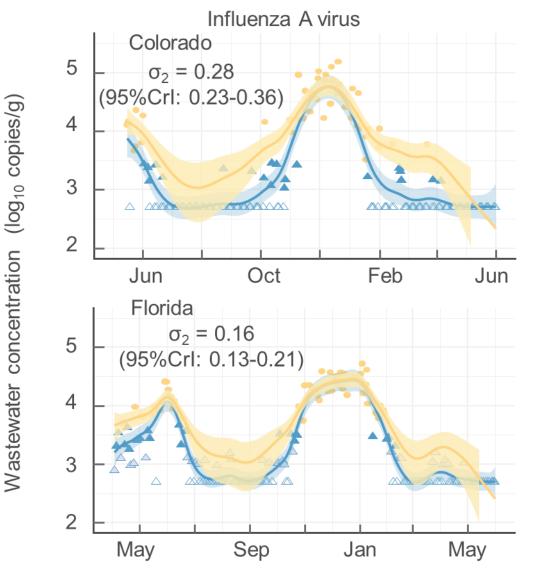
Brief guide for using the state-space model





Content

Name of used R and stan files (state_space_model_with_logistic.R) (state_space_model_with_logistic.stan)

Install and download (slide: 2 ~ 3)

- Import wastewater-based data (slide: 4 ~ 9)
- Set prior distribution (slide 10)
- Implement analysis (slide 11 ~ 13)

Name of used R and stan files (state_space_model_with_logistic_highspeed.R) (state_space_model_with_logistic_highspeed.stan)

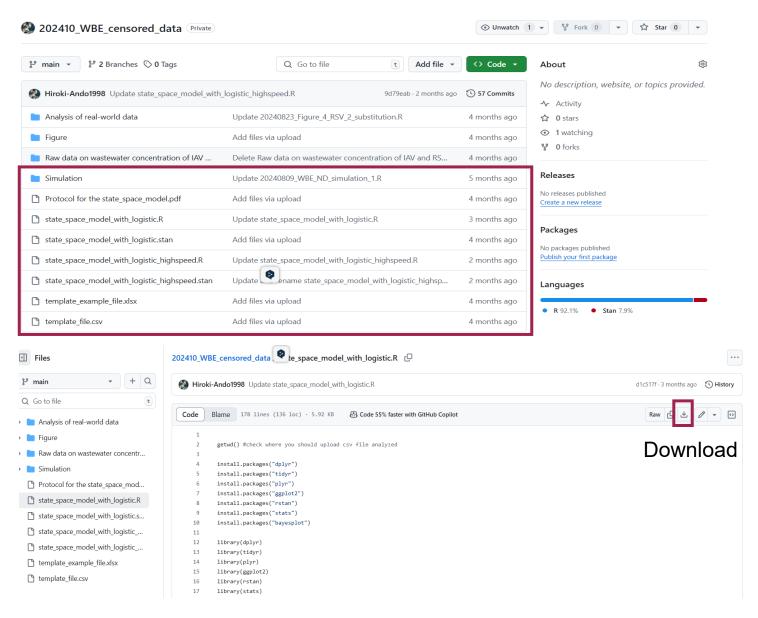
High speed analysis

Contact: hirokiando@arizona.edu

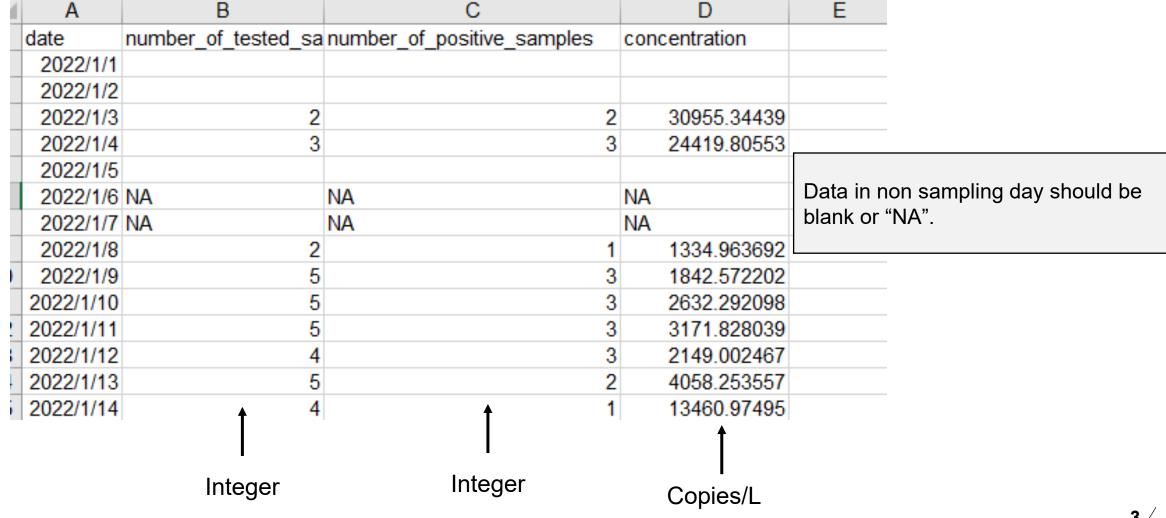
• Install "R" and "Rstudio"

https://rstudio-education.github.io/hopr/starting.html

 Download R file, csv file, and stan file from the github.



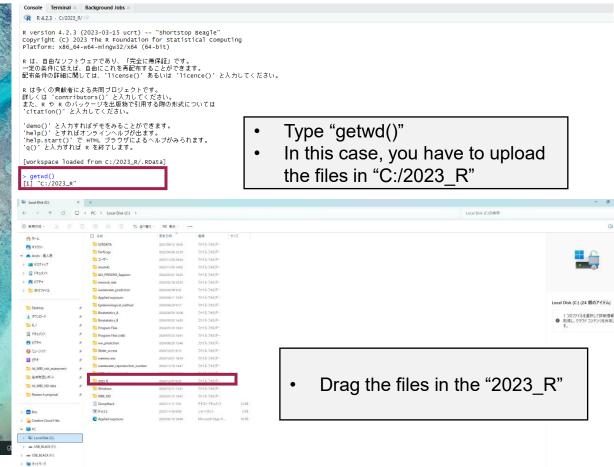
- Open the CSV file downloaded in your laptop
- Input wastewater-based data in the template CSV file



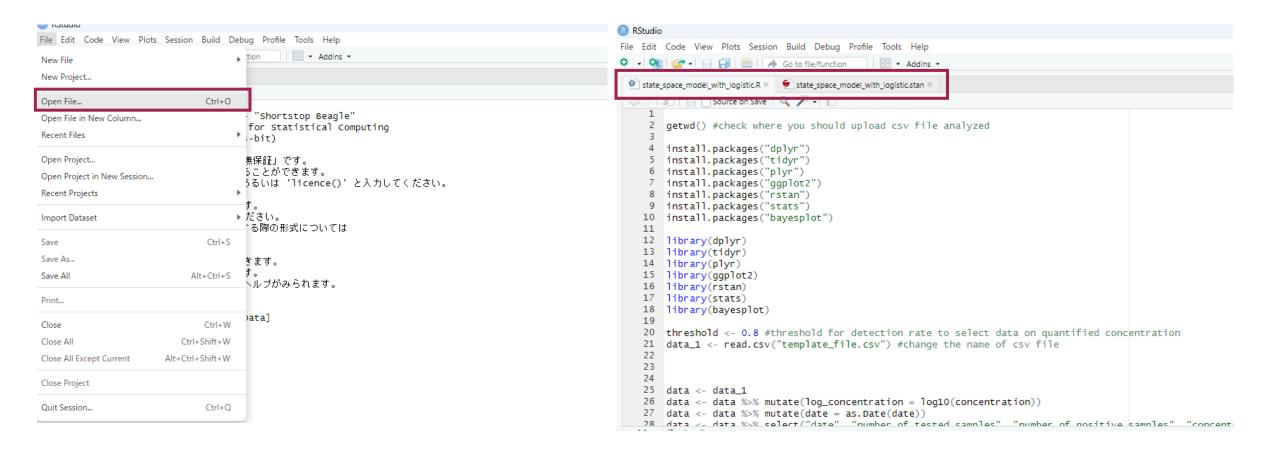
Open "Rstudio" in your desktop

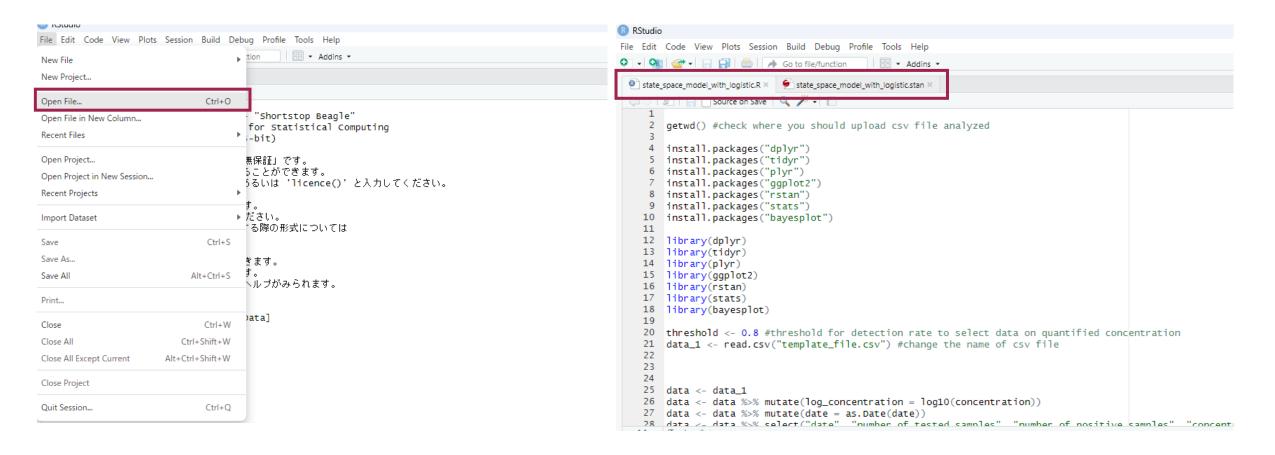
😤 🏴 🐠 🥦 🛗 🚯 🛲 🥬 📆 💮

 Check where you have to upload CSV file, R and Stan file.

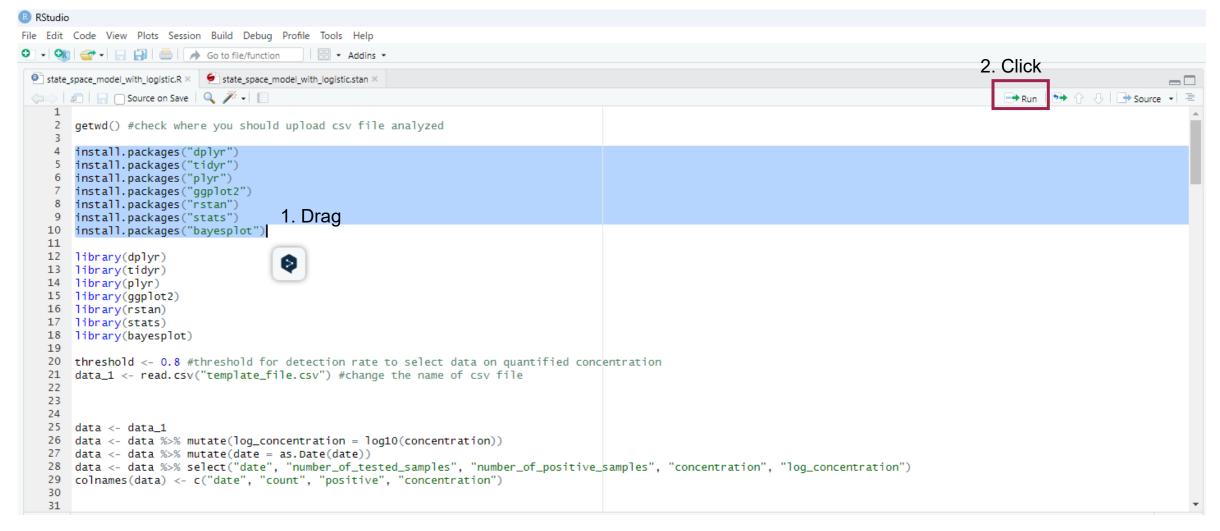


Open R file and Stan file in Rstudio



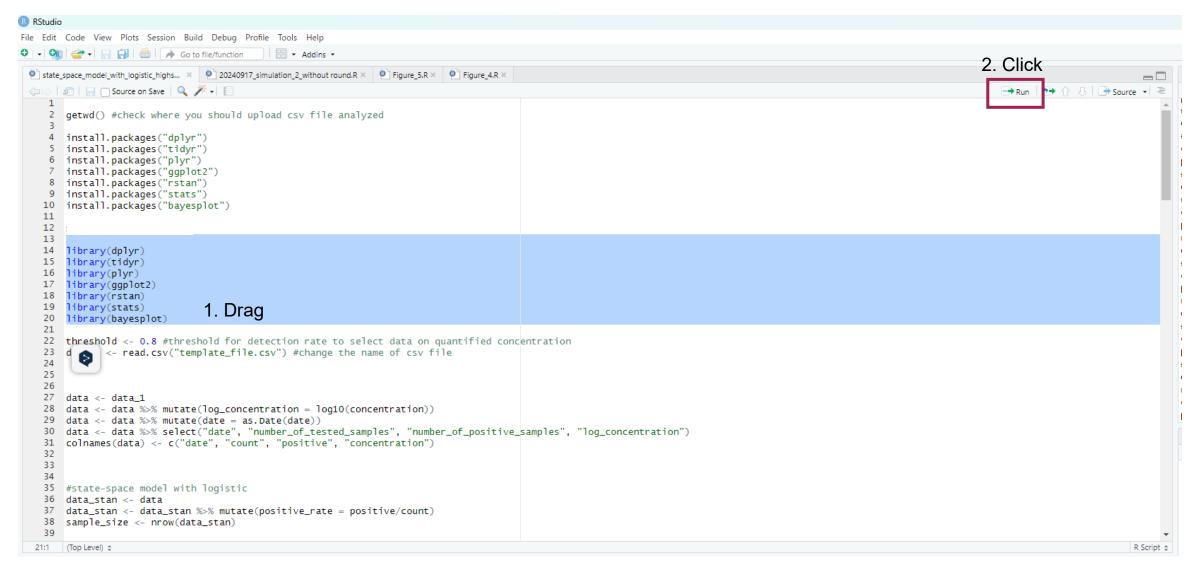


Install R packages used in the analysis



Note: You no longer need to repeat this process once the packages are installed.

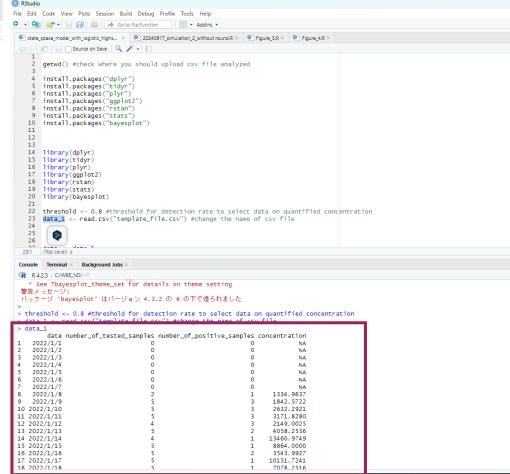
Upload library used in the analysis



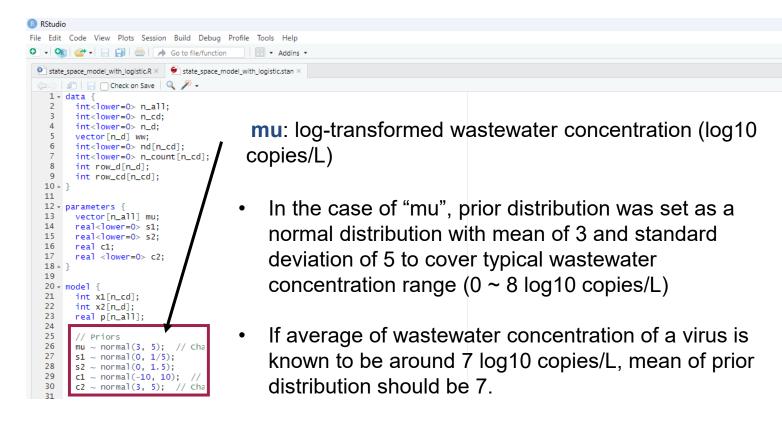
- Set arbitrary threshold (0.7 ~ 1.0)
- Import data

```
state_space_model_with_logistic.R ×
                           state_space_model_with_logistic.stan >
     getwd() #check where you should upload csv file analyzed
      install.packages("dplyr")
      install.packages("tidyr")
      install.packages("plyr")
      install.packages("ggplot2")
      install.packages("rstan")
      install.packages("stats")
      install.packages("bayesplot")
  11
      library(dplyr)
      library(tidyr)
      library(plyr)
      library(ggplot2)
     library(rstan)
      library(stats)
      library(bayesplot)
  19
      threshold <- 0.8 #threshold for detection rate to select data on quantified concentration
      data_1 <- read.csv("template_file.csv") #change the name of csv file
```

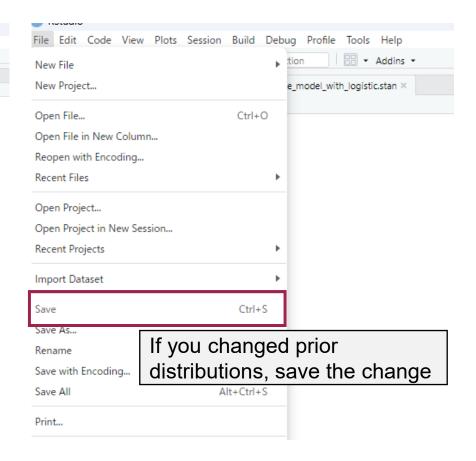
Check the name of CSV file you uploaded



• Prior distributions are important for convergence of parameters (Prior distribution should be decided from available information)



- S₁ is a parameter of the state-formula.
- S₂ is a parameter of the observation formula (i.e., measurement error).
- C₁ and C₂ are parameters of logistic function.



Drag the row from 25-87 and click Run

```
state_space_model_with_logistic.R × 🦸 state_space_model_with_logistic.stan ×
data <- data %>% mutate(log_concentration = log10(concentration))
      data <- data %>% mutate(date = as.Date(date))
      data <- data %>% select("date", "number_of_tested_samples", "number_of_positive_samples", "concentration", "log_concentration")
      colnames(data) <- c("date", "count", "positive", "concentration")</pre>
  30
  31
  32
      #state-space model with logistic
      data_stan <- data
      data_stan <- data_stan %>% mutate(positive_rate = positive/count)
      sample_size <- nrow(data_stan)
  37
      #vector of row number used for the analysis
  38
      #pick row numbers for censored data
      data_row_D <- data.frame(true = which((data_stan$positive_rate >= threshold)))
      sample_size_D <- nrow(data_row_D)</pre>
                                                                                          mcmc <- stan(
      #pick row numbers for censored data
                                                                                            file = "state_space_model_with_logistic.stan",
      data_row_CD <- data.frame(true = which(data_stan$count > 0))
                                                                                            data = data_list_ww,
                                                                                            seed = 1,
                                                                                            chain = 4,
                                                                                                                MCMC condition can be changed according to your
                                                                                      65
                                                                                            iter = 200000.
         Donice out pare
                                                                                      66
                                                                                            warmup = 100000
                                                                                                                data.(https://mc-stan.org/rstan/reference/stan.html)
      print(mcmc, pars = c("c1", "c2", "s1", "s2"), probe = c(0.025, 0.50, 0.975))
                                                                                            thin = 4
  71
                                                                                      68
      #check traceplots if you want
      #mcmc_combo(mcmc, pars = c("c1", "c2", "s1", "s2"))
  74
  75
  76
      #MCMC samples and 95% credible intervals
      mcmc_sample <- rstan::extract(mcmc)</pre>
     state_name <- "mu"
      result <- data.frame(t(apply(
       X = mcmc_sample[[state_name]],
  81
       MARGIN = 2,
        FUN = quantile,
  83
        probs = c(0.025, 0.5, 0.975) #credible interval can be changed
  84
       )))
  85
      colnames(result) <- c("low", "median", "upr")
      data_estimated_concentration <- cbind(data, result)</pre>
```

Check the convergence of parameters in the state-space model

```
> print(mcmc, pars = c("c1", "c2", "s1", "s2"), probe = c(0.025, 0.50, 0.975))
Inference for Stan model: anon_model.
4 chains, each with iter=4000; warmup=2000; thin=4;
post-warmup draws per chain=500, total post-warmup draws=2000.
                               25% 50% 75% 97.5% n eff Rhat
                  sd
                       2.5%
    mean se mean
            0.11 3.76 -32.08 -27.04 -24.37 -21.96 -17.60 1208 1.00
c1 -24.55
c2
    8.04
            0.03 1.18 5.82 7.21
                                    8.01 8.82
                                                10.39
                                                       1565 1.00
51
    0.04
            0.00 0.01 0.02 0.03 0.04 0.05 0.07
                                                        272 1.02
            0.00 0.15 0.71 0.85 0.94 1.04
                                                       1805 1.00
52
    0.96
                                                 1.31
```

- Rhat should be lower than 1.10 (https://mc-stan.org/misc/warnings.html#bulk-ess)
- N eff should be higher than 400 (ideally, 1000)

To improve Rhat and n eff

- Fix prior distribution
- Increase chain, iter (warmup), and thin
- Conduct re-parameterization (Slide number 14 15)

Create figures and check the estimation of wastewater concentration

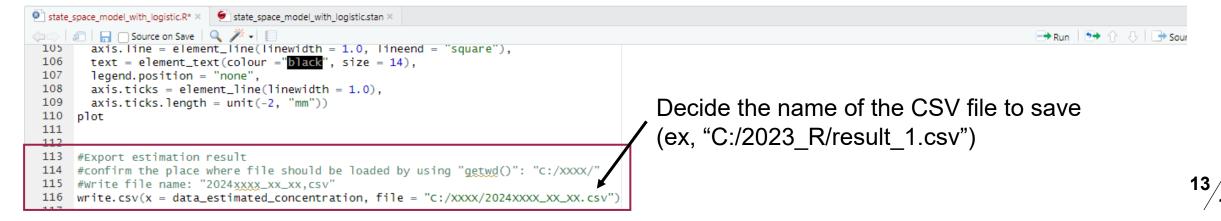
```
grante_space_model_with_logistic.R × state_space_model_with_logistic.stan ×
 (□□) | Image: Image | Image: Imag
                                                                                                                                                                                                                                                                                                                                                Run 🕪 🕆 🖯 🖶 Source 🕶
              #figure
              data_fig <- data_data_estimated_concentration
              data_fig <- data_fig %>% mutate(posi = if_else(count < 1, "no", if_else(positive >= threshold*count, "yes", "no")))
     93
             plot <- ggplot(data_fig, aes(x = as.Date(date)))</pre>
             plot <- plot + geom_point(aes(y = concentration, color = posi, shape = posi))</pre>
     96 plot <- plot + scale_shape_manual(values = c(24, 16))
     97 plot <- plot + scale_color_manual(values = c("#FEC44F", "#0570B0"))
     98 plot <- plot + geom_ribbon(aes(ymin = low, ymax = upr), fill = "#369000", alpha = 0.3)
     99 plot <- plot + geom_line(aes(y = median), color = "#0570B0", size = 1)
  100 plot <- plot + labs(x = "Date", y = "wastewater concentration")
  101 _plot <- plot + scale x date(limits = c(as.Date("2022-01-01"), as.Date("2023-06-01")), date breaks = "2 months", date labels = "%b") #change the date
  plot <- plot + scale_y_continuous(limits = c(2.0, 5.5), breaks = seq(2.0, 5.5, 1)) #change the scale of y axis
  103 plot <- plot + theme_bw()
  104 plot <- plot + theme(
                                                                                                                                                                           Change
                  axis.line = element_line(linewidth = 1.0, lineend = "square"),
                  text = element_text(colour ="black", size = 14),

    X axis (date)

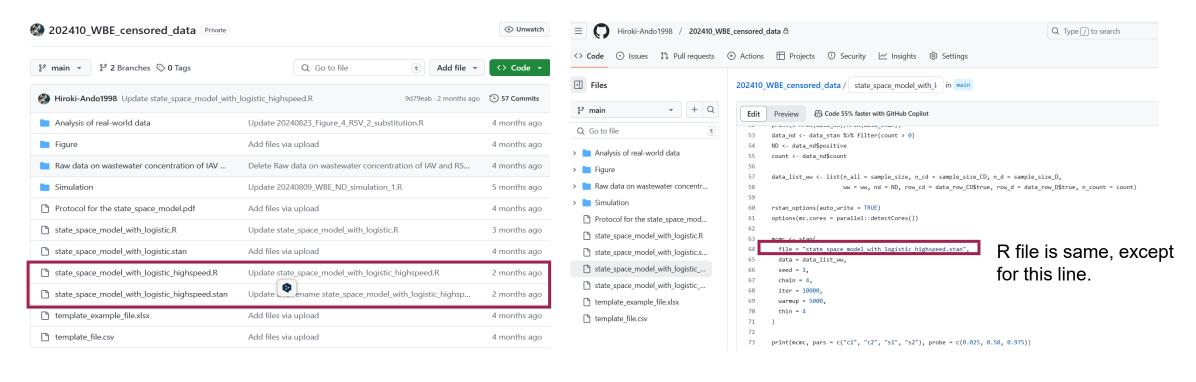
                  legend.position = "none",
  108
                  axis.ticks = element_line(linewidth = 1.0),
                                                                                                                                                                                 Y axis (log10 wastewater concentration)
                  axis.ticks.length = unit(-2, "mm"))
  110
             plot
                                                                                                                                                                           https://ggplot2.tidyverse.org/reference/scale continuous.html
  111
  112
```

Export the result in CSV file

Install and data input



- The above approach (file name: state_space_model_with_logistic.R & state_space_model_with_logistic.stan)
 requires a lot of analytical time.
- This problem is solved by using re-parameterization approach.
 - https://mc-stan.org/docs/2_18/stan-users-guide/reparameterization-section.html
 - https://mc-stan.org/docs/stan-users-guide/reparameterization.html



The purpose of reparameterization is to standardize the scale of the prior distributions so that the sampling space becomes narrower and more isotropic, allowing the sampler to explore the parameter space more efficiently.

state_space_model_with_logistic_highspeed.stan (Stan file)

```
15
      real<lower=-4, upper=4> s2_raw;
      real<lower=-4, upper=4> c1_raw;
17
      real<lower=-4, upper=4> c2_raw;
18
19
20 -
21
           vector[n_all] mu;
22
      for (i in 1:n_all) {
23
        mu[i] = 3.5 + 1.5 * mu_raw[i];
24
25
        real s1;
26
        s1 = exp(s1\_raw - 2);
27
28
        real s2;
29
        s2 = exp(s2\_raw - 2);
30
31
        real c1;
32
         c1 = -22 + 5*c1_raw;
33
34
        real c2;
35
        c2 = 6 + 3*c2_raw;
36
37 🗚
38
39
40 -
```

 $mu_raw \sim normal(0, 1);$ $s1_raw \sim normal(0, 1);$

 $s2_{raw} \sim normal(0, 1);$

 $c1_raw \sim normal(0, 1);$

 $c2_raw \sim normal(0, 1);$

// Autoregressive prior for mu

 $mu[3:n_all] \sim normal(2 * mu[2:n_all-1] - mu[1:n_all-2], s1);$

vector<lower=-4, upper=4>[n_all] mu_raw;

real<lower=-4, upper=4> s1_raw;

14

45

46

48 49 Range of parameters

Parameters are converted into reasonable scale values, which is expected from previous studies.

- In this case, typical range of wastewater concentration is expected to be 0.5 to 6.5 log₁₀ copies/L.
 - Typically, S₁ and S₂ are positive values, ranging from 0 to 1.
- C₁ and C₂ are probably in this range, according to a previous study.

These values can be changed, according to your dataset. (Do not forget to save file after changing values.)

The same prior distribution



- Run MCMC sampling from R file
- Check R-hat and n_eff
- Confirm estimated wastewater concentrations.