

## ADSP 31014 Statistical Models for Data Science

### Course Project Part 2 - Hira Stanley

#### Business Problem

Political Analysts would like to understand what factors drove the results of the 2020 U.S. Presidential election (specifically the percentage of votes for Joe Biden in each county), such as demographics, prior election results, and the impact of COVID.

#### Model Selection

The nature of this data set allows for either logistic or linear regression models to be performed. With logistic, we could predict a binary outcome of the 2020 election. However, because we also have access to percentage of vote share for the 2020 winner in each county, it would be more helpful in the context of the problem to do a linear regression so we can see how the other factors affect the vote share rather than only the final outcome.

#### Linear Regression Model

We build a linear regression model using a cleaned dataset of 3,021 rows. The predicted variable is `percentage20_Joe_Biden`. The model formula is:

```
percentage20_Joe_Biden ~ factor(state)*NonWhite + case_pct*Black + turnout_difference + Income +  
Men_pct + Transit
```

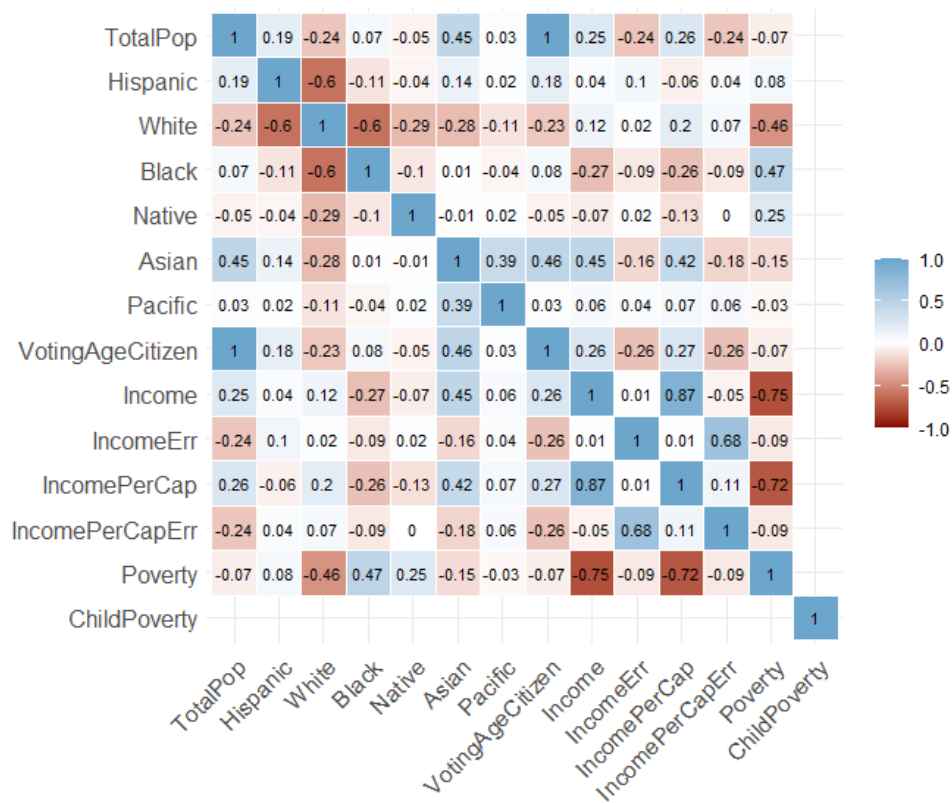
This model has 107 parameters with a  $R^2$  of 0.76. See Appendix 1 for model summary.

#### Multicollinearity and Feature Engineering

We divide our 54 potentially explanatory variables into five sections to investigate and omit any columns that represent multicollinearity with each other or our predicted variable:

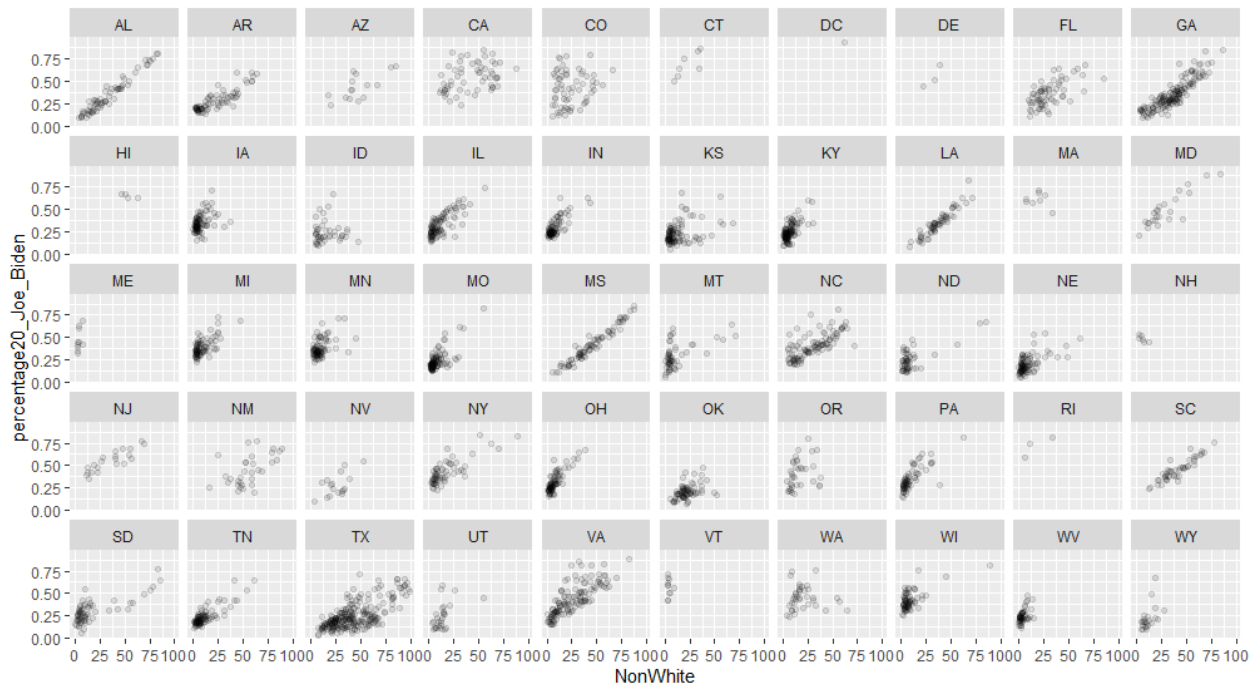
- Election results: The glaring multicollinearity is the 2016 election results with 0.98 correlation to our predicted variable. The simplest model would just be a linear relationship between `percentage16_Hillary_Clinton` and our predicted variable, which offers a r-squared of 0.95, but does not help us understand any other factors. We also omit `total_votes2020`, as it is multicollinear with `total_votes16` (0.96) and `turnout_difference` (0.78).
- Demographic: `TotalPop` and `VotingAgeCitizen` have perfect correlation of 1, we remove `TotalPop` because in this context, the vote share should represent only those who are eligible to vote. There are 5 columns representing racial demographics, and none stand out with high multicollinearity that would inhibit explainability. We feature engineer a column called `NonWhite`, which sums all racial categories that are not `White` to represent a percentage of the population. A heatmap of correlation showed other potential multicollinearities, that allow us to reduce the 6 income-related columns to just income.
- Commute: `Transit` would offer some explainability without high correlation.
- Employment: Knowing the context of the dataset, we just keep `Unemployment`.
- Others: We previously converted COVID cases and deaths into a percentage of the population in that county (`case_pct` and `death_pct`) to not be multicollinear with `TotalPop` or `VotingAgeCitizen`. We also previously converted gender in a similar way to just represent the male population as a percentage (`Men_pct`).

Correlation Matrix Heatmap of Demographic Data (remainder in Appendix 2)



Interaction Terms

Categorical field `state` interacts with percentage of the population being `NonWhite`.



## Useful and Less Useful Terms

Interaction terms:

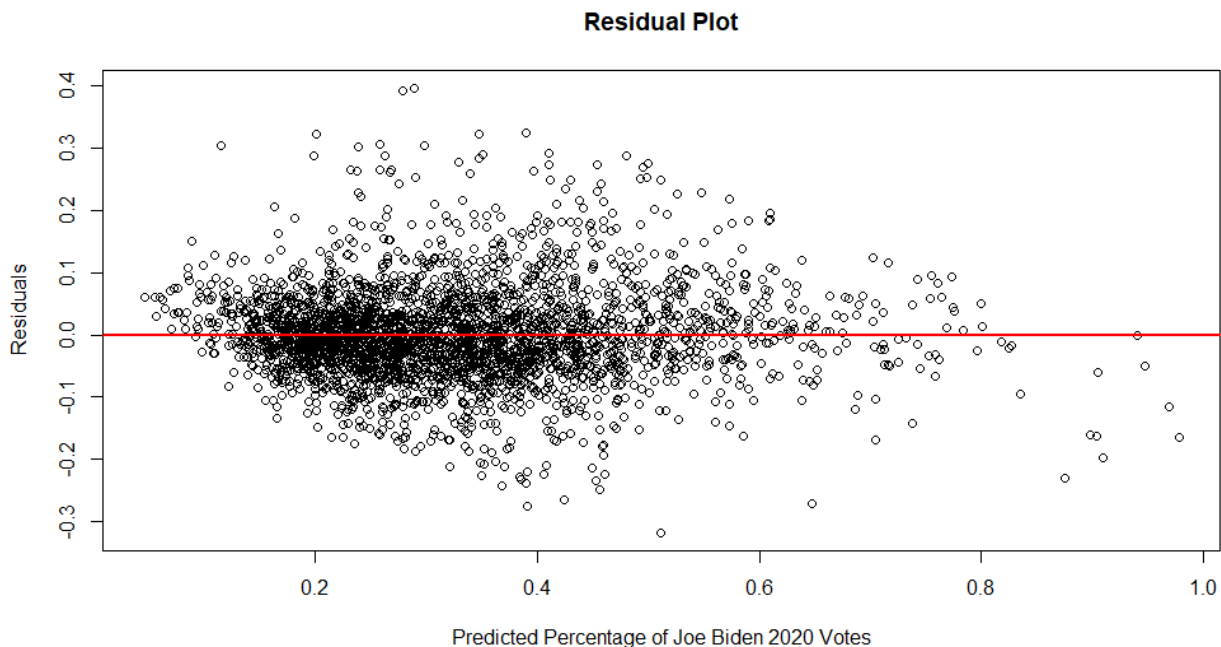
- **State** interacting with the **NonWhite** percentage of the population significantly impacts the response variable. The p-values that are less than 0.05 in 16 states indicate that the effect of NonWhite varies by state, with both positive and negative relationships observed.
- COVID cases (**case\_pct**) when interacting with race had p-value  $9.73e-05$  and the final model has adjusted  $R^2$  of 0.76. When input into the model separately without interaction, the adjusted  $R^2$  is 0.75. This means the interaction term is more useful in providing a nuanced understanding of the data.

Less useful terms that we omitted either due to high p-values, or that their removal did not change the model's explanatory power (adjusted  $R^2$ ).

- **Unemployment** had p-value 0.04
- **Lat** had p-value 0.26

## Residuals

Plot of the response variable vs. residuals shows the model is a good fit, with the residuals randomly scattered around the horizontal line.



## Model Trade-offs

The model where **state** interacted with **NonWhite** and **case\_pct** had a slightly higher  $R^2$  at 0.77, but the three-way interaction created 204 parameters. In the trade-off between model complexity and achieving a better fit, we choose the less complex one with 108 parameters.

Heteroscedasticity is present in multiple explanatory variables. When we take the log of the response variable, it reduces the  $R^2$  down to 0.70. Despite the violation of the homoscedasticity assumption, we prioritize prediction accuracy in this trade-off. More detail in Appendices 3 and 4.

## Appendix 1: Final Model Summary

call:

```
lm(formula = percentage20_Joe_Biden ~ factor(state) * Nonwhite +  
    case_pct * Black + turnout_difference + Income + Men_pct +  
    Transit, data = data)
```

Residuals:

Min	1Q	Median	3Q	Max
-0.31771	-0.04380	-0.00571	0.03599	0.39612

Coefficients: (1 not defined because of singularities)

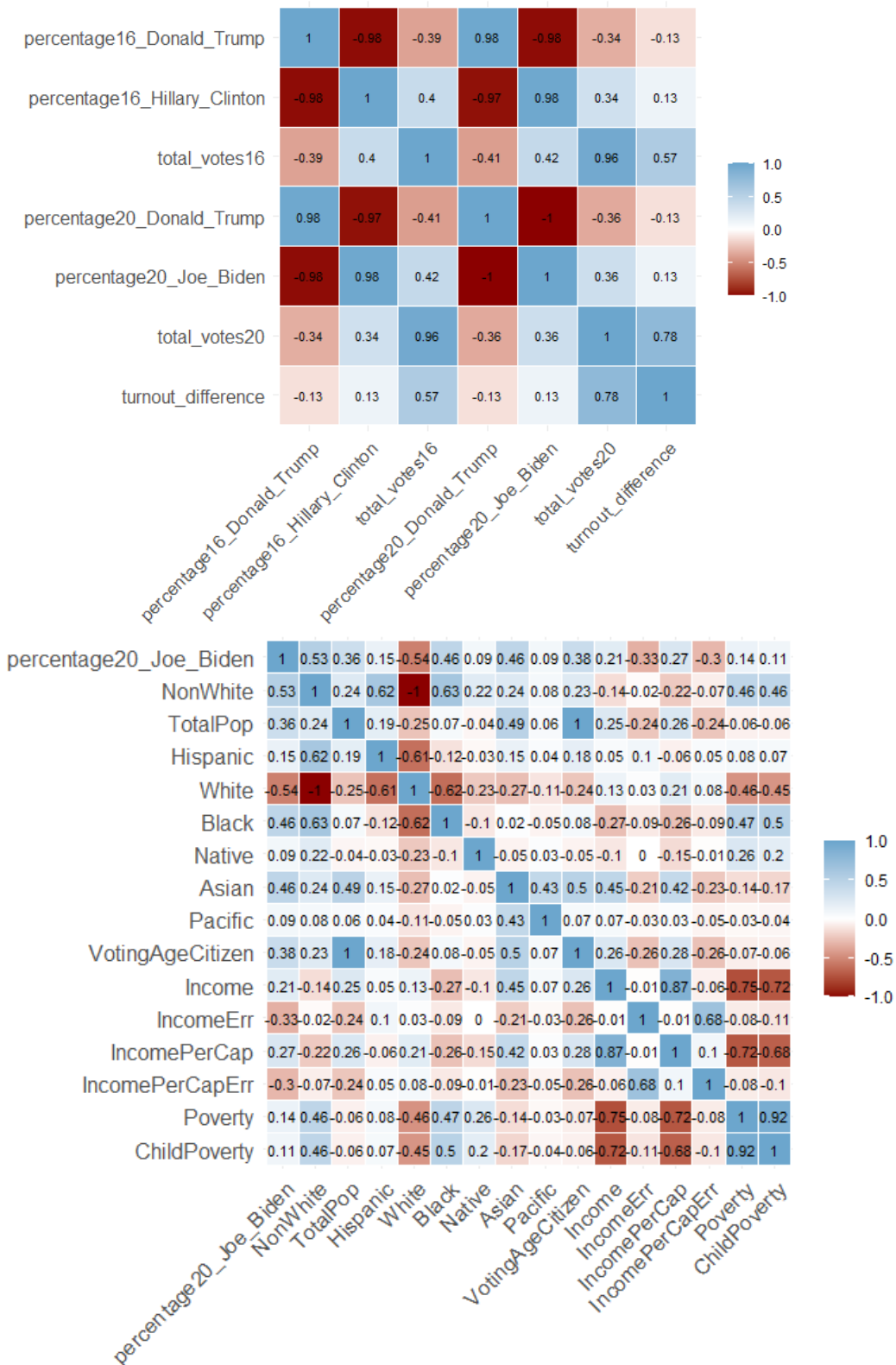
	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	4.060e-01	3.806e-02	10.667	< 2e-16	***
factor(state)AR	1.146e-01	2.289e-02	5.004	5.95e-07	***
factor(state)AZ	4.532e-02	5.893e-02	0.769	0.441999	
factor(state)CA	3.280e-01	3.045e-02	10.773	< 2e-16	***
factor(state)CO	2.267e-01	2.641e-02	8.583	< 2e-16	***
factor(state)CT	3.261e-01	7.152e-02	4.559	5.35e-06	***
factor(state)DC	-2.071e-02	8.452e-02	-0.245	0.806447	
factor(state)DE	9.797e-02	2.141e-01	0.458	0.647212	
factor(state)FL	1.270e-01	2.758e-02	4.604	4.33e-06	***
factor(state)GA	-2.923e-03	2.259e-02	-0.129	0.897044	
factor(state)HI	1.037e+00	3.439e-01	3.016	0.002587	**
factor(state)IA	2.062e-01	2.146e-02	9.607	< 2e-16	***
factor(state>ID	1.591e-01	2.692e-02	5.910	3.83e-09	***
factor(state)IL	1.480e-01	2.123e-02	6.972	3.85e-12	***
factor(state)IN	1.264e-01	2.155e-02	5.863	5.06e-09	***
factor(state)KS	9.636e-02	2.109e-02	4.570	5.09e-06	***
factor(state)KY	1.167e-01	2.125e-02	5.493	4.29e-08	***
factor(state)LA	-7.022e-02	3.358e-02	-2.091	0.036632	*
factor(state)MA	4.392e-01	6.809e-02	6.450	1.30e-10	***
factor(state)MD	1.480e-01	3.447e-02	4.294	1.82e-05	***
factor(state)ME	2.211e-01	6.196e-02	3.568	0.000365	***
factor(state)MI	2.420e-01	2.252e-02	10.744	< 2e-16	***
factor(state)MN	2.111e-01	2.247e-02	9.395	< 2e-16	***
factor(state)MO	1.050e-01	2.091e-02	5.022	5.42e-07	***
factor(state)MS	-3.268e-02	2.711e-02	-1.205	0.228136	
factor(state)MT	1.500e-01	2.207e-02	6.793	1.32e-11	***
factor(state)NC	1.680e-01	2.360e-02	7.120	1.36e-12	***
factor(state)ND	1.056e-01	2.205e-02	4.786	1.78e-06	***
factor(state)NE	5.492e-02	2.099e-02	2.617	0.008926	**
factor(state)NH	3.920e-01	6.827e-02	5.742	1.03e-08	***
factor(state)NJ	1.912e-01	4.196e-02	4.557	5.41e-06	***
factor(state)NM	-2.018e-03	5.002e-02	-0.040	0.967814	
factor(state)NV	-1.142e-02	5.172e-02	-0.221	0.825270	
factor(state)NY	2.717e-01	2.377e-02	11.427	< 2e-16	***
factor(state)OH	1.231e-01	2.192e-02	5.617	2.12e-08	***
factor(state)OK	2.312e-02	2.952e-02	0.783	0.433595	
factor(state)OR	2.248e-01	3.116e-02	7.214	6.90e-13	***
factor(state)PA	1.629e-01	2.263e-02	7.198	7.75e-13	***
factor(state)RI	3.878e-01	7.860e-02	4.934	8.52e-07	***
factor(state)SC	7.413e-02	3.739e-02	1.982	0.047534	*
factor(state)SD	1.501e-01	2.160e-02	6.948	4.55e-12	***
factor(state)TN	1.160e-01	2.094e-02	5.543	3.24e-08	***
factor(state)TX	-8.246e-02	2.173e-02	-3.795	0.000151	***
factor(state)UT	1.440e-01	5.686e-02	2.533	0.011377	*
factor(state)VA	1.219e-01	2.272e-02	5.364	8.77e-08	***
factor(state)VT	4.690e-01	6.330e-02	7.410	1.64e-13	***
factor(state)WA	3.214e-01	2.882e-02	11.153	< 2e-16	***
factor(state)WI	2.801e-01	2.139e-02	13.095	< 2e-16	***
factor(state)WV	1.253e-01	2.446e-02	5.123	3.21e-07	***
factor(state)WY	-3.563e-02	3.934e-02	-0.906	0.365090	
Nonwhite	4.939e-03	6.065e-04	8.145	5.58e-16	***

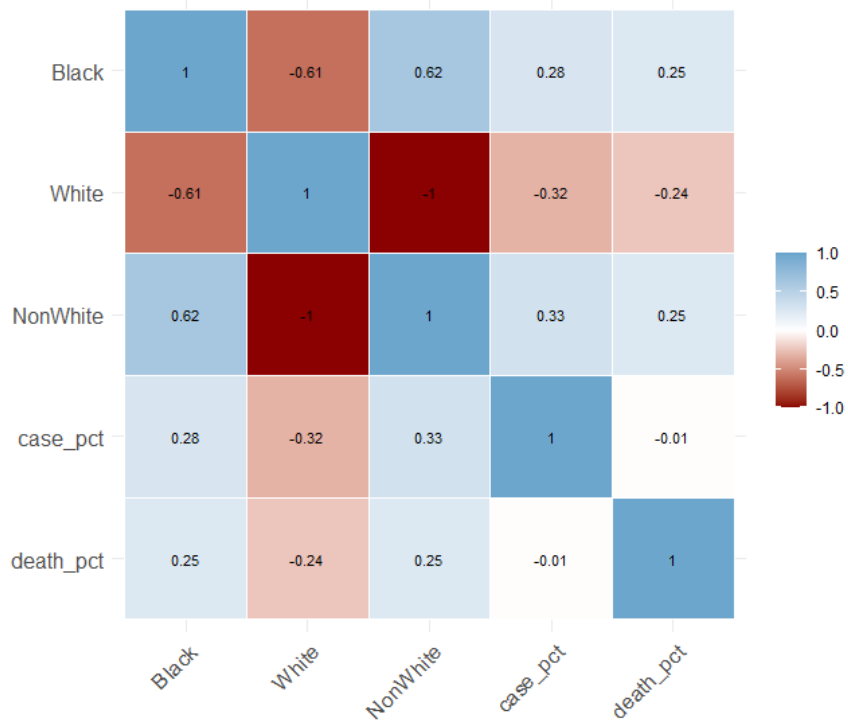
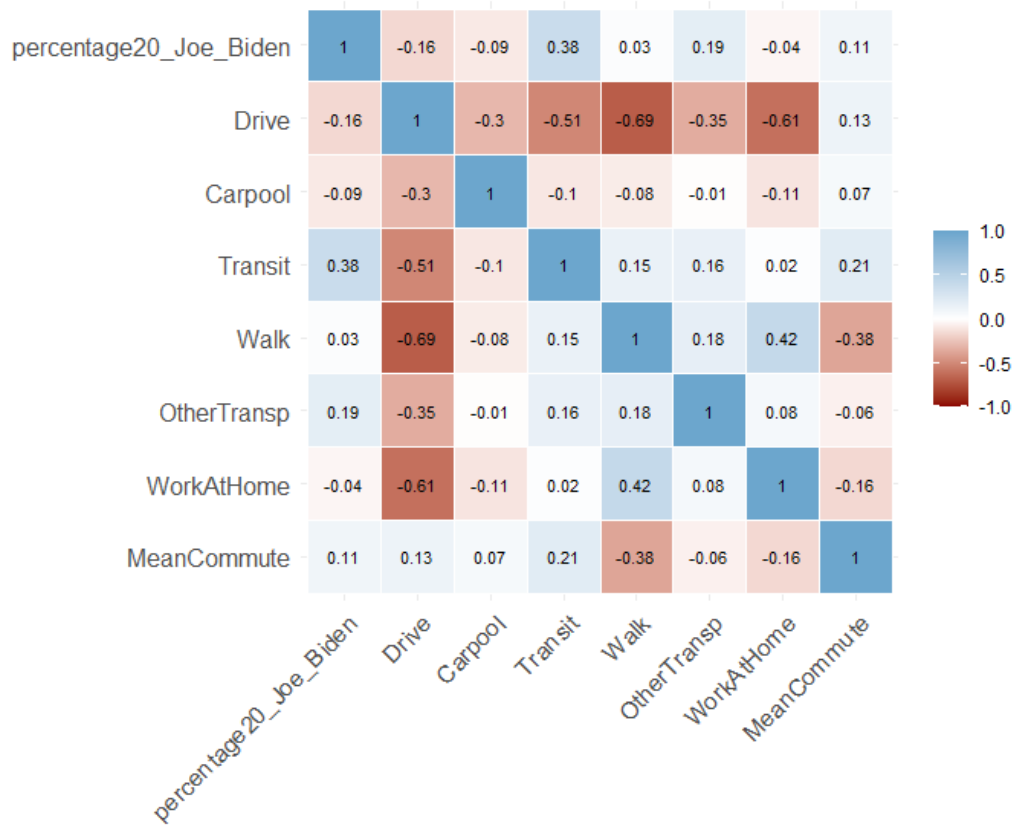
case_pct	-8.977e-01	1.418e-01	-6.329	2.85e-10	***
Black	3.044e-03	4.521e-04	6.733	1.99e-11	***
turnout_difference	1.620e-07	3.422e-08	4.735	2.30e-06	***
Income	2.634e-06	1.453e-07	18.125	< 2e-16	***
Men_pct	-8.661e-01	6.490e-02	-13.346	< 2e-16	***
Transit	9.703e-03	8.246e-04	11.767	< 2e-16	***
factor(state)AR:NonWhite	-2.859e-03	6.811e-04	-4.198	2.78e-05	***
factor(state)AZ:NonWhite	1.477e-03	1.261e-03	1.171	0.241865	
factor(state)CA:NonWhite	-3.795e-03	7.995e-04	-4.747	2.17e-06	***
factor(state)CO:NonWhite	-1.494e-03	9.124e-04	-1.637	0.101738	
factor(state)CT:NonWhite	2.934e-03	2.840e-03	1.033	0.301665	
factor(state)DC:NonWhite	NA	NA	NA	NA	
factor(state)DE:NonWhite	2.058e-03	6.560e-03	0.314	0.753737	
factor(state)FL:NonWhite	-1.361e-03	8.136e-04	-1.673	0.094443	.
factor(state)GA:NonWhite	-3.642e-05	5.788e-04	-0.063	0.949830	
factor(state)HI:NonWhite	-1.595e-02	6.469e-03	-2.466	0.013721	*
factor(state)IA:NonWhite	1.509e-03	1.336e-03	1.130	0.258703	
factor(state>ID:NonWhite	-3.838e-03	1.227e-03	-3.128	0.001779	**
factor(state)IL:NonWhite	2.576e-04	8.867e-04	0.290	0.771464	
factor(state)IN:NonWhite	2.788e-03	1.217e-03	2.292	0.021979	*
factor(state)KS:NonWhite	-1.527e-03	8.307e-04	-1.839	0.066062	.
factor(state)KY:NonWhite	1.749e-03	1.373e-03	1.273	0.203002	
factor(state)LA:NonWhite	1.117e-03	8.530e-04	1.310	0.190413	
factor(state)MA:NonWhite	-6.541e-03	3.232e-03	-2.024	0.043100	*
factor(state)MD:NonWhite	-2.328e-03	1.018e-03	-2.286	0.022314	*
factor(state)ME:NonWhite	2.905e-02	1.367e-02	2.124	0.033740	*
factor(state)MI:NonWhite	-5.177e-04	1.160e-03	-0.446	0.655541	
factor(state)MN:NonWhite	3.195e-04	1.239e-03	0.258	0.796483	
factor(state)MO:NonWhite	7.140e-04	1.215e-03	0.588	0.556678	
factor(state)MS:NonWhite	1.292e-05	6.132e-04	0.021	0.983195	
factor(state)MT:NonWhite	9.951e-04	8.989e-04	1.107	0.268381	
factor(state)NC:NonWhite	-2.317e-03	6.466e-04	-3.583	0.000345	***
factor(state)ND:NonWhite	8.075e-04	8.813e-04	0.916	0.359568	
factor(state)NE:NonWhite	1.088e-03	9.635e-04	1.129	0.258790	
factor(state)NH:NonWhite	-1.387e-02	9.639e-03	-1.439	0.150186	
factor(state)NJ:NonWhite	-2.921e-03	1.114e-03	-2.622	0.008787	**
factor(state)NM:NonWhite	1.734e-03	1.004e-03	1.727	0.084292	.
factor(state)NV:NonWhite	1.084e-03	1.795e-03	0.604	0.546041	
factor(state)NY:NonWhite	-7.948e-03	1.006e-03	-7.902	3.84e-15	***
factor(state)OH:NonWhite	4.054e-03	1.258e-03	3.224	0.001278	**
factor(state)OK:NonWhite	-5.149e-04	1.136e-03	-0.453	0.650405	
factor(state)OR:NonWhite	-3.386e-04	1.455e-03	-0.233	0.816016	
factor(state)PA:NonWhite	3.089e-04	1.047e-03	0.295	0.767959	
factor(state)RI:NonWhite	3.898e-03	3.672e-03	1.062	0.288522	
factor(state)SC:NonWhite	-9.033e-04	8.756e-04	-1.032	0.302323	
factor(state)SD:NonWhite	1.584e-04	7.534e-04	0.210	0.833501	
factor(state)TN:NonWhite	-2.062e-03	8.232e-04	-2.504	0.012317	*
factor(state)TX:NonWhite	5.121e-04	6.611e-04	0.775	0.438616	
factor(state)UT:NonWhite	3.223e-04	2.180e-03	0.148	0.882485	
factor(state)VA:NonWhite	-1.545e-03	7.028e-04	-2.198	0.027994	*
factor(state)VT:NonWhite	-1.351e-02	1.410e-02	-0.958	0.337939	
factor(state)WA:NonWhite	-4.851e-03	1.080e-03	-4.493	7.31e-06	***
factor(state)WI:NonWhite	3.008e-04	9.784e-04	0.307	0.758501	
factor(state)WV:NonWhite	2.749e-03	3.007e-03	0.914	0.360642	
factor(state)WY:NonWhite	7.235e-03	2.794e-03	2.590	0.009657	**
case_pct:Black	2.771e-02	7.101e-03	3.903	9.73e-05	***

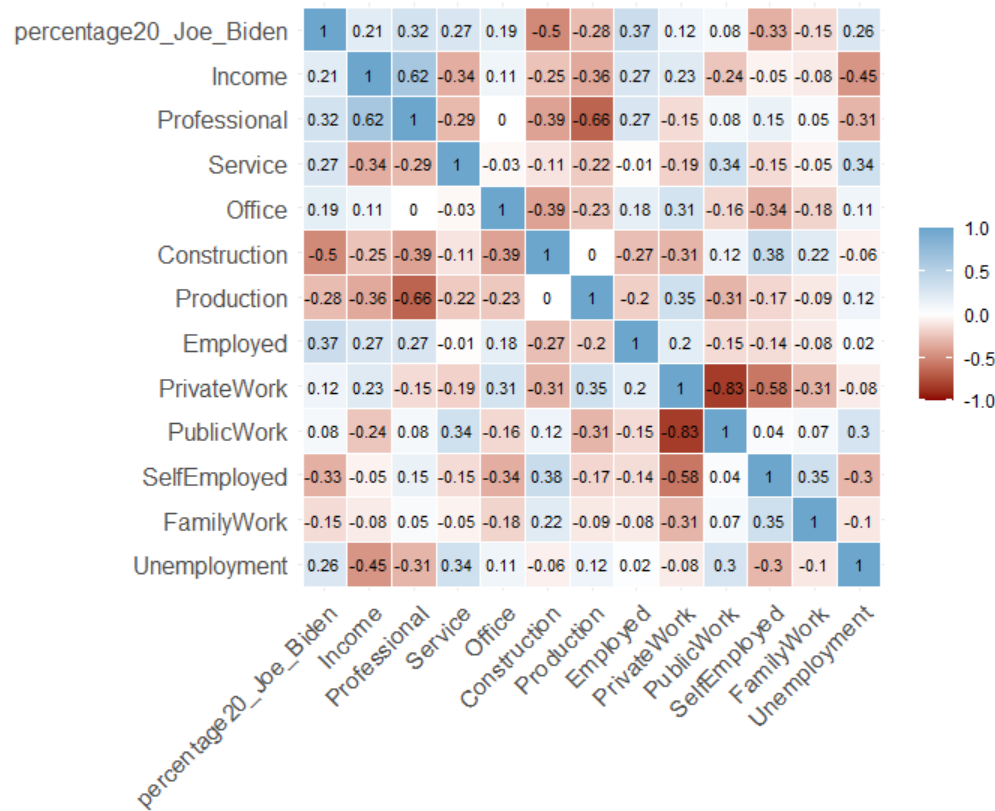
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 Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.0769 on 2915 degrees of freedom  
 Multiple R-squared: 0.7616, Adjusted R-squared: 0.753  
 F-statistic: 88.71 on 105 and 2915 DF, p-value: < 2.2e-16

## Appendix 2: Correlation Matrix Heatmaps

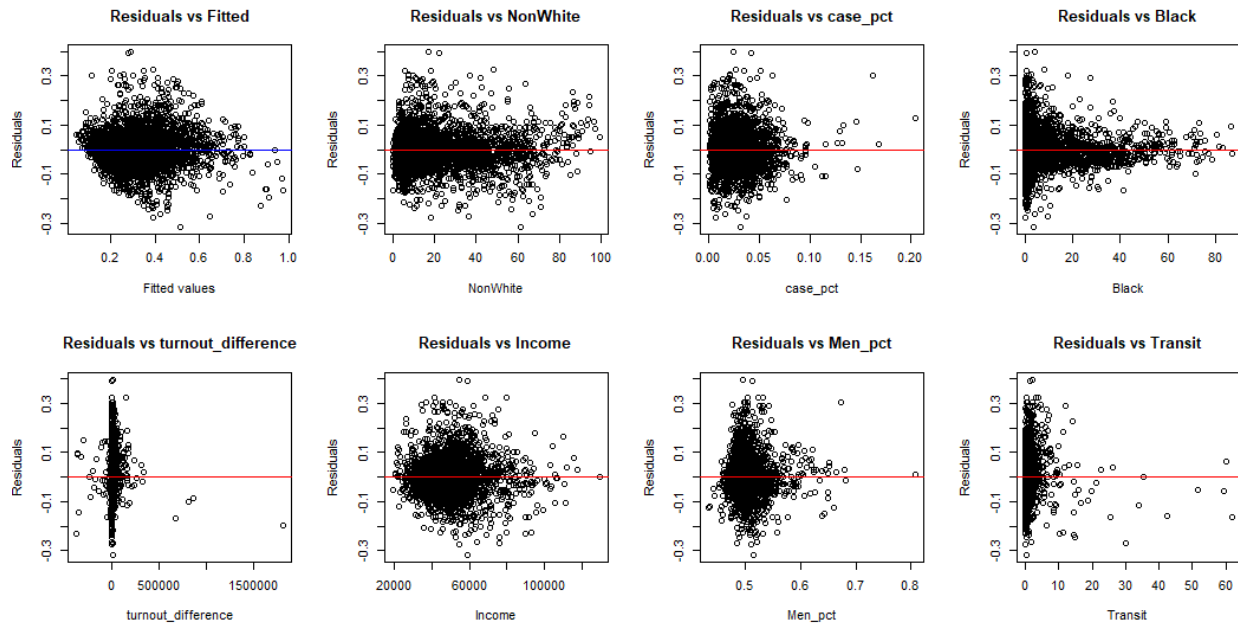






### Appendix 3: Heteroscedasticity in Model

Heteroscedasticity looks present in multiple explanatory variables, including NonWhite, Black, turnout\_difference, and Transit.





#### Appendix 4: Log Transformed Model

We take the log of the response variable to mitigate above heteroscedasticity. The new model has  $R^2$  of 0.70 and the same 107 parameters.

```
log(percentage20_Joe_Biden) ~ factor(state)*NonWhite + case_pct*Black + turnout_difference + Income  
+ Men_pct + Transit
```

