

**Artificial Intelligence**  
**Homework 5**  
**Reinforcement learning**  
**Part 2- Model free approach**

**A DC motor dynamics is defined as:**

$$\begin{cases} L \frac{di}{dt} + iR + K_e \omega = u \\ J \dot{\omega} + B \omega = K_t I \end{cases}$$
$$\omega(0) = 0, I(0) = 0$$

where

$\omega$  : motor speed (rad/sec)

$i$  : the current of the motor (Amp);

$u$  : the input voltage to the motor (V)

$R = 0.2\Omega$  : the resistance of the motor coils

$L = 0.000002$  : the inductance of the motor coil

$K_e = 0.0017$  : the electric constant of the motor (V/rad/sec)

$K_t = 0.0017$  : the torque constant of the motor (Nm/Amp)

$J = 2$  : the equivalent moment of inertia of the motor rotor and load

$B = 0.2$  : the equivalent damping coefficient of the motor system

$\omega_{targ}$  : the target speed (rad/sec)

**Objective :**

Define the speed error as

$$e = \omega_{targ} - \omega,$$

you are required to design a RL-based speed controller to stabilize the motor speed from initial conditions to the target speed of

$$\omega_{targ} = 2 \text{ rad/sec.}$$

**Remarks :**

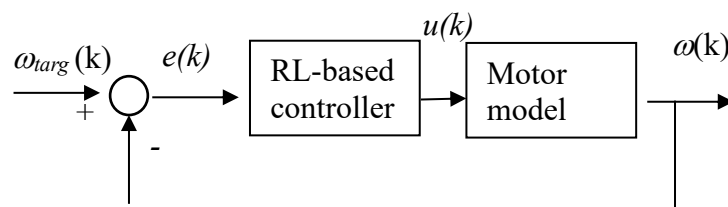
1. You are required to derive the discrete-time state space model of the original model with its parameters in the form as

$$x_{k+1} = f(x_k, u_k) = Ax_k + Bu_k$$

where

$$x(k) = \begin{bmatrix} i(k) \\ \omega(k) \end{bmatrix}$$

2. The block diagram of feedback speed control system:



3. The RL model is recommended as (but not limited to) :
  - State:  $(e(k), \Delta e(k))$ , where  $\Delta e(k) = e(k) - e(k-1)$
  - Action:  $u(k)$
  - Reward:  $r = e^2$
4. The followings are necessary in your report
  - a cover page
  - the 3D mesh plot of the finished Q-table
  - the control and simulation code,
  - simulation of controlling results
  - discussions
  - conclusions