

CLASSIFICATION METHODS FOR REMOTELY SENSED DATA



*SECOND
EDITION*

BRANDT TSO • PAUL M. MATHER



CRC Press
Taylor & Francis Group

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Preface to the Second Edition

The first edition of this book was written between 1998 and 2000, and was published in 2001. In the ten years that have elapsed since the start of this project, developments in image classification technology have been considerable. In order to keep this book relevant and up to date, two new chapters have been added and the existing chapters have been updated. The new chapters cover the topics of support vector machines (SVMs) and decision trees, both of which are now the subject of research articles in the major journals. SVMs represent a recent development in the computational aspects of image classification, and one of the problems they face is in the allocation of data to one of several (rather than one of two) classes. A number of approaches to this problem are presented in Section 4.4, but further experimentation is required. The number of potential approaches to the use of decision trees is considerable, and these are covered in Chapter 6. Developments such as boosting and random forest generation are described in Section 6.8. Lopping branches that do not contribute to the effectiveness of the decision tree is an important aspect of the design of the tree, which is covered in Section 6.7.

Acknowledgment is due to our institutions, the Management College, National Defense University and to The University of Nottingham, for providing support while this book was being revised. Brandt Tso also recognizes the benefits of his year as a postdoctoral fellow in the Remote Sensing Laboratory, Naval Postgraduate School, Monterey, California.

Preface to the First Edition

We classify objects in order to make sense of our environment, by reducing a multiplicity of phenomena to a relatively small number of general classes. On a country walk, for example, you might point to cows, trees, tractors, or swans. What you are actually doing is identifying an observed object and allocating it to a preexisting class, or giving it a name. Before setting out on the walk, you knew that swans existed, and you could specify their characteristics. When you saw a large white bird, possibly swimming in a canal or river, with an orange and black beak, you compared those characteristics to those of a swan and thus identified the bird, giving it the name or label of *swan*. We must be careful, therefore, to distinguish between the definition of the classes to which objects may belong and the identification or labeling of individual objects, and to avoid confusion between the two meanings of the word *classification*—the definition of categories of objects and the assignment or allocation of individual objects to these classes.

The example of the swan can also help to define other concepts. First, you must already have a model (or idealized representation) of the key features of a swan before you can recognize one. You learned, presumably in your childhood, the names of categories and subcategories of animals, plants, and other objects. Now you use that knowledge to identify and name the things you see and hear. In the literature of classification, this approach is termed *supervised learning*, meaning that you have divided the phenomena of interest into a number of *a priori* groups. You have observed a number of examples from each group, and have characterized them in terms of a number of discriminating features. The sample set is called *training data*, and this approach is known as *supervised classification*. In fact, it is supervised identification because it is assumed that the classification (the definition of the groups and their characteristics) has been defined before any previously unknown objects were identified.

An alternative approach, known as *unsupervised classification* or *clustering*, is also widely used. In this approach it is assumed that (1) you have little knowledge of the characteristics of the data set, (2) that you wish to determine whether any natural groupings exist in those data, and if so, (3) whether they can be identified in terms of phenomena of interest. In a sense, this procedure is akin to exploring the data (and visualization methods can help considerably in the process) whereas the supervised approach is inductive.

This book is about pattern recognition for remotely sensed data. We prefer the term *pattern recognition* to *classification* because the latter term can be misleading, as noted above. However, the two terms are used in this book, partly for reasons of tradition. A *pattern* is a set of measurements made on an object. It can be described as a mathematical vector of measurements. For example, a person's height and weight can be represented by the vector [192, 50] (in cm and kg, respectively). If a supervised approach is used, then the pattern is compared in some way to members of the sets of patterns that define the categories of interest, and the given pattern is

assigned to one of these categories (one of which may be “unknown”). This approach can be described as inductive. Alternatively, a clustering strategy may be used that is based on the similarity between patterns, in order to determine whether any distinct groups of patterns exist in the data.

In Earth observation by remote sensing, the objects to be labeled are normally the individual pixels forming a multispectral or hyperspectral image. Each pixel is represented by a pattern vector consisting of a set of measurements, one per image band plus, possibly, other measurements such as texture. If each spectral band is represented by one axis of a multidimensional space (the *feature space*), then the pixel can be represented as a point in that space. For simplicity, let the number of features be two, and let the x -axis represent the first feature and the y -axis represent the second. A pixel with a feature vector of $[1, 5]$ can therefore be shown on a graph as a point with Cartesian coordinates $[1, 5]$. Now imagine that all the pixels in the two-band image have been plotted on the graph, and that they fall into clearly defined groups. We can separate these groups by lines or curves. These lines or curves are called *decision boundaries*, for they show the positions of the boundaries of individual categories. If a point lies on one side of the boundary, it is given a label such as “A,” whereas if it lies at the other side of the boundary it is given the label “B.” In higher-dimensional problems, the lines and curves become *hyperplanes* and *hypersurfaces*. So the labeling problem can be thought of as one that involves the positioning of hyperplanes or hypersurfaces, representing decision boundaries, in a multidimensional feature space. The algorithm that determines the position of the pixel with respect to the decision boundaries, and thus allocates a specific label to that pixel, is called a *decision rule*. The word *classifier* is widely used as a synonym for the term *decision rule*.

The use of pattern recognition methods in remote sensing has a long history. Air photo interpreters were perhaps the first to use intuitive methods to determine the information contained in reconnaissance photographs, and these methods continue to be of great importance, particularly in the gathering of military intelligence, as the human eye–brain combination can make decisions and judgments on complex problems in milliseconds, using experience as a guide. Automatic methods are more suitable to the routine processing of images that show predictable patterns. Such methods have been developed and applied in a number of disciplines, ranging from speech and handwriting recognition, industrial process management, and medical diagnosis, as well as in the collection of military intelligence. The main distinguishing characteristic of Earth observation data is its volume. Hence, methods that can be applied in other applications may not be suited to the analysis of remotely sensed data because of the computational requirements. A further point to note is that there is often a discrepancy between the dimensionality of remotely sensed data sets and the volume of training data that is available. Where training data is sparse relative to the dimensionality of the data, it becomes difficult to estimate the characteristics of each training class, and so error may become significant. This phenomenon of increasing error with increasing data dimensionality is sometimes known as the *Hughes effect*.

Advances in technology have led to rapid developments in methods of pattern recognition, leading to the formulation of new and more sophisticated decision rules.

Some of those new methods have been introduced into the field of remote sensing and have shown encouraging results. A further feature of remote sensing applications in recent years is the use of combinations of data derived from different sensors or from different time periods, plus terrain and other data extracted from geographic information system (GIS) databases. In addition, the spectral information contained in remotely sensed images is often augmented by derived measures such as values of texture and context. In dealing with multidata sources, a significant problem is the considerable increase in the computational cost. Other problems, such as data scale and data reliability, must also be considered. There is an increasing interest in seeking methods for efficiently manipulating multisource data in order to increase classification accuracy. It should always be remembered, though, that sophisticated algorithms cannot compensate for lack of training data or an inadequate definition of the problem (in terms of the number and nature of the classes to be recognized relative to the scale of the study).

Texture is the tonal variation within an area. A simple example that illustrates the concept is the pattern on a carpet. If we treat each pattern as a whole, then the carpet can easily be described. If the carpet is seen as a set of small rectangular units, then the problem of describing its properties is more difficult. In some cases, texture information seems to be more effective than tonal information to describe the objects, and one can develop *texture features* corresponding to different kinds of patterns to improve the performance of a classifier.

Contextual information describes how the object of interest may be affected by its neighbors. For instance, English words starting with the letter “q” are more likely to be immediately followed by the letter “u” than “z” or “c.” In the case of classification of an agricultural area, a pixel labeled as “carrot” is more likely to be surrounded by pixels of the same class rather than by other classes such as “water” or “wheat.” The ability to model such contextual behavior may reduce confusion in the classification process.

The decision to write this book was triggered by our experience in attempting to use new methods of describing and labeling pixels in a remotely sensed image. While a number of valuable but more general textbooks are available for undergraduate use, we know of no coherent source of advanced information and guidance in the area of pattern recognition for research scientists and postgraduate research students in remote sensing, together with students taking advanced remote sensing courses. We hope that this book will contribute to the increased understanding and adoption of recently developed techniques of pattern recognition, and that it will provide readers with a link between the remote sensing literature and that of statistics, artificial intelligence, and computing. We do suggest, however, that attention be paid to experimental design and definition of the problem, for an advanced pattern recognition procedure is no substitute for thinking about the problem and defining an appropriate set of features.

Chapter 1 introduces the basic concepts of remote sensing in the optical and microwave region of the electromagnetic spectrum. This chapter is intended to introduce the field of remote sensing to readers with little or no background in this area, and it can be omitted by readers with adequate background knowledge of remote sensing.

Chapter 2 introduces the principles of pattern recognition. Traditional decision rules, including the supervised minimal distance classifier, Gaussian maximum likelihood, and unsupervised clustering techniques are described, together with other methods such as fuzzy-based procedures and decision trees. The chapter also contains brief accounts of dimension reduction methods, including orthogonal transforms, the assessment of classification accuracy, and the principles underlying the choice of training data.

Chapter 3 describes widely used neural network models and architectures including the multilayer perceptron (also called the feed-forward neural network), Kohonen's self-organized feature map, counterpropagation, the Hopfield network, and networks based upon adaptive resonance theory (ART).

Chapter 4 deals with pattern recognition techniques based on fuzzy systems. The main topics of this chapter are the construction of fuzzy rules, fuzzy mapping functions, and the corresponding decision processes.

Chapter 5 presents a survey of methods of quantifying image texture, including fractal- and multifractal-based theory, the multiplicative autoregressive random field model, the grey level co-occurrence matrix, and frequency domain filtering.

Chapter 6 addresses the theory and the application of Markov random fields. The main application of Markov random fields is to model contextual relationships. Other related topics, including function formulation, image restoration, robust estimation in the presence of noise (outliers), and the derivation of Markov-based texture measures, are also presented.

Chapter 7 provides several approaches for dealing with multisource data. The methods described include the extension of Bayesian classification theory, evidential reasoning, and Markov random fields.

No one is more aware of a book's deficiencies and inadequacies than its authors. Even Socrates, after a lifetime of learning, is reported to have been impressed by the extent of his own ignorance. Had more time and space been available, the book would have contained a longer account of the use of wavelets in texture analysis, and of the applications of decision tree classifiers. Publishers, who live in the real world, impose constraints of time and space while authors naturally attempt to rewrite their manuscripts every month in order to include the latest developments. We hope that we have reached a happy compromise that should satisfy most readers. We have included references to further work in order to guide the more advanced reader toward the relevant literature.

Most of the research underlying the ideas presented in this book was carried out while Dr. Brandt Tso was a postgraduate student, and later a postdoctoral fellow, in the School of Geography, The University of Nottingham, under the supervision of Professor Paul M. Mather. The second author provided encouragement, support, contributions to the first three chapters, and numerous rewrites of the draft. We realize that any book written by human authors is necessarily flawed, and we accept responsibility for any errors that may be contained in these pages.

The School of Geography, The University of Nottingham, provided computing facilities as well as a stimulating and encouraging environment for research. The second author is grateful to his many postgraduate research students from different parts of the world who have, over the past decade or so, educated and trained him in

many areas of remote sensing. In particular, he would like to thank Valdir Veronese, Taskin Kavzoglu, Carlos Vieira, and Mahesh Pal, who have carried out research projects in areas relevant to the subject matter of this book. The contribution of others, while not directly related to the topic of image classification, has helped by broadening the intellectual debate within my research group as well as helping in many other ways. We also thank Dr. M. Koch of Boston University for help and guidance with the Red Sea Hills data set, which is used in a number of examples in this book. The help, good humor, and patience of Tony Moore of Taylor & Francis is greatly appreciated. Finally, both authors recognize the contributions of their families, and dedicate this book to them.

Brandt Tso

Taipei, 2000

Paul M. Mather

Nottingham, 2000

Author Biographies

Dr. Brandt Tso has served as a scientific officer in the Taiwan military service, studying modeling and pattern recognition techniques since 1988. Dr. Tso completed his Master's degree in information science at the Management College, National Defense University, Taiwan. Between 1994 and 1998, Dr. Tso was awarded a scholarship by the Taiwan government to pursue a Ph.D. degree in the School of Geography, The University of Nottingham, U.K., under the supervision of Professor Paul M. Mather, concentrating on the field of remotely sensed data classification. In 2003, Dr. Tso was an invited postdoctoral fellow in the Remote Sensing Laboratory, Physics Department, Naval Postgraduate School, Monterey, California, U.S.A., to study more complex remotely sensed data classification skills. Currently, Dr. Tso is an associate professor in the information science department, Management College, National Defense University, Taiwan. His main research interests include remotely sensed data recognition, real scene image retrieval, and machine learning algorithms. He has published numerous research papers relating to these fields.

Professor Paul M. Mather graduated with a degree in geography from the University of Cambridge in 1966. He then moved to The University of Nottingham to conduct research for his Ph.D. in geomorphology, which was awarded in 1969. As lecturer, senior lecturer, and full professor (1988), his attention was focused on the use of multivariate analysis in physical geography, a subject on which he published a detailed and well-received monograph in 1976. By the 1980s his interest in multivariate analysis had branched out to include remote sensing. In 1987 the first edition of his book *Computer Processing of Remotely Sensed Data* was published. It is now in its third edition (2004) with a fourth edition in preparation. He has always been fascinated by the applications of computers in physical geography and the environmental sciences, and is a proficient Fortran programmer. He retired in 2006, and was made Emeritus Professor. He received the Back Award from the Royal Geographical Society for his work in remote sensing in 1992, and in 2002 was awarded the Order of the British Empire (OBE) by Her Majesty Queen Elizabeth II for services to remote sensing. He has lectured in a number of countries around the world.

1 Remote Sensing in the Optical and Microwave Regions

Remotely sensed image data is widely used in a range of oceanographic, terrestrial, and atmospheric applications, such as land-cover mapping, environmental modeling and monitoring, and the updating of geographical databases. Hence, the quantized pixel values making up an image may be converted to physical values of radiance and related to some property of the surface being sensed. An example of this approach is the calibration of thermal infrared imagery to produce maps of temperature fields, such as sea surface temperature. In other applications, thematic information is required. A thematic map is one that displays the spatial variation of a specified phenomenon, such as land surface elevation, soil type, geology, or vegetation. It is this second approach that is considered in this book. The term *pattern recognition* is used to describe the procedures involved in relating vectors of measurements that are spatially referenced to individual pixel locations to the types or categories into which the phenomenon of interest is subdivided. If, for example, the phenomenon of interest is agricultural crops, then the categories are the individual crop types. Each crop type is represented in the thematic image by a numerical label. Vectors of measurements that are spatially referenced to individual pixel locations include image pixel values plus derived values such as texture, coherence, or context, as well as other geographical data that can be related to the pixel location, such as terrain elevation and slope, geology, and soil type.

Digital thematic maps can be represented in two ways, using either the raster or the vector models. The *vector model* uses the classical cartographic representation of map objects in terms of points, lines, and areas. Using this model, a continuously varying spatial attribute such as terrain elevation is represented by contour lines and spot heights, while an attribute such as soil type or underlying geology is represented in terms of boundary lines that enclose areas that are homogenous with respect to the property of interest and at the chosen scale of observation. The *raster model* represents spatial attributes in terms of their values over a contiguous set of small individual (and usually square) areas. Thus, variations in land surface elevation over a region of interest are represented by numerical values stored in a rectangular grid or raster, each element of which is the average elevation of the ground area represented by that element or cell of the grid. This representation of terrain height variation is known as a *digital elevation model* or DEM.

In the same way, variations in geology in a study region are stored in raster format as a set of labels. Each cell in the data array is given a numeric label that is linked to a

description. For example, pixels with the Label 1 may be described as Carboniferous Limestone, while pixels given the Label 2 might be described as Silurian Grit. In this book, we are concerned with spatial data (specifically, remotely sensed images) that are represented in terms of rectangular rasters.

In the examples given in the preceding paragraphs, each cell of the raster stores either a physical value (such as elevation in meters above a given datum) or a label (such as 1 or 2, indicating rock types such as granite and basalt). In practice, rasters (and particular raster data sets containing images for display) are generally stored in the form of integer rather than floating-point numbers, in order to conserve storage space. Thus, a DEM may be represented in terms of an array of integers in the range 0 to 255, with each integer value representing a range of land surface elevations. The idea is similar to the use of a key in a printed map in which elevation is generally shown in shades of green and brown, with the map key showing the relationship between these hues and specific elevation ranges. In the same way, the values 0 to 255 contained in the DEM are connected to a range of real elevation values by the use of a table rather than a key. The table, known as a *lookup table* or LUT, allows the user to determine the actual range of elevations denoted by a particular label, such as 215. In some applications, the physical elevation value is required (for instance, if slope angle is to be calculated). Other questions can be answered by using the counts or labels directly. If Label 18 is used to represent land with a surface elevation between 200 and 205 meters, then the locations of such areas can be achieved by searching the raster for all values of 18 rather than converting the raster labels back to physical values and searching for cells holding numbers in the range 200 to 205.

Remotely sensed images are stored and manipulated in raster form. Each element of the raster is known as a pixel, and the value contained in any pixel location is simply a quantized count or a label rather than a physical value. For some applications, such as pattern recognition, these counts can be used directly as we are interested in interpixel similarities and differences. In other applications, such as sea-surface temperature determination, the pixel counts must be converted to physical values of radiance or reflectance, with corrections applied for such factors as sensor calibration changes and atmospheric influences. The range of quantized counts used in a raster representation of an image ranges from 0 to 255 (8-bit representation, for images derived from sensors such as Landsat Enhanced Thematic Mapper + (ETM++ and SPOT High Resolution Visible [HRV]), to 0 to 1023 (10-bit representation, as used for Advanced Very High Resolution Radiometer [AVHRR] data to more complex formats. For example, raw synthetic aperture radar data are commonly represented in terms of two 16-bit integers per pixel, with the first integer representing the real part and the second integer representing the imaginary part of a complex number. Whatever the precision (8-, 10-, or 16-bit) these pixel values are stored as rectangular rasters, and can be held in a computer in the form of a two-dimensional array. The data set used in pattern recognition consists of a number of co-registered raster images representing, for example, the measurements in the individual bands of a multispectral or hyperspectral image, the ground elevation (DEM), or some other spatial property of interest. The number of features used to represent terrain conditions is known as the *dimensionality* of the data. Multispectral and radar data have a low dimensionality; for instance, SPOT HRV produces three bands of data,

and Landsat-7 ETM+ generates seven bands in wavelengths ranging from the optical to the thermal infrared, plus a panchromatic band, while the radar satellite ERS-2 operates in a single band. Hyperspectral sensors such as Airborne Visible/Infrared Imaging Spectrometer (AVIRIS), Compact Airborne Spectrographic Imager (CASI) and the Digital Airborne Imaging Spectrometer (DAIS) have the ability to collect data in tens or hundreds of narrow spectral bands. One problem in the classification of high-dimensional remotely sensed data is the paucity of samples (“training data”) relative to the dimensionality of the feature space. This problem leads to difficulties in estimating statistical parameters such as the mean and covariance matrix.

The aim of pattern recognition in the context of remote sensing is to link each object or pixel in the study area to one or more elements of a user-defined label set, so that the radiometric information contained in the image is converted to thematic information, such as vegetation type. The process can be regarded as a mapping function that constructs a linkage between the raw data and the user-defined label set. A simple example is shown in Figure 1.1. Normally, each object or pixel is linked to a single label. However, it is also possible to perform a *one-to-many* mapping, so that a given pixel can be associated with more than one label, with the differing degrees of association between the pixel and each label being expressed as probabilities of membership. Alternatively, a *many-to-one* scheme will link groups of pixels to a single label. This approach can be used, for example, to give the same label to all of the pixels in a single agricultural field.

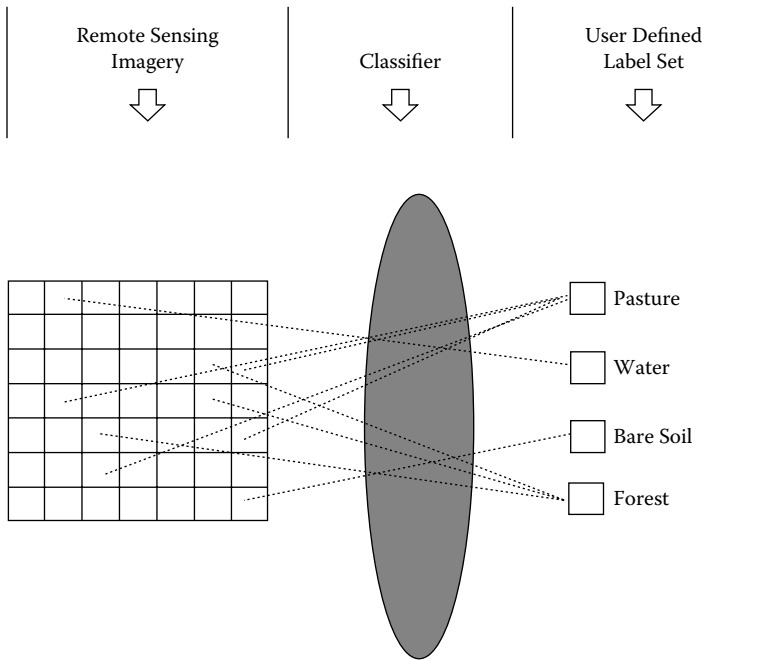


FIGURE 1.1 The concept of the classifier as a link between an image (left) and a set of labels.

Each application generally requires a different methodology, and each methodology is likely to generate different results. If reliable results are to be obtained, the analyst should understand the behavior of the method being used in order to achieve a satisfactory performance. For instance, the performance of a statistical procedure is strongly affected by the accuracy of the estimates of parameters such as the mean vector and the variance–covariance matrix for each class, which are obtained from samples of pixels called *training data sets*. Equally, the design of the architecture of a feed-forward neural net has an equally important impact on performance of the network.

The aim of this book is to provide a survey of pattern recognition methodology for use with remotely sensed imagery. Besides describing traditional approaches, more advanced techniques using artificial neural networks, support vector machines, fuzzy theory, and decision trees are introduced, and considerable space is devoted to the discussion of textural and contextual features. Some particular issues, such as pattern recognition using multiple data sources, change detection, and the analysis of mixed pixels, are also illustrated.

In the main part of this introductory chapter, the principles underlying remote sensing in the optical and microwave regions of the spectrum are described. Some important preprocessing techniques, such as corrections for atmospheric and topographic effects and noise filtering models, are also presented. These techniques are helpful in improving thematic accuracy in some kinds of applications, for example, in change detection.

1.1 INTRODUCTION TO REMOTE SENSING

Remote sensing is the use of sensors installed on aircraft or satellites to detect electromagnetic energy scattered from or emitted by the Earth's surface. This energy is associated with a wide range of wavelengths, forming the electromagnetic spectrum. Wavelength is generally measured in micrometers (1×10^{-6} m, μm). Discrete sets of continuous wavelengths (called *wavebands*) have been given names such as the *microwave band*, the *infrared band*, and the *visible band*. An example is given in Figure 1.2, which shows only a part of the overall electromagnetic spectrum. It is apparent that the visible waveband (0.4 to 0.7 μm), which is sensed by human eyes, occupies only a very small portion of the electromagnetic spectrum.

A specific remote sensing instrument is designed to operate in one or more wavebands, which are chosen with the characteristics of the intended target in mind. Thus, a sensor designed to detect electromagnetic radiation in the visible spectrum that has been reflected by chlorophyll in ocean waters will use different wavebands than would a sensor designed to detect the characteristics of soils. Apart from the reflectance characteristics of the target, an important factor governing the choice of waveband is the effect of interactions between the atmosphere and electromagnetic radiation. Such radiation passes downward through the atmosphere on its way from the sun to the Earth, and reflected radiation passes upward through the atmosphere on its way from Earth to the sensor. Absorption and scattering are the main mechanisms that alter the intensity and direction of electromagnetic radiation within the atmosphere. In some regions of the optical spectrum, these mechanisms (principally absorption) ensure that remote sensing is impossible. Spectral regions of

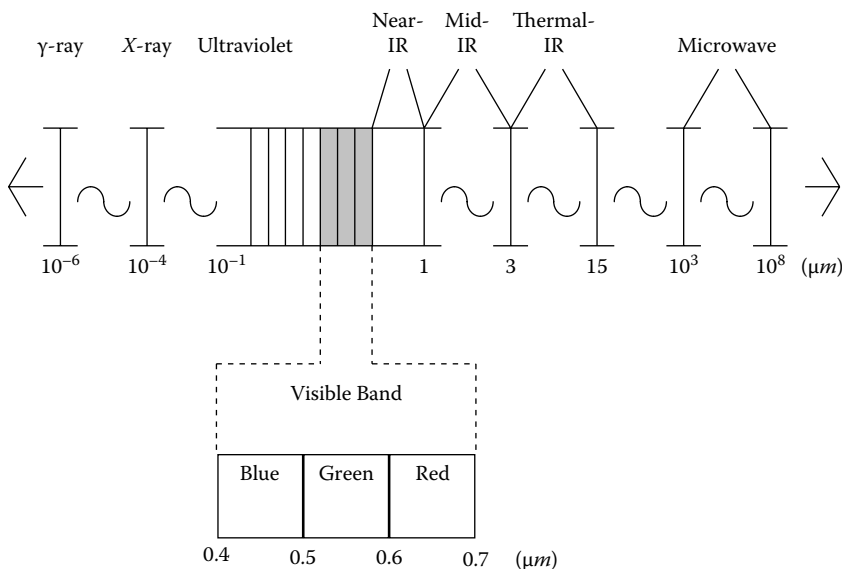


FIGURE 1.2 Regions of the electromagnetic spectrum that are of interest in remote sensing applications.

lower absorption are known as *atmosphere windows* (Figure 1.3), though it should be remembered that scattering and absorption affect all wavebands in the optical spectrum to a greater or lesser degree, and these effects are variable both in space and time.

1.1.1 ATMOSPHERIC INTERACTIONS

Electromagnetic radiation interacts with the Earth’s atmosphere, the degree of interaction depending on the wavelength of the radiation and the local characteristics of the atmosphere. The basic interactions are known as *scattering* and *absorption*. Scattering is more likely to occur at shorter wavelengths. The most common scattering behavior is known as *Rayleigh scattering*, which is the main cause of haze in remotely sensed imagery. The atmosphere has different levels of absorption at different wavelengths. Regions of the spectrum that have a relatively high transmission are called atmospheric windows (Figure 1.3). The energy in some wavebands (e.g., from 15 to $10^3 \mu\text{m}$) is almost completely absorbed by the atmosphere. These wavelengths cannot, therefore, be used for remote sensing. Wavebands with a high transmission could be potential candidates for remote sensing missions.

1.1.2 SURFACE MATERIAL REFLECTANCE

The choice of wavebands for remote sensing in the optical region is also affected by the characteristics of the surface material. Energy that is incident upon a target can be separated into three components, namely, energy that is transmitted,

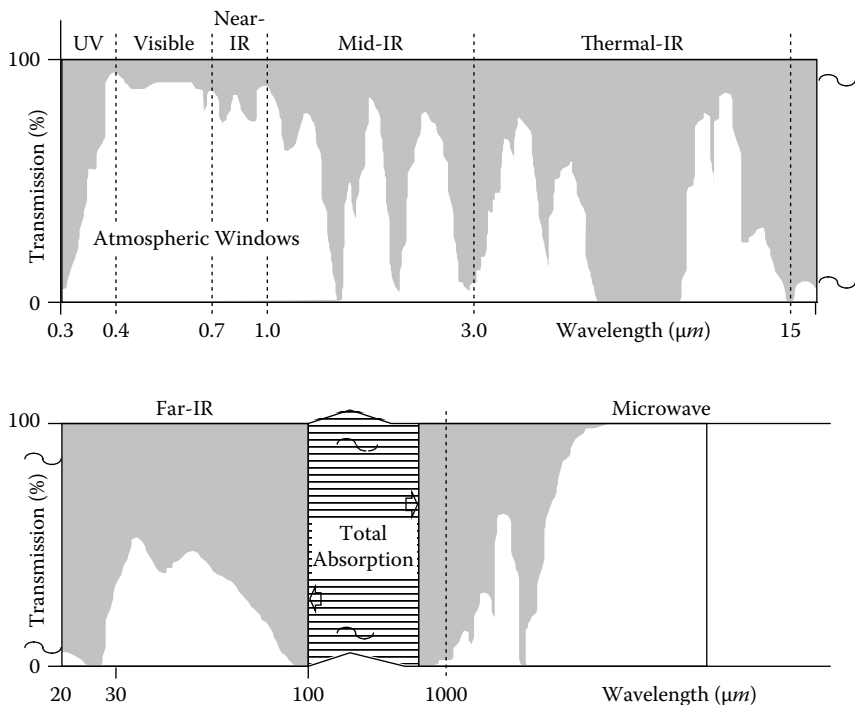


FIGURE 1.3 Atmospheric windows (unshaded). Vertical axis is atmospheric transmission (%). Horizontal axis is the logarithm of the wavelength in micrometers.

absorbed, and reflected. Surface material reflectance characteristics may be quantified by the spectral reflectance, which is a percentage measure obtained simply by dividing reflected energy in a given waveband by incident energy. The quantity of the reflected energy depends mainly on three factors: the magnitude of the incident energy, the roughness of the material, and the material type. Normally, the first two factors are regarded as constants. Therefore, only the third factor (i.e., the material type) is considered. However, it is worthwhile to first describe how roughness affects the reflected energy.

Surface roughness is a wavelength-dependent phenomenon. Given the same material, the longer the wavelength the smoother the material appears. For a perfectly smooth (specular) surface, reflected energy travels only in one direction such that the reflection angle is the same as incidence angle. In the case of a perfectly rough (Lambertian) surface, incident energy is reflected equally in all directions (Figure 1.4). However, in practical applications, most surface materials act neither as specular nor Lambertian reflectors; their roughness lies somewhere between these two extremes.

Figure 1.5 shows the average reflectance over the optical region of the spectrum for three ideal surface materials: dry bare soil, clear water, and green vegetation. This graph shows how these surface materials can be separated in terms of their reflectance spectra. It is apparent that vegetation reflectance varies considerably

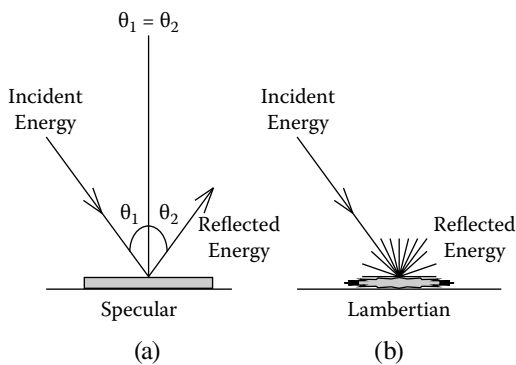


FIGURE 1.4 (a) Specular and (b) Lambertian reflectance.

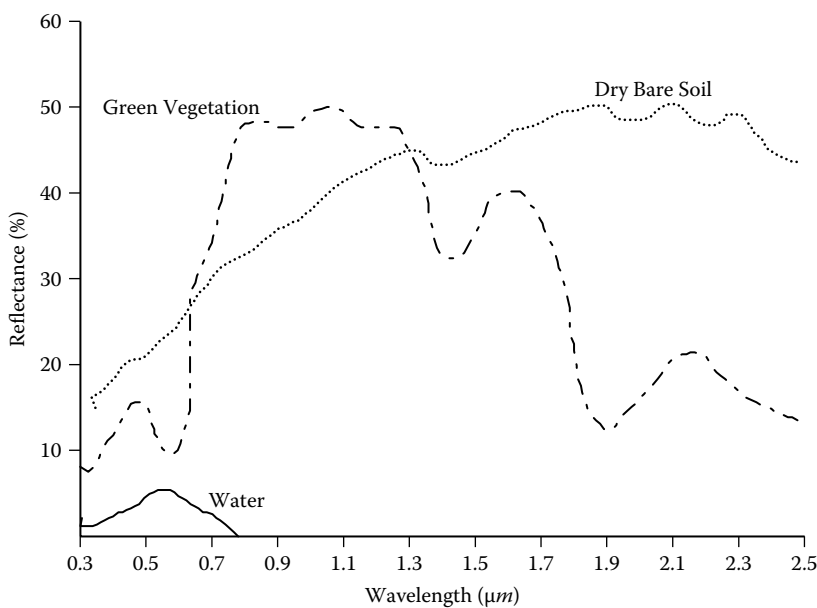


FIGURE 1.5 Typical spectral reflectance (%) of three materials: green vegetation, dry bare soil, and water.

across these wavebands. The lowest reflectance values occur at 0.4 μm (i.e., in the blue waveband), while the highest reflectance values occur around the near-infrared and part of the mid-infrared bands. The reflectance spectrum of bare soil, in contrast, shows reflectance increasing smoothly with wavelength. Its reflectance in the visible waveband is greater than that of vegetation, while in near-infrared and part of mid-infrared bands bare soil reflectance becomes less than that of vegetation, and eventually it dominates again beyond wavelengths of around 1.4 μm . The high near-infrared reflectance of vegetation, combined with its low reflectance in the

red waveband, is used in the construction of vegetation indices. One such index, the NDVI (Normalized Difference Vegetation Index), is described in the following text.

Recent interest in global environmental change has led to the development of global climate models, which require inputs describing land cover type. The AVHRR sensor carried by the National Oceanographic and Atmospheric Administration (NOAA) satellite series (from NOAA-6 to NOAA-18) provides data that are useful for large-scale studies of terrestrial vegetation (Eidenshink and Faundeen, 1994; Lim and Kafatos, 2002). A variety of mathematical combinations (e.g., subtraction, ratioing) of AVHRR band 1 (red) and band 2 (near infrared) have been developed to characterize the spatial distribution of vegetation and its condition. The best known of these vegetation indices is the Normalized Difference Vegetation Index (NDVI), defined as

$$\text{NDVI} = \frac{(\text{Near Infrared Band}) - (\text{Red Band})}{(\text{Near Infrared Band}) + (\text{Red Band})} \quad (1.1)$$

This index is based on the observation that vegetation has a high reflectance in the near infrared band, while reflectance is lower in the red band (Figure 1.5). NDVI is less sensitive to the changes of atmospheric conditions than are other indices (Jackson, 1983; Holben and Kimes, 1986) and therefore has been widely applied for vegetation monitoring. Data from other sensors that provide red and near-infrared (near-IR) images can also be used to generate NDVI images. For instance, in the case of Landsat Thematic Mapper TM images, NDVI is based on bands 5 and 7, while for SPOT HRV, NDVI is derived from bands 3 and 2.

Reflectance from water surfaces is relatively low, and is more or less zero at wavelengths beyond the visible red. Knowledge of surface material reflectance characteristics provides us with a principle on the basis of which suitable wavebands to scan the Earth surface for a particular mission can be selected (e.g., for vegetation monitoring, sea surface observation, or lithological identification). Such knowledge also provides an important basis to make the objects more distinguishable in terms of multiband image manipulations such as overlay, subtraction, or ratioing.

1.1.3 SPATIAL AND RADIOMETRIC RESOLUTION

The resolution of a remote sensing instrument can be expressed in terms of its spatial and radiometric resolution. The higher the spatial resolution the smaller the ground objects that can be distinguished. The spatial resolution is related to the *instantaneous field of view* (IFOV) of the sensor, which denotes the size of the area from which the sensor receives the energy at the given instant in time. In Figure 1.6 the energy transmission path to the sensor takes a conelike shape, and ground resolution is roughly equivalent to the diameter of the circle formed by the intersection of this cone and the ground surface. As the sensor scanning area moves away from the nadir, the larger the IFOV will be (Figure 1.6), and thus results in the distortion of the resulting image as the spatial scale decreases from the left and right edges of

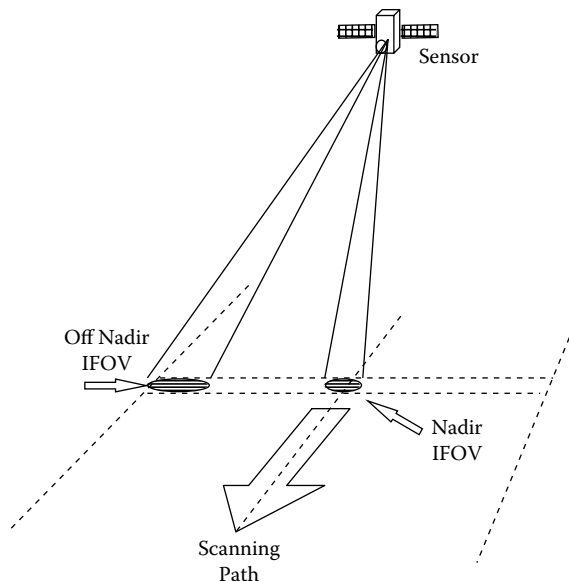


FIGURE 1.6 Showing the variation in the size of the instantaneous field of view (IFOV) of a sensor across a scan line.

the image toward the center. The correction for this scale distortion effect (and other effects due principally to the platform's orbit characteristics and to the eastward rotation of the Earth during scanning) is called *geometric correction*. This correction is usually performed by constructing a transform (using either an empirical procedure based on least squares methods or an analytical procedure using orbital information) in order to map ground coordinates to their corresponding image coordinates, and vice-versa. A review of local and global methods of geometric correction and image registration is provided by Brown (1992) and Zitová and Flusser (2003).

One's instinctive feeling might be that the finer the spatial resolution the better. However, in practice, this may not always be the case. The choice of spatial resolution should depend on what we want to see. For instance, in everyday life, we recognize a human face from the combination of features such as eyes, nose, lips, etc. Therefore, the appropriate spatial resolution should be set at a level to allow us to recognize each feature in the context of the whole face. It is arguable whether an increase in the spatial resolution of our eyes is likely to improve our identification of faces, once a certain limit has been reached. Thus, the choice of spatial resolution is case dependent.

Reducing the spatial resolution in terms of narrowing the instrument's IFOV also affects a related issue. The use of a smaller IFOV implies that the quantity of energy received by a detector is less (because area from which energy is collected is smaller, and the time available for the sensor to detect the upwelling energy is also shorter). It follows that the instrument's sensitivity to changes in the levels of energy will decrease, and thus the sensor may not be able to distinguish slight energy differences along a scan line. In other words, the radiometric resolution is degraded. A smaller

IFOV may thus result in a worse signal-to-noise ratio, which means that the signal is contaminated by more noise as IFOV decreases (assuming that the same radiometric resolution applies). Although such a decrease in signal-to-noise ratio can be compensated for by enlarging the scanning bandwidth (i.e., the region of the electromagnetic spectrum from which sensor receives energy), this will cause a reduction in the spectral resolution (i.e., sensor's ability to quantify spectral differences). Overall, it can be concluded that enhancement of both spatial and radiometric resolution cannot be achieved together, and some kind of compromise is needed.

1.2 OPTICAL REMOTE SENSING SYSTEMS

Over the past 20 to 25 years, the most widely used optical remote sensing systems have been the Landsat TM and Multispectral Scanning (MSS), the SPOT HRV, and the NOAA AVHRR instruments. Other remote sensing satellites carrying optical sensors have been launched by a number of national space agencies and private companies, and these have also gradually become the main sources for serving scientific study and environmental monitoring purposes. Examples are the Chinese-Brazilian remote sensing system, the Terra spacecraft, the Space Imaging Corporation's IKONOS satellite the European Envisat, the Indian IRS series, and several Japanese experimental projects. High-resolution sensing devices (4 m in multispectral mode, one meter or less in panchromatic mode) are now well established (e.g., the QuickBird satellite, and IKONOS). Radar systems are also becoming more numerous (Canada's Radarsat 1 and 2, the German TerraSAR-X, the European Advanced Synthetic Aperture Radar (ASAR) on Envisat, and the Italian COSMO-SkyMed X-band system). Considerable interest is also being shown in the application of hyperspectral imagery. Whereas multispectral sensors such as the Landsat ETM+ collect upwelling radiation in a small number of broad wavebands (seven in the case of the ETM+ instrument), a hyperspectral sensor collects data in a large number of very narrow wavebands. An example is the DAIS instrument, which collects data in 79 bands in the wavelength range 0.4 to 12.6 μm . The width of each spectral band varies from 15 to 20 nm in the visible to 2 μm in the middle infrared. The Compact Airborne Spectrographic Imager (CASI) instrument allows data to be collected for any 545-nm segment of the 0.4- to 1.0- μm region in 288 bands, with the bands spaced at intervals of approximately 1.9 nm. NASA's AVIRIS acquires data in 224 bands in the range 0.38 to 1.5 μm with a bandwidth of 10 nm. Up until the present time, hyperspectral data have been collected by aircraft-mounted sensors. NASA's Earth Observer I, launched in 2000, is the first orbiting spacecraft to carry a hyperspectral imager, Hyperion. The Hyperion instrument collects data over a narrow swath in 220 bands of 10 μm width. The large number of spectral bands produced by hyperspectral sensors (i.e., the high dimensionality of the data) poses significant problems in the pattern recognition process. These problems are discussed in Chapter 2.

Another class of satellites is the *small sat*, constructed using off-the-shelf components. The leader in this area is Surrey Satellite Technology Limited, which has developed the DMC or Disaster Monitoring Constellation of small satellites, which

have been purchased by several governments, including Algeria, Nigeria, China, and the United Kingdom. The imaging sensor carried by these satellites is comparable to Landsat's TM in the visible and near-IR bands.

An exhaustive list of sensors and satellites is not supplied here; such lists tend to become outdated very quickly. The advent of the World Wide Web (WWW) means that researchers, teachers, and students can readily obtain up-to-date information via the Internet. Professional and learned societies, such as the Remote Sensing and Photogrammetry Society, maintain WWW pages that provide links to international and national space agencies and projects. The Committee for Earth Observation Satellites (CEOS) also maintains an information site.

Details of the operation of the main types of sensor carried by remote sensing satellites can be found in textbooks (e.g., Lillesand and Keifer, 2000; Mather, 2004) and readers who may be unfamiliar with these details are referred to one of these sources.

1.3 ATMOSPHERIC CORRECTION

Electromagnetic energy detected by remote sensing instruments (especially those that operate in the optical region of the spectrum) consists of a mixture of energy reflected from or emitted by the ground surface and energy that has been scattered within or emitted by the atmosphere. The magnitude of the electromagnetic energy in the visible and near-infrared region of the spectrum that is detected by a sensor above the atmosphere is dependent on the magnitude of incoming solar energy (irradiance), which is attenuated by the process of atmospheric absorption, and by the reflectance characteristics of the ground surface. Hence, energy received by the sensor is a function of incident energy (irradiance), target reflectance, atmospherically scattered energy (path radiance), and atmospheric absorption. Interpretation and analysis of remotely sensed images in the optical region of the spectrum is based on the assumption that the values associated with the image pixels accurately represent the spatial distribution of ground surface reflectance, and that the magnitude of such reflectance is related to the physical, chemical, or biological properties of the ground surface. Clearly, this is not the case unless corrections are applied to take account of variations in solar irradiance and in the magnitude of atmospheric absorption and scattering, as well as in the sensitivity of the detectors used in the remote sensing instrument. The response of these detectors to a uniform input tends to change over time. Correction for these effects is vital if thematic images of a given area are to be compared over time; for example, over a crop-growing season.

The necessity for atmospheric correction depends on the objectives of the analysis. In general, land cover identification exercises that are based on single-date images do not require atmospheric correction, as pixels are being compared to other pixels within the image in terms of similarity, for example. The validity of this statement depends also on the quality of the image (for example, an image displaying severe haze effects, spatially varying haze phenomena, or cloud–cloud shadow effects may be unsuitable for classification). Atmospheric correction and sensor calibration are necessary when multisensor or multirate images are being classified, or where the aim of pattern recognition is to identify land cover change over time, in order to

ensure that pixel values are comparable from one image to the next in a temporal sequence. A more radical view is taken by Smith and Milton (1999, p. 2653), who emphasize that “to collect remotely sensed data of lasting quantitative value then data must be calibrated to physical units such as reflectance.”

The value recorded for each pixel in a remotely sensed image is a function of the sensor-detected radiance. Owing to the atmospheric interaction, this *apparent* radiance is the combination of the contribution of the target object and the atmospheric effect. Their relationship can be approximated as

$$L_{app} = \rho TE/\pi + L_p. \quad (1.2)$$

Here, L_{app} denotes the apparent radiance received by the sensor, L_p is the path radiance, ρ is the target reflectance (%), T is the atmospheric transmittance (%), and E is the solar irradiance on the target. Radiance is expressed in units of $Wm^{-2} sr^{-1} \mu m^{-1}$, and irradiance is expressed in the units of $Wm^{-2} \mu m^{-1}$. As these two terms are not expressed in equivalent units, solar irradiance is converted into *equivalent solar radiance* by introducing the term π into the denominator. This conversion is based on the assumption that the target behaves as a Lambertian reflector (as described in Figure 1.4) (Mackay et al., 1994).

In Equation (1.2), only the first term ρ contains information about the target. The atmosphere contributes the second term, the path radiance L_p , which varies inversely in magnitude with wavelength. In the case of multispectral images, the magnitude of the L_p term in the visible bands will be higher than that in the near- or mid-IR bands.

1.3.1 DARK OBJECT SUBTRACTION

Two kinds of methods are used for atmospheric effect correction. The first kind consists of the dark object subtraction techniques (Chavez, 1988; Ouaidrari and Vermote, 2001), which involve subtraction of a constant value (offset) from all pixels in a given spectral band. These methods are based on the assumption that some pixels in the image should have a reflectance of zero, and that the values recorded for these zero pixels result from atmospheric scattering. Thus, these pixel values represent the effects of atmospheric scattering. For example, the reflectance of deep clear water in the near-IR waveband is near zero. Dark object subtraction methods assume that nonzero pixel values over deep, clear, water areas in the near-IR band are contributed by the path radiance L_p , and that the path radiance is spatially constant (meaning that a single value of path radiance is subtracted from all pixel values in the image). In case the of the visible bands, one may use shadow areas due to topography as dark objects. In effect, one is using the histogram offset as a measure of atmospheric path radiance, as shown in Figure 1.7.

The empirical line method is described and evaluated by Smith and Milton (1999). The method requires that ground measurements of surface reflectance of dark and bright areas in the image are taken simultaneous with the overflight, though if the areas are spectrally stable, the measurements need not be simultaneous (though they must be taken under similar atmospheric and illumination conditions). The image data are converted to radiance using the standard calibration, and surface

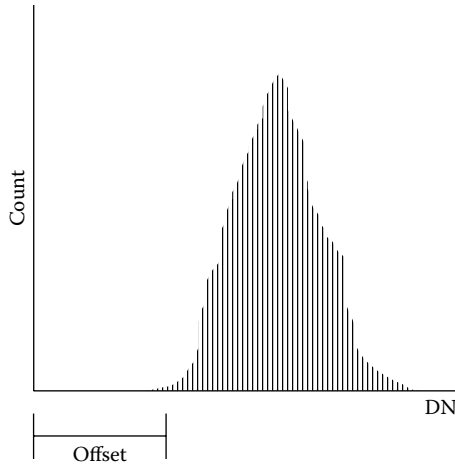


FIGURE 1.7 An estimate of path radiance is the image histogram offset from zero.

reflectance R is regressed against sensor radiance L to give a relationship of the form $R = (L - a) \times s$. The term a represents atmospheric radiance, which is subtracted from apparent radiance L before conversion to reflectance. Other descriptions of the empirical line methods are found in Moran et al. (2001) and Karpouzli and Malthus (2003).

1.3.2 MODELING TECHNIQUES

The methods described in Section 1.3.1 above involve the subtraction of the same pixel value from the whole image. They are easy to apply, but only provide an approximate correction. If the magnitude of the ground-leaving reflectance for each pixel is required, a more sophisticated method based on modeling techniques is necessary (e.g., Tanré et al., 1986, 1990; Vermote et al., 1997). These methods attempt to model atmospheric interactions, through which one can retrieve estimates of true target reflectance.

1.3.2.1 Modeling the Atmospheric Effect

The 5S model (Simulation of the Sensor Signal in the Solar Spectrum) developed by Tanré et al. (1986, 1990) is the best-known atmospheric calibration model. An improved version is the 6S (Second Simulation of the Sensor Signal in the Solar Spectrum) model (Vermote et al., 1997), which is capable of simulating a non-Lambertian surface to model the signal measured by the sensor. The 6S model also includes data for calculating atmospheric absorption using an increased number of atmospheric gases. In what follows, the core of the model is described in order to provide an introduction to atmospheric modeling.

Assume unit solar irradiance incident on top of the atmosphere. A fraction of the incident solar irradiance is scattered from the path between the sun and the ground target into the atmospheric volume, with the remainder of the radiation being

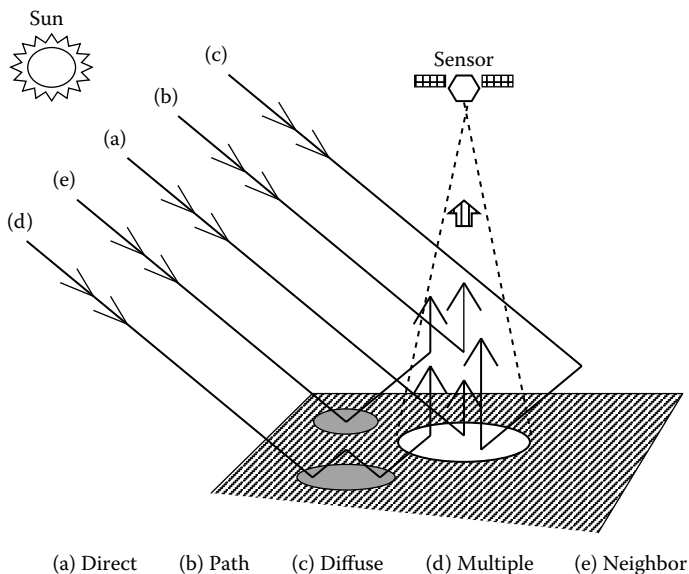


FIGURE 1.8 Five kinds of radiative interaction with the atmosphere.

incident on the ground target as direct solar radiation (Figure 1.8a). This transmitted fraction, denoted by $T(\theta_s)$, is defined as

$$T(\theta_s) = \exp\left(\frac{-\tau}{\cos(\theta_s)}\right). \quad (1.3)$$

The term τ is known as the optical depth, and θ_s is the solar zenith angle, which is illustrated in Figure 1.9.

A fraction of the solar radiation that is scattered into the atmosphere will also appear to contribute to the illumination of the ground target (Figure 1.8c, marked “diffuse”) and will compensate for some of the attenuation of the direct beam. If we

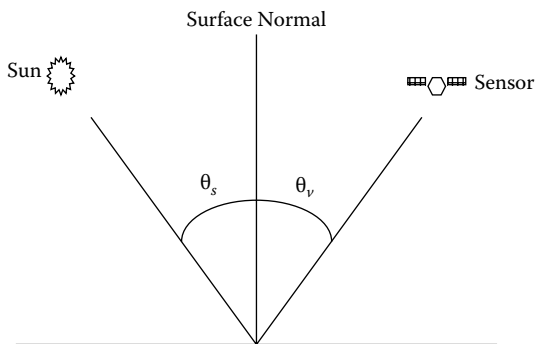


FIGURE 1.9 Solar and sensor view angles on a horizontal surface.

denote this diffuse skylight as $t_d(\theta_s)$, then the fraction of solar irradiance incident at the ground target becomes

$$T(\theta_s) = \exp\left(\frac{-\tau}{\cos(\theta_s)}\right) + t_d(\theta_s). \quad (1.4)$$

A second scattering flux that also should be taken into consideration is the trapping mechanism. The effect of this mechanism corresponds to the successive reflection and scattering of solar radiation between the ground target neighborhood and the atmosphere, so that the radiation then becomes incident upon the ground target, as shown in Figures 1.8d and 1.8e. The magnitude of this effect depends on the spherical albedo of the atmosphere, S , and the surface reflectance, ρ_s . The illumination at the ground target now becomes

$$\frac{1}{1 - \rho_s S} \times T(\theta_s). \quad (1.5)$$

The proportion of the solar radiation reflected from the ground target is expressed as

$$\frac{\rho_s}{1 - \rho_s S} \times T(\theta_s). \quad (1.6)$$

Consider a sensor that is receiving the reflectance from the ground target. The reflectance is generated by two main sources: one is the contribution of the total solar radiation reflected by the ground target and directly transmitted from the surface to the sensor, while the other is the contribution from the target neighborhood, which is scattered into the field of view of the sensor. The reflectance received by the sensor can thus expressed by

$$\frac{\rho_s}{1 - \rho_s S} \times T(\theta_s) \times T(\theta_v). \quad (1.7)$$

In this equation, θ_v is the sensor view zenith angle, and Equation (1.4) can be again applied to express $T(\theta_v)$ as

$$T(\theta_v) = \exp\left(\frac{-\tau}{\cos(\theta_v)}\right) + t_d(\theta_v). \quad (1.8)$$

The sensor also receives a fraction of the solar radiation that has been scattered out of the downward solar beam into the sensor's field of view without interaction with the ground target, as shown in Figure 1.8b. This component is the atmospheric reflectance, denoted by the function $\rho_a(\theta_s, \theta_v, \phi)$, where ϕ is the relative azimuth

between the sun and the sensor. Therefore, the apparent reflectance ρ^* at the sensor is

$$\rho^* = \frac{\rho_s}{1 - \rho_s S} \times T(\theta_s) \times T(\theta_v) + \rho_a(\theta_s, \theta_v, \phi). \quad (1.9)$$

Equation (1.9) is a linear equation that specifies the relationship between the apparent reflectance ρ^* and the surface reflectance ρ_s . The term $T(\theta_s) \times T(\theta_v)$ is the total atmospheric transmittance along the sun–target–sensor path.

A second atmospheric interaction should be considered, namely, the process of absorption. In the solar (optical) spectrum, atmospheric gaseous absorption is principally due to the presence of ozone (O_3), oxygen (O_2), water vapor (H_2O), and carbon dioxide (CO_2). Both O_2 and CO_2 are uniformly mixed in the atmosphere and are constant in terms of their concentrations, whereas H_2O and O_3 concentrations vary with time and geographical location. If $T_g(\theta_s, \theta_v)$ denotes atmospheric gas transmittance after absorption, then Equation (1.9) can be modified to give

$$\rho^* = T_g(\theta_s, \theta_v) \times \left[\frac{\rho_s}{1 - \rho_s S} \times T(\theta_s) \times T(\theta_v) + \rho_a(\theta_s, \theta_v, \phi) \right]. \quad (1.10)$$

In order to retrieve the surface target reflectance, ρ_s , Equation (1.10) is further expanded as

$$\begin{aligned} \frac{\rho^*}{T_g(\theta_s, \theta_v)} - \rho_a(\theta_s, \theta_v, \phi) &= \frac{\rho_s}{1 - \rho_s S} \times T(\theta_s) \times T(\theta_v) \\ \Rightarrow \frac{\rho^*}{T_g(\theta_s, \theta_v) \times T(\theta_s) \times T(\theta_v)} - \frac{\rho_a(\theta_s, \theta_v, \phi)}{T(\theta_s) \times T(\theta_v)} &= \frac{\rho_s}{1 - \rho_s S} \\ \Rightarrow \frac{\rho^*}{T_g(\theta_s, \theta_v) \times T(\theta_s) \times T(\theta_v)} - \frac{\rho_a(\theta_s, \theta_v, \phi)}{T(\theta_s) \times T(\theta_v)} &= \frac{\rho_s}{1 - \rho_s S}. \end{aligned} \quad (1.11)$$

If we define

$$A = \frac{1}{T_g(\theta_s, \theta_v) \times T(\theta_s) \times T(\theta_v)}, \text{ and } B = -\frac{\rho_a(\theta_s, \theta_v, \phi)}{T(\theta_s) \times T(\theta_v)}$$

then Equation (1.11) eventually gives

$$\rho_s = \frac{A \times \rho^* + B}{[1 + S \times (A \times \rho^* + B)]}. \quad (1.12)$$

Thus, knowing the apparent reflectance ρ^* , the spherical albedo S , and the coefficients A and B , the surface target reflectance ρ_s can be obtained. Methods for obtaining these parameters are illustrated in Section 1.3.2.2.

1.3.2.2 Steps in Atmospheric Correction

The procedure to obtain estimates of the ground target reflectance involves three steps, as illustrated in Figure 1.10. The first step, converting the pixel value to radiance, is sensor-dependent. For instance, in the case of Landsat TM images, the relationship between the pixel values and apparent radiance L_{app} is expressed as

$$L_{app} = A_i \times DN + B_i \quad (1.13)$$

while in the case of SPOT HRV data the relationship is

$$L_{app} = DN/A_i \quad (1.14)$$

where A_i and B_i are the calibration *gain* and *offset* for band i , respectively. These calibration coefficients can be found either from the literature (e.g., Gellman et al., 1993; Thome et al., 1997; Teillet et al., 2001; Meygret, 2005) or from image header files. Note that header files may contain prelaunch calibrations that may differ significantly from the actual calibrations due to sensor degradation over time.

The second step, conversion from apparent radiance L_{app} to apparent reflectance ρ^* , is based on the observation that in case of 100% reflectance, the radiance measured by the sensor is the result of multiplication of equivalent solar radiance (E/π), the cosine of solar zenith angle ($\cos(\theta_s)$), and the Earth-to-sun distance multiplicative factor d (Kowalik and Marsh, 1982). The factor d is measured in astronomical units (au) and is described further below. One au is equal to the average Earth-to-sun distance. About January 3, at perihelion, the Earth-to-sun distance is approximately 0.983 au, and on July 5, at aphelion, the Earth-to-sun distance is about 1.0167 au.

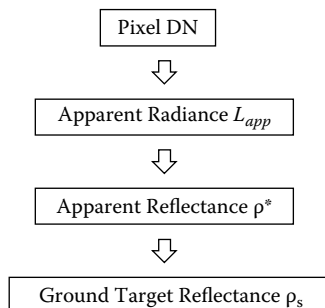


FIGURE 1.10 Procedure for retrieving ground radiance.

If the required coefficients are known, then the variation in sensor-detected apparent radiance L_{app} is caused by the difference in reflectance. One then obtains the following relation:

$$L_{app} = \frac{\rho^* \times \cos(\theta_s) \times E}{d\pi}$$

or, equivalently,

$$\rho^* = \frac{d \times L_{app}}{\cos(\theta_s) \times E / \pi}. \quad (1.15)$$

The value of the solar zenith angle can be retrieved from the image header file. The distance multiplicative factor d is used to compensate for the variation in solar irradiance E caused by the change in distance between the sun and the Earth. It is obtained from

$$d = au^2. \quad (1.16)$$

An alternative way to approximate Equation (1.16) is given by

$$d = \left(1 - 0.01673 \times \cos(0.9856 \times (JD - 4))\right)^2 \quad (1.17)$$

where the term JD denotes the Julian day (e.g., in the case of 5th February, $JD = 36$).

The introduction of the factor d into Equation (1.15) is justified by the following observations. Since at perihelion, the magnitude of solar irradiance is greater than that at aphelion, if a sensor obtains the same radiance L_{app} at perihelion and aphelion, respectively, the apparent reflectance ρ^* at perihelion should be less than that at aphelion. Thus, if the sun-to-Earth distance is smaller than the average sun-to-Earth distance, one should use a lower (< 1) weighting factor d , and as the Earth is approaching aphelion, a higher value of d should be used.

The final step—that of converting apparent reflectance to ground target reflectance—uses Equation (1.12). We already know the apparent reflectance ρ^* from Equation (1.15), while other parameters such as the spherical albedo, S , and the coefficients A and B can be obtained by running either the 5S or the 6S model. An example is given in Table 1.1, which shows part of the output generated by the 5S model. The spherical albedo S and relevant parameters for deriving A and B are displayed in bold type. For a detailed description of 5S and 6S usage, readers are referred to Tanré et al. (1986, 1990) and Vermote et al. (1997). Once ground reflectance is retrieved, one may use Equation (1.15) to retrieve radiance followed by using either Equation (1.13) or Equation (1.14) to convert the radiance back to a corrected pixel value.

TABLE 1.1
Results from the 5S Model Used for Atmospheric Correction

	Downward	Upward	Total
Global gas transmission	0.961	0.965	0.932 = $T_g(\theta_s, \theta_v)$
Water transmission	0.988	0.989	0.980
Ozone transmission	0.975	0.978	0.954
CO ₂ transmission	1.000	1.000	1.000
O ₂ transmission	0.999	0.999	0.998
NO ₂ transmission	1.000	1.000	1.000
CH ₄ transmission	1.000	1.000	1.000
CO transmission	1.000	1.000	1.000
Rayleigh scattering transmission	0.967	0.971	0.939
Aerosol scattering transmission	0.953	0.962	0.917
Total scattering transmission	0.922	0.934	0.861 = $T(\theta_s) T(\theta_v)$
	Rayleigh	Aerosols	Total
Spherical albedo	0.048	0.087	0.123 = S
Optical depth total	0.054	0.362	0.416
Optical depth plane	0.054	0.362	0.416
Atmospheric reflectance	0.019	0.017	0.037 = $p_a(\theta_s, \theta_v, \varphi)$
Phase function	0.993	0.099	0.215
Single scattering albedo	1.000	0.990	0.992

1.4 CORRECTION FOR TOPOGRAPHIC EFFECTS

Normally, the surface being measured by the remote sensor is assumed to be flat with a Lambertian reflectance behavior. Under this assumption, the magnitude of the radiance detected by the sensor is affected only by variations in the solar zenith angle, the wavelength, and the atmospheric interaction. The atmospheric correction model introduced in Section 1.3 is also based on such ideal assumptions, which may be invalid in the case of rugged terrain because the solar incidence angle will vary with topographic properties and will further contribute to differences in the level of radiance detected by the sensor. This is known as *topographic effect*. More specifically, the topographic effect can be defined as the variation in radiance exhibited by inclined surfaces compared to radiance from a horizontal surface as a function of orientation of the surface relative to the radiation source. Moreover, if we assume non-Lambertian reflectance for the surface being measured, the sensor position is another important variable that should be considered.

Calibration for topographic effects is intended to normalize the sensor-detected signal difference caused by the topographic variation. Various techniques (e.g., Smith et al., 1980; Colby, 1991; Dymond and Shepherd, 1999; Riano et al., 2003; Law and Nichol, 2004) have been published. Here, we present two approaches, using

band ratioing and the Minnaert model, due to their better performance (Smith et al., 1980; Colby, 1991; Law and Nichol, 2004).

Band ratioing (Colby, 1991, Mather, 2004) is the most commonly used method for reducing the topographic effect. Colby (1991) uses a Landsat TM band 5/4 ratio image to study the effectiveness of topographic effect calibration by comparing several sample sites having the same vegetation cover but with differences in topography. In other words, the same vegetation cover should have a similar spectral response, irrespective of location, thus the differences between sample sites are assumed to be caused by topographic effects. Results showed that the variance of spectral response between sample sites in ratio image was lower than that obtained from original TM band 4 and 5 images. Colby (1991) concludes that band ratioing does partially compensate for topographic effects.

Smith et al. (1980) present two empirical photometric functions for studying the effect of topography on the radiance field. The first such function is based on a Lambertian reflectance assumption, while the second function assumes that reflectance is non-Lambertian. Although this is a relatively old model, it generates quite robust calibration results (Colby, 1991; Law and Nichol, 2004).

Figure 1.11 shows the geometrical relationships among the sun, the sensor, and an arbitrary surface element. The Lambertian model assumes that the surface reflects the incident radiation uniformly in all directions. If we treat wavelength as a constant and ignore atmospheric interactions, the variation in radiance detected by the sensor is mainly caused by the local incidence angle θ_i (i.e., the angle formed between the

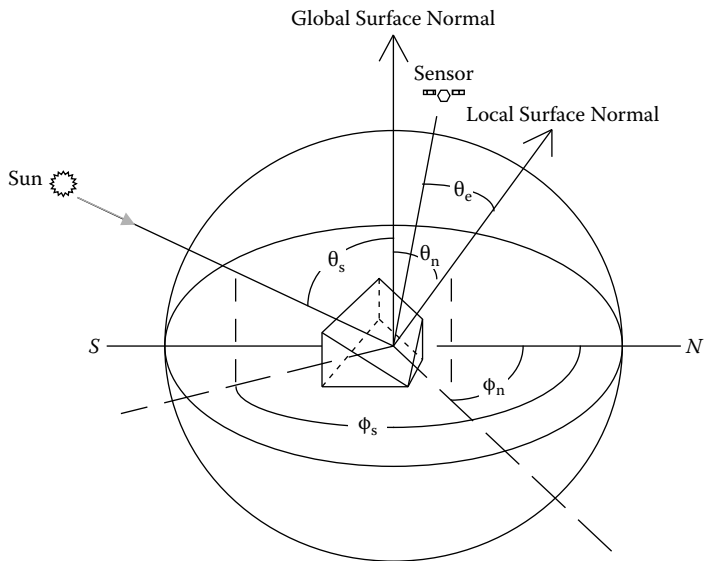


FIGURE 1.11 Geometrical relationships among the sun, the sensor, and the target position. Modified from Smith, J. A., T. L. Lin, and K. Ranson. “The Lambertian Assumption and Landsat Data,” Figure 1. *Photogrammetric Engineering and Remote Sensing* 46 (1980): 1183–1189. (Reprinted with permission from the American Society for Photogrammetry and Remote Sensing).

solar radiation path and local surface normal). In this case, sensor-detected radiance L can be normalized in terms of

$$L_n = L / \cos(\theta_i). \quad (1.18)$$

where L_n denotes the normalized radiance. The $\cos(\theta_i)$ term can be derived from the spherical law as follows:

$$\cos(\theta_i) = \cos(\theta_s) \cos(\theta_n) + \sin(\theta_s) \sin(\theta_n) \cos(\phi_s - \phi_n) \quad (1.19)$$

where θ_s is solar zenith angle, θ_n is the angle of slope of terrain surface, ϕ_s is the solar azimuth angle, and ϕ_n is the surface aspect of the slope angle (see Figure 1.11). Slope is defined as a plane tangent to the surface containing two components: one is gradient, which specifies the rate of change in elevation, and the other is aspect, which measures the direction of the gradient. The values of several parameters are required to solve these equations, namely, solar zenith angle θ_s , solar azimuth angle ϕ_s , the surface slope θ_n , and aspect ϕ_n . Both θ_s and ϕ_s can be obtained from the image header file, while slope and aspect can be derived by co-registering the image with a digital elevation model (DEM). A variety of approaches can be employed to calculate the slope and aspect from a DEM (Skidmore, 1989; Jones, 1998).

In the case of the non-Lambertian reflectance assumption, Smith et al. (1980) suggest the following function to correct for the topographic effect:

$$L \times \cos(\theta_e) = L_n \times [\cos(\theta_i) \cos(\theta_e)]^k \quad (1.20)$$

where θ_e is effective view angle (Figure 1.11), $\cos(\theta_i)$ is defined in Equation (1.19), and k is known as the Minnaert constant (Minnaert, 1941) describing the bidirectional reflection distribution function of the surface, the type of scattering dependence, and surface roughness, respectively. A Lambertian surface is defined by a k value of 1.0, and Equation (1.20) then reduces to Equation (1.18).

In order to solve Equation (1.20), one needs to relate the effective view angle θ_e and k (the method for deriving $\cos(\theta_e)$ is described in Equation [1.19]). If Landsat TM or MSS imagery is used, θ_e can be regarded as the same as θ_n (i.e., the slope of terrain surface) since Landsat has a narrow view angle. In the case of SPOT HRV data, which can acquire imagery through an angle of $\pm 27^\circ$, θ_e should be set to $\theta_e = \theta_n$, the satellite view angle. To estimate the Minnaert constant k , Equation (1.20) is converted into logarithmic form as

$$\log(L \times \cos(\theta_e)) = k \times \log(\cos(\theta_i) \cos(\theta_e)) + \log(L_n). \quad (1.21)$$

The term k is then equal to the slope of regression line of the plot made by the samples $\log(\cos(\theta_i) \cos(\theta_e))$ plotted on the x -axis and $\log(L \cos(\theta_e))$ plotted on the y -axis.

To calibrate for the topographic effect using a non-Lambertian assumption is more complicated than that based on a Lambertian reflectance assumption. As far as the computational cost and calibration accuracy is concerned, Smith et al. (1980)

suggest that when surface slopes are less than 25° and effective illumination angles are less than 45° , then the Lambertian assumption is more valid. Under such circumstances, one can use Equation (1.18) to carry out topographic effect correction, and the calibration accuracy should be preserved. If either of the above conditions is not satisfied, the use of Equation (1.20) is recommended.

It should also be appreciated that surface topographic variations will also cause distortions in the geometry of images. The map to which the image is referenced represents the relationship between features reduced to some datum such as sea level, while the image shows the actual terrain surface. If the terrain surface is significantly above sea level then the image pixel position will be displaced by an amount proportional to the pixel's elevation above sea level (or whatever datum is used).

1.5 REMOTE SENSING IN THE MICROWAVE REGION

The word *radar* is an acronym derived from the phrase “Radio Detection And Ranging.” Imaging microwave sensors are known as *imaging radars*. These instruments transmit a signal in the wavelength range approximately 3 cm to 1 m, and receive reflection (backscatter) from the target. The level of backscatter for each pixel over the imaged area is recorded and the set of pixels forms the radar image. Remote sensing in the microwave region differs from optical remote sensing in a number of ways, the most important of which are

1. Radar backscatter is related to the roughness and electrical conductivity of the target. This information is complementary to that which is acquired by optical and thermal sensors.
2. Energy in the microwave region can penetrate clouds.
3. Microwave imaging radars are active, not passive instruments, and thus can operate independently of solar illumination.

An increasing number of space-borne radar systems is now in orbit, including the recently launched German TerraSAR-1 and the Italian COSMO-SkyMed, and it is probable that radar imagery will play an increasingly important role in supporting our understanding and monitoring of our environment. The main disadvantage of active microwave systems vis-à-vis optical systems is their power requirements, for the sensor transmits as well as receives energy. Optical sensors passively detect reflected solar radiation. Passive microwave sensors, which are not considered in this chapter, detect microwave radiation that is generated by the target.

This section introduces radar remote sensing. In Section 1.6, basic ideas underlying the use of radar images, including geometrical effects and the main factors affecting surface reflection or backscatter at radar wavelengths, are introduced. Section 1.7 considers the extraction of surface information from this backscattered signal. One of the main problems associated with the interpretation of radar imagery is the presence of noise, or *radar speckle*. The use of filters to reduce the noise effect is described in Section 1.8.

1.6 RADAR FUNDAMENTALS

An active radar system repetitively transmits short microwave energy pulses (normally of the order of microseconds, i.e., 10^{-6} second, denoted by μs) toward the area to be imaged. The energy pulse is likely to scatter in all directions when it reaches the surface. Part of the backscattered energy is reflected back to the radar antenna and recorded for later processing. Normally, each energy pulse has a duration of between 10 and 50 μs , and utilizes a small range of microwave wavelengths. A waveform can be characterized in terms of its wavelength and amplitude. Wavelength is defined as the distance between two adjacent crests or troughs of the waves (Figure 1.12). Amplitude measures the strength of an electromagnetic wave in terms of the maximum distance achieved by the waveform relative to the mean position (shown by the horizontal line in Figure 1.12). The amplitude may be a function of a complex signal including both magnitude and the phase; this point is discussed further below.

Frequency, rather than wavelength, can also be used to describe wavebands. *Frequency* is the number of oscillations per unit time or number of wavelengths that pass a point per unit time. One can obtain the frequency f (normally of the order of Gigahertz, GHz) corresponding to wavelength λ in terms of

$$f = \frac{c}{\lambda} \quad (1.22)$$

where c is the velocity of light ($3 \times 10^8 \text{ ms}^{-1}$).

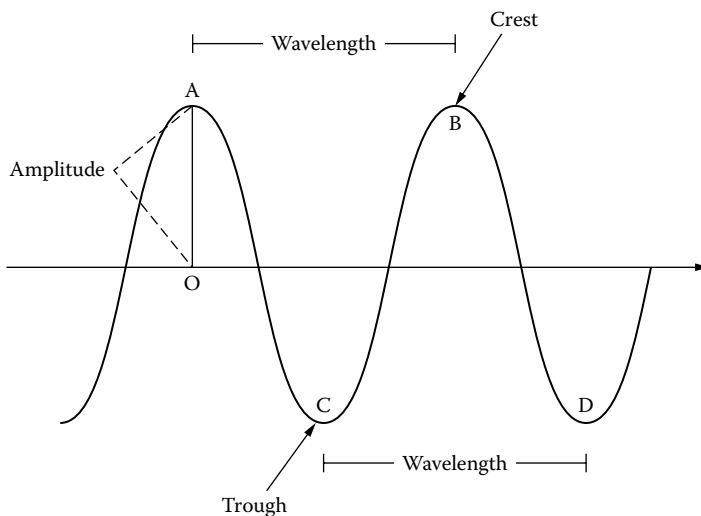


FIGURE 1.12 Wavelength is the distance between two adjacent crests (e.g., A and B) or troughs (e.g., C and D). The amplitude of a waveform (distance AO) measures the “power” or information carried by the wave.

The description of radar operation in the following pages is based on the most widely used radar system installed on aircraft platforms, the side-looking airborne radar (SLAR). Space-borne imaging radars operate on a similar basis, but use a synthetic rather than a real antenna. They are known as synthetic aperture radars (SAR).

1.6.1 SLAR IMAGE RESOLUTION

SLAR transmits and receives microwave energy using an antenna located to the side of the platform. The area imaged by the sensor is thus a strip of ground parallel to the flight track (known as the *azimuth direction*). SLAR image resolution is mainly dependent on pulse duration and antenna beam width, which is the ground area “illuminated” by the radar pulse at a given instant in time (Figure 1.13). Pulse duration affects the resolution in the range (cross-track) direction, while antenna beam width controls the azimuth (along-track) resolution. The ground range resolution and azimuth resolution are computed by

$$\text{Range Resolution} = \frac{c\tau}{2 \cos \theta} \quad (1.23)$$

$$\text{Azimuth Resolution} = \beta \times d \quad (1.24)$$

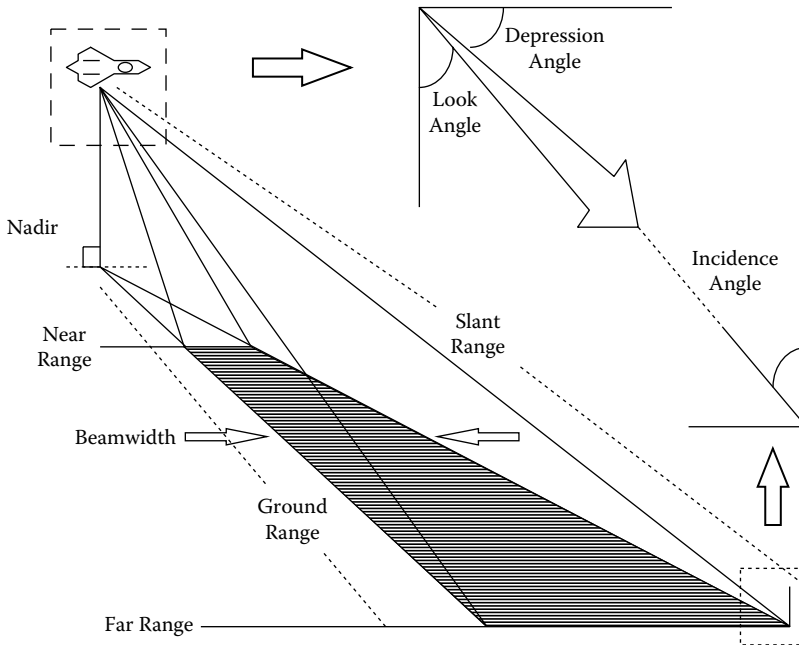


FIGURE 1.13 Some basic parameters of a SLAR system.

The term c is defined in Equation (1.22), while τ is the pulse duration, θ is the depression angle defined as the angle between the horizontal plane and the direction of emitted microwave energy (Figure 1.13), d is the ground range, and β is the antenna beam width. Range resolution can also be analyzed in terms of incidence angle or look angle (Figure 1.13). *Incidence angle* is defined as the angle between the radar beam and a line perpendicular to the illuminated surface. The *look angle* is complementary to the *depression angle*. If the illuminated surface is assumed to be flat, then one can also regard the incidence angle as the complement of the depression angle. The antenna beam width β , antenna length L , and wavelength λ are related as follows:

$$\beta = \frac{\lambda}{L}. \quad (1.25)$$

The combination of azimuth and range resolution determines the ground resolution of each pixel on a radar image.

It can be inferred from Equation (1.23) that the shorter the pulse duration τ , or the smaller the value of θ , the finer the range resolution. The depression angle θ varies across an image. The value of θ in the near range is relatively larger than that in the far range (Figure 1.13). Thus, the ground range resolution will also vary with respect to θ .

Equation (1.24) shows that the smaller the values of β and d , the finer the azimuth resolution will be. Thus, near ground range has a higher resolution than that in far ground range because both are smaller in near range than that in far range (Figure 1.13). According to Equation (1.25), one can use a long antenna length and short wavelength to obtain finer azimuth resolution. However, shorter wavelengths are more likely to be affected by the atmosphere and, furthermore, antenna length is constrained by physical limitations. For instance, to obtain an antenna beam width of 1×10^3 m at a wavelength of 20 cm, the required antenna length will be 200 m (Equation [1.25]). Clearly, if finer azimuth resolution is sought in terms of increasing antenna length, then serious practical difficulties will be encountered. An alternative strategy is to use a synthetic aperture radar (SAR), where the term *aperture* means the opening used to collect the reflected energy that is used to generate an image. In the case of radar, this opening is the antenna, while in the case of a camera, the opening is the shutter opening.

SAR increases the antenna length not in physical terms but by synthesizing a long antenna using the forward motion of a short antenna, a process that requires more complicated and expensive technology. SAR uses the Doppler principle in order to synthesize a longer antenna. The *Doppler effect* is the change in wave frequency as a function of the relative velocities of transmitter and reflector. A radar sensor can image a given target repeatedly from successive locations, as illustrated in Figure 1.14. Here, the frequency of the waveform reflected by the target will increase from location a to b because the distance between the sensor and the object is reducing. As the platform moves away from the target, from b to c , the frequency of the returned signal decreases. SAR uses the Doppler information to compute frequency shifts and thus determine the location and scattering properties of the target.

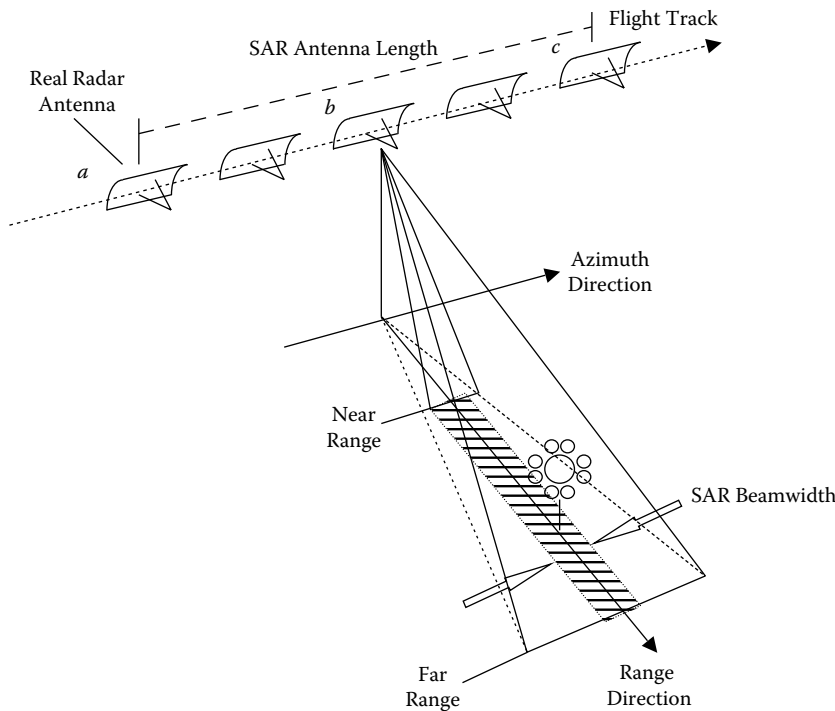


FIGURE 1.14 Concept of the synthetic aperture.

1.6.2 GEOMETRIC EFFECTS ON RADAR IMAGES

A radar image is generated from the timing data for transmitted energy to be returned to the radar antenna. This timing delay is dependent on the distance between the radar antenna and the target. This distance is the *slant range* (Figure 1.13), which is the path along which the microwave energy travels. Therefore, every target located on the terrain being observed by the radar will be mapped onto the slant range domain. Because of this slant range mapping, radar imagery is likely to be affected by geometric distortions. The most common distortions are those of layover, foreshortening, and shadow.

The *layover* effect results when the top of an illuminated target is seen by the radar as the bottom, and the bottom of the target is recorded by radar as the top. This phenomenon occurs when the time for the microwave energy to travel from the antenna to the top of an object is less than the time needed to travel to the bottom of the same object. Figure 1.15 shows two targets (a building and a mountain) that are illuminated by a radar sensor. The microwave energy transmitted by the radar will reach the tops of both objects (points *a* and *b* in Figure 1.15) before the bottoms (points *c* and *d*). The antenna will first receive the reflected energy from *a* and *b*, then some time later, the energy reflected from *c* and *d*. After projection onto the slant range domain, the result is called the *layover effect*.

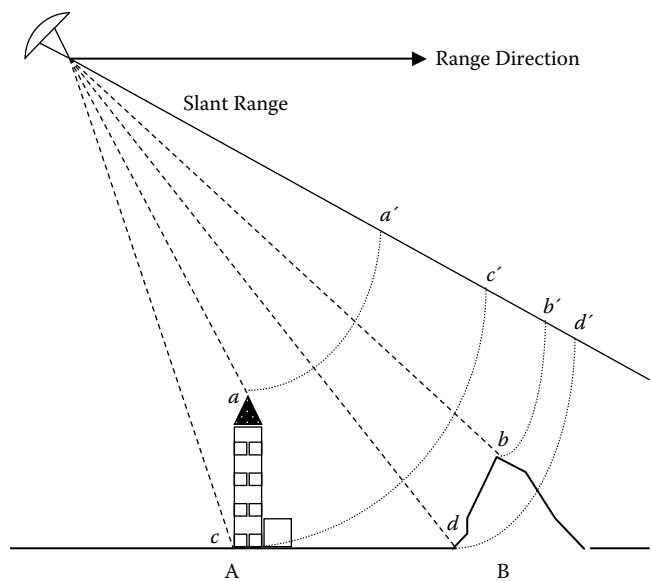


FIGURE 1.15 The layover effect in radar remote sensing.

It might be inferred from the preceding discussion that the higher the isolated target the greater the layover effect. However, layover is also controlled by another important factor: the angle, θ_f , between the front of the target and the energy path (Figure 1.16). Layover will occur only if θ_f exceeds 90° (see object A in Figure 1.16). If θ_f is smaller than 90° , as in the case of object B in Figure 1.16, then microwave

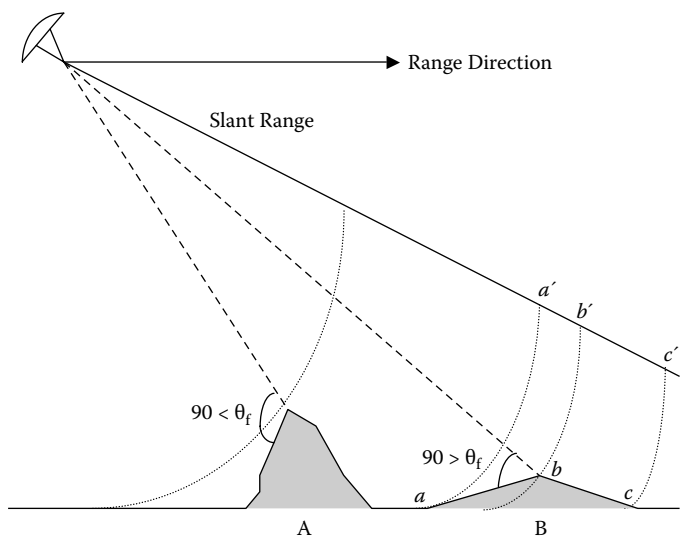


FIGURE 1.16 The angle θ_f controls layover effects (see text for discussion).

energy will first illuminate the bottom then the top of the object, and there will be no layover effect.

Foreshortening, like layover, results from the fact that radar is a side-looking sensor. The object labeled *B* in Figure 1.16 is symmetrical in cross-section, but the angle between its front slope *ab* and the microwave radiation emitted by the instrument is less than 90° . Hence, the front slope distance *ab* appears to be less than the back slope distance *bc* when projected onto slant range. Since the front slope also tends to reflect microwave energy more strongly than does the back slope, it will appear to be brighter, steeper, and shorter, while the back slope is shallower and darker. The darker back slope demonstrates another radar image geometry effect, that of shadow, as illustrated in the following text.

Radar shadow is due to the returned back energy from targets being affected by the nature of the terrain. A radar image is effectively a representation of returned energy levels plotted against the time taken for the energy to travel to and from the target. It follows that if, during a certain period, the antenna receives no reflection, then the image area corresponding to this time period will contain zero (dark) values.

The effect of radar shadow is controlled by the target height and angle θ_b (Figure 1.17), which is defined as the angle between the back slope of the target and the horizontal line parallel to the range direction. In Figure 1.17 the angle θ_b of object *A* is smaller than the corresponding depression angle θ_1 . Thus, the back slope of object *A* is illuminated by the microwave energy. However, since the angle θ_b of object *B* is larger than the corresponding depression angle θ_2 , the radar antenna will not receive any reflection from the back slope of object *B*, and this period of zero reflection is likely to continue until point *a* is reached. The resulting radar shadow after projection onto slant range is also illustrated in Figure 1.17.

The description of radar image distortions given above is a simplification. In real-world applications where terrains are often continuously sloping and rapidly varying,

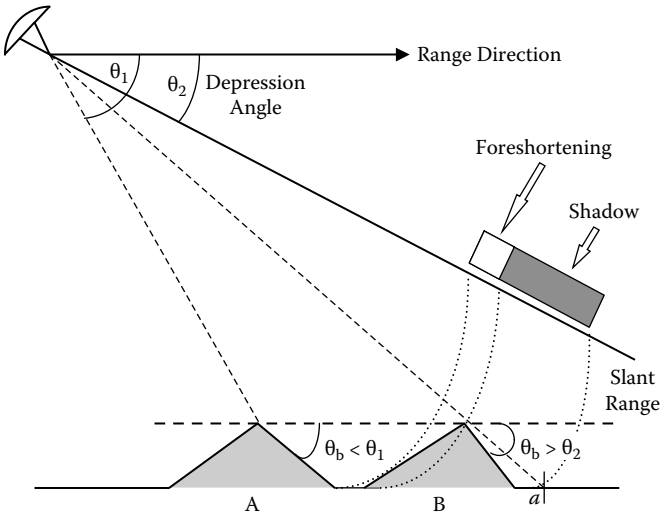


FIGURE 1.17 Showing the relationship between angle θ_b and radar shadow.

the resulting image will be a combination of different geometric effects. Hence, in order to compensate for these effects, one has to make careful case-by-case analyses (Kropatsch and Strobl, 1990; Goyal et al., 1999). That is, if one knows what effects are occurring at a given pixel, then one can use suitable algorithms to carry out calibration. As in the case of topographic calibration of optical imagery described above, geometric and radiometric correction of radar images requires a co-registration to a DEM. However, the calibration procedures are generally more complicated. Kwok et al. (1987), Riegler and Mauser (1998), and Hein (2003) provide descriptions.

1.6.3 FACTORS AFFECTING RADAR BACKSCATTER

It has already been noted that a radar image is a record of the strength of the backscatter from the targets making up the imaged area. The stronger the backscatter, the brighter the corresponding image element. The level of backscatter is determined by terrain conditions (such as roughness and electrical characteristics), and also by the parameters of the radar system. Understanding the factors affecting radar backscatter can help analyze landscape properties more knowledgeably.

1.6.3.1 Surface Roughness

Radar backscatter is stronger where the ground surface is rough relative to the radar wavelength. The roughness of a surface is dependent on both the wavelength of the incident energy and the angle of incidence. Rough surfaces act as Lambertian reflectors (Section 1.4) so that incident microwave energy is scattered in all directions and a portion is reflected back to the radar antenna. Smooth surfaces are specular, in that they act like a mirror and reflect the incident energy away from the sensor, resulting in extremely weak backscatter (Figure 1.18, point *a*). Normally, as the wavelength decreases, the surface appears rougher because smaller facets of the surface

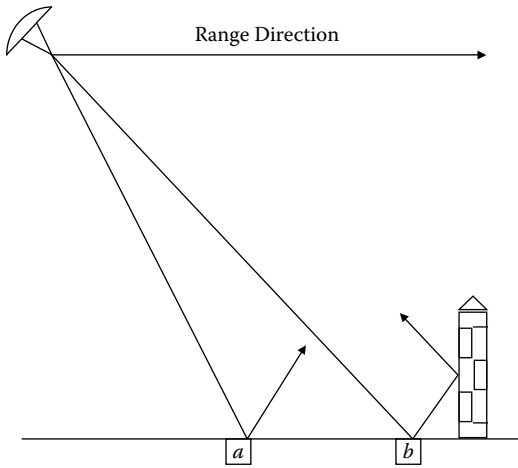


FIGURE 1.18 Microwave energy impinging on a smooth surface (point *a*) at which energy is reflected away from the sensor, and exhibiting a double bounce at point *b* when the reflected energy is reflected by a vertical wall.

contribute to the scattering process and thus stronger backscatter results. Likewise, as the wavelength increases, the surface tends to appear smoother. The strength of backscatter is also affected by the incidence angle. For a given wavelength, as the incidence angle increases, backscatter becomes weaker, and so the illuminated surface appears smoother. Some ground objects can behave like corner reflectors, which can reflect high energy back to the antenna and cause bright spots on the radar image. Such phenomena often occur in urban areas because energy can be returned by means of a *double bounce* from the corners of buildings (Figure 1.18, point *b*).

1.6.3.2 Surface Conductivity

Highly conductive ground surfaces tend to have higher reflectivity than surfaces with lower conductivities. Water and metal are good conductors. As a result, radar backscatter will be sensitive to metal objects and to the presence of moisture in the illuminated target area, even though the amount of moisture may be small. In a radar image, metal objects such as railway tracks and metal bridges generally result in bright spots. Moisture also affects the depth of microwave energy penetration of the soil surface. If soil contains a large amount of moisture, the signal does not penetrate the soil surface and is reflected back to the radar antenna. If the soil is dry, then the radar signal can penetrate more deeply into the soil surface layer. Wavelength is also another control on the depth of penetration. Lakes and other water bodies might be expected to exhibit high backscatter, but in fact the surfaces of rivers and lakes are generally smooth relative to radar wavelengths and act as specular reflectors. The ocean surface is generally rougher, and therefore the magnitude of backscatter depends on sea state as well as on wavelength and depression angle.

1.6.3.3 Parameters of the Radar Equation

The parameters of the radar equation (Van Zyl et al., 1993) are fundamental factors that influence the level of the returned signal. The radar equation is expressed as

$$P_r = \frac{P_t \lambda G_t(\gamma) G_r(\gamma)}{(4\pi)^3 R^4} \sigma^0 A. \quad (1.26)$$

P_t is the transmitted power from the antenna, λ is the transmitted wavelength, R is the distance to imaging area, γ is the radar look angle, A is the area on the ground responsible for scattering, G_t and G_r are the transmitted and received antenna gains (describing the system's ability to focus the transmitted microwave energy) at look angle γ , and σ^0 is the radar backscatter coefficient measured in decibels (dB). All of the parameters in Equation (1.26) affect the received power P_r . However, only σ^0 is related to the properties of the illuminated surface. Thus, the quantized pixel values (0 to 255) in a radar image are sometimes converted to σ^0 before being interpreted. The received power P_r in Equation (1.26) can also be characterized in terms of other parameters such as the scattering matrix (Equation [1.31]) and the coefficient of variation (Equation [1.35]), which also relate to the properties of surface objects, and can be used for classification purposes. A discussion of the scattering matrix is presented in the next section.

1.7 IMAGING RADAR POLARIMETRY

The polarimetry theory presented in this section is mainly derived from Evans et al. (1988), Zebker and Van Zyl (1991), Zebker et al. (1987, 1991), Van Zyl et al. (1987, 1993), Kim and Van Zyl (2000) and Hellmann (2002). Knowledge of radar polarimetry enables us to use a variety of features (such as complex format data, the elements of the scattering matrix, and the coefficient of variation of polarization signature) to perform image interpretation. Some basic concepts are described first.

An electromagnetic wave, besides being described in terms of wavelength and amplitude, can also be characterized using *complex number* format (a complex number consists of a two components, termed the *real* and *imaginary* parts). When the coordinate system is translated into both the real and imaginary axes (Figure 1.19), the wave is described by two parameters, namely, the *in-phase* I ($I = m \times \cos\phi$) and *quadrature* Q ($Q = m \times \sin\phi$) components. Both the I and Q parameters provide the wave's overall phase ϕ ($\phi = \tan^{-1} (Q/I)$) and magnitude m ($m = (I^2 + Q^2)^{0.5}$) as illustrated in Figure 1.19. Radar phase represents the degree of coincidence in time between a repetitive radar signal and a reference signal having the same frequency. Over the complex domain, the amplitude a is expressed as $a = I + iQ$, where $I = (-1)^{0.5}$. The relationship between the magnitude m and a complex amplitude a , by definition, can be expressed as $m = |a|$, i.e., the absolute value of amplitude. The radar image can thus be formed by using any of the m , I , or Q components. As a result, this kind of radar image is said to be represented in *complex* format.

Complex format radar imagery can be used to generate interferometric information (Massonnet and Rabaute, 1993; Zebker et al., 1994; Gens and Van Genderen, 1996; Kim and Van Zyl, 2000), which is useful in producing digital elevation models (DEM) (Zebker et al., 1994; Lanari et al., 1996; Kim and Van Zyl, 2000), or in monitoring large-scale surface changes (Massonnet et al., 1993; Preiss et al., 2003). The potential of SAR interferometry (in the form of coherence maps) in land cover classification is the subject of current investigations (e.g., Ichoku et al., 1998).

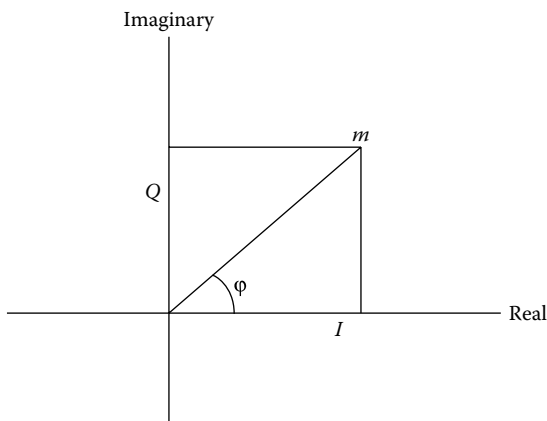


FIGURE 1.19 Wave described by complex (real and imaginary) coordinates.

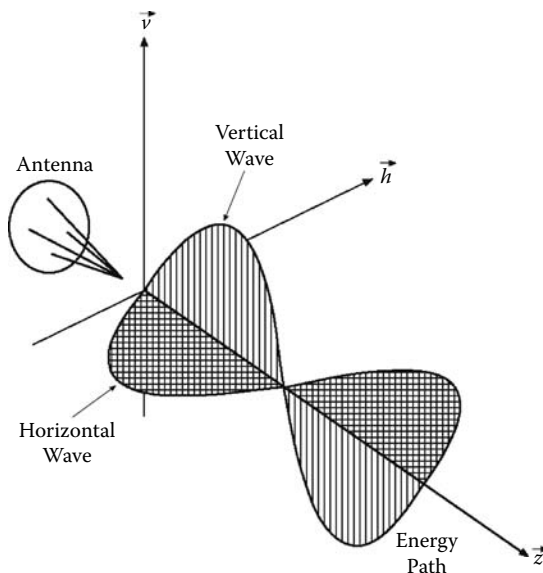


FIGURE 1.20 Polarized microwaves.

1.7.1 RADAR POLARIZATION STATE

Normally, microwave energy transmitted and received by a radar antenna can travel in all directions perpendicular to the direction of wave propagation. However, most radar systems polarize microwaves in such a way that the transmitted and received waves are restricted to a single plane perpendicular to the direction of wave propagation (Figure 1.20). The polarized wave is therefore transmitted and received in either the horizontal (H) or the vertical (V) plane. Consequently, there are four combinations of transmission and reception for the polarized waves. These combinations are HV, HH, VV, and VH, where HV denotes a wave transmitted in V direction and received in H direction. The other combinations can be inferred in a similar manner. Radar imagery generated in terms of HH or VV is called co- or like-polarized imagery, while imagery resulting from HV or VH polarization is called cross-polarized imagery. Cross-polarization detects multiple scattering from the target and thus generally results in weaker backscatter than that measured by a co-polarization configuration.

The coordinate system shown in Figure 1.20 determines the radar polarimetry, in which horizontally and vertically polarized waves lie in the unit vector \vec{h} and \vec{v} directions, respectively, while unit vector \vec{z} denotes the direction of wave propagation. The relationship among unit vectors \vec{h} , \vec{v} , and \vec{z} can be represented by

$$\vec{z} = \vec{h} \times \vec{v}. \quad (1.27)$$

The overall electric field can be represented by

$$\vec{E}(z, t) = \Re \left[(E_h \vec{h} + E_v \vec{v}) e^{-i(\omega t - kz)} \right] \quad (1.28)$$

where E_h and E_v denote the electric field of vertical and horizontal plane, respectively, which are expressed by

$$\begin{aligned} E_h &= a_h e^{-i\delta_h} \\ E_v &= a_v e^{-i\delta_v} \end{aligned} \quad (1.29)$$

The terms a_h and a_v denote the positive amplitudes in the \vec{h} and \vec{v} directions (Figure 1.21), respectively, and the corresponding phases are δ_h and δ_v relative to the phase factor $\omega t - kz$, where ω is frequency, t is time, k is wave number, and z is distance traveled in the \vec{z} direction (i.e., the direction of wave propagation).

In the most general case, the electric field vector of a plane monochromatic wave rotates in a plane perpendicular to the direction of microwave energy propagation, and in doing so traces out an ellipse, as shown in Figure 1.21. The wave is said to be *elliptically polarized*. If one refers to the relative amplitude and phase relationships of the components of a given wave as the elliptic polarization state, Equation (1.28) can be rewritten as

$$\vec{E}(z, t) = a\vec{p} \cos \chi \sin(\omega t - kz + \delta) + a\vec{q} \sin \chi \cos(\omega t - kz + \delta) \quad (1.30)$$

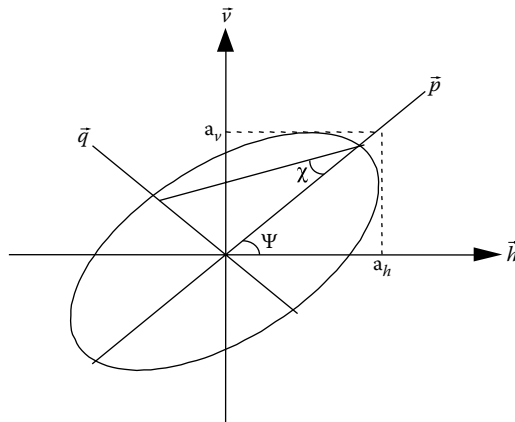


FIGURE 1.21 Elliptical polarization state for polarization synthesis. See text for explanation. Modified from Evans, D. L., T. G. Farr, J. J. Van Zyl, and H. A. Zebker. “Radar Polarimetry: Analysis Tools and Application.” *IEEE Transactions on Geoscience and Remote Sensing* 26 (1988):774–789 © 1988 IEEE.

where $a^2 = a_h^2 + a_v^2$ is the intensity of the wave, $\delta = \delta_h - \delta_v$ is the phase angle, both \vec{p} and \vec{q} are unit vectors in a coordinate system rotated by angle ψ with respect to \vec{h} , and χ is the ellipticity angle. Note that the width of the ellipse is given by the parameter χ ; so that $\chi = \pm 45^\circ$ results in left- and right-handed circular polarizations, respectively. The orientation parameter ψ determines the orientation of the major axis of the ellipse; if $\chi = 0^\circ$, then the values $\psi = 0^\circ$ or 180° represent horizontal polarizations, while $\psi = 90^\circ$ represents vertical polarization.

A polarimetric imaging radar measures the magnitude of the backscatter from a target as a vector quantity in such a way that the complex backscattered characteristics of any transmitting and receiving polarization configuration can be determined. Such backscattered characteristics are represented in terms of a scattering matrix $[\mathbf{S}]$ (Van de Hulst, 1981):

$$[\mathbf{S}] = \begin{pmatrix} \mathbf{S}_{hh} & \mathbf{S}_{hv} \\ \mathbf{S}_{vh} & \mathbf{S}_{vv} \end{pmatrix} \quad (1.31)$$

where element \mathbf{S}_{hv} is determined by measuring both the amplitude and phase of the electric field where a vertically polarized wave is transmitted and the scattered wave is received in horizontal polarization. The remaining elements are obtained in a similar fashion. The relationship among the electric field E_s of the scattered wave, the electric field E_t of the transmitting wave, and $[\mathbf{S}]$ is expressed as

$$E_s = \frac{e^{ikr}}{kr} [\mathbf{S}] E_t \Rightarrow \begin{pmatrix} E_h \\ E_v \end{pmatrix}_s = \frac{e^{ikr}}{kr} \begin{pmatrix} \mathbf{S}_{hh} & \mathbf{S}_{hv} \\ \mathbf{S}_{vh} & \mathbf{S}_{vv} \end{pmatrix} \begin{pmatrix} E_h \\ E_v \end{pmatrix}_t \quad (1.32)$$

where r is the distance between the scatterer and the receiving antenna and k denotes the wave number of the illuminating wave. The scattering matrix thus describes how the ground scatterer transforms the illuminating electric field.

1.7.2 POLARIZATION SYNTHESIS

Knowledge of the scattering matrix $[\mathbf{S}]$ permits calculation of the received power P_r for any possible combination of transmit and receive antenna polarizations. This process is called *polarization synthesis*. The observed power P_r can be derived by evaluating the matrix equation:

$$P_r = K(\lambda, \theta, \phi) |E_s[\mathbf{S}]E_t|^2 \quad (1.33)$$

where

$$K(\lambda, \theta, \phi) = \frac{1}{2} \frac{\lambda^2}{4\pi} \sqrt{\frac{\epsilon_0}{\mu_0}} \frac{g(\theta, \phi)}{|E_s|^2} \quad (1.34)$$

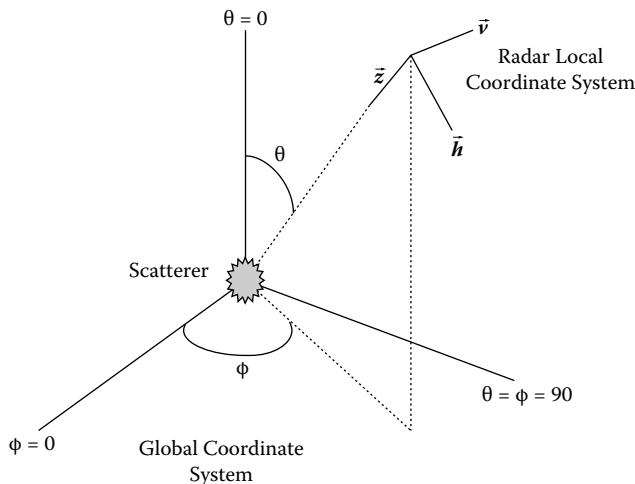


FIGURE 1.22 The local and global coordinate systems determine the angles θ and ϕ .

and $g(\theta, \phi)$ is the antenna gain function, θ and ϕ are the angles between the radar local coordinate system and the scatterer-centered global coordinate system shown in Figure 1.22, $[(\lambda^2/4\pi) \times g(\theta, \phi)]$ is the effective area of the antenna, and ϵ_0 and μ_0 are the permittivity and permeability of free space (i.e., transmission medium), respectively. Note that both permittivity ϵ_0 and permeability μ_0 determine the propagation velocity v (or phase velocity) of the wave; the relationship can be expressed as $v = 1/(\epsilon_0 \times \mu_0)^{0.5}$.

Polarization synthesis can also be expressed in terms of either the Stokes matrix or the covariance matrix. Both of these representations consist of linear combinations of the cross-products of the four basic elements of the scattering matrix. The entries of these matrices can also provide a variety of features for classification purposes.

1.7.3 POLARIZATION SIGNATURES

A particular graphical representation of the variation of received power (or cross-section σ) as a function of polarization is called the *polarization signature* of an object. A polarization signature is a three-dimensional representation consisting of a plot of synthesized scattering power as a function of the ellipticity and orientation angles (i.e., χ and ψ in Figure 1.21) of the transmitted and received wave. Normally, analyses are based on only two types of polarization signatures, namely, co-polarization and cross-polarization.

Figure 1.23 illustrates the polarization signature based on a theoretical model of a large conducting sphere. Note that at the ellipticity angle $\chi = 0^\circ$, the co-polarization signature reaches its highest value of cross-section, while the cross-polarization signature shows the lowest value at the same point. There is a measurement of surface roughness in accordance with polarization signature called the *coefficient of variation* (*CoV*), which is defined as

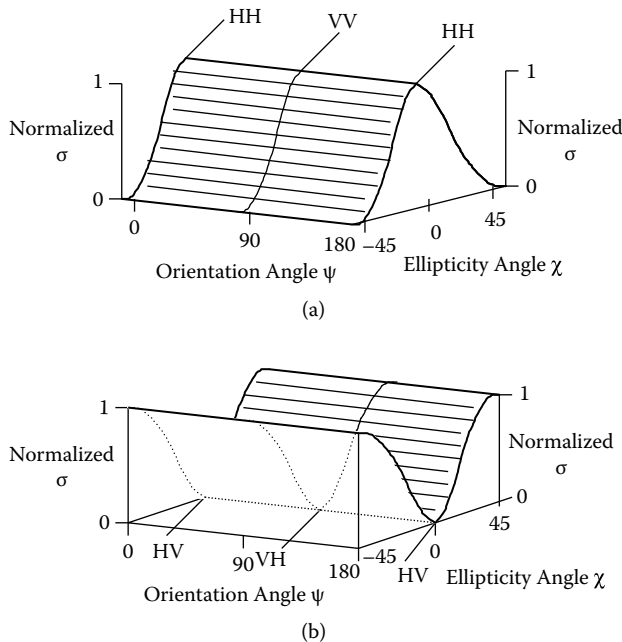


FIGURE 1.23 Polarization signature based on a theoretical model of a large conducting sphere. (a) At ellipticity angle 0 degrees the co-polarization signature reaches its highest cross-section value. (b) The cross-polarization value reaches its minimum point at the same ellipticity angle.

$$CoV = \frac{P_{r\min}}{P_{r\max}}. \quad (1.35)$$

$P_{r\min}$ and $P_{r\max}$ each denote minimal power and maximal power occurring within a polarization signature, respectively. Since CoV relates to the surface roughness, it can be used as a discriminating feature in classification. As the value of CoV increases, the measured surface tends to be rougher. The concept of CoV is based on the following observations. The polarization signature for each resolution element represents the sum of the polarization signatures of many individual measurements. If the surface being measured is smooth, the scattering mechanisms from a group of scatterers should be identical. Therefore, the maxima (minima) of a scattering mechanism should coincide with the maxima (minima) of the other scattering mechanisms. When the composite polarization signature is derived, it will produce a composite signature in which there is a large difference in magnitude between maximal and minimal backscatter, and thus the polarization signature will result in more peak- and valley-like shapes. As a result, the value of the CoV will be small (i.e., closer to 0). Conversely, if the measured ground surface is rough, several different scattering mechanisms may result, the backscatter maxima and minima may occur together from different individual scatterers, and a relatively flat polarization signature shape will be produced (equivalently, CoV will be large, i.e., close to 1).

1.8 RADAR SPECKLE SUPPRESSION

Due to random fluctuations in the signal observed from a spatially extensive target represented by a pixel (or image resolution element), *speckle noise* is generally present on a radar image. Speckle has the characteristics of a random multiplicative noise (defined below) in the sense that as the average grey level of a local area increases, the noise level increases. In a SAR imaging system, speckle effects are more serious (Lopez-Martinez and Fabregas, 2003). SAR can achieve high resolution in the azimuth direction independent of range, but the presence of speckle decreases the interpretability of the SAR imagery. If such imagery is to be used in classification, then some form of preprocessing to reduce or suppress speckle is necessary.

There are two approaches to the suppression of radar image speckle. The first method is known as the multilook process, while the second method uses filtering techniques to suppress the speckle noise.

1.8.1 MULTILOOK PROCESSING

Radar speckle can be suppressed by averaging several looks (images) to reduce the noise variance. This procedure is called *multilook processing*. As the radar sensor moves past the target pixel, it obtains multiple looks (i.e., returned samples). If these looks are spaced sufficiently far apart they can be considered to represent individual observations. The relationships among the radar aperture length L , the resolution R , and the number of independent samples N_s is expressed by (Ulaby et al., 1982, 1986a)

$$N_s \approx \frac{R}{0.5L}. \quad (1.36)$$

For instance, if radar aperture length is 10 m, and the desired spatial resolution is 25-m resolution, then the number of independent samples is $25/5 = 5$. Figure 1.24 illustrates the relationship between the resolution and number of samples. Although the averaging of independent looks can reduce the noise variance, it also causes degradation in image resolution.

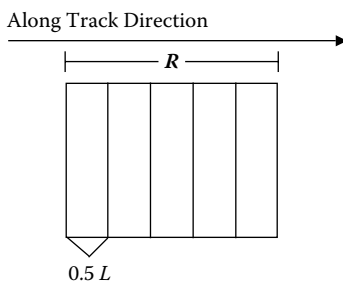


FIGURE 1.24 The relationship between resolution and number of looks in a SAR image. See text for explanation.

1.8.2 FILTERS FOR SPECKLE SUPPRESSION

The second method of speckle suppression uses filtering methods, which fall into two main categories, namely, adaptive and nonadaptive filters. *Adaptive filters* use weights that are dependent on the degree of speckle in the image, whereas *nonadaptive filters* use the same set of weights over the entire image. Adaptive filters are more likely to preserve details such as edges or high-texture areas (e.g., forest or urban areas) because the degree of smoothing is dependent on local image statistics.

The best-known nonadaptive filters are those based on the use of the mean or the median. The mean filter uses the same set of smoothing weights for the whole image without regard for differences in image texture, contrast, etc. The median filter does not use a weighting procedure, but is based on the ranking of image pixel values within a specified rectangular window (Mather, 2004). Both of these filters have a speckle-suppression capability, but they also smooth away other high-frequency information. The median is more effective than the mean in eliminating spike noise while retaining sharp edges. Both filters are easily implemented and require less computation than adaptive filters.

In comparison with nonadaptive speckle filters, adaptive speckle filters are more successful in preserving subtle image information. A number of adaptive speckle filters have been proposed, the best known being the Lee filter (Lee, 1980, 1981, 1986), the Kuan filter (Kuan et al., 1987), the Frost filter (Frost et al., 1982), and the Refined Gamma Maximum-A-Posteriori (RGMAP) filter (Touzi et al., 1988; Lopes et al., 1990; Baraldi and Parmiggiani, 1995). The effectiveness of these adaptive filters is dependent on the following three assumptions (Lee, 1980; Lopes et al., 1990; Baraldi and Parmiggiani, 1995a,b):

1. SAR speckle is modeled as a multiplicative noise (note that the visual effect of multiplicative noise is that the noise level is proportional to the image gray level).
2. The noise and signal are statistically independent.
3. The sample mean and variance of a pixel is equal to its local mean and local variance computed within a window centered on the pixel of interest.

All of the speckle filters described above rely strongly on a good estimate of local statistics (e.g., σ_z and μ_z) from a window. If the window center is located close to the boundary of an image segment (such as a boundary between agricultural fields), the resulting local statistics are likely to be biased and will thus degrade the filtering result. Nezry et al. (1991) notes this point, and proposes a refined GMAP filter called the RGMAP filter in which the local statistics extracted from a window do not cross image feature boundaries. Readers are referred to Sheng and Xia (1996) and Liu, Z. (2004) for comparisons of the above filters.

In recent years, the wavelet transform has been used for radar imagery denoising (Donoho, 1995; Fukuda and Hirose, 1998, 1999; Achim et al., 2003). The wavelet transform can decompose the multiplicative noise, and so simplify the speckle filtering process. Details of the wavelet transform are described in Chapter 7. Normally, using the wavelet transform for speckle suppression involves

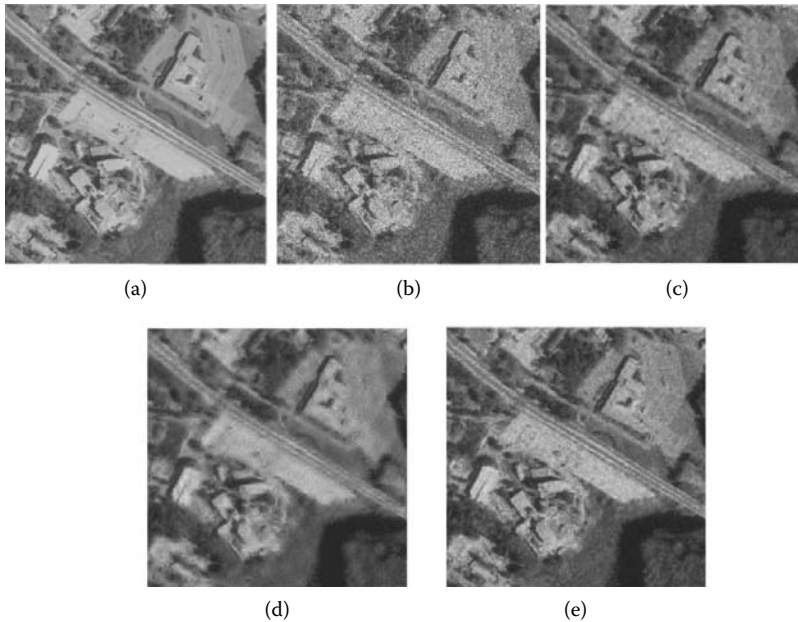


FIGURE 1.25 Calculation of median and mean filters for 3×3 window.

three steps as follows. First, the SAR image is translated into logarithmic domain and is then decomposed by means of the wavelet transform in a multiscale sense. Note that translating the raw SAR image into logarithmic domain is to convert the multiplicative noise to an additive noise. Second, the empirical wavelet coefficients are shrunk using a thresholding mechanism. Finally, the denoised signal is synthesized from the processed wavelet coefficients through the inverse wavelet transform. It is noted that the quality of wavelet transform for speckle suppression is closely related to the thresholding method used (Donoho, 1995). Some good estimators and modeling techniques proposed by Simoncelli (1999), Pizurica et al. (2001), and Achim et al. (2003) can be applied for solving such thresholding issues and so as to make the speckle suppression quality well controlled. Gagnon and Jouan (1997) and Achim et al. (2003) conducted comparative studies between wavelet-based filters and several statistical adaptive speckle filters described in the previous paragraph and show that, from the perspectives of both qualitative and quantitative measures, the wavelet-based approaches outperform other kinds of filters for speckle removal. Figure 1.25 illustrates the results of speckle suppression in terms of various filters. In Figure 1.25a, the original remotely sensed imagery is shown. The image contaminated by the noise is displayed in Figure 1.25b. The noisy image is then subjected to a GMAP filter (Figure 1.25c), and wavelet based filters developed by Donoho (1995) (Figure 1.25d) and Achim et al. (2003) (Figure 1.25e), respectively.

Further reading on the material covered in this chapter is provided in Elachi (1987), Liang (2004), Slater (1980), and contributors to Asrar (1989).

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