The necklace problem

Define:

 $\forall k \in \mathbb{N}, \forall F[\![k]\!]$