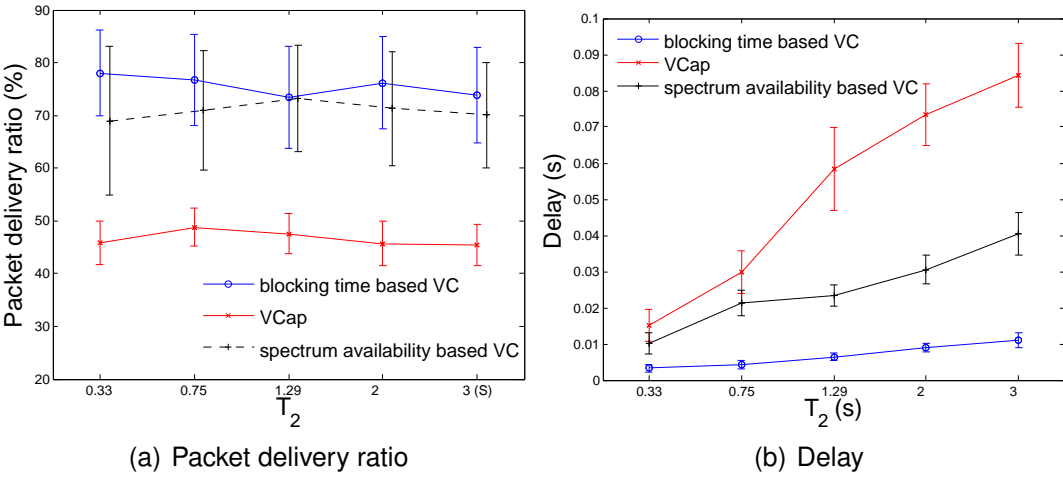
Figure 5.10(b) shows as  $T_2$  increases from 0.33s to 3s, the delay of successfully delivered packets also increases for both blocking time based virtual coordinate and VCap, but a constant gap exists in between. Whereas, the delay of spectrum availability based virtual coordinate is random as respect to sojourn time, the reason is the routing metric in this scenario doesn't involve blocking time imposed by primary users.

The packet delivery ratio shown in Figure 5.10(a) are constant with both blocking time based virtual coordinate and VCap, because all the primary users have the same  $P_{\text{OFF}}$  which is 0.9. Particularly, blocking time based virtual coordinate achieves higher packet delivery ratio than the other two virtual ordinates, the reason is when the former is applied, less packets are dropped from buffer as the time of being blocked is shorter for the secondary users on the path.



**Figure 5.10** Geographic routing in single secondary channel scenario,  $P_{\text{OFF}} = 0.9$  for all primary users,  $T_1 = 3s$ ,  $T_2$  varies.

Now we have a look at the CRN with two licensed channels. As to performance of delay, because of the second available channel, blocking time based virtual coordinate achieves very delay, in contrast, spectrum availability based virtual coordinate still demonstrates obvious randomness, as is shown in Figure 5.11(b). Compare Figure 5.11(a) and 5.10(a), we can see the packet delivery ratio in two channel network is obviously higher than that in single channel network, as the second channel provides extra transmission opportunities. Blocking time based virtual coordinate achieves up to 10% better performance than that with spectrum availability based VC, the reason is packets in buffer have greater likelihood to be sent out before getting dropped.



**Figure 5.11** Geographic routing in two secondary channel scenario,  $P_{\text{OFF}} = 0.9$  for all primary users,  $T_1 = 3s$ ,  $T_2$  varies.

## 5.7 CONCLUSION

The proposed virtual coordinate SAViC reshapes the topology of cognitive radio network based on sensing results on spectrum availability. As SAViC adjusts the distance be-



tween nodes based on the communication obstruction caused by primary users, the virtual coordinate comprises a part of the routing decision, so that geographic routing is able to detour the areas seriously affected by primary user. Geographic routing with SAViC greatly simplifies the computation and communication burden on each secondary user involved in routing in CRN. Together with SAViC, geographic routing achieves better performances than other geographic routing designed for CRN through extensive simulation. This paradigm of routing is especially suitable for CRN network where the resource limited CR nodes can only support geographic routing.



# 6

## Conclusion

Cooperation is also one paradigm which is claimed to be able to improve the network performance. It requires extra control overheads because of organization.



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# List of Figures

3.1	System model: WBS cells and DTV systems . . . . .	16
3.2	QuasiSINR . . . . .	17
3.3	Distribution of maximal transmission power levels obtained from convex and linear programming respectively . . . . .	22
3.4	Layout of WBSs and TV contours . . . . .	30
3.5	Power consumed by different distributed spectrum allocation schemes under different ways deciding the maximal transmission power map . . . . .	31
3.6	QuasiSINR achieved by different distributed spectrum allocation schemes under different ways deciding the maximal transmission power map . . . . .	32
3.7	CDF of SINR on end users obtained by different CA schemes under different methods to decide the maximal transmission power map . . . . .	32
3.8	The average SINR of the 20% worst end terminals . . . . .	33
3.9	summed utility of all WBSes, which is the objective in problem <b>??fopt</b> . . . . .	34
3.10	Average transmission power of one WBSes . . . . .	34
3.11	quasiSINR: SINR at the reference point . . . . .	34
3.12	SINR on end users after channel allocation . . . . .	35
3.13	SINR on end users after channel and power allocation . . . . .	35
3.14	Convergence with three different schemes in one simulation instance . . . . .	36
3.15	Average Power consumption and QuasiSINR . . . . .	38
3.16	Cumulative distribution of SINR on all end terminals when applying different schemes . . . . .	38
4.1	Connectivity graph and the connectivity vector $\{D_i, G_i\}$ on each node. The available channels sensed by each CR node are: $V_A = \{1, 2, 3, 4, 5, 6, 10\}$ , $V_B = \{1, 2, 3, 5, 7\}$ , $V_C = \{1, 3, 4, 10\}$ , $V_D = \{1, 2, 3, 5\}$ , $V_E = \{2, 3, 5, 7\}$ , $V_F = \{2, 4, 5, 6, 7\}$ , $V_G = \{1, 2, 3, 4, 8\}$ , $V_H = \{1, 2, 5, 8\}$ . Dashed lines indicates two end nodes are within transmission range of each other. Each edge is labeled by the number of common channels between the two ends. . . . .	50
4.2	Possible clusters in dense CRN . . . . .	53

4.3	Number of clusters formed . . . . .	53
4.4	Clusters formation after the first phase of ROSS. Some nodes remain debatable nodes after the first phase. . . . .	55
4.5	debatable nodes and claiming clusters . . . . .	57
4.7	Final formation of clusters, common channels for each cluster is shown. .	59
4.8	Matrix Q . . . . .	62
4.9	Final clustering of the example CRN . . . . .	63
4.10	Number of common channels for non-singleton clusters, the numbers in the names of schemes annotate the desired cluster size. . . . .	65
4.11	Number of CRs which are not included in any clusters . . . . .	66
4.12	Distribution of CRs residing in Clusters with different sizes, as to ROSS with size control feature, the desired cluster size is 3. . . . .	67
4.13	Number of control messages . . . . .	68
4.14	Number of common channels for non-singleton clusters. As to ROSS with size control feature, $x = 2$ when $N = 100$ and $200$ , $x = 3$ when $N = 300$ . .	69
4.15	Number of CRs which are not included in any clusters, $N = 100$ . . . . .	70
4.16	Number of CRs which are not included in any clusters, $N = 300$ . . . . .	71
4.17	Cluster sizes . . . . .	71
5.1	Sensing duration $T_s$ and sensing period $T_p$ . . . . .	76
5.2	Left: nodes with physical locations, Right: nodes with doublet virtual coordinate, each virtual coordinate is the number of hops away from corresponding anchor. Connecting lines denote the communication is possible. .	77
5.3	A network under primary users' influence assigned with SAViC, only anchor 1 is involved. Flooding of anchor messages is not shown. . . . .	77
5.4	Normalized spectrum availability with respect to the likelihood of spectrum being available one a node . . . . .	79
5.5	Reachability of different virtual coordinates, the average number of neighbors is 6, 12, and 14 . . . . .	83
5.6	Routing paths and corresponding PDR . . . . .	85
5.7	Packet delivery ratio with single secondary channel, over 50 randomly located CR nodes and PUs . . . . .	85
5.8	Packet delivery ratio with multiple secondary channel scenario . . . . .	86
5.9	Routing paths in one network, $T_1 = 3s$ . Circles denote the transmission range of primary users. . . . .	87
5.10	Geographic routing in single secondary channel scenario, $P_{\text{OFF}} = 0.9$ for all primary users, $T_1 = 3s$ , $T_2$ varies. . . . .	88
5.11	Geographic routing in two secondary channel scenario, $P_{\text{OFF}} = 0.9$ for all primary users, $T_1 = 3s$ , $T_2$ varies. . . . .	88



# List of Tables

3.1	.....	30
3.2	.....	36
3.3	.....	37
4.1	Notations .....	49
4.2	Singalling overhead. Notations: $n$ -number of CR nodes in CRN, $h$ -number of cluster heads, $m$ -number of debatable nodes, $c$ -number of demanding clusters, $\delta$ -desired cluster size .....	68