

merge-insertion sort or the Ford–Johnson algorithm

Integer sequence X , of n elements, in this case $n = 9$

7 - 8 - 27 - 100 - 11 - 46 - 2 - 53 - 0



- STEP 1 :

Group the elements of X into $\lceil n / 2 \rceil$ pairs of elements

7 - 8 - 27 - 100 - 11 - 46 - 2 - 53 - 0

pair

if the number of elements is odd, the last element will be unpaired we will call a Struggler, in this case, '0' is a Struggler we should not care about it for know

- STEP 2:

Determine the larger of the two elements in each pair

Before

7 - 8 - 27 - 100 - 11 - 46 - 2 - 53

After

8 - 7 - 100 - 27 - 46 - 11 - 53 - 2

- STEP 3:

Recursively sort the $[n / 2]$ larger elements from each pair

Before

8 7	100 27	46 11	53 2
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After

8 7	46 11	53 2	100 27
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- STEP 4: Create the Main chain and pend

since $a1 \geq b1$ we can
push $b1$ into the front of
the main chain

Main chain

$a1 \ a2 \ a3 \ a4$
7 - 8 - 46 - 53 - 100

Pend

$b1 \ b2 \ b3 \ b4$
~~7~~ - 11 - 2 - 27

- STEP 5:

Generate the order of insertion

To make life
easier
generate the
order of
insertion first

use
jacobsthal
sequence

with a
specially
chosen
insertion
ordering

The order of insertion is a combination between the Jacob
sequence and the real indexes

Jacobsthal numbers

0, 1, 1, 3, 5, 11, 21, 43, 85, 171, 341 ...

generate the jacob number
based on the size of your
pend

Real indexes

0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12 ...

The combination

3, 2, 5, 4, 11, 10, 9, 8, 7, 6, 21, 20 ...

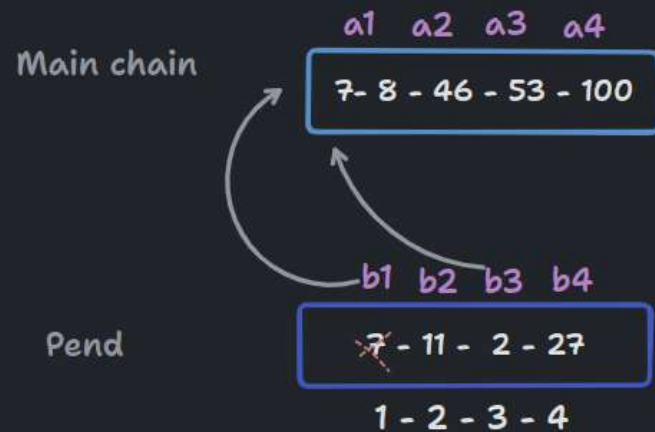
To apply
specially
chosen
insertion
ordering we
will start
from the
element 3
since we
already pushed
the element
num 1

The trick here is to insert Jacob number first
then the indexes before it

- STEP 6:

Insert the elements of the pend into the main chain

Use binary search in the pend to determine the position at which each element should be inserted



a1 a2 a3 a4 a5 a6

2 - 7 - 8 - 46 - 53 - 100

b1 b2 b3 b4

~~7~~ - 11 - ~~2~~ - 27

1 - 2 - 3 - 4

2 - 7 - 8 - 11 - 46 - 53 - 100

b1 b2 b3 b4

~~7~~ - ~~11~~ - ~~2~~ - 27

1 - 2 - 3 - 4

2 - 7 - 8 - 11 - 46 - 27 - 53 - 100

b1 b2 b3 b4

~~7~~ - ~~11~~ - ~~2~~ - ~~27~~

1 - 2 - 3 - 4

- STEP 7:

Do you remember the struggler ?

now you can push it

0 - 2 - 7 - 8 - 11 - 46 - 27 - 53 - 100