

**Subject : Computer Vision (CS 6643)**  
**Project 2 : Face Recognition**

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## 1. Code (Matlab Code)

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% Face Recognition using Eigenface Method %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

%closes all the previous open windows
close all;

%clears command window
clc

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% Training Process %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

% Providing path for Training and Testing folder

% The training Images are renamed in training folder as 1.jpg, 2.jpg, ...
% 8.jpg for the convenience of the program.

% The testing Images are renamed in testing folder as 1.jpg, 2.jpg, ...
% 18.jpg for the convenience of the program. (17 test faces and apple being the 18th image)

TrainDatabasePath = 'C:\Users\Hitarthi\Desktop\Project2\Face Dataset\training\';
TestDatabasePath = 'C:\Users\Hitarthi\Desktop\Project2\Face Dataset\testing\';

% Training images(8) are saved in I1, I2,... I8
I1 = strcat(TrainDatabasePath,'1','.jpg');
I2 = strcat(TrainDatabasePath,'2','.jpg');
I3 = strcat(TrainDatabasePath,'3','.jpg');
I4 = strcat(TrainDatabasePath,'4','.jpg');
I5 = strcat(TrainDatabasePath,'5','.jpg');
I6 = strcat(TrainDatabasePath,'6','.jpg');
I7 = strcat(TrainDatabasePath,'7','.jpg');
I8 = strcat(TrainDatabasePath,'8','.jpg');

% 1. We are reading the image and converting it into 2-D array of type double. This will
% create matrix for the image on with which we can work further.
% 2. Saving images after resizing in A, B...H
% 3. Plotting the images in figure window all together

% Figure(Name,Value): modifies properties of the figure using one or more name-value pair arguments
% Subplot : Create axes in tiled positions
% pcolor(C) : draws a pseudocolor plot. The elements of C are linearly mapped to an index into the
current colormap.
% flipud : Flip array up to down
% shading interp varies the color in each line segment and face by interpolating the colormap index or
% true color value across the line or face.

% 'Xtick' and 'Ytick' : Set or query x-axis and y-axis tick values. Here
% they are set to null.
```

```

figure('Name','Training Data')
A = imresize(double(imread(I1)),[195,231]);
subplot(3,3,1), pcolor(flipud(A)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('1.jpg');

B = imresize(double(imread(I2)),[195,231]);
subplot(3,3,2), pcolor(flipud(B)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('2.jpg');

C = imresize(double(imread(I3)),[195,231]);
subplot(3,3,3), pcolor(flipud(C)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('3.jpg');

D = imresize(double(imread(I4)),[195,231]);
subplot(3,3,4), pcolor(flipud(D)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('4.jpg');

E = imresize(double(imread(I5)),[195,231]);
subplot(3,3,5), pcolor(flipud(E)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('5.jpg');

F = imresize(double(imread(I6)),[195,231]);
subplot(3,3,6), pcolor(flipud(F)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('6.jpg');

G = imresize(double(imread(I7)),[195,231]);
subplot(3,3,7), pcolor(flipud(G)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('7.jpg');

H = imresize(double(imread(I8)),[195,231]);
subplot(3,3,8), pcolor(flipud(H)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('8.jpg');

% Number of Training images = n = 8, Each of dimension MxN (195x231)
% For each training image, the rows are stacked together to form a column
% vector Ri of dimension MN x 1

% MN * 1 (Column Vector)
% reshape : Reshape array returned as a vector, matrix, multidimensional array, or cell array.
% The data type and number of elements in the reshaped array are the same as the data type and number of
elements in original array.

% A,B .. H are reshaped in vector R1,R2, ... R8

R1= reshape(A,195*231,1);
R2= reshape(B,195*231,1);
R3= reshape(C,195*231,1);
R4= reshape(D,195*231,1);
R5= reshape(E,195*231,1);
R6= reshape(F,195*231,1);
R7= reshape(G,195*231,1);
R8= reshape(H,195*231,1);

```

```

% Generating mean face : By taking the average of n training face images
Avg_face = (R1+R2+R3+R4+R5+R6+R7+R8)/8;

% reshaping the Avg_face into original dimensions to plot it as figure on screen.
Show_Avg_face = reshape(Avg_face,195,231);
figure('Name','Mean Image'),subplot(1,1,1), pcolor(flipud(Show_Avg_face)), shading interp,
colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);

% Subtract mean face from each training images and save that value
% reshape to plot the output after subtraction process.
% All training images after subtracting the average face is then plotted
% altogether.

figure('Name','Original Image - Mean Image')
s1 = R1-Avg_face;
sr1 = reshape(s1,195,231);
subplot(3,3,1), pcolor(flipud(sr1)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('1.jpg');

s2 = R2-Avg_face;
sr2 = reshape(s2,195,231);
subplot(3,3,2), pcolor(flipud(sr2)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('2.jpg');

s3 = R3-Avg_face;
sr3 = reshape(s3,195,231);
subplot(3,3,3), pcolor(flipud(sr3)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('3.jpg');

s4 = R4-Avg_face;
sr4 = reshape(s4,195,231);
subplot(3,3,4), pcolor(flipud(sr4)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('4.jpg');

s5 = R5-Avg_face;
sr5 = reshape(s5,195,231);
subplot(3,3,5), pcolor(flipud(sr5)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('5.jpg');

s6 = R6-Avg_face;
sr6 = reshape(s6,195,231);
subplot(3,3,6), pcolor(flipud(sr6)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('6.jpg');

s7 = R7-Avg_face;
sr7 = reshape(s7,195,231);
subplot(3,3,7), pcolor(flipud(sr7)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('7.jpg');

s8 = R8-Avg_face;
sr8 = reshape(s8,195,231);

```

```
subplot(3,3,8), pcolor(flipud(sr8)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick', []);
title('8.jpg');
```

```
% Creating data matrix by putting all training faces into a single matrix 'Data'
% Data is a 8x45045 vector, where each row represent one training image.
```

```
Data = [reshape(s1,1,195*231)
        reshape(s2,1,195*231)
        reshape(s3,1,195*231)
        reshape(s4,1,195*231)
        reshape(s5,1,195*231)
        reshape(s6,1,195*231)
        reshape(s7,1,195*231)
        reshape(s8,1,195*231)];
```

```
% Covariance matrix
L = (Data)*(Data');
```

```
% L is of nxn dimension
size(L)
```

```
% eigs : returns subset of eigenvalues and eigenvectors of covariance matrix
% eigs of L will grab largest magnitude of 8 eigenvectors possible.
```

```
%%%%%%%%%% Di %%%%%%%%%%
```

```
% is diagonal matrix, the elements of this eigenvalues are arranged from
% largest to smallest, largest being the most important and smallest being
% the least.
```

```
%%%%%%%%%% V %%%%%%%%%%
```

```
% are the eigenvectors, the first eigenvector of this has dominant average face,
% second eigenvector tells about the feature space.
```

```
[V,Di] = eigs(L,8,'largestabs');
```

```
% Eigenfaces/ Facespace/ Eigenspace can be found as follows:
% U is dimension of MN x n
```

```
u = V*Data;
U = u';
```

```
% Each column of U represents an eigenface. we can output each eigenface as
% an MxN image
% Eigen faces of Training images are combined and plotted in figure to
% display.
```

```

figure('Name','EigenFaces')
subplot(3,3,1), face1=reshape(U(:,1),195,231); pcolor(flipud(face1)), shading interp, colormap(gray),
set(gca, 'Xtick', [], 'Ytick', []); title('1.jpg');
subplot(3,3,2), face1=reshape(U(:,2),195,231); pcolor(flipud(face1)), shading interp, colormap(gray),
set(gca, 'Xtick', [], 'Ytick', []); title('2.jpg');
subplot(3,3,3), face1=reshape(U(:,3),195,231); pcolor(flipud(face1)), shading interp, colormap(gray),
set(gca, 'Xtick', [], 'Ytick', []); title('3.jpg');
subplot(3,3,4), face1=reshape(U(:,4),195,231); pcolor(flipud(face1)), shading interp, colormap(gray),
set(gca, 'Xtick', [], 'Ytick', []); title('4.jpg');
subplot(3,3,5), face1=reshape(U(:,5),195,231); pcolor(flipud(face1)), shading interp, colormap(gray),
set(gca, 'Xtick', [], 'Ytick', []); title('5.jpg');
subplot(3,3,6), face1=reshape(U(:,6),195,231); pcolor(flipud(face1)), shading interp, colormap(gray),
set(gca, 'Xtick', [], 'Ytick', []); title('6.jpg');
subplot(3,3,7), face1=reshape(U(:,7),195,231); pcolor(flipud(face1)), shading interp, colormap(gray),
set(gca, 'Xtick', [], 'Ytick', []); title('7.jpg');
subplot(3,3,8), face1=reshape(U(:,8),195,231); pcolor(flipud(face1)), shading interp, colormap(gray),
set(gca, 'Xtick', [], 'Ytick', []); title('8.jpg');

```

```

% Each training face then can be projected onto the face space
% generating PCA coefficients of training faces
%  $\Omega_i = u \cdot s_i$  for  $i = 1$  to  $8$  as face1 to face8

```

```

face1 = u*s1;
face2 = u*s2;
face3 = u*s3;
face4 = u*s4;
face5 = u*s5;
face6 = u*s6;
face7 = u*s7;
face8 = u*s8;

```

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% Testing Process %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

```

```

%Extracting the PCA features from test image

```

```

% Enter the number of test image that needs to be recognised into Test 1.
% Test image path is stored in Test1, and it is then being read and
% converted into matrix form.

```

```

Test1 = strcat(TestDatabasePath,'18','.jpg');
T1 = imresize( double( imread(Test1)), [195,231]);

```

```

% reshaping the test image to show at the end as the input of the program.
input1 = reshape(T1,195*231,1);

```

```

%subtract mean face from Input face
figure('Name','Test Image - Mean Image');
Diff = input1-Avg_face;

```

```

% reshaping the test image after subtracting the mean to display.
Difference = reshape(Diff,195,231);

% plotting it as figure.
subplot(1,1,1), pcolor(flipud(Difference)), shading interp, colormap(gray), set(gca, 'Xtick', [],
'Ytick', []);

%Compute its projection onto face space
%Test image feature vector
%PCA coefficients of each test image are stored in variable ProjectedTestImage.
ProjectedTestImage = u*Diff;

%Reconstruct input face image from eigenfaces.
figure('Name','Reconstructed Image');
Recon = U*ProjectedTestImage;

%plotting the reconstructed face.
Reconstruction = reshape(Recon,195,231);
subplot(1,1,1), pcolor(flipud(Reconstruction)), shading interp, colormap(gray), set(gca, 'Xtick', [],
'Ytick', []);

% Computing distance between input face image and its reconstruction
% n = norm(v) returns the Euclidean norm of vector v.
distance = norm( Recon - input1 );

% concatenating all projected training faces into single array.
% C = horzcat(A1,...,AN) horizontally concatenates arrays A1,...,AN.
% All arrays in the argument list must have the same number of rows.
ProjectedImages = horzcat(face1,face2,face3,face4,face5,face6,face7,face8);

% Calculating Euclidean distances
% Euclidean distances between the projected test image and the projection
% of all centered training images are calculated. Test image is
% supposed to have minimum distance with its corresponding image in the
% training database.
% Euc_dist will have Euclidean distances between all training image and
% test image.

Euc_dist = [];
for i = 1 : 8
    q = ProjectedImages(:,i);
    temp = norm( ProjectedTestImage - q );
    Euc_dist = [Euc_dist temp];
End

% Minimum Euclidean distance is generated in Euc_dist_min
% Whichever distance is minimum between the projected test image and the projection
% of all centered training images, that training image's index is noted.
[Euc_dist_min , Recognized_index] = min(Euc_dist);

```

```
% The recognised output image name is saved and it is showed as Equivalent
% image compared to the test image.
figure('Name','Test Image');
input1 = imresize(double(imread(Test1)),[231,195]);
subplot(1,1,1), pcolor(flipud(input1)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick',
[]);

% the fetched recognized index is then saved in OutputName
% the training image at that index is fetched.
OutputName = strcat(int2str(Recognized_index),'.jpg');
SelectedImage = strcat(TrainDatabasePath,OutputName);
figure('Name','Equivalent Image');

%output is then plotted into figure window.
output1 = imresize(double(imread(SelectedImage)),[231,195]);
subplot(1,1,1), pcolor(flipud(output1)), shading interp, colormap(gray), set(gca, 'Xtick', [], 'Ytick',
[]); title('Matched Training Image');
```

## 2. Language & Compiler

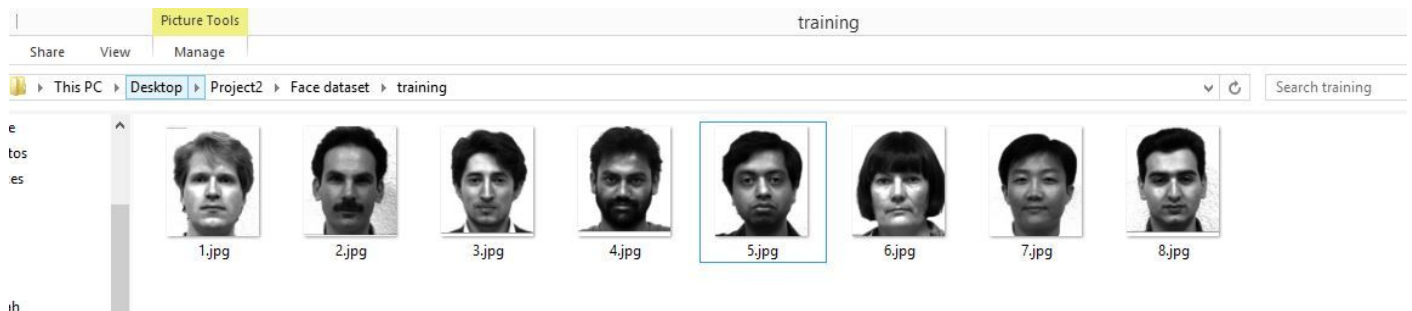
- Language Used : Matlab
- File extension : \*.m
- Compiler : MATLAB Compiler ([www.mathworks.com/help/compiler/index.html](http://www.mathworks.com/help/compiler/index.html))

## 3. Instructions on executing the program

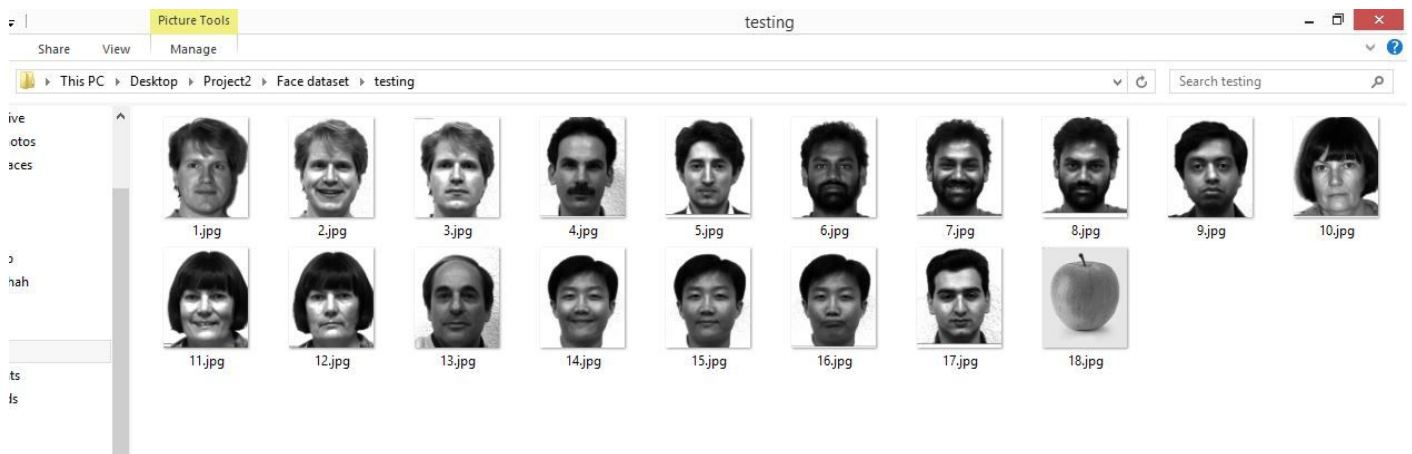
- Load the above mentioned code in Matlab R2017b under the file name Face\_Recognition.m
- Rename the strings which specify the name of the training and testing folders based on the system path where the training and testing folders are located.
- Rename the files to be named 1.jpg through 8.jpg in the training folder, as I have renamed those files for the sake of simplicity.
- Rename the files in testing folder from 1.jpg to 18.jpg, for the sake of simplicity, or simply pass the name of the file on which testing has to be done. If more number of images have to be tested, rename them accordingly or pass the correct name of image to be tested in the "Test1" variable.
- Click on "Compiler & Run" button available in Matlab R2017b and the output would be shown in several new windows.
- The workspace in matlab shows calculated variables for each test image incase we want to varify with the values written here.
- Following images show how the training and testing folders should look for my project :



## 1. Training Images Data Folder :



## 2. Testing Images Data Folder :



- Hence, it is not necessary to rename all the names of files in testing data folder, but it is necessary that training folder contains only 8 images labelled from 1.jpg to 8.jpg.

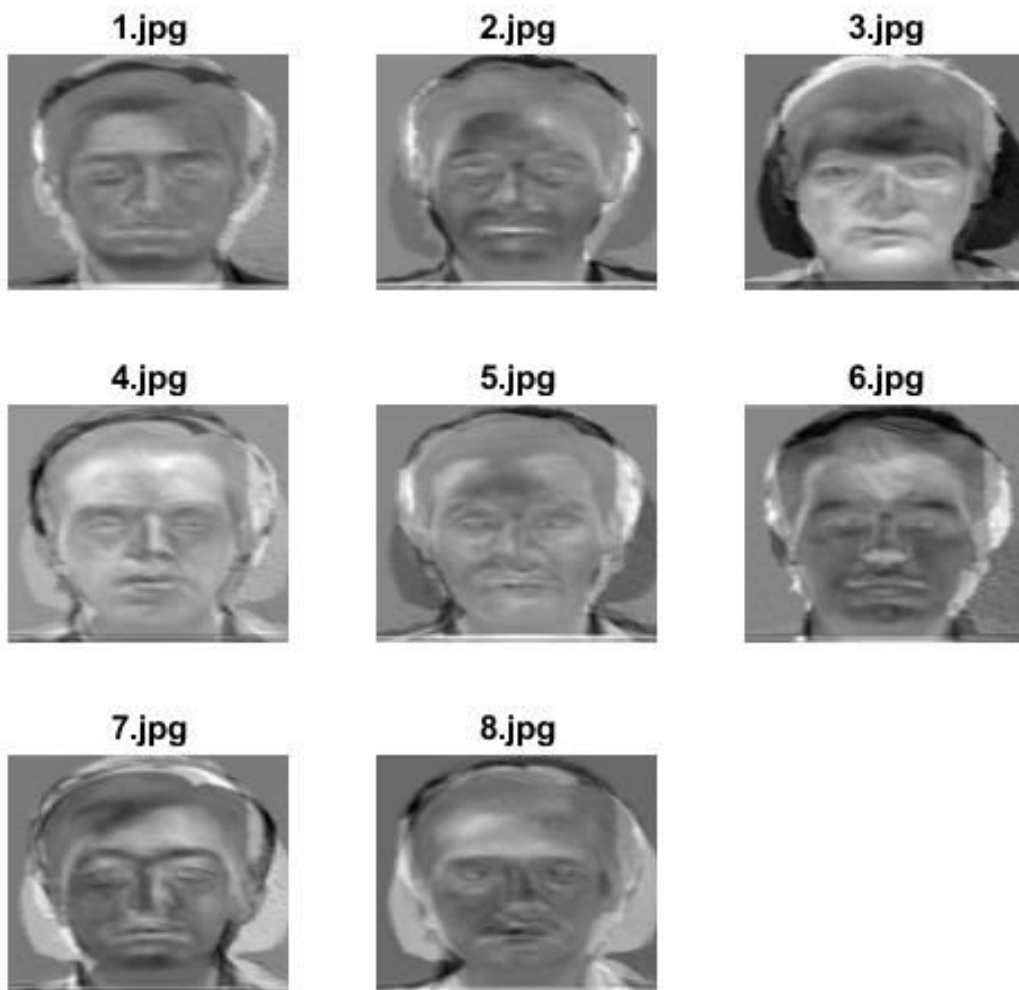
#### 4. Mean Face m

- The Mean Face obtained from all the given 8 training faces is as shown below :



## 5. Eigenfaces

- The Eigenfaces for each training image that is generated is as shown below :



## 6. The PCA coefficients for each Training Image

- The PCA coefficients value for each training image is as shown below :

### 1. Subject 1 :

- 45465159.8438012
- 37182030.8693160
- 62268936.6416469
- 31921622.1793352
- 18331989.4172045
- 109476571.345616
- 1916801.24769890
- 32086661.5608897

### 2. Subject 2 :

- 25267233.4301786
- 15523403.4051443
- 67343593.4575588
- 46331455.2159492
- 12016135.7995268
- 81262009.6416997
- 31247363.3525023
- 33337381.5254491

### 3. Subject 3 :

- 71586685.9304944
- 22442864.8689439
- 26838795.5499260
- 16755510.6000549
- 31062301.5610203
- 3827511.81158293
- 4972939.14625926
- 61771946.8204623

### 4. Subject 7 :

- 61865388.9085934
- 46023684.4636647
- 132252772.887412
- 18013810.3684925
- 40637176.8453830
- 69543453.3871319
- 8126320.95479954
- 48256194.5426077

### 5. Subject 10 :

- 7530637.97909631
- 9406385.35416027
- 8238308.84402016
- 19201251.1233737
- 63750362.6256691
- 15863694.2726755

- g. 57024391.4109556
  - h. -63610031.0083028
6. Subject 11 :
- a. -81368179.4896583
  - b. 6578144.48610068
  - c. 206524843.478925
  - d. -70935738.0160370
  - e. 37942936.8305273
  - f. -56452086.1575121
  - g. -106905439.936225
  - h. -189272341.418878
7. Subject 14 :
- a. -51065463.3673782
  - b. -16734846.8750620
  - c. 20021464.2458230
  - d. -48809504.5604108
  - e. -38905357.1684611
  - f. -49610979.5756523
  - g. 53615384.4916647
  - h. -9447723.55515200
8. Subject 15 :
- a. 77244599.2710244
  - b. 17640895.6125729
  - c. -54141773.6274766
  - d. 57060235.0263369
  - e. 61453761.2969176
  - f. 76770356.5110417
  - g. 26276446.8252656
  - h. 86877911.5329249

## 7. Testing Images result.

### 1. Subject 01 - Center Light

#### a. Test Image after Subtracting Mean Face



#### b. Reconstructed Face Image



#### c. PCA Coefficients

- i. -30244591.1247202
- ii. -7589079.13167136
- iii. 29154658.9302855
- iv. 14471650.2451715
- v. -767515.219443414
- vi. -22074378.6219023
- vii. -15179729.7018291
- viii. -8335337.20038529

#### d. Distances $d_i$

- i. 110751806.826435
- ii. 154021219.431589
- iii. 145974444.031279
- iv. 228736070.982650
- v. 119222346.821205

- vi. 292234609.749850
- vii. 107479477.613849
- viii. 212998843.023769

e. Classification Result : Subject 01 - Normal

2. Subject 01 - Happy

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. -31654282.9601907
- ii. -23408549.4378143
- iii. 26356877.2589447
- iv. 31260371.2124790
- v. -8972438.45365907
- vi. -63761227.3184477
- vii. -6421151.04815534
- viii. 37450542.4226739

d. Distances  $d_i$

- i. 62426890.2939423
- ii. 180745471.746671
- iii. 146440303.382916
- iv. 248417739.118140
- v. 147151728.272609
- vi. 331707775.711178
- vii. 117357133.487273
- viii. 221158003.803358

e. Classification Result : Subject 01 - Normal

3. Subject 01 - Normal

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. -45465159.8438012
- ii. -37182030.8693160
- iii. 62268936.6416469
- iv. 31921622.1793352



- v. -18331989.4172045
- vi. -109476571.345616
- vii. -1916801.24769890
- viii. 32086661.5608897

d. Distances  $d_i$

- i. 0
- ii. 241571793.542559
- iii. 195239496.651352
- iv. 307673740.489579
- v. 175504172.252824
- vi. 317165995.620829
- vii. 132543939.204745
- viii. 277663944.426984

e. Classification Result : Subject 01 - Normal

4. Subject 02 - Normal

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. -25267233.4301786
- ii. 15523403.4051443
- iii. -67343593.4575588
- iv. 46331455.2159492
- v. 12016135.7995268
- vi. 81262009.6416997
- vii. -31247363.3525023
- viii. 33337381.5254491

d. Distances  $d_i$

- i. 241571793.542559
- ii. 0
- iii. 160603381.726869
- iv. 140018649.995924
- v. 193727210.168367
- vi. 408533295.656098
- vii. 217125742.036521
- viii. 139435953.876930

e. Classification Result : Subject 02 - Normal

5. Subject 03 - Normal

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. 71586685.9304944
- ii. -22442864.8689439
- iii. -26838795.5499260
- iv. -16755510.6000549
- v. -31062301.5610203
- vi. 3827511.81158293
- vii. -4972939.14625926
- viii. 61771946.8204623

d. Distances  $d_i$

- i. 195239496.651352
- ii. 160603381.726869

- iii. 0
- iv. 160341910.570695
- v. 170554770.832653
- vi. 404277524.894721
- vii. 172399224.684626
- viii. 152707730.057506

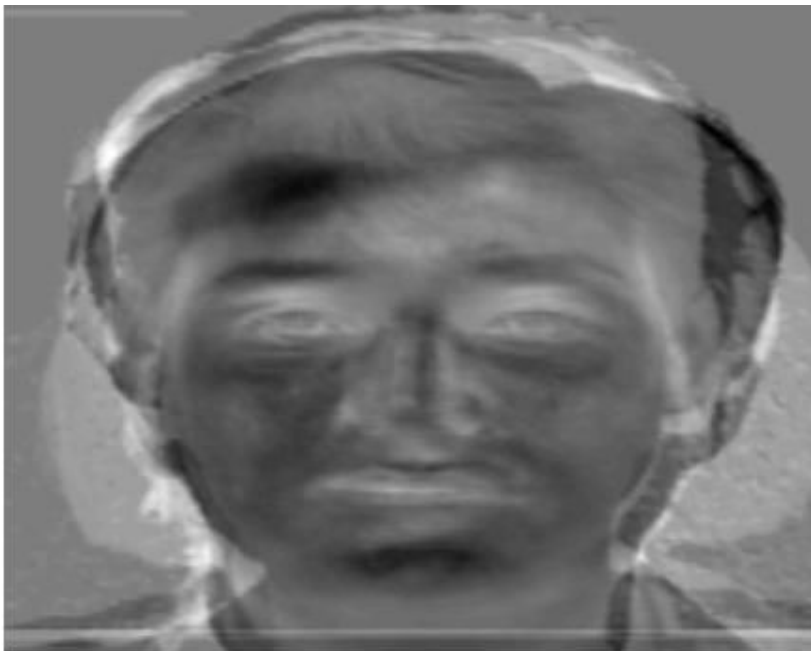
e. Classification Result : Subject 03 - Normal

6. Subject 07 - Center Light

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. -17396008.4957121
- ii. 10415928.9257975
- iii. -34114389.1200964

- iv. -30899541.5605468
- v. -20257474.0948151
- vi. 6893643.66420389
- vii. 33645103.5418783
- viii. -24673420.1784695

d. Distances  $d_i$

- i. 185261376.213672
- ii. 145963606.728741
- iii. 135428609.489862
- iv. 175927712.283431
- v. 90233525.8302830
- vi. 343314045.747584
- vii. 96402303.7159470
- viii. 202989016.711296

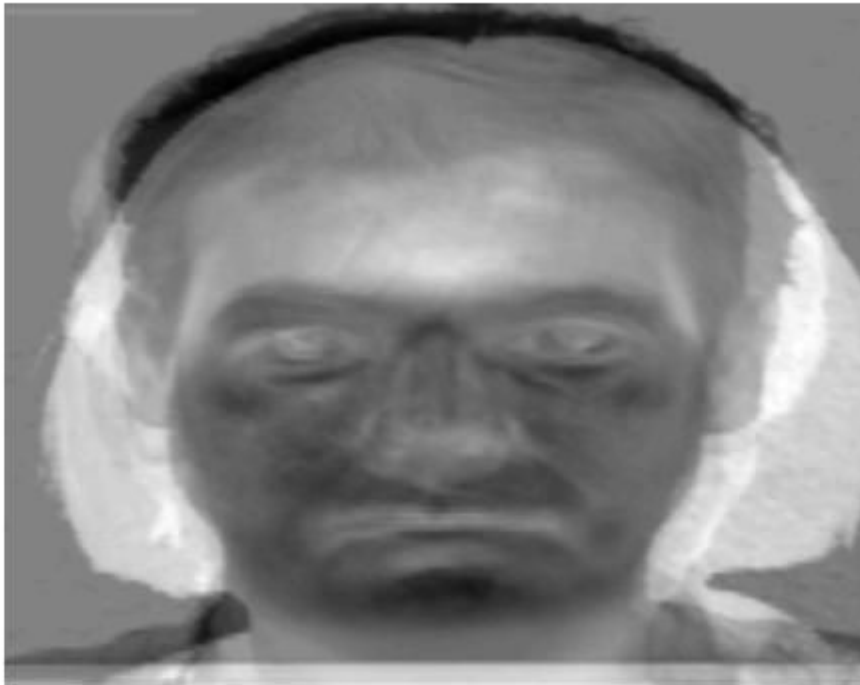
e. Classification Result : Subject 10 - Normal

7. Subject 07 - Happy

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. 31915486.7078409
- ii. 15597306.3954348
- iii. -77502296.4177258
- iv. 6695118.58574729
- v. 5387421.55526371
- vi. 44799260.9352116
- vii. 25560694.7148933
- viii. 38945469.0419249

d. Distances  $d_i$

- i. 232618778.013750
- ii. 97857985.7450390
- iii. 102947551.855411
- iv. 87614920.3833202
- v. 164628997.494131
- vi. 424917454.462808
- vii. 185814326.045243
- viii. 107725950.589187

e. Classification Result : Subject 07 - Normal

8. Subject 07 - Normal

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. 61865388.9085934
- ii. 46023684.4636647
- iii. -132252772.887412
- iv. -18013810.3684925
- v. 40637176.8453830
- vi. 69543453.3871319
- vii. 8126320.95479954
- viii. 48256194.5426077

d. Distances  $d_i$

- i. 307673740.489579

- ii. 140018649.995924
- iii. 160341910.570695
- iv. 0
- v. 240310345.726450
- vi. 474528245.567224
- vii. 258363347.640803
- viii. 122825753.492712

e. Classification Result : Subject 07 - Normal

9. Subject 10 - Normal

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. -7530637.97909631



- ii. -9406385.35416027
- iii. -8238308.84402016
- iv. 19201251.1233738
- v. -63750362.6256691
- vi. -15863694.2726755
- vii. 57024391.4109556
- viii. -63610031.0083028

d. Distances  $d_i$

- i. 175504172.252824
- ii. 193727210.168367
- iii. 170554770.832653
- iv. 240310345.726450
- v. 0
- vi. 338538515.845197
- vii. 109883554.146810
- viii. 243532387.903863

e. Classification Result : Subject 10 - Normal

10. Subject 11 - Center Light

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. -60295049.3995911
- ii. 22773625.0467066
- iii. 119315389.044649
- iv. -46841435.5826537
- v. 52401519.6896027
- vi. 9708821.91151891
- vii. -102589887.700900
- viii. -128885741.236968

d. Distances  $d_i$

- i. 261778714.519141
- ii. 288026408.822973
- iii. 307544717.979845
- iv. 356282524.383544
- v. 261407858.118308
- vi. 130934627.208750
- vii. 249059376.751693
- viii. 357163999.917770

e. Classification Result : Subject 11 - Normal

11. Subject 11 - Happy

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. -82408597.4968826
- ii. 9695052.39353175
- iii. 193904184.373891
- iv. -69333430.2555289
- v. 42651261.5978256
- vi. -44403780.9053276
- vii. -108182248.026654
- viii. -178304729.018654

d. Distances  $d_i$

- i. 307657293.069981
- ii. 390345531.033459
- iii. 390241223.574648
- iv. 457156844.923547
- v. 327498856.127994
- vi. 21491736.8577676
- vii. 306116191.474248
- viii. 454414034.347091

e. Classification Result : Subject 11 - Normal

12. Subject 11 - Normal

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. -81368179.4896583
- ii. 6578144.48610068
- iii. 206524843.478925
- iv. -70935738.0160370
- v. 37942936.8305273
- vi. -56452086.1575121
- vii. -106905439.936225
- viii. -189272341.418878

d. Distances  $d_i$

- i. 317165995.620829
- ii. 408533295.656098
- iii. 404277524.894721
- iv. 474528245.567224
- v. 338538515.845197
- vi. 0
- vii. 317476172.550880
- viii. 471070915.788474

e. Classification Result : Subject 11 - Normal

13. Subject 12 - Normal

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. -60821390.3761192
- ii. -6794875.13983478
- iii. 43357854.8079859
- iv. -1861388.33550452
- v. -11865537.2160805
- vi. -39856812.9913125
- vii. 1747453.75911826
- viii. -40597168.6930999

d. Distances  $d_i$

- i. 113327867.568314
- ii. 195280935.130114
- iii. 189017455.119664
- iv. 267586252.859595
- v. 113160769.186822
- vi. 262033939.870862
- vii. 86194893.6487806
- viii. 261660932.151127

e. Classification Result : Subject 11 - Normal

14. Subject 14 - Happy

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. -37778699.0284510
- ii. -16029768.8088801
- iii. 10471391.9563193
- iv. -36277242.4491295
- v. -31329695.9750712
- vi. -54304310.7913392
- vii. 39106199.6044730
- viii. 7075009.15197863

d. Distances  $d_i$

- i. 115593938.888483
- ii. 199819750.586563
- iii. 148624254.738784
- iv. 240117591.801279
- v. 110602656.763863
- vi. 326686882.613490
- vii. 31436155.2779180
- viii. 244076346.250688

e. Classification Result : Subject 14 - Normal

15. Subject 14 - Normal



a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. -51065463.3673782
- ii. -16734846.8750620
- iii. 20021464.2458230
- iv. -48809504.5604108
- v. -38905357.1684611
- vi. -49610979.5756523
- vii. 53615384.4916647
- viii. -9447723.55515200

d. Distances  $d_i$

- i. 132543939.204745
- ii. 217125742.036521
- iii. 172399224.684626
- iv. 258363347.640803
- v. 109883554.146810
- vi. 317476172.550880
- vii. 0
- viii. 265375190.467984

e. Classification Result : Subject 14 - Normal

16. Subject 14 - Sad

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. -38425827.4832853
- ii. -12497776.7863330
- iii. 1380150.50814328
- iv. -43343218.0173024
- v. -37314159.1507082
- vi. -36435897.1531181
- vii. 43988609.8507837
- viii. -3620540.41662508

d. Distances  $d_i$

- i. 138234145.354257
- ii. 192445966.605726
- iii. 148453735.146490
- iv. 230798092.580242
- v. 99293271.5935073
- vi. 329170947.041930
- vii. 29288864.5383487
- viii. 241921419.359326

e. Classification Result : Subject 14 - Normal

17. Subject 15 - Normal

a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



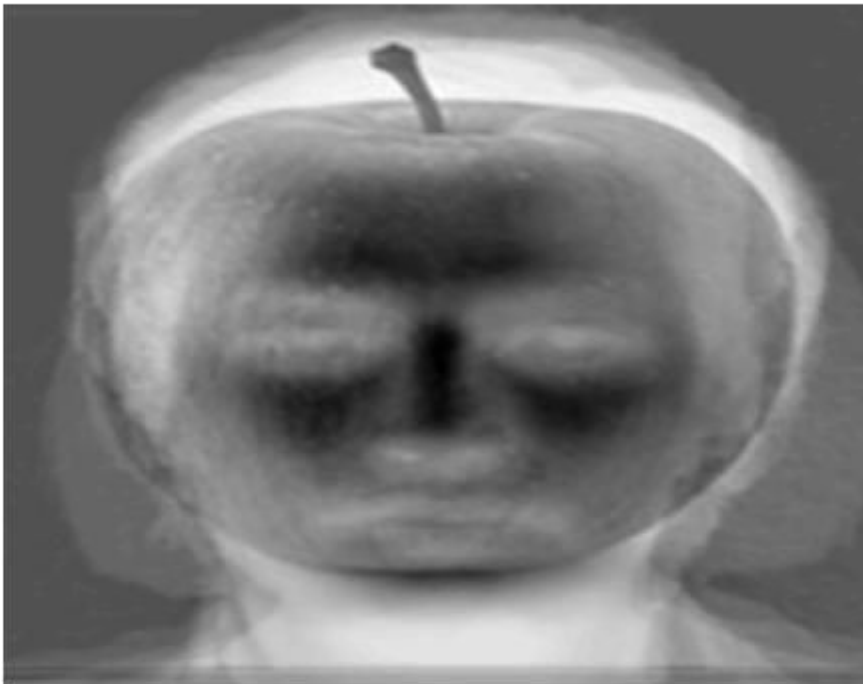
c. PCA Coefficients

- i. 77244599.2710244
- ii. 17640895.6125729
- iii. -54141773.6274766
- iv. 57060235.0263369
- v. 61453761.2969176
- vi. 76770356.5110417
- vii. 26276446.8252656
- viii. 86877911.5329249

- d. Distances  $d_i$
- i. 277663944.426984
  - ii. 139435953.876930
  - iii. 152707730.057506
  - iv. 122825753.492711
  - v. 243532387.903863
  - vi. 471070915.788474
  - vii. 265375190.467984
  - viii. 0
- e. Classification Result : Subject 15 - Normal

18. Apple

- a. Test Image after Subtracting Mean Face



b. Reconstructed Face Image



c. PCA Coefficients

- i. -22220126.8239289
- ii. -4924421.59330461
- iii. 18942914.3514933
- iv. -2786227.22914090
- v. 22107423.0506407
- vi. -52091944.5531915
- vii. -19572059.6835171
- viii. 33874108.7029032

d. Distances  $d_i$

- i. 99528430.7367422
- ii. 168246897.546787
- iii. 135436880.947719
- iv. 221067105.390168
- v. 159725879.166500
- vi. 318046174.251508
- vii. 118544264.239992
- viii. 205889561.589982

e. Classification Result : Non Face Image

**Threshold :**

$T_0 = 9.0000e+10$ ;

When I apply this threshold I am getting apple as a non face image, as it is satisfying the condition  $d_0 > t_0$ .