

## Numericals

# Consider the following table of Segment

| Segment | Base | Limit |
|---------|------|-------|
| 0       | 219  | 600   |
| 1       | 2300 | 14    |
| 2       | 90   | 100   |
| 3       | 1387 | 580   |
| 4       | 1952 | 96    |

What are the physical addresses of the following logical addresses?

(i) 0430

$$\text{Seg no} = 0$$

$$\text{offset} = 430$$

table is base = 219 , size = 600

As offset < size

$$430 < 600 \text{ (True)}$$

$$\begin{aligned}\text{Physical address} &= \text{Base} + \text{offset} \\ &= 219 + 430\end{aligned}$$

$$= 649$$

ii) 110

$$\text{Seg no} = 1$$

$$\text{Seg offset} = 10$$

Base = 8300 } from segment table  
limit = 14

10 < 14 True

$$PA = 8300 + 10$$

$$\boxed{PA = 8310}$$

(3) 8500

s = Seg no = 2

d = offset = 500

from Segment table:-

Base = 90

limit = 100

500 < 100 false

Hence, reference of physical address of logical address (8500) will result in an error.

## Numericals

### Important formulas

: Physical address Space = Size of main memory

: Size of main memory = Total no of frames  $\times$  Page size

: no of pages = Logical address space  $= 2^{m-n}$   
Page size

: no of frames = Physical address space  
Page size

: Size of page table = no of entries in Pt  $\times$  Page entry size

: no of entries in page table = no of pages

: entry size = Size of page entry

: Page size  $= 2^n$  = n-bit directive

: no of bits used to represent page no = m - n

: max length of page table = no of pages

: PT = (Page no.  $\times$  no of bits / Page) + complement

∴ Page table entry size: No of bits in the frame number + no of bits used for optional fields  
if any.

1 words = 1 bytes

$$1\text{MB} = 2^{20}$$

$$1\text{GB} = 2^{30}$$

$$1\text{KB} = 2^{10} \times 2^2 = 2^{12}$$

$$1\text{k} = 2^{10}$$

### Example:

Consider a system in which logical address equal to 27 bits and the physical address space requires 21 bits. The page size 4k words. Calculate the number of pages and no of frames?

⇒ if logical address requires 32-bits  
then the total size =  $2^{32}$

⇒ if physical address requires 21-bit  
then physical address Space =  $2^{21}$   
Page size =  $2^{12}$  (4k implies  $2^2 \times 2^{10}$ )

∴ no of pages =  $\frac{\text{Logical address space}}{\text{Page size}}$

$$= \frac{2^{32}}{2^{12}}$$

$$= 2^{16} = 2^{10} \times 2^5 = 32\text{k}$$

∴ no of frames =  $\frac{\text{Physical address space}}{\text{frame size}}$

$$= \frac{2^{21}}{2^{12}}$$

$$= 2^9 = 512 \text{ frames}$$

Q) Consider a system with logical address of 32-bits and physical address space 64M words. The page size is 4k. Page table entry size = 2 bytes? what is the approximate size of the page table?

if logical address requires 32 bits,  
then the total size of logical address Space =  $2^{32}$   
⇒ Page size = 4k =  $2^{12}$

Logical address space =  $2^{32}$   
 No. of pages =  $2^{20}$   
 Page size =  $2^{12}$

No. of frames = PAS / frame size  
 PAS =  $2^{16}$   
 $2^{16} / 2^{12} = 2^4 = 16$

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## Practice Exercise

Q.9.1) Name two differences b/w logical address and physical address?

Solved. on previous page.

Q.9.2) Why are page sizes always powers of 2?

- Paging is implemented by breaking up an address into a page and offset number.

- It is most efficient to break the address into a integer page bits and offset bits, rather than doing by arithmetic operations.

- Since each bit represents a power of 2. Splitting an address bits results in page size that is power of 2.

Q.4) Consider a logical address space of 64 pages of 1024 words each, mapped onto a physical memory of 32 frames

How many bits are used in logical address?

b) How many bits are used in the physical address?

(a)

$$\Rightarrow \text{no of pages} = 64 = 2^6$$

$$\Rightarrow \text{size of each page} = 1024 \text{ words} \cdot 2^{10}$$

$\Rightarrow$  So, logical address space will be

logical address space = page size  $\times$  no of pages

$$= 2^{10} \times 2^6 = 2^{16}$$

$\Rightarrow$  Hence, 16-bits are used in LA.

(b)

$$\text{no of frames} = 32 = 2^5 \quad \text{given}$$

$$\therefore \text{size of page} = \text{size of frame}$$

$$\text{size of frame} = 2^{10}$$

$\therefore$  Physical address space = frame size  $\times$  no of frames

$$= 2^{10} \times 2^5 = 2^{15}$$

$\Rightarrow$  Hence, 15-bits are required

to represent PAS.

9.8) The BTU OS has 21-bit logical address, yet on certain embedded devices, it has only a 16-bit physical address. It also has 2-KB page size. How many entries are there in each of the following?

- (a) A conventional, single-level page table
- (b) An inverted page table

$$\Rightarrow 21\text{-bit for logical address} \quad \text{given}$$

$$\Rightarrow 16\text{-bit for physical address} \quad \text{given}$$

$$\Rightarrow \text{Page size} = 2\text{-KB} \quad \text{given}$$

$$= 2^10 \times 2^10$$

$$= 2^{20}$$

(a)  
no of entries?

$\Rightarrow$  if 21-bit of logical address are given then the total size =  $2^{21}$  bytes

$\therefore$  no of entries = no of pages

$$\therefore \text{no of entries} = \frac{\text{LAS}}{\text{Page size}}$$

$$\text{no of entries} = 2^{21}/2^{10} = 2^{10} \text{ bytes}$$

b) If 16-bit for physical address space, then total size will be  $2^{16}$

$\therefore$  no of entries = number of frames

$\therefore$  no of frames = PAS / frame size

$\therefore$  frame size = page size

no of frames =  $\frac{2^{16}}{2^{10}} = 2^6$

Given offence.  $2^6$  bytes will be in the inverted page table.

c) maximum amount of physical memory in the BTU OS?

Physical memory = no of entries in Conventional Table \* (page size)

$$= 2^{10} \times 2^{10}$$

$$= 2^{20} \text{ bytes}$$

9.9)

Consider a logical address space of 256 pages with a 4-KB page-size, mapped into a

## physical memory of 64-frames

- (a) How many bits are required in the logical address?  
(b) How many bits are required in the physical address?

(a)

$$\Rightarrow \text{no of pages} = 856 \quad \text{Given}$$

$$\Rightarrow \text{Page size} = 4 \text{KB} = 4 \times 10^10 = 2^2 \times 2^{10} = 2^{12}$$

$$\Rightarrow \text{no of frames} = 64 \quad \text{Given}$$

$$\therefore \text{LAS} = \text{no of pages} \times \text{page size}$$
$$= 2^8 \times 2^{12}$$
$$= 2^{20}$$

Hence, 20-bits are required.

b)  $\therefore \text{PAS} = \text{no of frames} \times \text{frame size}$

$$\text{frame size} = \text{page size}$$

$$\text{frame size} = 2^{12}$$

$$\text{PAS} = 2^{12} \times 2^6$$

$$= 2^{18}$$

Hence, 18-bits are required.

9.10) Consider a computer system with a 32-bit logical address and 4KB page size. The system supports upto 512MB of physical memory. How many entries are there in each of the following?

- a) Conventional page table,  
single-level page table  
b) An inverted page table

for LAS 38-bits are given so total size =  $2^{32}$

$$\Rightarrow \text{Page size given} = 4 \text{KB} = 2^2 \times 2^{10} = 2^{12}$$

$$\Rightarrow \text{Physical memory} = 512 \text{MB}$$
$$= 512 \times 2^{20} \quad \because 1 \text{MB} = 2^{20}$$
$$= 2^9 \times 2^{20}$$
$$= 2^{29}$$

a)  $\Rightarrow \text{no of entries} = \text{no of pages}$

$$\Rightarrow \text{no of pages} = \frac{\text{LAS}}{\text{Page size}} = \frac{2^{32}}{2^{12}}$$

$$\Rightarrow \text{no of pages} = 2^{20}$$

Hence, 20-bits are required.

(b)

no. of entries in index table = no. of frames

$$\therefore \text{no. of frames} = \frac{\text{PAS}}{\text{frame size}} \quad \because P_2 = P_3$$
$$= \frac{999}{2^{18}} = 128k$$

9.1) Assuming a 1-KB page size, what are the page no and offsets for the following addresses (provided as decimal numbers)

- a) 3085
- b) 42095
- c) 215201
- d) 650000
- e) 2000001

$\Rightarrow$  Given page size 1KB, it can be written as  $= 2^n = 2^10 = 1024 = 2^{10}$ , so, the no. of bits in the offset part ( $n$ ) = 10.

$\Rightarrow$  To solve this problem, following steps:

1) Convert logical address: Decimal to binary.

2) Split binary address to 2 parts (page no, offset) :  $n$  digits

3) Convert offset and page no, binary to decimal.

(a) 3085 as Decimal

- o Binary form: 0110000001101
- o page no = 011 = 3
- o page offset = 0000001101 = 13

(b) 42095 as Decimal

- o Binary form: 1010010001101111
- o page no = 101001 = 41
- o page offset = 0001101111 = 111

(c) 215201

- o Binary form: 110100100010100001
- o page no: 11010010 = 210
- o page offset: 00010100001 = 161

(d) 650000 as decimal

o Binary form: 100111101000010000

o page no: 1001111010 = 634

o page offset: 1100010000 = 784

(e) 200001 as decimal

o Binary form: 1111010000100100000001

o page no: 11110100001 = 1953

o page offset: 0010000001 = 189

Extra) Consider a system with byte-addressable memory, 32-bit logical addresser, 4KB page size and page table entries of 4bytes each. find the page table size in MB?

$\therefore$  Page table size = no of page table entries \* entry size

$$\therefore \text{no of pages} \times 4 \text{ bytes}$$

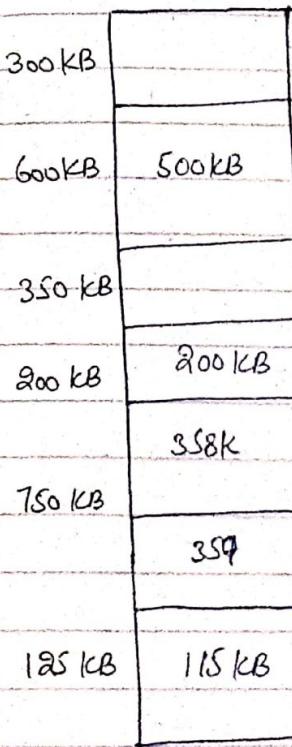
$$= \frac{2^{32}}{2^{12}}$$

$$= 4 \text{ MB}$$

#96) Given a six memory partitions 300KB, 600KB, 350KB, 200KB, 750 KB, & 125 KB (in order), how would the first fit, best fit, and worst fit algorithm places processes of size 115KB, 500 KB, 358 KB, 200KB and 357 KB (in order)?

(i) Best fit:

wastage of memory



$$\begin{aligned}\text{Wastage: } & (600-500) + (750-(500+ \\ & 358)) + (125-115) + 850 + 300 \\ & = 100 + 35 + 10 + 350 + 300 \\ & \boxed{795 \text{ KB}}\end{aligned}$$

### a) First fit:

|        |        |  |
|--------|--------|--|
| 300KB  | 115 KB | wastage of memory  |
| 600    | 500    | $= (300 - 115) + (600 - 500)$  |
| 350    | 200    | $+ (350 - 200) + 300 +$<br>$(750 - (350 + 200)) + 125$                                     |
| 200    |        | $= 185 \text{ KB} + 100 \text{ KB} + 150 \text{ KB}$<br>$+ 35 \text{ KB} + 125 \text{ KB}$ |
| 750KB  | 358    | 375KB  |
|        | 357    |  |
| 185 KB |        | 300KB  |

### 3) Worst fit

|                       |       |
|-----------------------|-------|
| 600KB                 | 358   |
| 357 KB need to wait   |       |
| 300                   | 200   |
| 350                   |       |
| 200                   |       |
| 750KB                 | 115   |
| 125                   |       |
| 300 + 200 + 125 + 185 | 125KB |
| + 83 = 777KB          |       |

Extn: Given 5 memory partition of 100KB, 300KB, 200KB, 300KB, 600 KB (in order). How would each of first fit, best fit, worst fit & Next fit, places processes of 212KB, 417KB, 1124KB, 426 KB (in order). Which algorithm makes efficient use of memory.

Given memory positions are:-

100KB, 300KB, 200KB, 300KB, 600KB

Given processes are:-

212KB, 417KB, 1124KB, 426 KB

Solution:

#### (1) First fit

|        |        |  |
|--------|--------|--|
| 100KB  |        | $\Rightarrow 426 \text{ KB cannot get memory}$ |
| 300KB  | 212 KB | <u>Total wastage</u>                           |
| 200 KB | 112 KB | $\Rightarrow 1700 - (212 + 112 + 417)$         |
| 300 KB |        | $= 1700 - 741$                                 |
| 600KB  | 417KB  | $= 959 \text{ KB}$                             |

### 2) Best fit:-

|        |        |
|--------|--------|
| 100 kB |        |
| 500 kB | 417 kB |
| 200 kB | 112 kB |
| 300 kB | 212 kB |
| 600 kB | 42 kB  |

Total wastage:

$$= 1700 - (417 + 112 + 212 + 42) =$$

$$= 1700 - 783 = 917 \text{ kB}$$

### 3) Worst fit:

|        |  |
|--------|--|
| 100 kB | $\Rightarrow 426 \text{ kB}$ can not get memory. |
| 500 kB | 417 kB   |
| 200 kB | 112 kB   |
| 300 kB | 212 kB   |
| 600 kB | 42 kB  |

∴ find partitioning memory of 600 can not be assigned to 426.

### 4) Neat fit:

|        |        |   |
|--------|--------|---|
| 100 kB |        | $\Rightarrow 426 \text{ kB}$ cannot get memory. |
| 500 kB | 819 kB | Wastage:-                                       |
| 200 kB | 112 kB | $= 1700 - (819 + 112 + 417)$                    |
| 300 kB |        | $= 959 \text{ kB}$                              |
| 600 kB | 417 kB |   |

So, best-fit algorithm is best for this process.

### Part Paper:-

Given memory partitions of 100k, 600k, 200k, 300k, and 500k (in order), how would each of the first fit, best fit, and worst fit algorithms place processes of 409K, 236K, 125K, and 514K (in order)? Also define them.

o Given processes:-

409K, 236K, 125K, 514K

o Given memory partitions:-

100k, 600k, 200k, 300k, 500k

(i) first-fit:

|      |      |   |
|------|------|---|
| 100K |      | $\Rightarrow 514K$ need to wait will<br>not get memory. |
| 600K | 409K |   |
| 200K | 185K | <u>wastage of memory:</u>                               |
| 300K | 236K | $= 1700 - (409 + 185 + 236)$                            |
| 500K | 5    | $= 1700 - (710)$<br>$= 930K$                            |

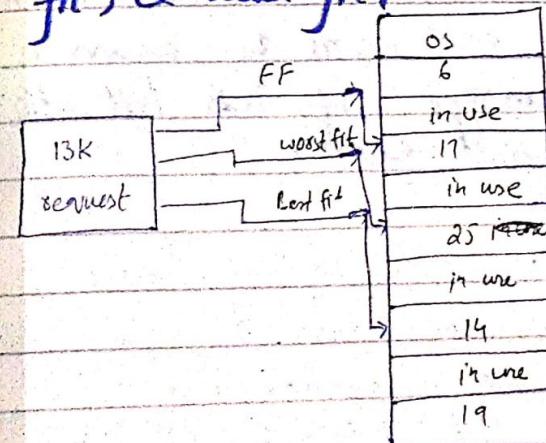
(iii) worst-fit:

|      |      |   |
|------|------|---|
| 100K |      | $\Rightarrow 514K$ need to wait will<br>not get memory. |
| 600K | 409K | <u>Wastage of memory:</u>                               |
| 200K |      | $O = 1700 - (409 + 185 + 236)$                          |
| 300K | 125K | $= 1700 - (710)$  |
| 500K | 236K | $= 930K$  |

(ii) Best-fit:

|      |      |                                    |
|------|------|------------------------------------|
| 100K |      | <u>Wastage of memory:</u>          |
| 600K | 514K | $= 1700 - (514 + 185 + 236 + 409)$ |
| 200K | 185K | $= 1700 - (1889)$                  |
| 300K | 236K | $= 416K$                           |
| 500K | 409K |                                    |

Suppose that we have free segment with sizes : 6, 17, 25, 14 and 19. Place a program with size 13kB in the free segment using first-fit, best-fit, & worst-fit?



## Numericals

### Topic: TLB

#### Formula:

$\Rightarrow$  Hit ratio of  $\neq 1$  Accounting of TLB + Access time of main memory

+ miss ratio of TLB + {Access time of TLB +  
 $(L+1) \times$  Access time of main memory}  
 where L = no. of levels of page table

$\Rightarrow$  valid formula if there is no page fault.

#### Example:

Consider a single level paging scheme with a TLB. Assume no page fault occurs. It takes 20ns to search the TLB and 100ns to access the physical memory. If TLB hit ratio is 80%, find CMT?

Given -

- o Number of levels of page table = 1
- o TLB access time = 20 ns
- o main memory access time = 100 ns
- o TLB hit ratio = 80% = 0.8

#### Calculating TLB miss ratio:

$$\text{TLB miss ratio} = 1 - \text{TLB hit ratio}$$

$$= 1 - 0.8$$

$$= 0.2$$

#### Calculating effective access time:

$$\begin{aligned} \text{CMT} &= 0.8 \times \{20\text{ns} + 100\text{ns}\} + 0.2 \times \{20\text{ns} + (1+1) \times 100\text{ns}\} \\ &= 0.8 \times 120\text{ns} + 0.2 + 2 \times 100\text{ns} \\ &= 96\text{ns} + 44\text{ns} = 140\text{ns} \end{aligned}$$

#### What are Pros and Cons of paging?

| Pros  | Cons  |
|---|---|
| o No external fragmentation.                    | o Larger memory access time.  |
| o Efficient use of memory.                      | o Internal fragmentation to every last page of the process.                       |
| o Swapping of pages are easy as of same size.   | o Large memory space is required as page table are stored in main memory as well. |
| o Allocating memory to pages is easy and cheap. | o Size of page is crucial (not too small and not too large).                      |