

# VISVESVARAYA TECHNOLOGICAL UNIVERSITY

“JnanaSangama”, Belgaum -590014, Karnataka.



**LAB REPORT on**

## **Artificial Intelligence (23CS5PCAIN)**

*Submitted by*

**Hiran B (1BM23CS113)**

*in partial fulfillment for the award of the degree of*  
**BACHELOR OF ENGINEERING**  
*in*  
**COMPUTER SCIENCE AND ENGINEERING**



**B.M.S. COLLEGE OF ENGINEERING**

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**B.M.S. College of Engineering,**

Bull Temple Road, Bangalore 560019

(Affiliated To Visvesvaraya Technological University, Belgaum)

**Department of Computer Science and Engineering**



**CERTIFICATE**

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by **Hiran B (1BM23CS113)**, who is a bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

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GITHUB: <https://github.com/Hitish-Rao-P/AI-1BM23CS116>

Program 1: Implement Tic – Tac – Toe Game & Implement vacuum cleaner agent.

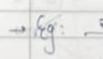
**ALGORITHM (Tic-Tac-Toe) :**

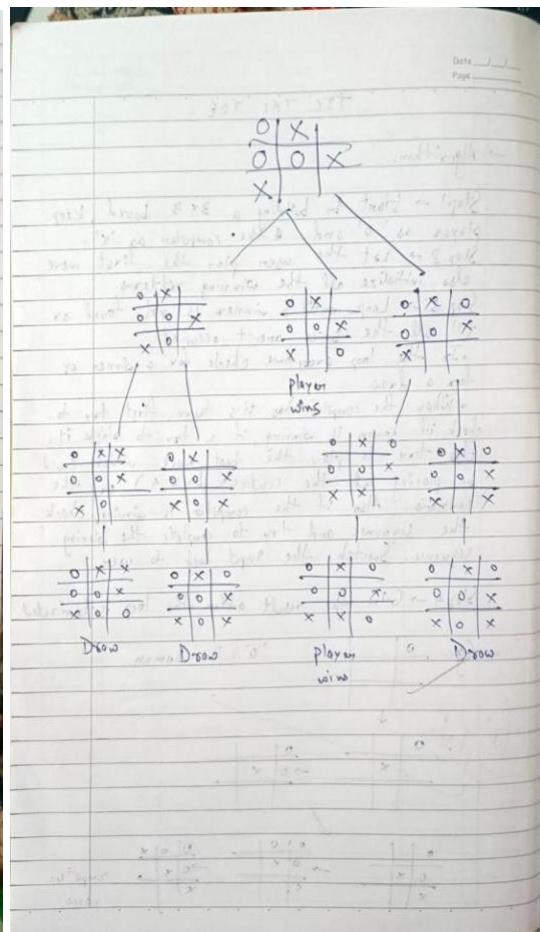
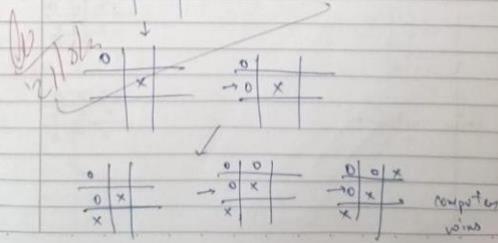
## TIC TAC TOE

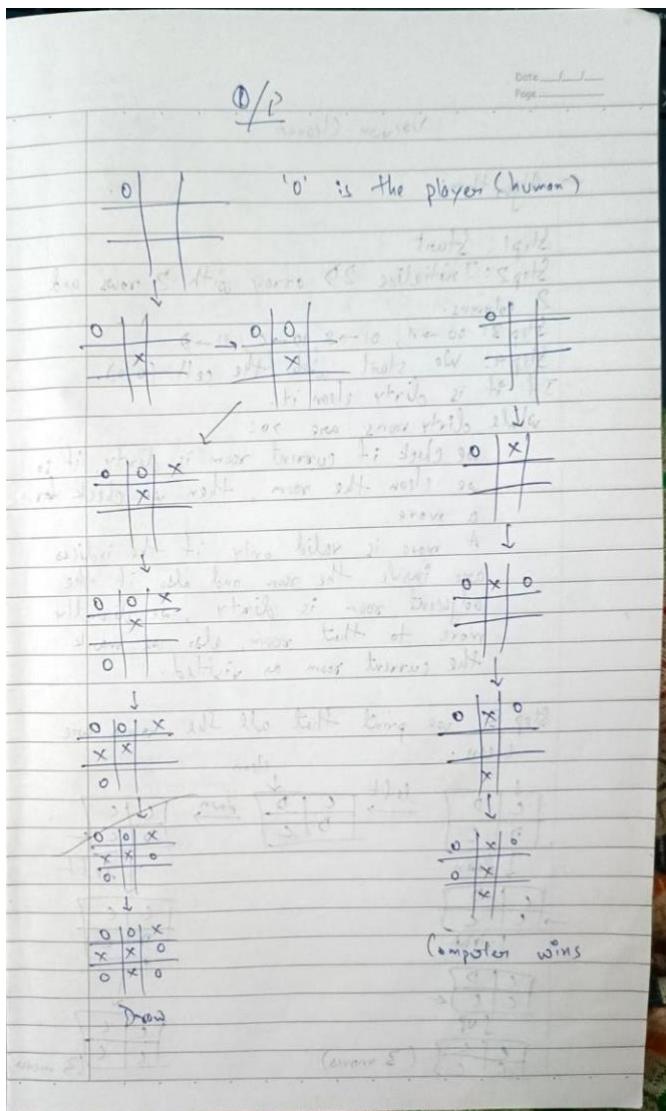
→ Algorithm:

- Step 1 → Start by building a  $3 \times 3$  board, keep player as 'o' and the computer as 'x'.
- Step 2 → Let the user play the first move, also initialize all the winning patterns.
- Step 3 → Loop until a winner is not found or till all the boxes aren't occupied.
  - In the loop everytime check for a winner or for a draw.
  - When the computer has it's turn, first try to check if human is winning, if so try to block it. Else → try to play the best move which could be placing at the centre (block 4) or the corners. Also if the computer is winning, check the sequence and try to complete the winning sequence. Switch the input back to user.

- Step 4 → Give the result after the loop is terminated.

→ Eg:  'o' is human





## CODE (Tic-Tac-Toe) :

```

import math import
random         def
print_board(board):
    """Prints the current state of the game board."""
    for
        row in [board[i:i+3] for i in range(0, 9, 3)]:
            print('| ' + ' | '.join(row) + ' |') def
available_moves(board):
    """Returns a list of available spots on the board."""
    return
        [i for i, spot in enumerate(board) if spot == ' ']
def check_winner(board, player):
    """Checks if the given player has won the game."""

```

```

# Check for winning rows for
i in range(0, 9, 3):
    if all(s == player for s in board[i:i+3]): return
        True

# Check for winning columns for
i in range(3):
    if board[i] == board[i+3] == board[i+6] == player: return
        True

# Check for winning diagonals if board[0] ==
board[4] == board[8] == player: return True
if board[2] == board[4] == board[6] == player: return
    True

return False

def minimax(board, is_maximizing):
    """
    Minimax algorithm to find the best move.
    'X' is the maximizing player (computer), 'O' is the minimizing player (human).
    """
    ai_player = 'X'
    human_player = 'O'

    if check_winner(board, ai_player):
        return 1, None
    if check_winner(board, human_player):
        return -1, None
    if not available_moves(board): return
        0, None

    if is_maximizing: best_score = -
        math.inf best_move = None for

```

```

move in available_moves(board):
    board[move] = ai_player score, _ =
    minimax(board, False) board[move]
    = '' if score > best_score: best_score
    = score best_move = move
return best_score, best_move else:
    best_score = math.inf best_move =
    None for move in
available_moves(board):
    board[move] = human_player score,
    _ = minimax(board, True)
    board[move] = ' ' if score <
best_score: best_score = score
best_move = move
return best_score, best_move

```

```
def get_computer_move(board):
```

```
    """
```

Gets a beatable move for the computer. It finds all moves with a positive score and chooses one randomly. If no such moves exist, it chooses a random move to prolong the game.

```
    """ ai_player = 'X'
```

```
    human_player =
    'O'
```

```
# If the board is empty, take the center.
```

```
if not available_moves(board): return
```

```
4
```

```
# Check for an immediate win for the computer
for move in available_moves(board):
    board[move] = ai_player if
check_winner(board, ai_player):
```

```

board[move] = '' return
move
board[move] = ''

# Check for an immediate block of the human player
for move in available_moves(board): board[move] =
human_player      if      check_winner(board,
human_player):
    board[move] = '' return
move
board[move] = ''

# If no immediate win or block, use a simplified minimax approach.
# Find all moves that result in a positive score.
positive_moves = [] for move in
available_moves(board):
    board[move] = ai_player score, _ =
minimax(board, False) board[move]
=   '   '   if   score   >   0:
positive_moves.append(move)

# If there are any moves that lead to a win or a draw, pick one at random.
if      positive_moves:      return
random.choice(positive_moves)

# If all remaining moves lead to a loss, choose a random available move to delay the loss.
return random.choice(available_moves(board))

```

```

def get_player_move(board):
    """Gets a valid move from the human player."""
    while True: try:

```

```

move = int(input("Enter your move (1-9): ")) - 1 if
move not in available_moves(board):
    print("Invalid move. Please enter a number from 1-9 that is not taken.")
else:
    return move
except ValueError: print("Invalid input. Please
enter a number.")

def play_game():
    """The main function to run the Tic-Tac-Toe game loop."""
    board
    = [' '] * 9
    print("Welcome to Tic-Tac-Toe!") print_board(board)
    # Let the human player ('O') go first. turn
    = 'O'

    while True:
        if turn == 'O':
            # Human's turn move =
            get_player_move(board)
            board[move] = 'O' else:
                # Computer's turn print("Computer
                is     thinking...")     move     =
                get_computer_move(board)
                board[move] = 'X'

        print(f"Player {turn} makes a move to square {move + 1}") print_board(board)

        # Check for a winner after the move
        if check_winner(board, turn):
            print(f"{turn} wins!") break

        # Check for a tie if not
        available_moves(board):

```

```
    print("It's a draw!") break
```

```
# Switch turns turn = 'X' if turn  
== 'O' else 'O'
```

```
if __name__ == "__main__":
```

```
    play_game()
```

### OUTPUT:

```
Welcome to Tic-Tac-Toe!  
| | | |  
| | | |  
| | | |  
Enter your move (1-9): 5  
Player O makes a move to square 5  
| | | |  
| | O | |  
| | | |  
Computer is thinking...  
Player X makes a move to square 6  
| | | |  
| | O | X |  
| | | |  
Enter your move (1-9): 1  
Player O makes a move to square 1  
| O | | |  
| | O | X |  
| | | |  
Computer is thinking...  
Player X makes a move to square 9  
| O | | |  
| | O | X |  
| | | X |  
Enter your move (1-9): 3  
Player O makes a move to square 3  
| O | | O |  
| | O | X |  
| | | X |  
Computer is thinking...  
Player X makes a move to square 2  
| O | X | O |  
| | O | X |  
| | | X |  
Enter your move (1-9): 7  
Player O makes a move to square 7  
| O | X | O |  
| | O | X |  
| O | | X |  
O wins!
```

### ALGORITHM (Vacuum Cleaner):

Vacuum Cleaner

→ Algorithm:

Step 1: Start  
 Step 2: Initialize 2D array with 2 rows and 2 columns.  
 Step 3: 00 → A, 01 → B, 10 → C, 11 → D  
 Step 4: We start with the cell (0,0). If it is dirty clean it.  
 while dirty rooms are > 0:  
 we check if current room is dirty, if so we clean the room, then we check for a move.  
 A move is valid only if the indices are inside the room and also if the adjacent room is dirty, we directly move to that room, also we mark the current room as visited.

Step 5: we print that all the rooms were clean:

→ Output:

Room =  $\begin{bmatrix} D & C \\ D & D \end{bmatrix}$

Started with (0,0) & cleaned it  
 Moved to (1,0) & cleaned it  
 Moved to (1,1) & cleaned it  
 Room is clean!

Room is clean!

## CODE (Vacuum cleaner) :

```
# Initialize room (2x2 grid), each cell could be 'dirty' or 'clean' room
= [
  ['dirty', 'clean'],
  ['dirty', 'dirty']
]
# Starting position x,
y = 0, 0
# Function to check if the current cell is dirty def
is_dirty(x, y):
    return room[x][y] == 'dirty'
```

```

# Function to clean the current cell def
clean(x, y):
    room[x][y] = 'clean' print(f'Cleaned
cell ({x},{y})')

# Function to move to a new position (up, down, left, or right) def
move_to(new_x, new_y):
    global x, y x, y = new_x,
    new_y print(f'Moved to
({x},{y})')

# Function to check if all cells are clean def
all_clean():
    for i in range(2):
        for j in range(2):
            if room[i][j] == 'dirty':
                return False
    return True

# Cleaning path: Visit each cell and clean (left to right, top to bottom)
# The allowed moves are up, down, left, right cleaning_path
= [(0, 0), (0, 1), (1, 1), (1, 0)]

# Start cleaning the room following the path
for cell in cleaning_path: move_to(cell[0],
cell[1]) if is_dirty(cell[0], cell[1]):
    clean(cell[0], cell[1])

# Final check to see if the room is clean if
all_clean():
    print("Room is clean!")
else:
    print("Some cells are still dirty.")

```

### **OUTPUT :**

```

Moved to (0,0)
Cleaned cell (0,0)
Moved to (0,1)
Moved to (1,1)
Cleaned cell (1,1)
Moved to (1,0)
Cleaned cell (1,0)
Room is clean!

```

## Program 2: Implement 8-puzzle

## **ALGORITHM:**

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## 8 - Puzzle Problem

→ Algorithm:

- 1) Initialize the board, start with the initial state where pieces are placed randomly.
- 2) Store the initial state in a queue and keep a visited array to check if the sequence has occurred or not, we will use BFS here.
- 3) → Until the queue is empty:
  - if we reach the final state, return
  - else, we try to move the blank piece in a valid place by doing a valid move.
  - A move is valid if the sequence hasn't occurred before and we are moving inside the box.
- 4) We add the next state to the queue and keep moving until we find the solution.

1	2	3
4	5	6
-	7	8

↑ right
up →

1	2	3
-	5	6
4	7	8

left →

1	2	3
5	-	6
4	7	8

No solution found after 2 moves

1	2	3
4	5	6
7	-	8

↑ right

C

1	2	3
4	5	6
7	8	-

Solution found in 2 steps (optimal)

→ Output:

▷ Best case  
 initial state = 

1	2	3
4	5	6
0	7	8

Solution found in 2 moves. Right → Right

▷ Average case = 

1	0	3
4	5	6
7	8	2

R → D → D → L → U → R → V → L → D → D → R

Solution found in 11 moves

▷ Worst case = 

1	0	4
3	5	6
7	8	2

No solution exists! (Solved in 156 moves)

→ Best is the best time with numbers  
 → Average number of steps etc.

## CODE:

```
from collections import deque
import copy
```

```
# Define the goal state
GOAL_STATE = [[1, 2, 3],
               [4, 5, 6],
               [7, 8, 0]]
```

```
# Directions for moving the blank tile  
DIRECTIONS = {
```

```

'Up': (-1, 0),
'Down': (1, 0),
'Left': (0, -1),
'Right': (0, 1)
}

def find_blank(state):
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                return i, j

def is_valid(x, y):
    return 0 <= x < 3 and 0 <= y < 3

def get_neighbors(state):
    neighbors = []
    x, y = find_blank(state)

    for move, (dx, dy) in DIRECTIONS.items():
        new_x, new_y = x + dx, y + dy
        if is_valid(new_x, new_y):
            new_state = copy.deepcopy(state) # Swap blank with adjacent tile
            new_state[new_x][new_y] = new_state[new_x][new_y], new_state[x][y]
            neighbors.append((move, new_state))

    return neighbors

def bfs(start_state):
    queue = deque([(start_state, [])])
    visited = set()

    while queue:
        current_state, path = queue.popleft()
        state_tuple = tuple(tuple(row) for row in current_state)

        if current_state == GOAL_STATE:
            return path # Return the solution if we reach the goal state

        if state_tuple in visited:
            continue
        visited.add(state_tuple)

        for move, neighbor in

```

```

get_neighbors(current_state):
    queue.append((neighbor, path + [move]))

# Example usage
start_state = [[1, 2, 3],
               [0, 4, 6],
               [7, 5, 8]]

solution = bfs(start_state)

# Since we removed "no solution" handling, it will keep exploring until it finds the solution if
# solution:
    print("Solution found in", len(solution), "moves:")
    -> .join(solution))

```

## **OUTPUT:**

```

Solution found in 3 moves:
[1, 2, 3]
[0, 4, 6]
[7, 5, 8]
-----
[1, 2, 3]
[4, 0, 6]
[7, 5, 8]
-----
[1, 2, 3]
[4, 5, 6]
[7, 0, 8]
-----
[1, 2, 3]
[4, 5, 6]
[7, 8, 0]
-----
```

## **Program 3:** Implement IDDFS

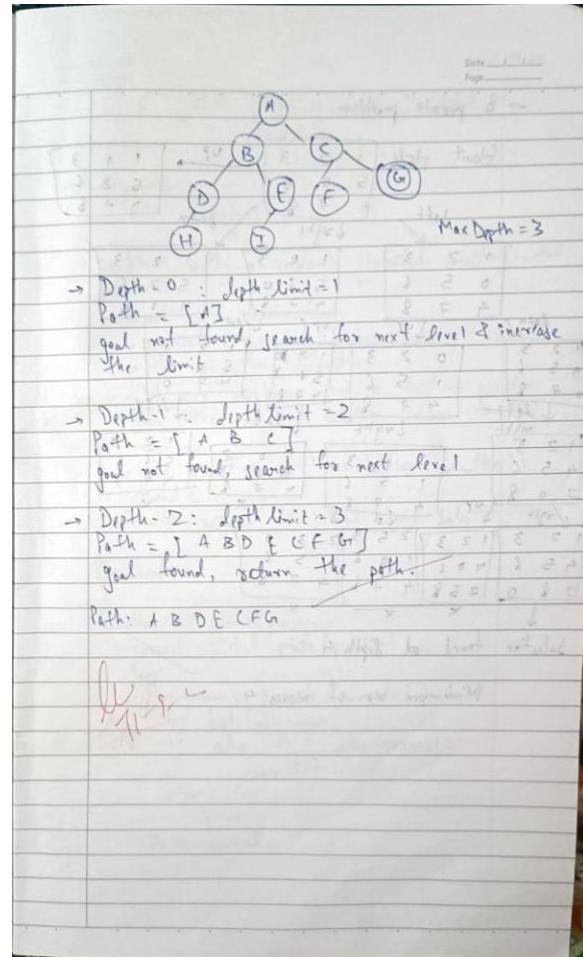
## **ALGORITHM :**

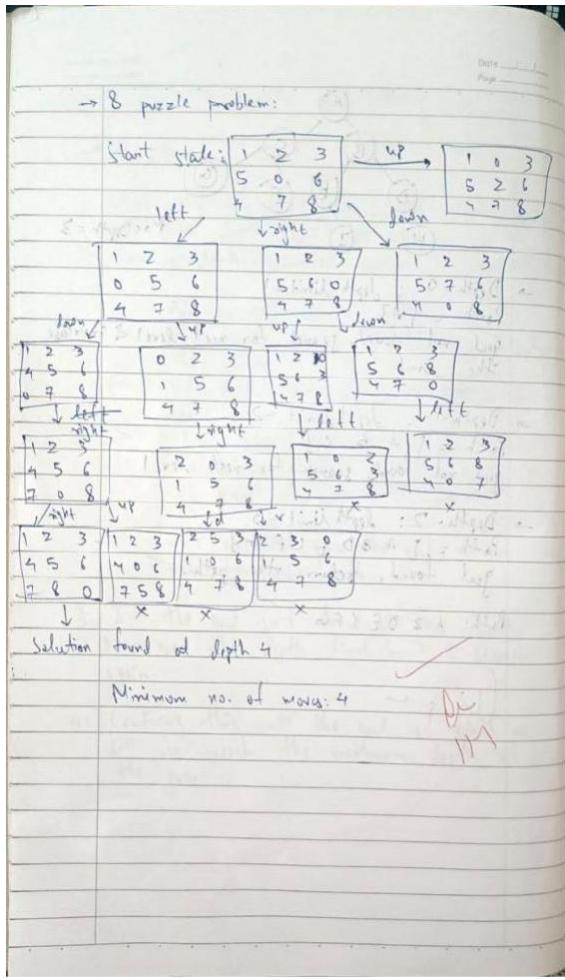
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**8-Puzzle using IDDFS**

→ Algorithm:

1. Start with the root node as the starting point, set the depth-limit to zero.
2. Run a depth-limited search with current limit:
  - Add current node to path
  - if current node is the goal, stop & return the path.
  - else if depth-limit reaches 0, remove this node from path & return failure. (not found at this level).
  - else for children of this node:
    - use recursion with Depth=1.
    - if no child gives the goal, remove this node from the path.
3. If the goal isn't found at this depth, increase the depth limit by 1 & search again.
4. Continue this until the goal is found or till we reach the maximum depth of the graph.





## CODE :

```
from collections import deque
```

```
# Directions for movement
```

```
MOVES = {
```

```
    'Up': -3,
```

```
    'Down': 3,
```

```
    'Left': -1,
```

```
    'Right': 1
```

```
}
```

```
# Define the goal state
```

```
GOAL_STATE = (1, 2, 3,
```

```
    4, 5, 6,
```

```
    7, 8, 0)
```

```
# Valid indices for moves def
```

```
valid_moves(index): moves
```

```

= [] row, col = divmod(index,
3)

    if row > 0: moves.append('Up') if
    row < 2: moves.append('Down') if
    col > 0: moves.append('Left') if
    col < 2: moves.append('Right')
    return moves

# Apply move to a state def
apply_move(state, move):
    idx = state.index(0) new_idx =
    idx + MOVES[move]

    # Special case for left/right edge wrapping
    if move == 'Left' and idx % 3 == 0: return
    None
    if move == 'Right' and idx % 3 == 2:
        return None

    state = list(state) state[idx], state[new_idx] =
    state[new_idx], state[idx] return tuple(state)

# DFS with depth limit def
dls(state, depth, visited, path): if
state == GOAL_STATE: return
path

    if depth == 0:
        return None

    visited.add(state) for move in
    valid_moves(state.index(0)): next_state =
    apply_move(state, move) if next_state and
    next_state not in visited:
        result = dls(next_state, depth - 1, visited.copy(), path + [(move, next_state)]) if
        result:
            return result
    return None

```

```

# IDDFS main function def
iddfs(start_state, max_depth=50):
    for depth in range(max_depth):
        print(f"\n--- Iteration {depth + 1}: Depth Limit = {depth} ---")
        visited = set() path = dls(start_state, depth, visited, [])
        if path is not None:
            return path
    return None

# Function to print the puzzle state in a readable format def
print_state(state):
    for i in range(0, 9, 3):
        print(state[i:i+3])
    print()

# Example usage if __name__ == '__main__':
start = (1, 2, 3,
          4, 5, 6,
          0, 7, 8)

print("Initial State:")
print_state(start)

solution = iddfs(start) if
solution:
    print(f"Solution found in {len(solution)} moves:")
    current_state = start for move, state in solution:
        print(f"Move: {move}") print_state(state)
        current_state = state
else:
    print("No solution found.")

```

## **OUTPUT :**

```
Initial State:  
(1, 2, 3)  
(4, 5, 6)  
(0, 7, 8)  
  
--- Iteration 1: Depth Limit = 0 ---  
  
--- Iteration 2: Depth Limit = 1 ---  
  
--- Iteration 3: Depth Limit = 2 ---  
Solution found in 2 moves:  
Move: Right  
(1, 2, 3)  
(4, 5, 6)  
(7, 0, 8)  
  
Move: Right  
(1, 2, 3)  
(4, 5, 6)  
(7, 8, 0)
```

#### Program 4: Implement Hill Climbing & Simulated Annealing

##### ALGORITHM:

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### Hill Climbing and Simulated Annealing

→ Algorithm:

- Hill Climbing

is Start with a randomly generated solution (initial solution).

repeat until termination:

- Generate the neighbouring solution using the objective function.
- If any neighbour has a better solution than the current solution, move to that neighbour.
- Keep repeating until no better solution is found.
- Finally return the best found solution.

Pseudocode

```

function hillClimb(problem):
    current = initial-state(problem)
    loop:
        neighbours = generate(current)
        b = best(neighbours)
        if value(b) > value(current):
            current = b
        else:
            break
    return current

```

Date \_\_\_\_\_  
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### N Queens using Hill Climb

1. Start with a random board.
2. Generate neighbours by moving a queen to every other row.
3. Choose the neighbour with the least no. of pair of queens attacking each other.
4. Move to the best neighbour if it exists else stop.
5. Continue until we reach optimal solution.
6. Return the best found solution.

→ Output:

Initial board:

Q . Q .  
. . . Q  
. Q .  
. . .

Move to board with 1 attack:

Q . Q .  
. . . Q  
. Q .  
. . .

Move to board with 0 attacks:

. Q .  
Q . .  
. . . Q  
. Q .

Solution found!  
Steps taken = 2

• Simulated Annealing:  
 1. Start with a random solution.  
 2. Initialize temperature  $T$  to a large value.  
 3. Loop until  $T$  is very small:  
    • generate a random neighbour solution.  
    • if the new soln is better, directly accept the soln.  
    • if not, we accept the solution based on probability ( $P = e^{-\Delta E/T}$ ) where  $\Delta E$  is change in the value of solution.  
    • update the temperature as  $T_{new} = \alpha \times T$  ( $\alpha$  is the cooling factor  $\Rightarrow$  generally between 0.7 & 0.9)  
 4. Return the best found solution.  
 → Pseudocode:  
 function simulated annealing (n):  
    curr = random state (n);  
    cost = cost (curr);  
    temp = 1000;  
    while temp != 0:  
        neighbour = neighbourstate (curr);  
        if random() < exp(-delta / temp):  
            update curr to neighbour;  
    temp = cooling  
 return curr

• N Queens using simulated annealing:  
 1. Start with a random board.  
 2. Set temp.  $T$  with a high value.  
 3. Pick a random neighbour, calculate  $\Delta E$ .  
 4. If the new neighbour is better, accept that else accept it based on probability  $p$ .  

$$P = e^{-\Delta E/T}$$
  
 5. Update the temperature using the cooling rule.  
 6. Return the final solution.  
 → Output:  
 Initial board:  
 ... Q . . .  
 . . . Q . .  
 . . . . Q .  
 . . . . . Q .  
 Iteration -1  $\Rightarrow$  1 attacks  
 . Q .  
 . . .  
 Q . .  
 . . Q .  
 Iteration -2  $\Rightarrow$  3 attacks  
 . Q .  
 . . Q .  
 Q . .  
 . . . .  
 Iteration -3  $\Rightarrow$  4 attacks

## CODE (Hill Climbing) :

```

import random
def heuristic(board):
    h = 0
    n = len(board)
    for i in range(n):
        for j in range(i+1, n):
            if board[i] == board[j] or abs(board[i]-board[j]) == abs(i-j):
                h += 1
    return h

def hill_climbing_restart(initial_board, max_restarts=100):
    N = len(initial_board)
    board = [x-1 for x in initial_board]
    # 0-based h = heuristic(board)

    restart_count = 0
    while h != 0 and restart_count < max_restarts:
    
```

```

steps = 0 while True:
best_board = board[:]
best_h = h for col in
range(N):
    for row in range(N):
        if row != board[col]: neighbor =
            board[:] neighbor[col] = row h_neighbor
            = heuristic(neighbor) if h_neighbor <
            best_h: best_board = neighbor best_h =
            h_neighbor steps += 1 if best_h >= h: #
            stuck
                break
            board =
            best_board h =
            best_h if h == 0:
                break
        if h == 0: print(f"Solution found after {restart_count} restarts and {steps} steps.") break # Random restart board = [random.randint(0, N-1) for _ in range(N)] h = heuristic(board) restart_count += 1 return [x+1 for x in board], h

```

# User input

```

N = int(input("Enter number of queens (N): ")) print(f"Enter the initial positions of {N} queens (row numbers 1 to {N}):") initial_board =
list(map(int, input().split()))

```

```

solution, h_val = hill_climbing_restart(initial_board)
print("Final board:", solution) print("Heuristic H =", h_val)

```

### OUTPUT (Hill Climbing) :

```

Enter number of queens (N): 4
Enter the initial positions of 4 queens (row numbers 1 to 4):
3 4 1 2
Solution found after 0 restarts and 3 steps.
Final board: [2, 4, 1, 3]
Heuristic H = 0

==== Code Execution Successful ====

```

### CODE (Simulated Annealing):

```

from datetime import datetime
import random, time, math from

```

```

copy import deepcopy, copy
import decimal

class Board:
    def __init__(self, queen_count=4):
        self.queen_count = queen_count
        self.reset()

    def reset(self):
        self.queens = [-1 for i in range(0, self.queen_count)]

        for i in range(0, self.queen_count): self.queens[i] =
            random.randint(0, self.queen_count - 1)
            # self.queens[row] = column

    def calculateCost(self):
        threat = 0

        for queen in range(0, self.queen_count):
            for next_queen in range(queen+1, self.queen_count):
                if self.queens[queen] == self.queens[next_queen] or abs(queen - next_queen) ==
                    abs(self.queens[queen] - self.queens[next_queen]): threat += 1 return threat

    @staticmethod
    def calculateCostWithQueens(queens):
        threat = 0
        queen_count = len(queens)

        for queen in range(0, queen_count):
            for next_queen in range(queen+1, queen_count):
                if queens[queen] == queens[next_queen] or abs(queen - next_queen) ==
                    abs(queens[queen] - queens[next_queen]):

                    threat += 1 return threat

    @staticmethod
    def toString(queens):
        board_string = ""

        for row, col in enumerate(queens):
            board_string += "(%s, %s)\n" % (row, col)

```

```

    return board_string

def getLowerCostBoard(self):
    displacement_count = 0  temp_queens =
    self.queens           lowest_cost       =
    self.calculateCost(temp_queens)

    for i in range(0, self.queen_count):
        temp_queens[i] = (temp_queens[i] + 1) % (self.queen_count - 1)

        for j in range(queen+1, self.queen_count):
            temp_queens[j] = (temp_queens[j] + 1) % (self.queen_count - 1)

def __str__(self):
    board_string = ""

    for row, col in enumerate(self.queens):
        board_string += "%s, %s\n" % (row, col)

    return board_string

class SimulatedAnnealing:
    def __init__(self, board):
        self.elapsedTime = 0;
        self.board = board
        self.temperature = 4000
        self.sch = 0.99
        self.startTime =
        datetime.now()

    def run(self):
        board = self.board board_queens =
        self.board.queens[:] solutionFound
        = False

        for k in range(0, 170000):
            self.temperature *= self.sch
            board.reset() successor_queens =
            board.queens[:]
            dw = Board.calculateCostWithQueens(successor_queens) -
            Board.calculateCostWithQueens(board_queens) exp =
            decimal.Decimal(decimal.Decimal(math.e) ** (decimal.Decimal(-dw) *

```

```

decimal.Decimal(self.temperature)))

if dw > 0 or random.uniform(0, 1) < exp:
    board_queens = successor_queens[:]

if Board.calculateCostWithQueens(board_queens) == 0:
    print("Solution:")      print(Board.toString(board_queens))
    self.elapsedTime = self.getElapsedTime()  print("Success,
Elapsed Time: %sms" % (str(self.elapsedTime))) solutionFound
= True break

if solutionFound == False:
    self.elapsedTime = self.getElapsedTime()  print("Unsuccessful,
Elapsed Time: %sms" % (str(self.elapsedTime))) return self.elapsedTime

def getElapsedTime(self):    endTime = datetime.now()
    elapsedTime = (endTime - self.startTime).microseconds / 1000
    return elapsedTime

if __name__ == '__main__':
    board = Board()
    print("Board:")
    print(board)
    SimulatedAnnealing(board
    ).run()

```

## **OUTPUT (Simulated Annealing):**

**Board:**

(0, 1)  
(1, 0)  
(2, 1)  
(3, 3)

**Solution:**

(0, 2)  
(1, 0)  
(2, 3)  
(3, 1)

*Success, Elapsed Time: 7.9ms*

## Program 5: A\* Algorithm

### ALGORITHM :

8 - Puzzle using A\*

→ Pseudo code:

1. Initialize  
Open list

2. Start with the defined goal state.

3. Initialize open list with a priority queue with start state.

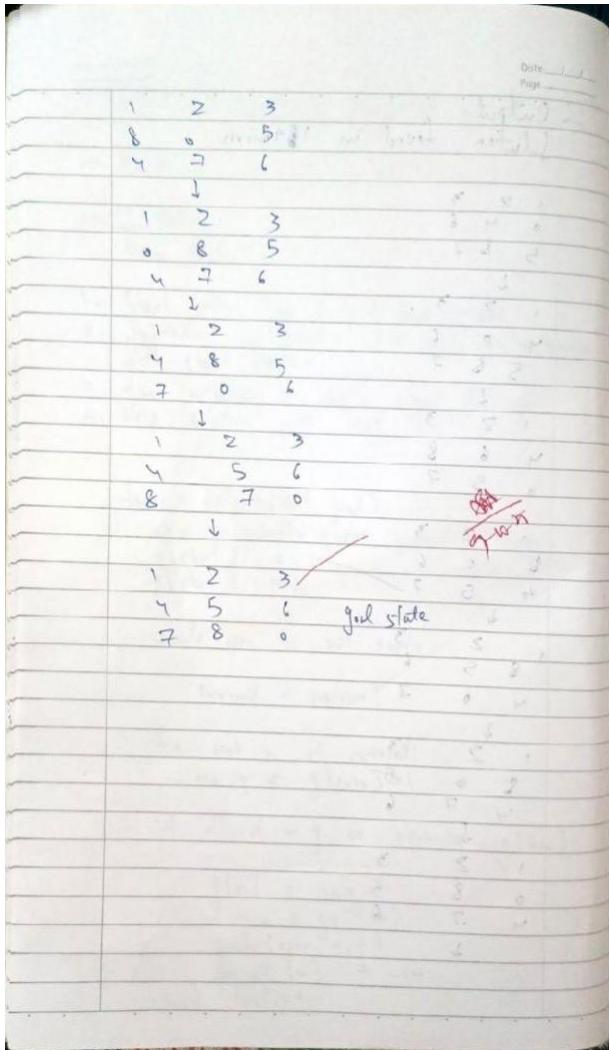
4. Also initialize an empty closed list.

5. Keep solution with least f(n).

func Astart(start, goal):  
open ← priority queue ordered by f - g[n]  
g[start] = 0  
f[start] = None  
while open is not empty:  
    current ← pop(open)  
    for each n of current:  
        new ← g[current] + 1  
        if n not in g or new - g < g[new]:  
            g[n] ← new  
            f[n] ← g[n] + h(n)  
            push(open, n, f)  
            print[n] ← new  
    solution ← failure

→ Output:  
Solution found in 184 moves

1 2 3  
0 4 6  
5 8 7  
↓  
1 2 3  
4 0 6  
5 8 7  
↓  
1 2 3  
4 6 8  
0 5 7  
↓  
1 2 3  
8 0 6  
4 5 7  
↓  
1 2 3  
8 5 6  
4 0 7  
↓  
1 2 3  
0 8 5  
4 7 6  
↓  
1 2 3



## CODE :

```

import heapq

class PuzzleState:
    def __init__(self, board, parent=None, move="", depth=0, cost=0):
        self.board = board
        self.parent = parent
        self.move = move
        self.depth = depth
        self.cost = cost

    def __lt__(self, other):
        return self.cost < other.cost

    def blank_pos(self):

```

```

        return self.board.index(0)
def expand(self):
    b = self.blank_pos()
    row, col = divmod(b, 3)
    dirs = {
        "Up": (row - 1, col),
        "Down": (row + 1, col),
        "Left": (row, col - 1),
        "Right": (row, col + 1)
    } nxt = [] for mv, (r, c) in
    dirs.items():
        if 0 <= r < 3 and 0 <= c < 3:
            idx = r * 3 + c nb = self.board[:] nb[b], nb[idx] =
            nb[idx], nb[b] nxt.append(PuzzleState(nb, self, mv,
            self.depth + 1))
    return nxt

def
    build_path(self):
        p, node = [], self
        while node:
            p.append((node.move, node.board, node.depth)) node
            = node.parent
        return list(reversed(p))

def misplaced_tiles(state, goal):
    return sum(1 for i in range(9) if state.board[i] not in (0, goal[i]))

def      manhattan_distance(state,
    goal): d = 0 for i, v in
    enumerate(state.board):
        if v != 0:
            r1, c1 = divmod(i, 3) r2, c2 =
            divmod(goal.index(v), 3) d +=
            abs(r1 - r2) + abs(c1 - c2)
    return d

def a_star(start, goal, h):
    opened = [] closed =
    set() nodes = 0 s =
    PuzzleState(start)
    s.cost = h(s, goal)

```

```

heapq.heappush(opened, s)

while opened:
    cur = heapq.heappop(opened)
    nodes += 1

    if cur.board == goal: return
    cur.build_path()
    nodes
    closed.add(tuple(cur.board))

    for nxt in cur.expand():
        if tuple(nxt.board) in closed: continue
        nxt.cost = nxt.depth + h(nxt, goal)
        heapq.heappush(opened, nxt)

return None, nodes

def print_solution(path, total_nodes):
    print("Steps:\n")
    print("Move {mv} | Depth {d}" for mv, st, d in path)
    print(" ".join(str(x) if x != 0 else " " for x in st[1:-1]))
    print()
    print(f"Total Moves: {len(path)-1}")
    print(f"Nodes Expanded: {total_nodes}")

if __name__ == "__main__":
    start = [1, 2, 3, 4, 0, 6, 7, 5, 8]
    goal = [1, 2, 3, 4, 5, 6, 7, 8, 0]

    print("A* (Misplaced Tiles)\n")
    sol1, n1 = a_star(start, goal, misplaced_tiles)
    if sol1:
        print_solution(sol1, n1)
    else:
        print("No solution.")

```

```

print("\nA* (Manhattan Distance)\n") sol2, n2 =
a_star(start, goal, manhattan_distance) if sol2:
print_solution(sol2, n2)
else:
    print("No solution.")

```

## OUTPUT :

```

A* (Misplaced Tiles)

Steps:

Start | Depth 0
1 2 3
4   6
7 5 8

Move Down | Depth 1
1 2 3
4 5 6
7   8

Move Right | Depth 2
1 2 3
4 5 6
7 8

Total Moves: 2
Nodes Expanded: 3

A* (Manhattan Distance)

Steps:

Start | Depth 0
1 2 3
4   6
7 5 8

Move Down | Depth 1
1 2 3
4 5 6
7   8

Move Right | Depth 2
1 2 3
4 5 6
7 8

Total Moves: 2
Nodes Expanded: 3

```

## Program 6: Propositional Logic

### ALGORITHM :

<p style="text-align: right;">Date 16/10/25 Page</p> <p>Propositional Logic</p> <p>→ Pseudocode</p> <pre> function TT-Entails(KB, α)     inputs: KB (knowledge base, a sentence in propositional logic),             α (query, a sentence in propositional logic)     symbols → a list of proposition symbols in KB and α     return TT-Check-All(KB, α, symbols, { }) </pre> <p>function TT-Check-All(KB, α, symbols, model)</p> <pre> if EMPTY?(symbols) then     if P1-TRUE?(KB, model) then return     P1-TRUE?(α, model)     else return false // when KB false, always return true else do     P ← FIRST(symbols)     rest ← REST(symbols)     return (TT-Check-All(KB, α, rest,                          model ∪ {P = true})) ∨            (TT-Check-All(KB, α, rest, model ∪                          {P = false})) </pre>	<p style="text-align: right;">Date 16/10/25 Page</p> <p>Q. <math>\neg q \rightarrow p</math>  <math>\neg p \rightarrow \neg q</math>  <math>\neg q \vee r</math></p> <p>Truth Table</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th>P</th> <th>Q</th> <th>R</th> <th><math>\neg q</math></th> <th><math>q \rightarrow p</math></th> <th><math>p \rightarrow \neg q</math></th> <th><math>\neg q \vee r</math></th> <th>KB</th> </tr> </thead> <tbody> <tr><td>f</td><td>t</td><td>f</td><td>t</td><td>t</td><td>t</td><td>t</td><td>f</td></tr> <tr><td>f</td><td>t</td><td>t</td><td>t</td><td>t</td><td>t</td><td>t</td><td>t</td></tr> <tr><td>f</td><td>f</td><td>f</td><td>t</td><td>t</td><td>t</td><td>t</td><td>f</td></tr> <tr><td>t</td><td>f</td><td>f</td><td>t</td><td>f</td><td>f</td><td>t</td><td>f</td></tr> <tr><td>t</td><td>t</td><td>f</td><td>t</td><td>t</td><td>f</td><td>t</td><td>f</td></tr> <tr><td>t</td><td>f</td><td>t</td><td>t</td><td>t</td><td>t</td><td>t</td><td>t</td></tr> <tr><td>t</td><td>t</td><td>t</td><td>t</td><td>t</td><td>t</td><td>t</td><td>t</td></tr> <tr><td>t</td><td>t</td><td>f</td><td>t</td><td>t</td><td>f</td><td>t</td><td>f</td></tr> </tbody> </table> <p>⇒ Does KB entail P?</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th>P</th> <th>KB</th> </tr> </thead> <tbody> <tr><td>f</td><td>f</td></tr> <tr><td>t</td><td>t</td></tr> <tr><td>t</td><td>f</td></tr> <tr><td>f</td><td>f</td></tr> <tr><td>t</td><td>t</td></tr> <tr><td>f</td><td>f</td></tr> <tr><td>t</td><td>t</td></tr> <tr><td>f</td><td>f</td></tr> </tbody> </table> <p>• Whenever KB is true, P is also true.</p> <p>• KB entails P</p>	P	Q	R	$\neg q$	$q \rightarrow p$	$p \rightarrow \neg q$	$\neg q \vee r$	KB	f	t	f	t	t	t	t	f	f	t	t	t	t	t	t	t	f	f	f	t	t	t	t	f	t	f	f	t	f	f	t	f	t	t	f	t	t	f	t	f	t	f	t	t	t	t	t	t	t	t	t	t	t	t	t	t	t	t	f	t	t	f	t	f	P	KB	f	f	t	t	t	f	f	f	t	t	f	f	t	t	f	f
P	Q	R	$\neg q$	$q \rightarrow p$	$p \rightarrow \neg q$	$\neg q \vee r$	KB																																																																																				
f	t	f	t	t	t	t	f																																																																																				
f	t	t	t	t	t	t	t																																																																																				
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Does KB entail $R \rightarrow P$ ?			
R	P	$R \rightarrow P$	KB
f	f	t	f
t	f	f	t
f	t	t	f
t	t	f	f
f	t	t	f
t	t	t	t
t	t	t	f
t	t	t	f

We can see that when KB is true  $R \rightarrow P$  is false.

∴ KB doesn't entail  $R \rightarrow P$ .

Does KB entail $Q \rightarrow R$ ?	
$Q \rightarrow R$	KB
t	f
t	t
f	f
t	f
t	t
t	t
t	t
t	f
t	t

Whenever KB is true,  $Q \rightarrow R$  is also true.

∴ KB entails  $Q \rightarrow R$

## CODE:

```
import itertools
```

```
# Logical operations def
implies(a, b):
    return not a or b
```

```
def or_operator(a, b):
    return a or b
```

```
def not_operator(a):
    return not a
```

```
# Constructing the truth table
def construct_truth_table():
```

```

truth_values = [True, False]
truth_table = []

# Generate all combinations for Q, P, R for values in
itertools.product(truth_values, repeat=3): Q, P, R =
values

# Evaluate KB sentences q_implies_p =
implies(Q, P) p_implies_not_q = implies(P,
not_operator(Q)) q_or_r = or_operator(Q, R)

# KB = (Q → P) ∧ (P → ¬Q) ∧ (Q ∨ R) kb_is_true =
q_implies_p and p_implies_not_q and q_or_r

# Entailment expressions entail_r =
R entail_r_implies_p = implies(R,
P) entail_q_implies_r = implies(Q,
R)

# Add row to truth table truth_table.append(( Q, P,
R, q_implies_p, p_implies_not_q, q_or_r,
kb_is_true, entail_r, entail_r_implies_p,
entail_q_implies_r
))
return truth_table

# Print the truth table nicely def
print_truth_table(truth_table):
    header = [
        "Q", "P", "R",
        "Q → P", "P → ¬Q", "Q ∨ R",
        "KB (all true)",
        "R", "R → P", "Q → R"
    ]
    print(" | ".join(header)) print("-"
    * 85)

    for row in truth_table:
        # Format True/False as T/F for compactness
        formatted_row = [("T" if val else "F") for val in row]
        print(" | ".join(formatted_row))

# Generate and print truth table
truth_table =

```

```

construct_truth_table()
print(truth_table)

# Additionally, check entailment by verifying if for all models where KB is true, entailment is true

def check_entailment(truth_table, entailment_index):
    for row in truth_table: kb_true = row[6]
        entailment_val = row[entailment_index]
        if kb_true and not entailment_val:
            return False
    return True

print("\nEntailment Results:")
print(f"Does KB entail R? {check_entailment(truth_table, 7)}")
print(f"Does KB entail R → P? {check_entailment(truth_table, 8)}")
print(f"Does KB entail Q → R? {check_entailment(truth_table, 9)}")

```

### **OUTPUT :**

```

Q | P | R | Q → P | P → ¬Q | Q ∨ R | KB (all true) | R | R → P | Q → R
-----
```

T	T	T	T	F	T	F	T	T	T	T
T	T	F	T	F	T	F	F	T	F	
T	F	T	F	T	T	F	T	F	T	
T	F	F	F	T	T	F	F	T	F	
F	T	T	T	T	T	T	T	T	T	
F	T	F	T	T	F	F	F	T	T	
F	F	T	T	T	T	T	T	F	T	
F	F	F	T	T	F	F	F	T	T	

Entailment Results:

```

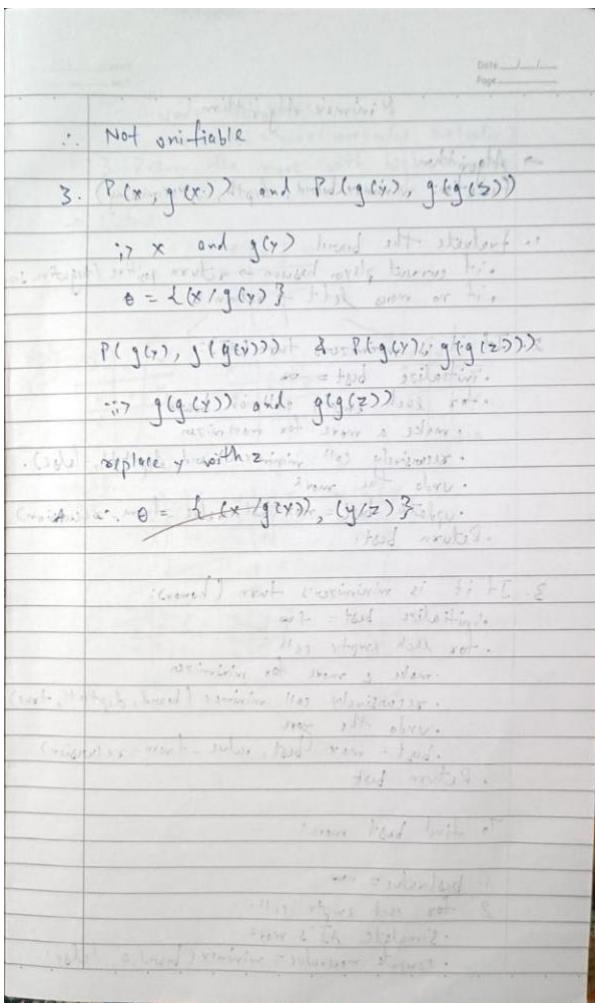
Does KB entail R? True
Does KB entail R → P? False
Does KB entail Q → R? True

```

### **Program 7:** Unification

#### **Algorithm:**

<p style="text-align: center;">Date 30.10.26 Page _____</p> <p><b>Unification</b></p> <p>→ Algorithm (C) for Unification</p> <p>Unify (<math>\varphi_1, \varphi_2</math>)</p> <p>(C) If <math>\varphi_1 = \varphi_2</math> is a variable or constant, then return <math>\varphi_1</math>.</p> <p>a) If <math>\varphi_1 \neq \varphi_2</math> are identical, return NIL.</p> <p>b) Else if <math>\varphi_1</math> is a variable:</p> <ul style="list-style-type: none"> <li>• If <math>\varphi_1</math> occurs in <math>\varphi_2</math>, return FAILURE.</li> <li>• Else return <math>\{\varphi_2 / \varphi_1\}</math>.</li> </ul> <p>c) Else if <math>\varphi_2</math> is a variable:</p> <ul style="list-style-type: none"> <li>• If <math>\varphi_2</math> occurs in <math>\varphi_1</math>, return FAILURE.</li> <li>• Else return <math>\{\varphi_1 / \varphi_2\}</math>.</li> </ul> <p>d) Else return FAILURE.</p> <p>2. If the initial predicate symbol in <math>\varphi_1</math> and <math>\varphi_2</math> isn't same, return FAILURE.</p> <p>3. If <math>\varphi_1, \varphi_2</math> have diff no. of arguments, return FAILURE.</p> <p>4. Set substitution <math>\text{SUBST} = \text{NIL}</math>.</p> <p>5. For i=1 to no. of elements in <math>\varphi_1, \varphi_2</math> do</p> <ul style="list-style-type: none"> <li>• as (C) unify function with i-th element of both <math>\varphi_1, \varphi_2</math>, put result in S.</li> <li>• If S = failure, then return FAILURE.</li> <li>• If S ≠ NIL, then do       <ul style="list-style-type: none"> <li>• Apply S to remaining of both <math>\varphi_1, \varphi_2</math></li> <li>• <math>\text{SUBST} = \text{APPEND}(S, \text{SUBST})</math></li> </ul> </li> </ul> <p>6. Return SUBST</p>	<p style="text-align: center;">Date 30.10.26 Page _____</p> <p>17 <math>P(f(x), g(y), z)</math> <math>P(f(g(z)), g(f(x)), f(a))</math></p> <p>int <math>f(x)</math> and <math>f(g(z))</math></p> <p><math>x \rightarrow g(z)</math> (as both have same predicate)</p> <p>∴ we replace <math>x</math> with <math>g(z)</math>.</p> <p><math>\theta = \{x/g(z)\}</math> and <math>P(f(g(z)), g(\theta), f(a))</math></p> <p><math>P(f(g(z)), g(f(a)), f(a))</math></p> <p><math>y \rightarrow f(a)</math> (as both have same predicate)</p> <p><math>\theta = \{x/g(z), y/f(a)\}</math></p> <p><math>P(f(g(z)), g(f(a)), f(a))</math></p> <p><math>\therefore \theta = \{x/f(a)\}</math> and <math>P(f(f(a)), g(f(a)), f(a))</math></p> <p><math>P(f(f(a)), g(f(a)), f(a))</math></p> <p><math>f(f(a))</math> and <math>g(f(a))</math> and <math>g(f(f(a)))</math></p> <p><math>\therefore y</math> occurs on both sides</p>
--	---



## CODE :

```

class Variable:
    def __init__(self, name):
        self.name = name

    def __eq__(self, other):
        return isinstance(other, Variable) and self.name == other.name

    def __hash__(self):
        return hash(self.name)

    def __repr__(self):
        return self.name

class Constant:
    def __init__(self, value):
        self.value = value

```

```

def __eq__(self, other):
    return isinstance(other, Constant) and self.value == other.value

def __hash__(self):
    return hash(self.value)

def __repr__(self):
    return str(self.value)

class Function:
    def __init__(self, name, args):
        self.name = name
        self.args = args

    def __eq__(self, other):
        return (isinstance(other, Function) and self.name ==
               other.name and len(self.args) == len(other.args) and all(a == b for a, b in
               zip(self.args, other.args)))

    def __hash__(self):
        return hash((self.name, tuple(self.args)))

    def __repr__(self):
        return f'{self.name}({", ".join(map(str, self.args))})'

def unify(term1, term2, substitution=None):
    """
    Unifies two first-order logic terms and returns the MGU (substitution) or
    None if unification is not possible.
    """
    if substitution is None:
        substitution = {}

    # Apply existing substitutions
    term1 = substitute(term1, substitution)
    term2 = substitute(term2, substitution)

    if term1 == term2:
        return substitution
    elif isinstance(term1, Variable):
        return unify_var(term1, term2, substitution)
    elif isinstance(term2, Variable):

```

```

        return unify_var(term2, term1, substitution)
    elif isinstance(term1, Function) and isinstance(term2, Function):
        if term1.name != term2.name or len(term1.args) != len(term2.args):
            return None # Function symbols or arity don't match
        for arg1, arg2 in zip(term1.args, term2.args):
            substitution = unify(arg1, arg2, substitution)
        if substitution is None:
            return None # Sub-unification failed
        return substitution
    else:
        return None # Cannot unify different types (e.g., Constant and Function)

def unify_var(var, x, substitution):
    """Handles unification when one of the terms is a variable."""
    if var in substitution: return unify(substitution[var], x,
                                         substitution)
    elif x in substitution:
        return unify(var, substitution[x], substitution)
    elif occurs_check(var, x, substitution):
        return None # Occurs check fails
    else:
        substitution[var] = x
        return substitution

def occurs_check(var, term, substitution):
    """Checks if a variable occurs within a term, preventing infinite substitutions."""
    term = substitute(term, substitution) # Apply current substitutions if var == term:
    return True
    elif isinstance(term, Function):
        return any(occurs_check(var, arg, substitution) for arg in term.args)
    return False

def substitute(term, substitution):
    """Applies a given substitution to a term."""
    if isinstance(term, Variable): return
    substitution.get(term, term)
    elif isinstance(term, Function):
        return Function(term.name, [substitute(arg, substitution) for arg in term.args])
    return term

# Example Usage:
if __name__ == "__main__":
    # Define terms

```

```

x, y, z = Variable('x'), Variable('y'), Variable('z')
a, b = Constant('a'), Constant('b') f = Function('f',
[x, Constant('b')]) g = Function('g',
[Constant('a'), y]) h = Function('h', [z])

print(f"Unify(f(x, b), f(a, y)): {unify(Function('f', [x, b]), Function('f', [a, y]))}")
print(f"Unify(g(a, y), g(a, b)): {unify(Function('g', [a, y]), Function('g', [a, b]))}")
print(f"Unify(x, f(x, b)): {unify(x, Function('f', [x, b]))}" # Occurs check failure
print(f"Unify(f(x, y), f(a, g(z))): {unify(Function('f', [x, y]), Function('f', [a, Function('g',
[z])]))}")
print(f"Unify(P(x, A), P(B, y)): {unify(Function('P', [x, Constant('A')]),
Function('P', [Constant('B'), y]))}")

print("\n--- Your Requested Tests ---")

# 1. p(f(x), g(y), y) and p(f(g(z)), g(f(a)), f(a)) term1_1 =
Function('p', [Function('f', [x]), Function('g', [y]), y])
term1_2 = Function('p', [Function('f', [Function('g', [z])]), Function('g', [Function('f', [a])]),
Function('f', [a])]) print(f"Unify(p(f(x), g(y), y), p(f(g(z)), g(f(a)), f(a))): {unify(term1_1, term1_2)}")

# 2. q(x, f(x)) and q(f(y), y) term2_1 = Function('q', [x,
Function('f', [x])]) term2_2 = Function('q', [Function('f', [y]), y])
print(f"Unify(q(x, f(x)), q(f(y), y)): {unify(term2_1,
term2_2)}")

# 3. p(x, g(x)) and p(g(y), g(g(z))) term3_1 = Function('p', [x, Function('g',
[x])]) term3_2 = Function('p', [Function('g', [y]), Function('g', [Function('g',
[z])])]) print(f"Unify(p(x, g(x)), p(g(y), g(g(z)))): {unify(term3_1,
term3_2)}")

```

## OUTPUT :

```

unify(f(x, b), f(a, y)): {x: a, y: b}
unify(g(a, y), g(a, b)): {y: b}
unify(x, f(x, b)): None
unify(f(x, y), f(a, g(z))): {x: a, y: g(z)}
unify(P(x, A), P(B, y)): {x: B, y: A}

--- Your Requested Tests ---
unify(p(f(x), g(y), y), p(f(g(z)), g(f(a)), f(a))): {x: g(z), y: f(a)}
unify(q(x, f(x)), q(f(y), y)): None
unify(p(x, g(x)), p(g(y), g(g(z)))): {x: g(y), y: z}

```

## Program 8: MinMax & AlphaBeta

### ALGORITHM :

Minimax Algorithm  
& Alpha-Beta Pruning

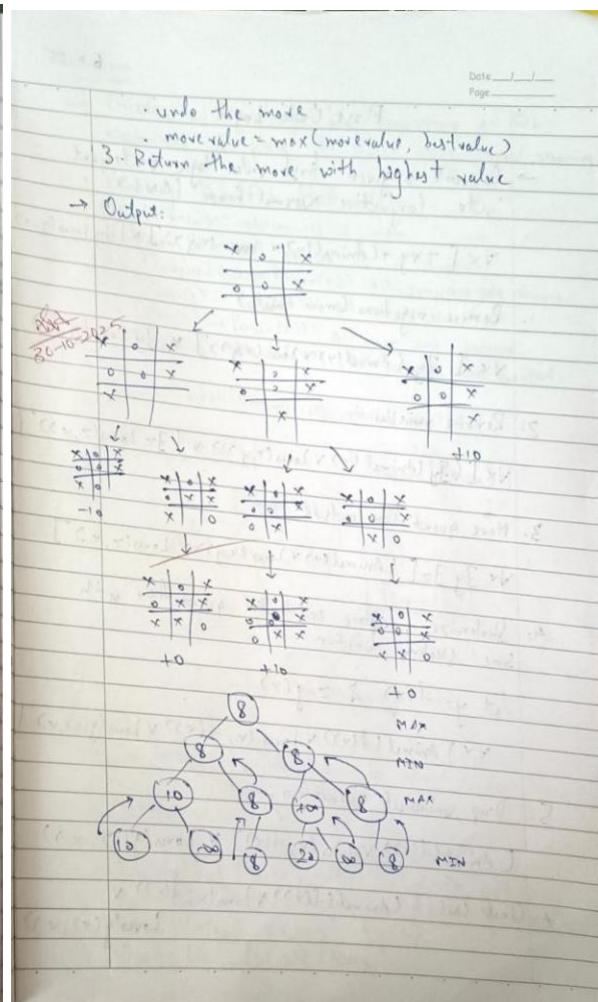
→ Algorithm

```
function minimax(board, depth, isMaximizing)
    alphabeta(state, α, β)
```

- Evaluate the board
  - if current player has won → return positive/negative
  - if no moves left → return 0
- If it is maximizer's turn (A):
  - initialize best = -∞
  - for each empty cell:
    - make a move for maximizer
    - recursively call minimax (board, depth+1, false).
    - undo the move; if best ≥ β → return best
    - update best = max(best, value - from recursion)
  - Return best &  $\alpha = \max(\alpha, \text{best})$
- If it is minimizer's turn (B):
  - initialize best = +∞
  - for each empty cell:
    - make a move for minimizer
    - recursively call minimax (board, depth+1, true).
    - undo the move; if best ≤ α → return best
    - update best = min(best, value - from recursion)
  - Return best &  $\beta = \min(\beta, \text{best})$

To find best move:

- bestValue = -∞
- for each empty cell:
  - simulate A/B's move
  - compute nextValue = minimax (board, 0, !isMaximizing)



## CODE :

```
def alpha_beta(node, depth, alpha, beta, maximizing_player, path):
    # Base case: if node is a leaf (integer), return its value and path
    if isinstance(node, int):
        return node, path

    if
        maximizing_player
        : value = float('-inf') best_path =
        None
        for i, child in enumerate(node):
            child_value, child_path = alpha_beta( child,
                depth + 1, alpha, beta, False, path + [i]
            )
            if maximizing_player:
                if child_value > best_value:
                    best_value = child_value
                    best_path = child_path
            else:
                if child_value < best_value:
                    best_value = child_value
                    best_path = child_path
            if best_value == alpha or best_value == beta:
                break
        return best_value, best_path
```

```

if child_value > value:
    value = child_value
    best_path =
        child_path

# Artifact '62' removed here alpha
= max(alpha, value)

if alpha >= beta:
    print(f" [PRUNE] MAX (Depth {depth}): Alpha ({alpha}) >= Beta ({beta})")
break return value, best_path

else:
    value = float('inf') best_path
    = None

for i, child in enumerate(node):
    child_value, child_path = alpha_beta( child,
        depth + 1, alpha, beta, True, path + [i]
    )

    if child_value < value:
        value = child_value
        best_path = child_path
        beta = min(beta, value)

    if beta <= alpha:
        print(f" [PRUNE] MIN (Depth {depth}): Beta ({beta}) <= Alpha ({alpha})")
break return value, best_path

if __name__ == "__main__":
    # Tree structure with artifact '63' removed tree
    =
    [
        [
            [
                [10, 11],
                [9, 12]
            ],
            [
                [14, 15],

```

```

        [13, 14]
    ],
],
[
[
    [
        [5, 2],
        [4, 1]
    ],
    [
        [3, 22],
        [20, 21]
    ],
]
]

print("Starting Alpha-Beta Pruning...\n" + "-"*30) value, best_path =
alpha_beta(tree, 0, float('-inf'), float('inf'), True, [])

print("-" * 30)
print(f"FINAL MINIMAX VALUE AT ROOT: {value}") print(f"BEST
PATH INDICES: {best_path}")

```

### OUTPUT :

```

Starting Alpha-Beta Pruning...
-----
[PRUNE] MIN (Depth 3): Beta (9) <= Alpha (10)
[PRUNE] MAX (Depth 2): Alpha (14) >= Beta (10)
[PRUNE] MIN (Depth 3): Beta (5) <= Alpha (10)
[PRUNE] MIN (Depth 3): Beta (4) <= Alpha (10)
[PRUNE] MIN (Depth 1): Beta (5) <= Alpha (10)
-----
FINAL MINIMAX VALUE AT ROOT: 10
BEST PATH INDICES: [0, 0, 0, 0]

```

### Program 9: Forward Chaining & Conversion to CNF

### ALGORITHM :

Date: 6/11/25  
Page: \_\_\_\_\_

**First Order Logic**

→ Convert a given first-order logic statement into Conjunctive Normal Form (CNF)

$$\forall x \neg \forall y \neg (\text{Animal}(y) \wedge \text{Loves}(x, y)) \vee \neg \exists y \text{Loves}(y, x)$$

1. Remove negations (move inside)
$$\forall x \neg \forall y (\neg \text{Animal}(y) \vee \neg \text{Loves}(x, y)) \vee \neg \exists y \text{Loves}(y, x)$$
2. Rename variables
$$\forall x \neg (\exists y (\neg \text{Animal}(y) \vee \text{Loves}(x, y)) \vee \exists z \text{Loves}(z, x))$$
3. Move quantifiers outside
$$\forall x \exists y \exists z (\neg \text{Animal}(y) \vee \text{Loves}(x, y) \vee \text{Loves}(z, x))$$
4. Eliminate existential quantifiers with Skolem function
$$\text{let } y = f(x) \text{ and } z = g(x)$$

$$\forall x (\text{Animal}(f(x)) \vee \text{Loves}(x, f(x)) \vee \text{Loves}(g(x), x))$$
5. Drop universal quantifier
$$(\text{Animal}(f(x)) \vee \text{Loves}(x, f(x)) \vee \text{Loves}(g(x), x))$$

A. Find CNF =  $(\text{Animal}(f(x)) \vee \text{Loves}(x, f(x)) \vee \text{Loves}(g(x), x))$

Date: \_\_\_\_\_  
Page: \_\_\_\_\_

→ Create a knowledge base consisting of FOL statements & prove the query using forward chaining.

- Knowledge Base (FOL Statements):
  - $\text{Man}(\text{Markus}) \wedge \text{Mortal}(\text{Markus})$ : man & mortal
  - $\text{Pompeian}(\text{Markus})$ : markus is a Pompeian.
  - $\forall x (\text{Pompeian}(x) \rightarrow \text{Roman}(x))$ : all Pompeians are Romans.
  - $\forall x (\text{Roman}(x) \rightarrow \text{Loyal}(x))$ : all Romans are loyal.
  - $\forall x (\text{Man}(x) \rightarrow \text{Person}(x))$ : all men are persons.
  - $\forall x (\text{Person}(x) \rightarrow \text{Mortal}(x))$ : all persons are mortal.

Query:  $\text{Mortal}(\text{Markus})$  is it mortal markus?

$\text{Man}(\text{Markus})$	$\text{Pompeian}(\text{Markus})$
$\text{Markus}$	$\text{Markus}$

$\text{Markus} \rightarrow \text{Pompeian}(\text{Markus})$   
 $\text{Pompeian}(\text{Markus}) \rightarrow \text{Roman}(\text{Markus})$   
 $\text{Roman}(\text{Markus}) \rightarrow \text{Loyal}(\text{Markus})$   
 $\text{Markus} \rightarrow \text{Person}(\text{Markus})$   
 $\text{Person}(\text{Markus}) \rightarrow \text{Mortal}(\text{Markus})$

Q4/11 → Implement unification in first order logic

- OUTPUT:

None of (a, b) satisfies this unification

Unify( $f(a, b), f(b, c)$ ):  $\{x:a, y:b\}$   
 Unify( $f(x, y), f(a, g(z))$ ):  $\{x:a, y:g(z)\}$   
 Unify( $g(x, y), g(a, b)$ ):  $\{y:b\}$   
 Unify( $x, f(y, z)$ ): None

## CODE (Forward Chaining) :

```

import re

def isVariable(x):
    return len(x) == 1 and x.islower() and x.isalpha()

def getAttributes(string):
    expr = r'([^\wedge]+)' matches =
    re.findall(expr, string)
    return matches

def getPredicates(string):
    expr = r'([a-zA-Z~]+)([^\wedge]+)' return
    re.findall(expr, string)

class Fact:

```

```

def __init__(self, expression):
    self.expression = expression.strip()  predicate,
    params = self.splitExpression(expression)
    self.predicate = predicate self.params = params

def splitExpression(self, expression):  predicate =
    getPredicates(expression)[0]      params =
    getAttributes(expression)[0].strip(')').split(',')  return
    [predicate, [p.strip() for p in params]]

def substitute(self, var_map):
    params = [var_map.get(p, p) for p in self.params] return
    Fact(f"{{self.predicate}}{{','.join(params)}}")

def __repr__(self):
    return self.expression

class Implication:
    def __init__(self, expression): self.expression =
        expression.strip() lhs, rhs =
        expression.split('=>') self.lhs =
        [Fact(f.strip()) for f in lhs.split('&')] self.rhs
        = Fact(rhs.strip())

    def infer(self, known_facts):
        substitutions = {}

        for fact in self.lhs: matched
            = False for known in
            known_facts:
                if known.predicate == fact.predicate:
                    mapping = {} for i, param in
                    enumerate(fact.params): if
                    isVariable(param):
                        mapping[param] = known.params[i]
                    elif param != known.params[i]:
                        break
                    else:
                        substitutions.update(mapping)
                        matched = True break
            if not matched:

```

```

        return      None      return

    self.rhs.substitute(substitutions)

class KB:
    def __init__(self):
        self.facts = set()
        self.implications = set()

    def tell(self, expr):
        if '=>' in expr:
            self.implications.add(Implication(expr))
        else:
            self.facts.add(Fact(expr))

    def infer_all(self):
        added = True
        while added:
            added = False
            for rule in self.implications:
                new_fact = rule.infer(self.facts)
                if new_fact and new_fact.expression not in [f.expression for f in self.facts]:
                    print(f'Derived: {new_fact.expression}')
                    self.facts.add(new_fact)
                    added = True

    def ask(self, query):
        print(f'\nQuerying {query}:')
        self.infer_all()
        facts = [f.expression for f in self.facts]
        if query in facts:
            print(f'Yes, {query.split('(')[1].strip(')')} is {query.split('(')[0]}')
        else:
            print(f'No, cannot infer {query}.')

    def display(self):
        print("\nAll facts in Knowledge Base:")
        for i, f in enumerate(sorted([f.expression for f in self.facts])):
            print(f"\t{i+1}. {f}")

def main():
    kb = KB()
    n = int(input("Enter number of FOL expressions: "))
    print("Enter expressions:")
    for _ in range(n):
        kb.tell(input().strip())

```

```
query = input("Enter query:  
").strip() kb.ask(query) kb.display()  
  
if __name__ == "__main__": main()
```

## OUTPUT (Forward Chaining) :

```
Enter number of FOL expressions: 6
Enter expressions:
Man(Marcus)
Pompeian(Marcus)
Pompeian(x) => Roman(x)
Roman(x) => Loyal(x)
Man(x) => Person(x)
Person(x) => Mortal(x)
Enter query: Mortal(Marcus)

Querying Mortal(Marcus):
Derived: Person(Marcus)
Derived: Roman(Marcus)
Derived: Mortal(Marcus)
Derived: Loyal(Marcus)
Yes, Marcus is Mortal.

All facts in Knowledge Base:
1. Loyal(Marcus)
2. Man(Marcus)
3. Mortal(Marcus)
4. Person(Marcus)
5. Pompeian(Marcus)
6. Roman(Marcus)
```

## CODE (CNF) :

```
import re def getAttributes(string):
expr = r'\([^\)]+\)' matches =
re.findall(expr, string)
return [m for m in str(matches) if m.isalpha()]
```

```
def getPredicates(string):
```

```

expr = r'[A-Za-z~]+([A-Za-z,]+)' return
re.findall(expr, string)

def DeMorgan(sentence):
    string = ".join(list(sentence).copy())"
    string = string.replace('~~', " ")
    flag = '[' in string
    string = string.replace('~[', " ")
    string = string.strip(']')
    string = string.replace(']', '')

    for predicate in getPredicates(string):
        string = string.replace(predicate, f"~{predicate}'")

    s = list(string)
    for i, c in enumerate(s):
        if c == 'V':
            s[i] = '^'
        elif c == '^':
            s[i] = 'V'

    string = ".join(s)"
    string = string.replace('~~', " ")
    return f"[{string}]" if flag else string

def Skolemization(sentence):
    SKOLEM_CONSTANTS = [f'{chr(c)}' for c in range(ord('A'), ord('Z')+1)] statement
    statement = ".join(list(sentence).copy())"
    matches = re.findall('[\forall\exists].', statement)

    for match in matches[::-1]:
        statement = statement.replace(match, "")


```

```

statements = re.findall(r'\[\[^]+\]', statement) for
s in statements:
    statement = statement.replace(s, s[1:-1])

for predicate in getPredicates(statement):
    attributes = getAttributes(predicate) if
    ".join(attributes).islower():
        statement = statement.replace(predicate, predicate)
    else:
        aL = [a for a in attributes if a.islower()]
        aU = [a for a in attributes if not a.islower()][0] if attributes else " "
        aU:
            statement = statement.replace(aU, f'{SKOLEM_CONSTANTS.pop(0)}({aL[0]} if
len(aL) else match[1]}))')
    return
statement

def clean_output(expr):
    # Remove multiple brackets and redundant negations
    expr = expr.replace('~~', '') while '[' in expr or ']' in
expr: expr = expr.replace('[', '[').replace(']', ']')

    expr = expr.strip('[] ')

    # Remove redundant outer brackets like [(p | q)] -> p | q if
    expr.startswith('(') and expr.endswith(')'):
        expr = expr[1:-1]

    # Replace internal redundant patterns
    expr = re.sub(r's+', ' ', expr)
return
expr

def fol_to_cnf(fol):

```

```

statement = fol.replace("<=>",
"_) while '_' in statement: i =
statement.index('_')

new_statement = '[' + statement[:i] + '=>' + statement[i+1:] + ']'^[' + statement[i+1:] + '=>' +
statement[:i] + ']' statement =
new_statement

```

```
statement = statement.replace("=>", "-")
```

```

expr = r'\[([^\]]+)\]\'
statements = re.findall(expr, statement)
for i, s in enumerate(statements): if '['
in s and ']' not in s:
    statements[i] += ']'
for s in statements:
    statement = statement.replace(s, fol_to_cnf(s))

```

```
while '-' in statement:
```

```

i = statement.index('-')
br = statement.index('[') if '[' in statement else 0 new_statement
= '¬' + statement[br:i] + 'V' + statement[i+1:]
statement = statement[:br] + new_statement if br > 0 else new_statement

```

```
while '¬∀' in statement: i =

```

```

statement.index('¬∀')
statement = list(statement)
statement[i], statement[i+1], statement[i+2] = '∃',
statement[i+2], '¬'
statement = ".join(statement)
```

```

while '~∃' in statement: i =
    statement.index('~∃')
    s = list(statement)
    s[i], s[i+1], s[i+2] = '∀', s[i+2], '~'
    statement = ''.join(s)

statement = statement.replace('~[∀', '[~∀') statement
= statement.replace('~[∃', '[~∃')

```

```

expr = r'(~[∀∨∃].)'
statements = re.findall(expr, statement) for
s in statements:
    statement = statement.replace(s, fol_to_cnf(s))

```

```

expr = r'~\[[^\]]+\]'

statements = re.findall(expr, statement) for
s in statements:
    statement = statement.replace(s, DeMorgan(s))

```

return statement

```

def main():
    print("\n" + "="*50)
    print(" FOL to CNF Converter (Simplified Output)" + "="*50)
    print("Supports: ∀, ∃, ~, &, |, >>, <=>, brackets [] () {}")
    print("NOTE: Use 'V' for OR inside the formula if needed." + "-" * 50)
    fol = input("Enter FOL formula: ").strip() + "-" * 50
    try:

```

```

raw_cnf = fol_to_cnf(fol) result
=      Skolemization(raw_cnf)
cleaned = clean_output(result)
print(f"Original:      {fol}")
print(f"CNF Form: {cleaned}")
except Exception as e: print("\nError: Could not
    parse the formula.") print("Details:", e)
print("=*50 + "\n")
if __name__ == "__main__": main()

```

### **OUTPUT (CNF);**

```

=====
FOL to CNF Converter (Simplified Output)
=====
Supports: ∀, ∃, ~, &, |, >>, <=>, brackets [] () {}
NOTE: Use 'V' for OR inside the formula if needed.
-----
Enter FOL formula: ∀x[~∀y~(Animal(y)V Loves(x,y))]V[∃y Loves(y,x)]
-----
Original:  ∀x[~∀y~(Animal(y)V Loves(x,y))]V[∃y Loves(y,x)]
CNF Form:  Animal(y)V Loves(x,y))]V[ Loves(y,x
=====
```

### **Program 10: Resolution**

#### **ALGORITHM :**

Date 13.11.25  
Page \_\_\_\_\_

Resolution in fOL

→ Algorithm:

- 1) Convert all sentences to CNF.
- 2) Negate conclusions & convert the results to CNF.
- 3) Add negated conclusion via no premise clause.
- 4) Repeat until contradiction or no progress is made.

- Example:

- allergies ( $x$ )  $\rightarrow$  sneeze ( $x$ )  
 $\Rightarrow \neg \text{allergies} (x) \vee \neg \text{sneeze} (x)$
- cat ( $y$ )  $\wedge$  allergic\_to\_cat ( $x$ )  $\rightarrow$  allergies ( $x$ )  
 $\Rightarrow \neg \text{cat} (y) \vee \neg \text{allergic\_to\_cat} (x) \vee \text{allergies} (x)$
- cat (Felix)
- allergic\_to\_cat (Many)
- To prove: sneeze (Many)

→ So we include  $\neg \text{sneeze} (\text{Many})$  to the KB & try to prove contradiction.

Date \_\_\_\_\_  
Page \_\_\_\_\_

→ Resolution:

$$\begin{array}{c} \neg \text{allergies} (x) \vee \neg \text{sneeze} (x) \quad \neg \text{cat} (y) \vee \neg \text{allergic\_to\_cat} (x) \\ \neg \text{allergies} (x) \quad \neg \text{cat} (y) \\ \neg \text{allergies} (x) \quad \neg \text{allergic\_to\_cat} (x) \\ \neg \text{sneeze} (x) \end{array}$$

$$\begin{array}{c} \neg \text{allergic\_to\_cat} (\text{Many}) \quad \neg \text{cat} (\text{Felix}) \\ \neg \text{allergic\_to\_cat} (\text{Many}) \quad \neg \text{allergic\_to\_cat} (\text{Many}) \\ \neg \text{allergic\_to\_cat} (\text{Many}) \quad \neg \text{allergic\_to\_cat} (\text{Many}) \\ \neg \text{allergic\_to\_cat} (\text{Many}) \quad \neg \text{allergic\_to\_cat} (\text{Many}) \end{array}$$

$\therefore$  We have a contradiction  
 $\Rightarrow \neg \text{sneeze} (\text{Many})$  is false

$\therefore$  sneeze (Many) is true  
 $\Rightarrow$  Hence we prove that many sneezes.

→ OUTPUT:

The negation is unsatisfiable. By resolution, Many sneezes is proven.

## CODE:

```
from sympy import symbols from sympy.logic.boolalg import
Implies, And, Or, Not, to_cnf from sympy.logic.inference
import satisfiable
```

```
# Define symbols
Food = symbols('Food')
Apple = symbols('Apple')
Vegetables = symbols('Vegetables')
Peanuts = symbols('Peanuts')
John_likes_x = symbols('John_likes_x')
Anil_eats_x = symbols('Anil_eats_x')
Harry_eats_x = symbols('Harry_eats_x')
```

```

Alive_x = symbols('Alive_x')
Killed_x = symbols('Killed_x')

# Knowledge Base in propositional logic
# a. John likes all kind of food -> For each food x, John_likes_x if Food(x)
kb = And(
    Implies(Food, John_likes_x), # a
    Implies(Or(Apple, Vegetables), Food), # b
    Implies(And(Anil_eats_x, Not(Killed_x)), Food), # c
    And(Anil_eats_x, Alive_x), # d
    Implies(Anil_eats_x, Harry_eats_x), # e
    Implies(Alive_x, Not(Killed_x)), # f
    Implies(Not(Killed_x), Alive_x) # g
)

# We want to prove: John likes peanuts -> John_likes_x for Peanuts
# Assume the negation of the goal for resolution goal_negation
goal_negation = Not(John_likes_x)

# Combine KB with negated goal combined
combined = And(kb, goal_negation)

# Check satisfiability sat_result =
sat_result = satisfiable(combined)

if sat_result:
    print("The negation is satisfiable. Cannot prove John likes peanuts from KB.")
else:
    print("The negation is unsatisfiable. By resolution, John likes peanuts is proven!")

```

## OUTPUT :

```
The negation is unsatisfiable. By resolution, John likes peanuts is proven!
```