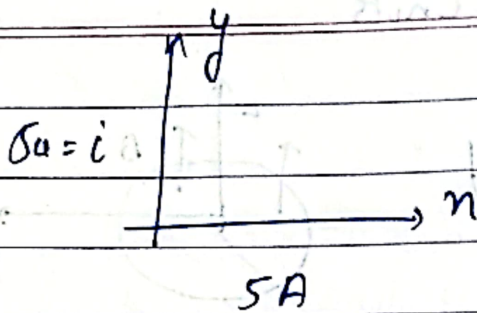
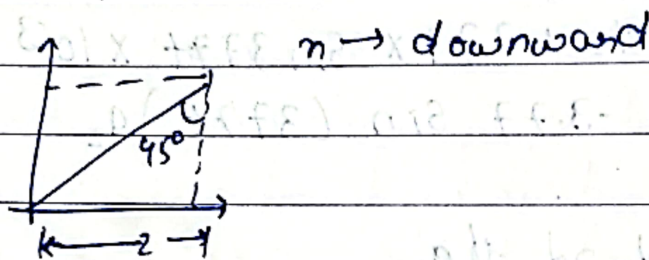


# Assignment - 3

Ans-1-



(a) (2, 2, 0)



$$B = \left( \frac{\mu_0}{4\pi} \right) \times \frac{5}{2} \left[ \sin 45^\circ + \sin 90^\circ \right] \times 2$$

$$B = 10^{-7} \times 5 \left[ \frac{1}{\sqrt{2}} + 1 \right] \left[ \frac{\mu_0}{4\pi} = 10^{-7} \right]$$

$$B = 8.52 \times 10^{-7}$$

$$\vec{H} = \frac{B}{\mu} = \frac{8.52 \times 10^{-7}}{\frac{\mu_0}{4\pi}} \times \frac{1}{9\pi} = \frac{8.52}{9\pi}$$

$$\vec{H} = 6.69 a_z \text{ A/m}$$

Similarly (b)  $0.1989 a_z \text{ A/m}$

$$(c) 0.1989 a_x + 0.1989 a_y \text{ A/m}$$

Ans-2: (a)  $\vec{J} = \nabla \times \vec{H}$

$$\vec{J} = \begin{vmatrix} a_n & a_y & a_z \\ d/dn & d/dy & d/dz \\ A_n & A_y & A_z \end{vmatrix} = \begin{vmatrix} a_n & a_y & a_z \\ d/dn & d/dy & d/dz \\ yz(n^2+y^2) & 4n^2y^2 & (-n^2yz) \end{vmatrix}$$

$$\begin{aligned} \vec{J} = & \left[ \frac{d(4n^2y^2)}{dy} - \frac{d(-ny^2z)}{dz} \right] a_n \\ & - \frac{d(4n^2y^2)}{dn} - \frac{d}{dz} y^2(n^2+y^2) n y \\ & + \frac{d}{dn} (-ny^2z) - \frac{d}{dy} (yz(n^2+y^2)) a_z \end{aligned}$$

$$\begin{aligned} \vec{J} = & (8n^2y + ny^2) a_n - (8ny^2 - y(n^2+y^2)) a_y \\ & - (y^2z + (n^2z + 3yz^2)) a_z \end{aligned}$$

(b)  $\vec{I} = \int \vec{J} \cdot d\vec{s}$

$$\vec{I} = \int_0^2 \int_0^2 (8n^2y + ny^2) a_n - (8n^2 - y(n^2+y^2)) a_y - y^2z + (n^2z + 3yz^2) a_z$$

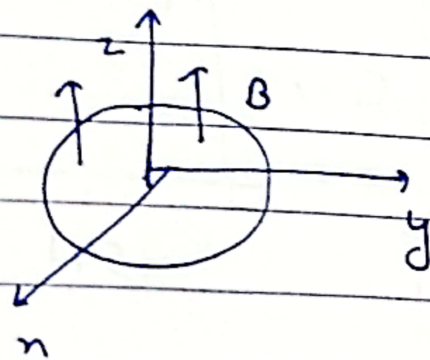
$$\vec{I} = \int_0^2 \int_0^2 (8n^2y - ny^2) dy dz$$

$$\vec{I} = \int_0^2 \int_0^2 (8y + y^2) dy dz$$

$$I = (16 + \frac{8}{3})(2) = 37.33 \text{ A}$$



Ans-3. Transformer  $V_{emf}$



$$\Rightarrow - \int \frac{dB}{dt} dS$$

$$\frac{dB}{dt} = -10 \times 377 \times \sin 377t \times 10^{-3} a_z$$

$$\Rightarrow -3.77 \sin(377t) a_z$$

$$dS = \rho d\rho d\phi a_z$$

$$V_{emf} = - \int \frac{dB}{dt} \cdot dS = - \int_{\phi=0}^{2\pi} \int_{\rho=0}^{0.2} -3.77 \sin(377t) \rho d\rho d\phi$$

$$V_{emf} = 3.77 \sin(377t) \int_{\phi=0}^{2\pi} \int_{\rho=0}^{0.2} \rho d\rho d\phi = 0.473 \sin(377t) V$$

It is the voltage induced.

Ans-4. Transformer = Is a device that transfers electric energy from one alternating current circuit to one or more other circuit, either increasing & reducing the voltage. Eg door bells, toy electric trains.

Motional emf  $\Rightarrow$  An emf induced by motion relative to a magnetic field is called motional emf and given by

$$\text{emf} = B l v$$

Where  $B, l, v$  are perpendicular

$l \rightarrow$  length of object.

$v \rightarrow$  relative speed to field.