

Application

- At this stage user interacts with the scene and alters it as per his requirements.
- In this stage 3D objects are created using modeling tools ~~and~~.
3D objects can be moved by transformation.
Model created needs to be positioned and oriented correctly in 3D space.

Geometry Stage

The geometry step which is responsible for the majority of the operation with polygons and their vertices.

Sub-stages are

- a) Model Transformation
- b) View Transformation → Perspective Geometric view
- c) Lighting
- d) Projection
- e) Clipping
- f) Screen Mapping

Basics of computer graphics pipeline

1) Modeling → The first step is to create a 3D model of object that you want to render.

2) Transformation → Once the 3D model is created, it needs to be positioned and oriented correctly in 3D space.

3) ~~Mapping~~ →

Computer graphics pipeline or rendering pipeline defines the primitive operations required for this mapping.

Graphics pipeline primarily works in 3 stages.

- (i) Application
- (ii) Geometry
- (iii) Rasterization

c) Clipping

3D model is clipped so that only parts within the view are kept.

d) Area Mapping

Object which survive of clipping stage are passed to screen mapping stage.

Rasterization Stage

In this stage all primitives are converted into pixels in the window.

Model Transform

Transform the vertices and normals of 3D objects from model space to world space.

View transform

The camera and all the 3D objects are transformed here.

Lighting

A lighting equation used to calculate color for each vertex of 3D object that is to be affected by lighting.

Projection

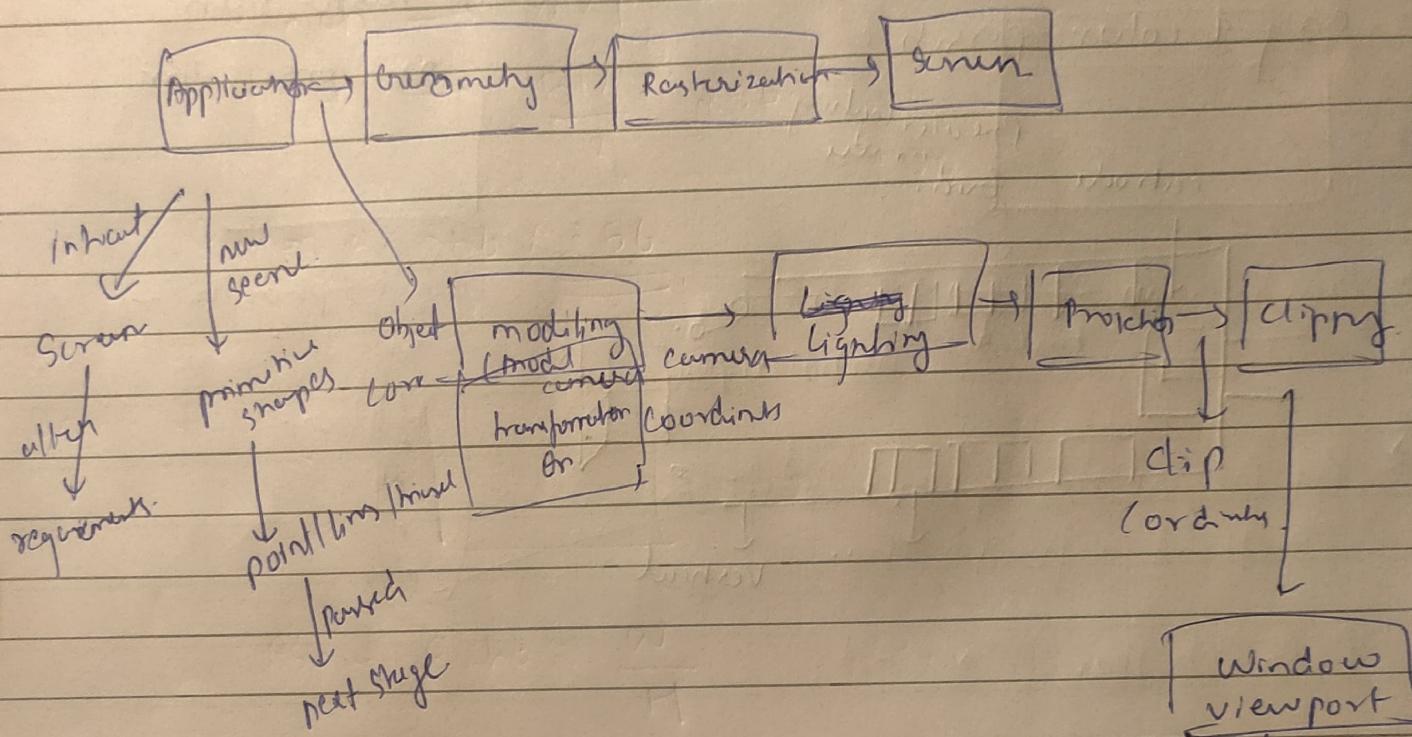
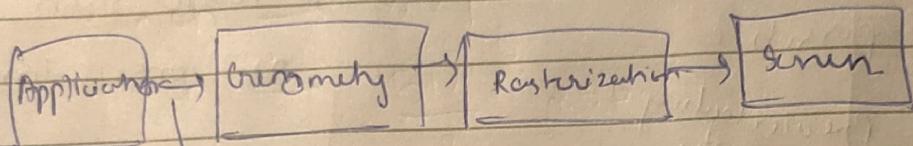
The purpose of projection is to simplify rendering.

Done by orthographic projection

Graphics pipeline / rendering pipeline

defining primitive operation required for mapping.

- Application
- ↓ geometry
- Rasterization



Application (perform
collision detection, morphing
animation)

it helps in reducing memory
requirements

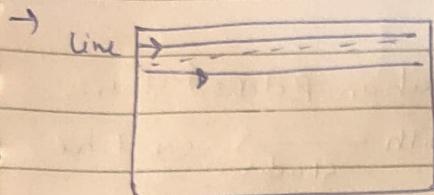
Raster Scan System. 2

→ Refresh rate. (60, 80) Hz
[Independent picture comprising]

→ It is scanning technique in which

c-beam move horizontally along with screen

→ It moves top → bottom, left → right
Covering one scan line at time.



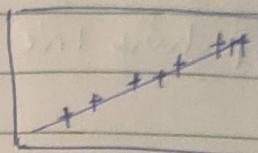
Random Scan System.

→ Refresh (30, 60) Hz
[depends number of line]

→ It is scanning technique

c-beam directly directed
on areas where picture to be drawn

→ Vector.



→ raster scan → pixel intensity.

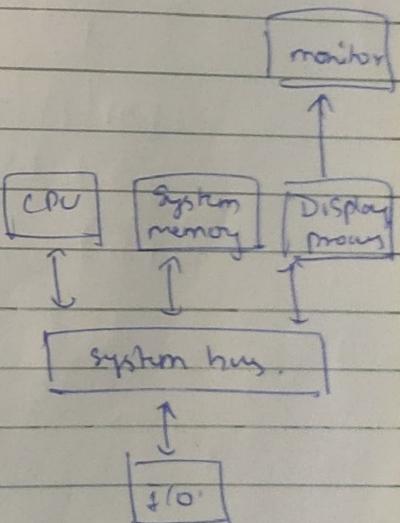
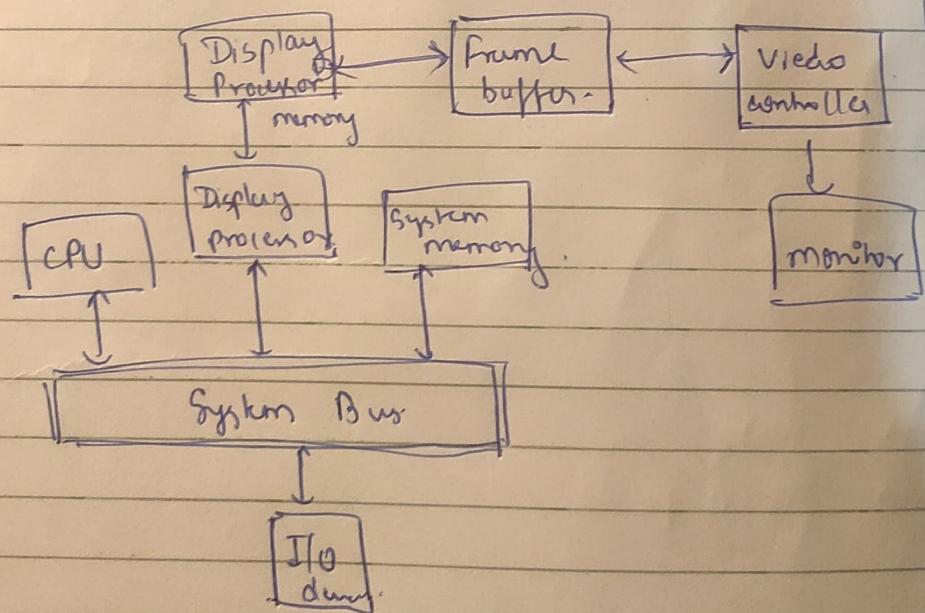
[buffer] control display rectangle of box.

→ In random we does not require any frame buffer.

→ Picture description shared frame buffer refresh buffers.

→ Frame buffer also known as bit map

Eg Television



Eg Pen plotter

→ Special memory area allocated for graphics only.

→ Frame buffer store intensity values

Advantages

- ① Real image
- ② many colors produced
- ③ Dark screen.

Disadvantages

- ① Low resolution
- ② Display picture line by line
- ③ More costly. invert of time

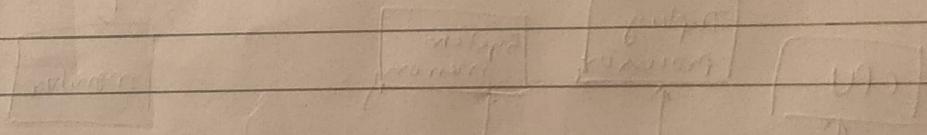
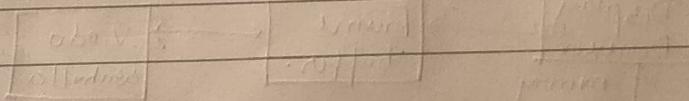
Advantages

- ① High resolution
- ② Draw smooth line
- ③ less required \rightarrow fine buffer not used

Disadvantages

- ① less resolution. Real static image with \rightarrow cannot be drawn

- ② Color palette limitations.

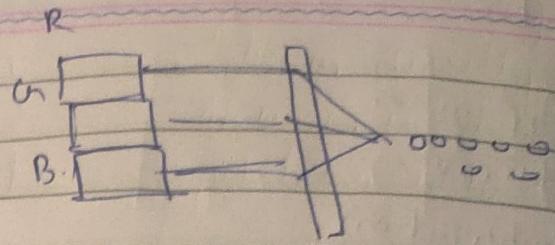
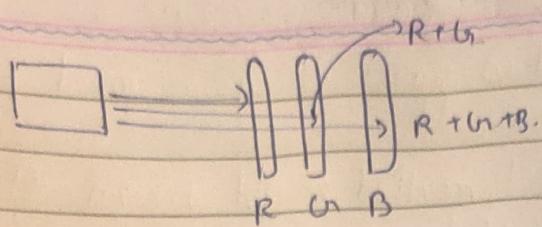


and instead

OLT

Beam Penetration method.

Shadow mask



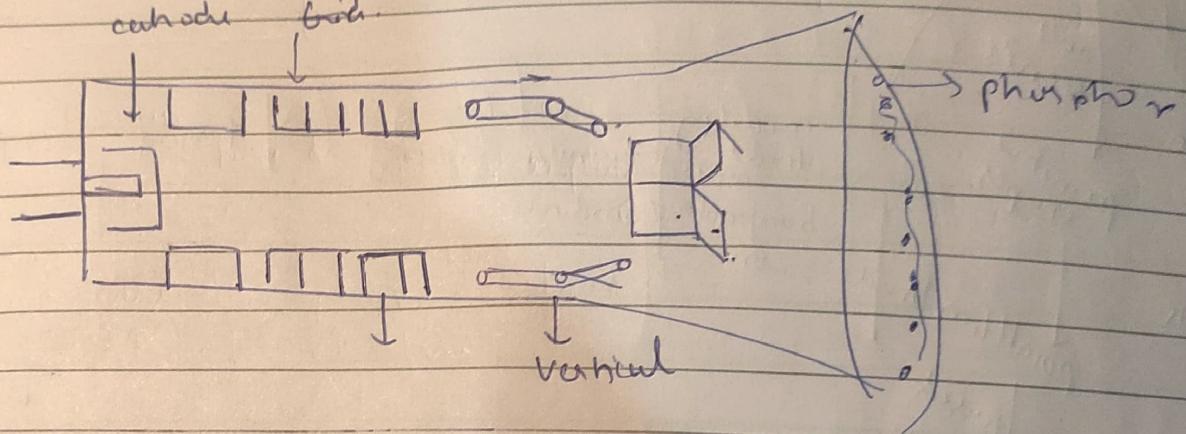
Und. Random scan →

only 4 color possible.

Und. raster scan.

millions color

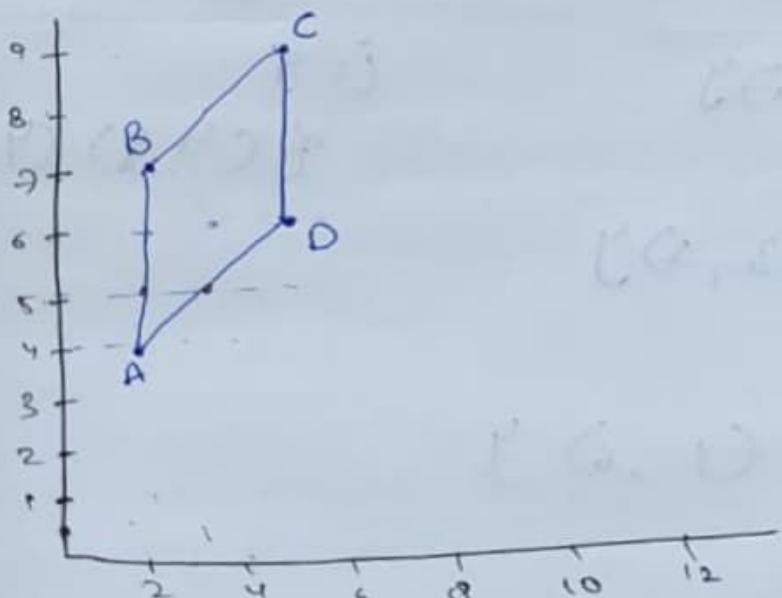
Preaccelerating
cathode uncl.
grid.



~~Inside / outside Test~~

- If the scan line pass through a vertex both the edges that are connected to the vertex are on same side of the scanline. Then we need to count a vertex twice.
- If the scanline pass through a vertex both the edges that are connected to the vertex are on the opposite sides of the scanline. Then we need to count a single intersection point.

Q Explain the data structures used by scanline polygon filling alg. Determining the content of active edge table to fill the polygon with the vertex A(2,4) B(2,7) C(4,9)
D(4,6)



A(2,4) B(2,7) C(4,9) D(4,6)

x_{k+1}	y_{k+1}	d_{k+1}
1	6	72
2	6	144
3	6	216
4	5	288
5	5	360
6	4	432
7	3	504

Ques $x_0 = 8$ $y_0 = 6$
start $(0, 6)$

x_k	y_k	$P_{1,0}$	dy	dx
0	6	-332	768	0
1	6	-224	768	-72
2	6	-44	768	144
3	6	208	640	216
4	5	-108	640	288
5	5	288	512	360
6	4	244	384	432

$$\rightarrow \text{Find } P_{20} = \pi^2 y \left(\frac{x-1}{x_0} - \frac{1}{2} \right)^2 + \pi^2 (y-1)^2 - 2\pi^2 xy$$

Repeat till ($y > 0$)

Plot (x, y)

if $P_2 > 0$

else

$$x = x \quad y = y - 1$$

$$\text{update } dy \rightarrow dy - 2\pi^2 x$$

$$P_2 = P_2 - dy + \pi^2 x$$

y

else

$x = x + 1$

$$y = y - 1$$

$$dy = dy - 2\pi^2 x$$

$$dx = dx + 2\pi^2 y$$

$$P_2 = P_2 + dx - dy + \pi^2 x$$

y

computer graphics

→ DDA (Digital Differential Analysis)
 Scan conversion, integrated approach
Straight line equation

$$y = mx + c$$

$$\text{slope} = \frac{y_2 - y_1}{x_2 - x_1}$$

case I

$$m > 1$$

$$x_n = x_1 + 1/m$$

$$y_n = y_1 + m$$

case II

$$m < 1$$

$$x_n = x_1 + 1$$

$$y_n = y_1 + m$$

case III

$$m = 1$$

$$x_n = x_1 + 1$$

$$y_n = y_1 + 1$$

Algorithm

- ① calculate the slope m
- ② check the cases
- ③ fetch the new coordinates
- ④ based on new coordinates calculate fetch coordinate
- ⑤ calculate the final coordinate by abs(New coordinate)
- ⑥ End

$$A(0,0) \text{ & } B(8,4)$$

$$m = \frac{4-0}{8-0} = 0.5 \text{ cm II}$$

$$x_n = \frac{0+1}{0+0.5} = 1$$

$$y_n = \frac{0+0.5}{0+0.5} = 0.5$$

x_1	y_1	x_n	y_n	final
0	0	1	0.5	(1,1)
1	0.5	2	1	(2,1)
2	1	3	1.5	(3,2)
3	1.5	4	2	(4,2)
4	2	5	2.5	(5,3)
5	2.5	6	3	(6,3)
6	3	7	3.5	(7,4)
7	3.5	8	4	(8,4)

$$x_n = x_1 + l/m = 0 + \frac{1}{0.5} = \frac{10+1}{10} = \frac{11}{10}$$

$$y_n = y_1 + m = 0 + 2 = 12$$

$$x_n = 20 + 1$$

$$y_n = 30 + 0.8$$

$$x_n = 21 + 1$$

$$30.8 + 0.8$$

$$\frac{18 - 6}{30 - 20} = \frac{12}{10}$$

NOTE

on the boundary b/w two regions / octants
slope of curve is -1

Algorithm

- Read radius r_x & r_y
- Initialise start point of region 1 as $x=0, y=r_y$
- calculate $P_1 = r_y^2 - r_x^2 r_y + \frac{1}{4} r_x^2$
- calculate $dx = 2r_y x, dy = 2r_x^2 y$
- repeat while $dx < dy$

Plot (x, y)

if $P_1 < 0$

 q

$$x = x + 1$$

update $dx \rightarrow dx + 2r_y^2$

$$P_1 = P_1 + 2r_y^2 x + r_y^2$$

 y

else

 q

$$x = x + 1 \quad y = y - 1$$

update $dx \rightarrow 2r_y^2 * dx$

update $dy \rightarrow dy - 2r_x^2$

$$P_1 \rightarrow P_1 + \underline{dx - dy - 1} r_y^2$$

 y

when

$dx \geq dy$ plot P_2 as

Bresenham's Algorithm

It determines the pixels of n-dimensional raster that should be selected in order to form a close approximation to a straight line between two points.

$$m = \frac{\Delta y}{\Delta x}$$

P_k = Decision Parameter

$$P_k = 2\Delta y - \Delta x$$

$$\Delta y = y_2 - y_1, \quad \Delta x = x_2 - x_1$$

Case I

$$P_k > 0$$

$$P_{k+1} = P_k + 2\Delta y - 2\Delta x$$

$$x_n = x_1 + 1$$

$$y_n = y_1 + 1$$

Case II

$$P_k < 0$$

$$P_{k+1} = P_k + 2\Delta y$$

$$x_n = x_1 + 1$$

$$y_n = y_1$$

Line A(20, 10) (B(30, 18))

$$\Delta x = 10$$

$$\Delta y = 8.$$

$$P_k = 2 \cdot 8 - 10$$

$$= 16 - 10$$

$$= 6$$

$$P_k = 2 + 16 - 20$$

$$= 2 - 4$$

$$= -2$$

Case I

$$x_n = 20 + 1$$

$$x_n = 21 + 1$$

$$y_n = 10 + 1$$

$$y_n =$$

$$P_{k+1} = 6 + 16 - 20$$

$$-2^{-4}$$

$$= -4$$

$$x_n = 28 + 1$$

$$= 12$$

$$y_n = 12 + 1$$

$$-2^{-4}$$

$$-6^{-4}$$

$$6^{-4}$$

$$-14 + 16 - 20$$

$$17 = -4$$

$$= 10$$

$$10^{-4}$$

$$6$$

Advantages

- ① fastest method than method of using direct use of lin equation
- ② this method does not use multiply
- ③ this allows us to tolerate to change in the value of x & y value so plotting of same
- ④ it gives overflow indication when a point a reposition
- ⑤ it is easy method because easy step involves just two addition

Dis

- ① It involves floating point addition rounding of ~~error~~ ^{accumulation} of round off error cause accumulation of error
- ② rounding of operation & floating point operation consume lot of time

This more suitable for generating lin using the software but it is less suited hardware implementation

Circle Generation Algorithm

given $y = 10$

$y = RR = \text{radius}$

mid point

Bresenham's circle

given $(x_c, y_c) = (2, 2)$

Decision Parameter

$$P_k = 1 - R$$

Case I

$$P_k < 0$$

$$P_{k+1} = P_k + 2x + 1$$

$$x_n = x + 1$$

$$y_n = y$$

Case II

$$P_k > 0$$

$$P_{k+1} = P_k + 2x + 1 - 2y$$

$$x_n = x + 1$$

$$y_n = y - 1$$

Note when $x = y$ stop "x is always less than y"

case I

$$P = 3 - 2R$$

$$P_k < 0$$

$$P_{k+1} = P_k + 4x + 6$$

$$x_n = x + 1$$

$$y_n = y$$

case II

$$P_k > 0$$

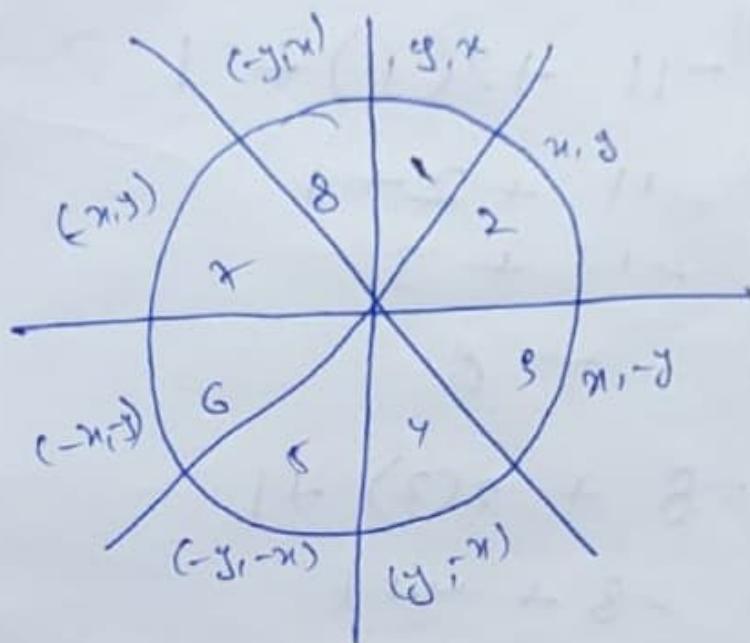
$$P_k = P_k + 4(x-y) + 10$$

$$x_n = x + 1$$

$$y_n = y - 1$$

Alg

- ① Input of circle radius r & (x_e, y_e)
- ② Initial value $x=0, y=r$
- ③ Plot pixel $(x+xe, y+ye)$
- ④ D.P. $P_x = 1 - r^2$
- ⑤ Start of loop



P_{k+1}	x_n	y_n	$2(x_n + y_n)$
-9	0	10	2
-6	1	10	3
-1	2	10	4
6	3	10	5
-3	4	9	6
8	5	9	7
-8	6	8	8

Liang-Burke Algo.

$$① \quad x = x_i + t \Delta x$$

$$y = y_i + t \Delta y$$

$$② \quad x_{w\min} \leq x \leq x_{w\max}$$

$$y_{w\min} \leq y \leq y_{w\max}$$

$$③ \quad P \neq q$$

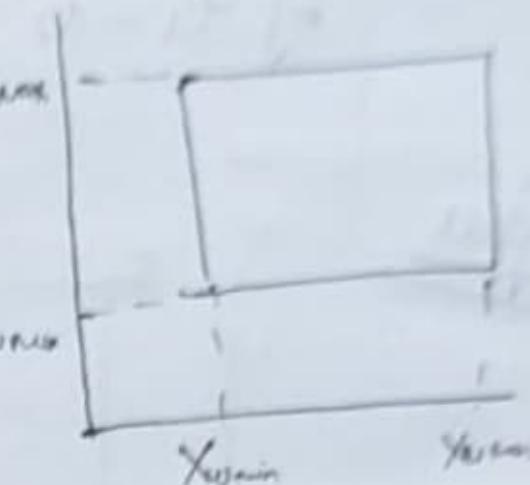
$$tP_k \leq q_k$$

$$P_1 = -\Delta x \quad q_1 = x_i - x_{w\min}$$

$$P_2 = \Delta x \quad q_2 = x_{w\max} - x_i$$

$$P_3 = -\Delta y \quad q_3 = y_i - y_{w\min}$$

$$P_4 = \Delta y \quad q_4 = y_{w\max} - y_i$$



$$x_{w\min} \leq x_i + t \Delta x$$

$$x_{w\max} \geq x_i + t \Delta x$$

$$y_{w\min} \leq y_i + t \Delta y$$

$$y_{w\max} \geq y_i + t \Delta y$$

$$t \Delta y \geq y_{w\max} - y_i$$

$$t \Delta y \leq y_{w\max} - y_i$$

$$④ \quad \text{if } P_k = 0$$

then line is parallel to window

$$\text{if } P_k < 0$$

then line is completely outside

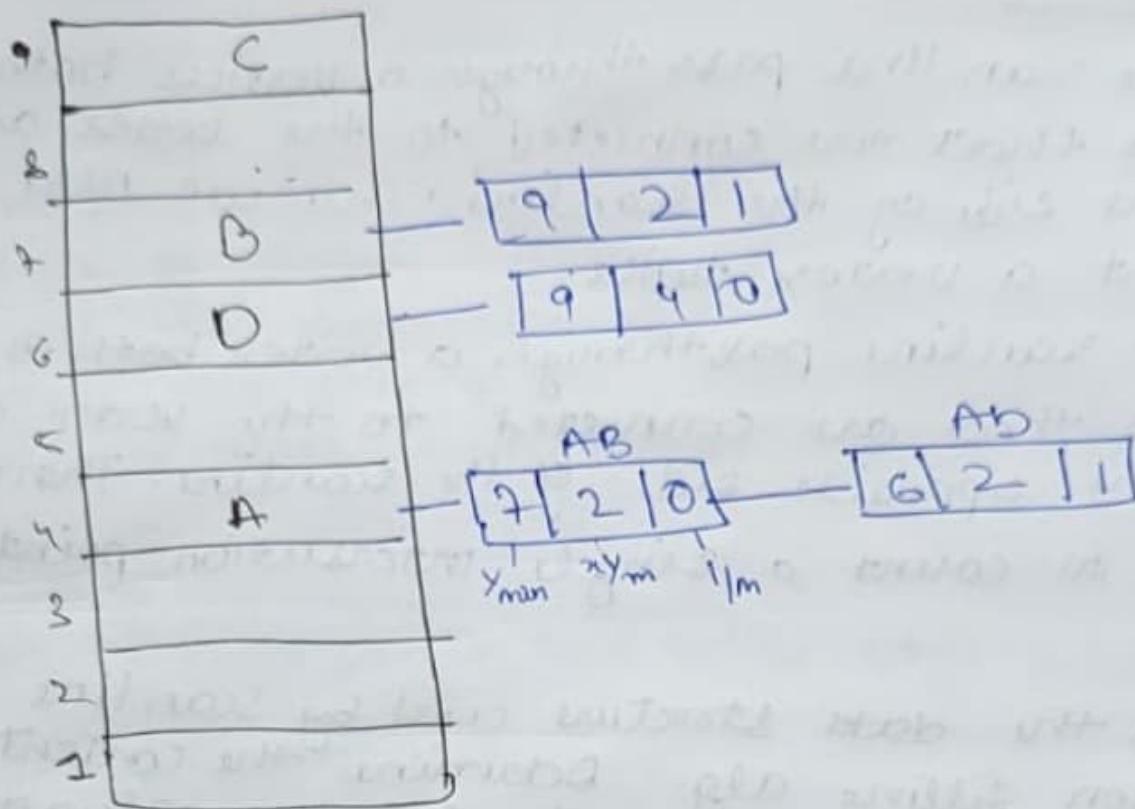
$$\text{if } P_k < 0$$

$$t_1 = \min(0, \frac{q_k}{P_k})$$

$$\text{if } P_k > 0$$

$$t_2 = \min(1, \frac{q_k}{P_k})$$

GET (Global Edge Table)



AET (Active Edge Table)

$i = 4$

$\{ (2,4) \ (2,4) \} Y$

$i = 9$

$\{ (4,9) \ (4,9) \} Y$

$i = 5$

$\{ (2,5) \ (3,5) \} Y$

$i = 6$

$\{ (2,6) \ (1,6) \} Y$

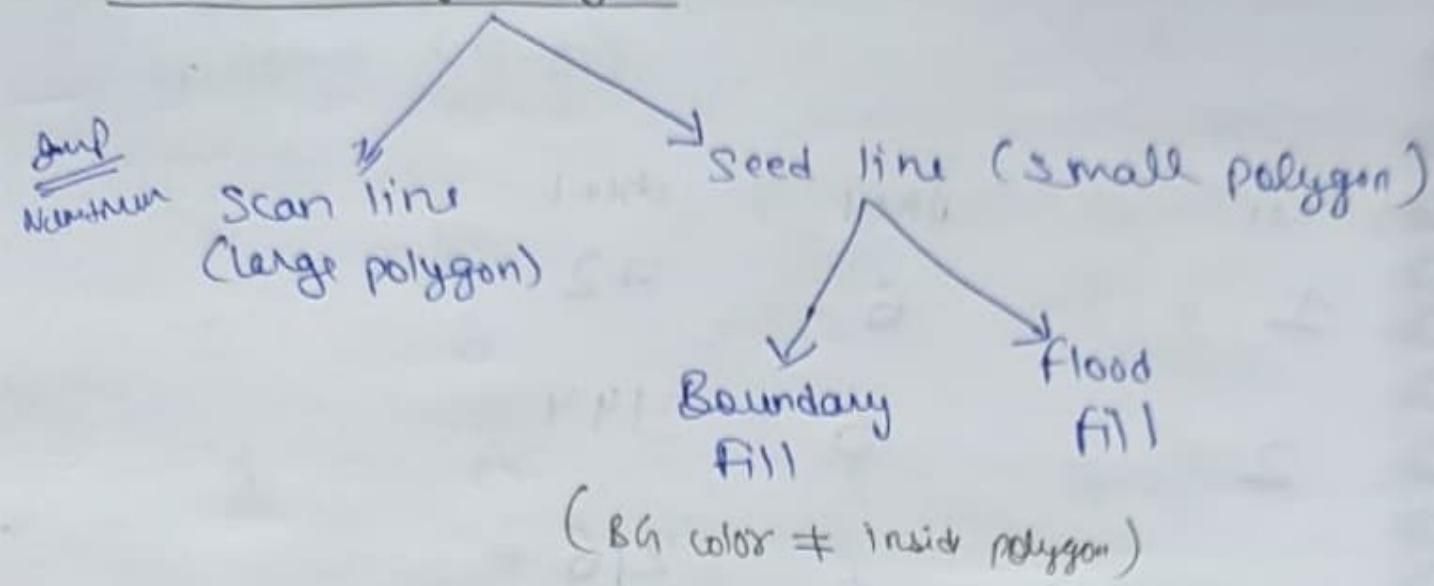
$i = 7$

$\{ (2,7) \ (4,7) \} Y$

$i = 8$

$\{ (3,8) \ (4,8) \} Y$

Polygon filling Alg.



- * In case of boundary filling edges of polygon are first drawn then starting with the seed any pixel of polygon, we examine neighbouring pixel to check whether boundary pixel is reached
- * Boundary drawn here is a boundary pixel (R) and highlight each pixel till it is reached

R	R	R	R
R			R
R			R
R	R	R	
			R
			R
R			R
R	R	R	R

	(x-1, y+1)	
(x+1, y+1)	x, y+1	x+1, y
x+1, y	x, y	x+1, y-1
(x-1, y-1)	x, y-1	(x+1, y-1)

Inside | outside Test (odd & even parity rule)

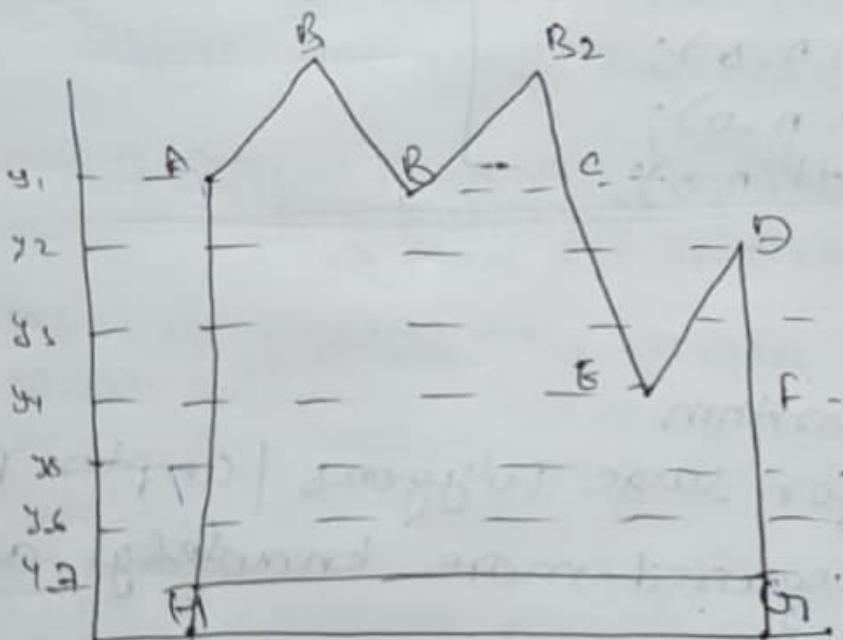


Algorithm Scan line :-

- find the intersecting point of the scan lines with all edges of polygon
- sort the intersection of the point by incⁿt x coordinate
- make the pair of the intersection
- All the areas coming within these all points pairs

Note

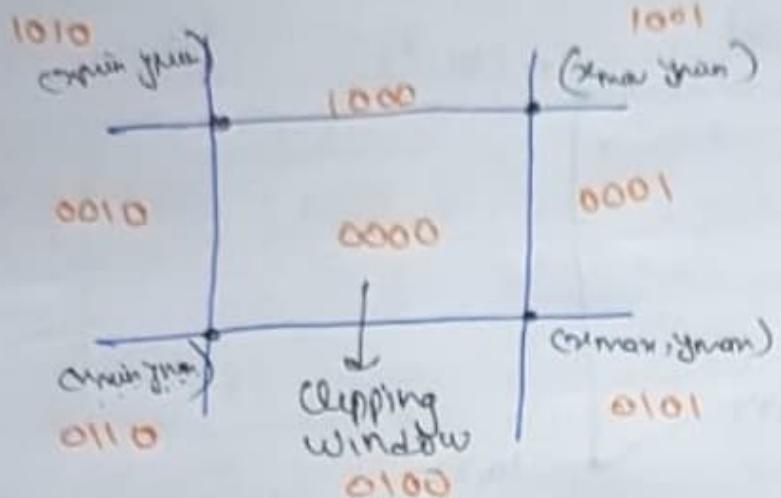
We need to create and active edge table



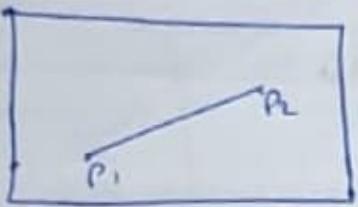
AB
AB
B B2
B2 E
E F
F G
G H
H A

Line Clipping (Cohen Sutherland)

T B {R-right
↓ Top Bottom



Case I :-

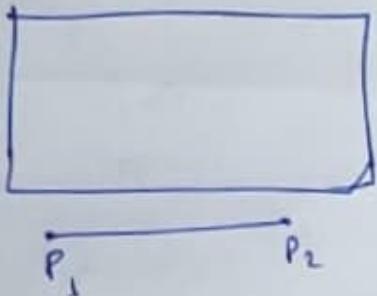


$$P_1 = 0000$$

$$P_2 = 0000$$

No clipping required

Case II :-



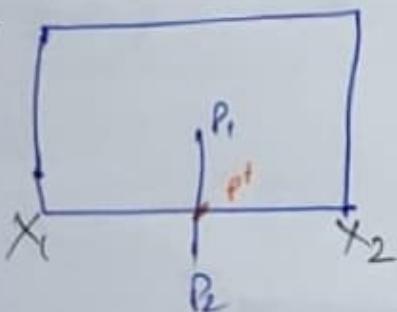
$$P_1 = 0100$$

$$P_2 = 0100$$

$$\underline{0100} \quad \text{AND}$$

Line is removed

Case III :-



$$P_1 = 0000$$

$$P_2 = \underline{0100}$$

Line clipping is required

P^* = is end point

(P_2^* is removed to P_1)

Problem with ~~4~~ connected boundary

Fill algorithm

- In this approach for some particular category of polygons the diagonals pixels are left uncoloured
- It may not filled ~~when~~ Requiring some time correctly
with colo. ~~when~~ some interior pixel ~~that~~ is already filled
The algorithm will checked of boundary pixel
for filling & will found already filled so
recursive process is terminate. So there
is need to check all pixel colour
before applying the colours

Flood fill → flood fill required use amount of
memory. → flood fill is simple and efficient

- It can process the image containing more than boundary colours
- flood fill algo. comparatively slower than boundary fill algo.
- In flood fill the random colour can be used to paint the interior position than the old one is replaced with the new one

Boundary fill

- It can only process the image containing single boundary colours
- It is faster than flood fill Algo.
- Boundary fill interior points are painted by continuously searching for boundary colour
- memory consumption is relatively low
- boundary fill have high complexity

Algorithm flood fill

$m = \text{new color}$
 $o = \text{old color}$

flood (x, y, n, o)

if get pixel (x, y) == o

y

put pixel (x, y, n)

z

flood ($x+1, y, n, o$);

flood ($x, y+1, n, o$);

flood ($x-1, y, n, o$);

flood ($x, y-1, n, o$);

flood ($x-1, y-1, n, o$);

flood ($x-1, y+1, n, o$);

flood ($x+1, y-1, n, o$);

flood ($x+1, y+1, n, o$);

8 connectors

4 corner

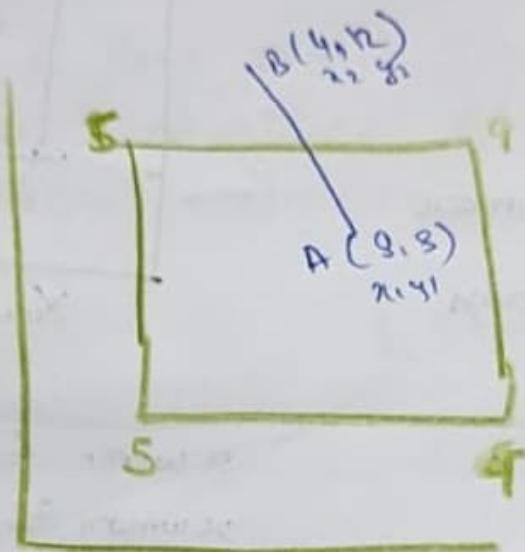
Disadvantages

- very slow algorithm.
- may fail for large polygons / complex polygons
- initial pixel required more knowledge about surrounding pixels.

If $t_1 > t_2$ (x)

If $t_1 < t_2$ then move to step 1

Ques



$$X_{wmax} = 5 \quad X_{wmin} = 5$$

$$X_{wmax} = 9 \quad X_{wmin} = 9$$

$$P_1 = -4 \quad q_1 = -1$$

$$P_2 = 4 \quad q_2 = 5$$

$$P_3 = -4 \quad q_3 = 7$$

$$P_4 = 4 \quad q_4 = 1$$

$$t_1 = \max(0, \frac{q_k}{P_k}) \quad \max(0, 0.25)$$

$$t_2 = \min(1, \frac{q_k}{P_k}) \quad \min(1, 0.25)$$

Algorithm

boundary (x, y, f, b)

if (get pixel (x,y) != b)

 get pixel (x,y) = f

 2

 put pixel (x, y, f)

 boundary (x+1, y, f, b);

 boundary (x, y+1, f, b);

 boundary (x-1, y, f, b);

 boundary (x, y-1, f, b);

 boundary (x-1, y-1, f, b);

 boundary (x-1, y+1, f, b);

 boundary (x+1, y-1, f, b);

 boundary (x+1, y+1, f, b);

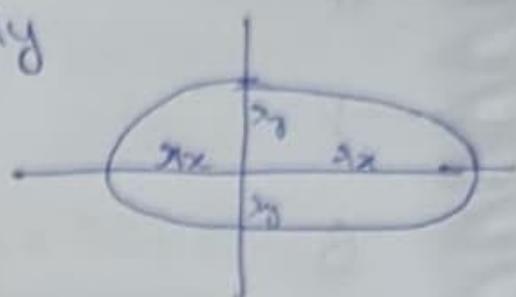
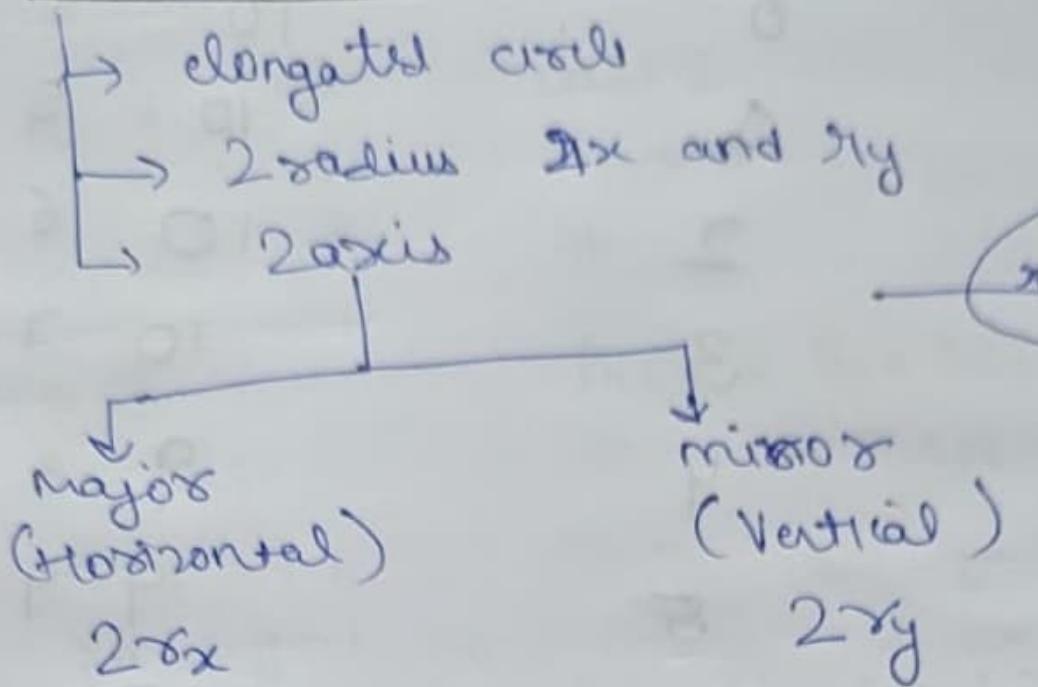
It is required

minimum value with current value and the

maximum value with current value
of boundary and using relation the previous

pixels previous of previous pixels
be printed. if minimum greater
than previous region and it's value

Ellipse Generation Algorithm (mid-point)



<u>circle</u> → 8 ways symmetry → 1 octant \rightarrow 7 other octants	<u>ellipse</u> 4 ways symmetry 2 regions \rightarrow 1 quadrant
--	---

Intersacting tangent slope = -1

eq. of ellipse = $x^2/a^2 + y^2/b^2 - r^2/r_y^2 = 0$
where

$$a = rx$$

$$b = ry$$

slope = $\frac{dy}{dx}$ (eq of ellipse)

$$= \frac{-2ry^2 x}{2r^2 y^2 b}$$

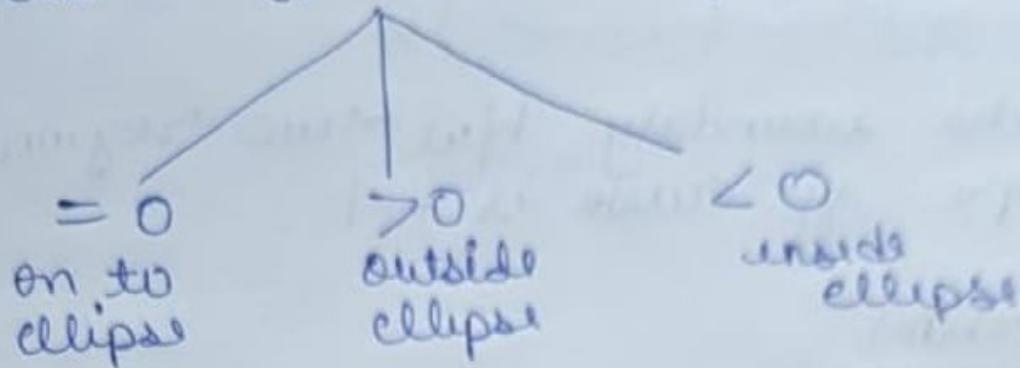
P_k	x_1	y_1	x_n	y_n
6	20	10	21	11
-2	21	11	22	12
-2	22	12	23	12
+14	23	12	24	13
+10	24	13	25	14
6	25	14	26	15
2	26	15	27	16
-2	27	16	28	16
+14	28	16	29	17
10	29	17	30	18

$$A(-20, -10) \quad B(30, 18)$$

Advantages

- It involves only integer arithmetic so it is simple
- It avoids the generation of duplicates points
- It can be implemented using hardware because it does not use multiplications & division
- It is faster as compare to DDA because it does not involve floating point calculation like DDA algorithm

If a point (x, y) satisfies an eq - then



→ ellipse is an elongated circle with two radius \sqrt{x} and \sqrt{y} and two axis major axis and minor axis

→ The difference b/w circle and ellipse are

* In circle we need to plot only 1 octant of any quadrant but in ellipse we need to plot 2 regions that is (i.e) one complete quadrant. entire ellipse

⇒ Quadrant 1 :- Region 1

Slope < -1

Start point $(0, \sqrt{y})$

e.g. $(x+1)$

Take unit step in +ve x direction till boundary b/w region is reached

⇒ Quadrant 2 :- Region 2

Slope > -1

Take unit step in negative direction till end of quadrant

e.g. $(y-1)$

Disadvantages

→ This algorithm is meant for basic line drawing only initially is not a part of Bresenham's line algorithm so to draw smooth line you should work to look for another algorithm.

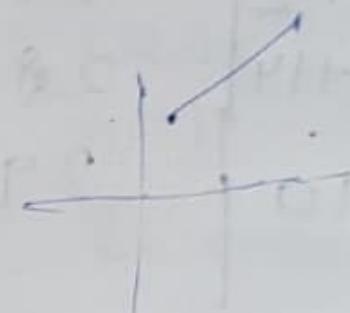
Ques $(1, 4) \rightarrow (8, 12)$

$$\Delta x = 8 - 1 \\ = 7$$

$$\Delta y = 12 - 4 \\ = 8$$

$$m = \frac{8}{7}$$

$$P_k = 2\Delta y - \Delta x \\ = 2(8) - 7 \\ = 16 - 7 \\ = 9$$



case I
 $P_k > 0$

$$x_n = x_1 + 1 = 1 + 1 = 2$$

$$y_n = y_1 + 1 = 4 + 1 = 5$$

$$P_{k+1} = 9 + 2(8) - 2(7) \\ = 9 + 16 - 14 \\ = 9 + 2$$

3 possibilities for the line

- 1) line can be completely inside the window
[which should be accepted]
- 2) line can be completely outside the window
[the line will be completely removed from the region]
- 3) line can be partially inside and partially outside
then we will find the intersection point of the line with the edge of the clipping window

Algorithm

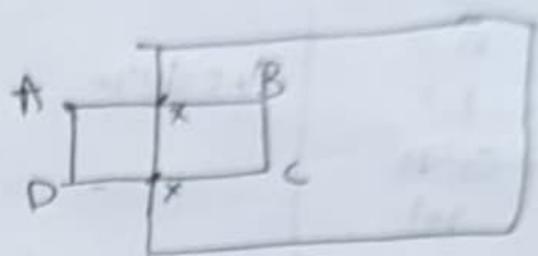
- 1) Assign a region code for each end point.
 - 2) If both end point have the region code 0000 then ~~exp excepted~~ accept the line.
 - 3) Else perform the logical AND operations for both the region code
- * If the result is not 0000 then reject the line.
- * If the result is 0000 then you need line clipping

How to perform clipping

- ① choose an end point of the line that is outside the window
- ② find the intersection point at the window boundary (based on region code)
- ③ replace end point with the intersection point and update the region code

Sutherland Hodgesman Polygon Clipping

case 1 : O \rightarrow I
 (XB) save



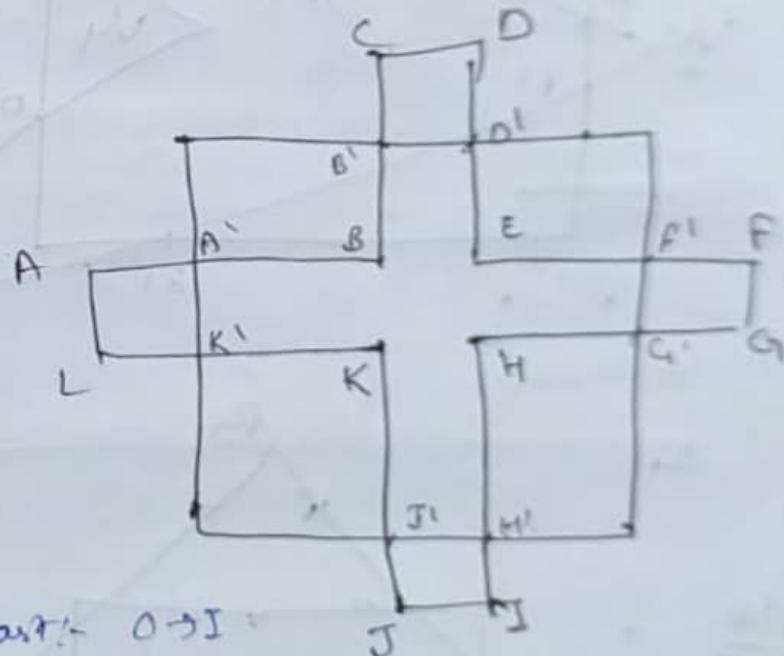
case 2 :- I \rightarrow I
 (C) save

case 3 : I \rightarrow O
 (Y) save

case 4 : O \rightarrow O
 ignore

4.4

case 1 : O \rightarrow I
 (A'B') save



case 2 :- I \rightarrow O
 (B'K) save

case 3 :- O \rightarrow O
 ignore

case 4 :- O \rightarrow I
 (D'E)

case 5 :- I \rightarrow O
 (F') save

case 6 :- O \rightarrow O
 ignore

case 7:- O \rightarrow I
 (G'H)

case 8: I \rightarrow O
 (H')

case 9:- O \rightarrow O
 ign

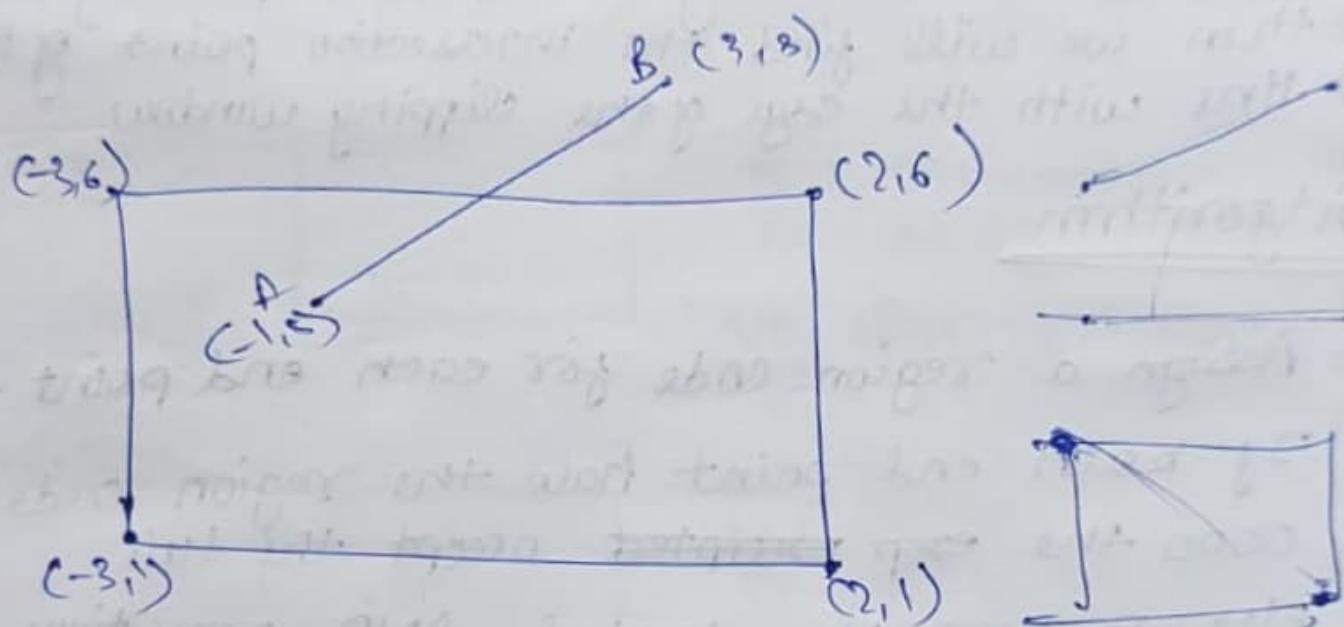
case 10:- O \rightarrow I
 (J'K)

case 11:- I \rightarrow O
 K

case 12 + O \rightarrow O
 ign

- ④ Repeat step 2 until we find the clipped line either trivially accepted or trivially rejected
- ⑤ Repeat step 1 for all the lines

Ques Clip a line A (-1, 5) and B (3, 8) using Cohen Sutherland Algorithm with window coordinate (-3, 1) and (2, 6)



$$A = 0000$$

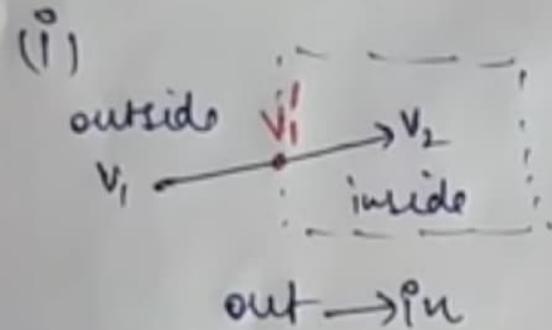
$$B = 1001$$

POLYGON CLIPPING ALGO

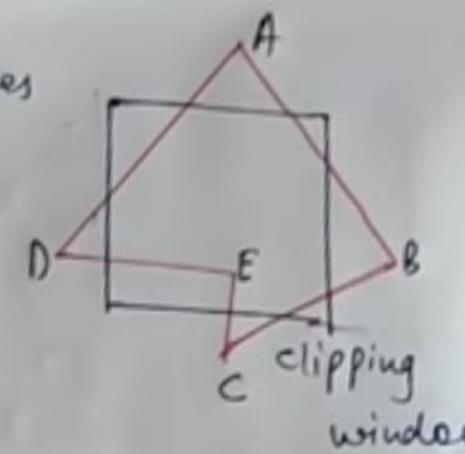
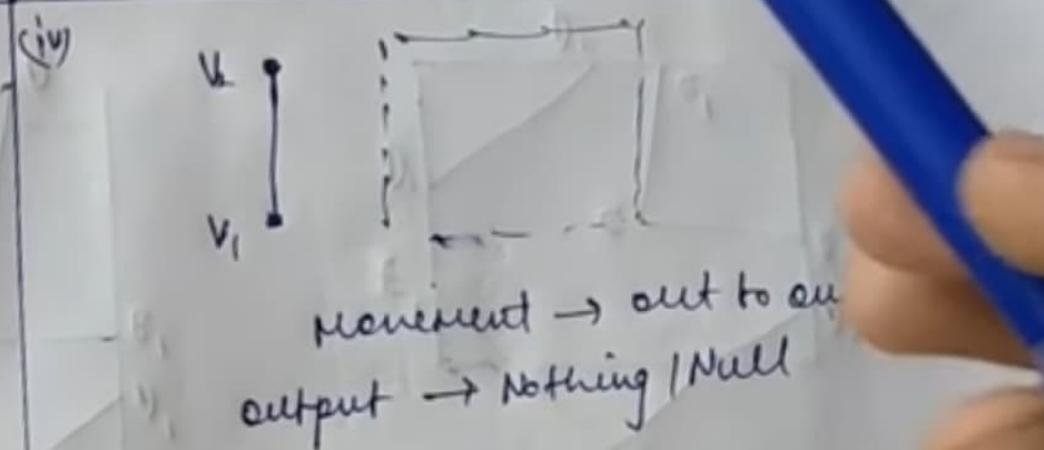
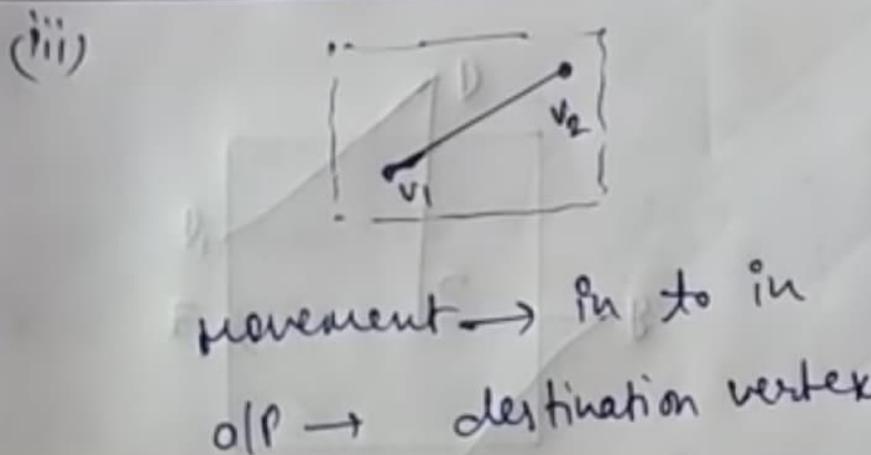
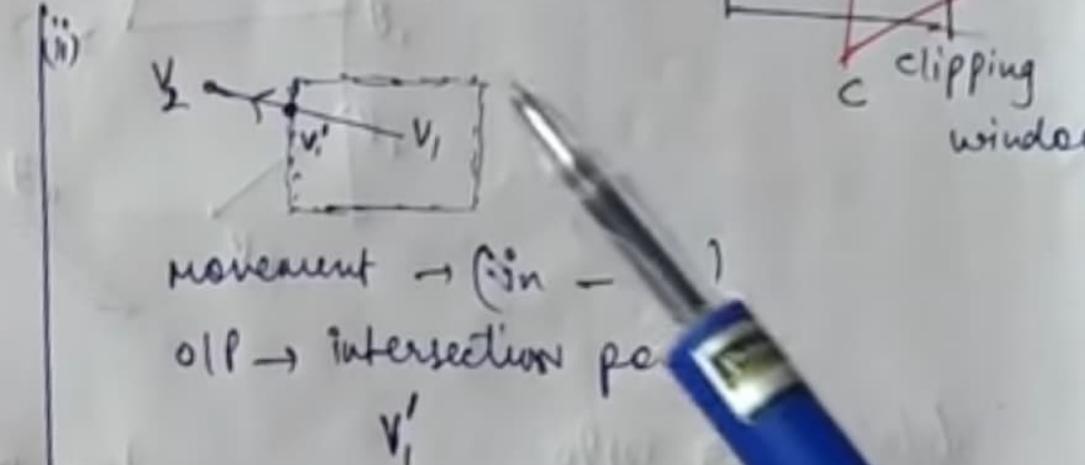
* It clips the region of the polygon lying outside the window.

* clip against each edge of window & obtain new set of vertices

for finding new sequence of vertices, there are 4 cases:



OP \rightarrow intersect point + destination point
 $\rightarrow v_1' v_2$



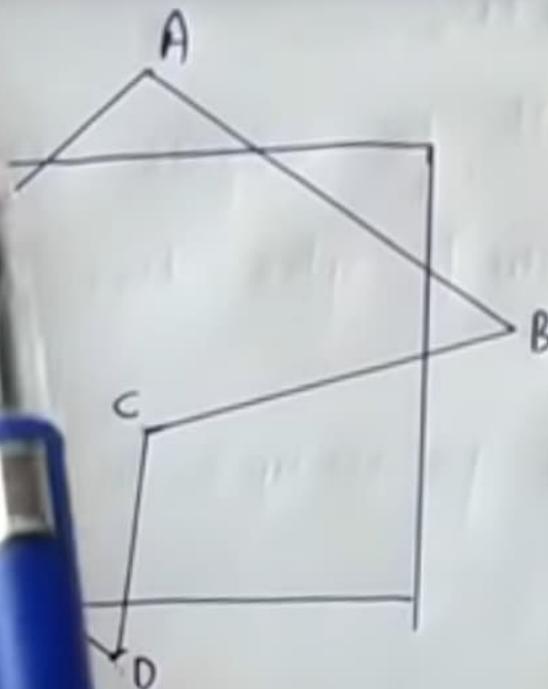
Steps of Sutherland Hodgeman Polygon Clipping Algorithm:

- ① Read the coordinates of all vertices of the polygon ✓
- ② Read the coordinates of the clipping window ✓
- ③ Consider the left edge of the window ✓
- ④ Compare the vertices of the edge of the polygon, individually with the clipping plane.
- ⑤ Save the resulting intersections and the vertices according to the rule
- ⑥ Repeat step ④, ⑤ for the remaining edges of the clipping window
- ⑦ Each time ^{pass} the resultant list of vertices to the next edge of the clipping window.
- ⑧ STOP.

Algorithm:

- ① Input four clippers & $C_l = X_{\min}$,
 $C_r = X_{\max}$, $C_t = Y_{\max}$, $C_b = Y_{\min}$
corresponding to the left, right,
top, and bottom window boundaries.
The polygon is specified in term of
its vertex list $V_{in} = \{v_1, v_2, \dots, v_n\}$
where the vertices are named anticlockwise
- ② For each clipper in the order C_l, C_r, C_t, C_b do
③ Set output vertex list $V_{out} = \text{NULL}$, $i=1, j=1$
- ④ repeat
- ⑤ Consider the vertex pair v_i & v_j in V_{in}
- ⑥ if v_i is inside and v_j outside then
ADD the intersection
of the
clipper with the edge
to V_{out}
- ⑦ else if v_i is outside & v_j
inside of the clipper then
⑧ ADD v_j to V_{out}
- ⑨ else if v_i is outside & v_j
inside of the clipper then
⑩ ADD the intersection point of
the clipper with the edge (v_i, v_j)
and v_j to V_{out}
- ⑪ else
ADD NULL to V_{out}
- ⑫ end if
- ⑬ Until all edge (ie consecutive
vertex pairs) in V_{in} are checked.
- ⑭ Set $V_{in} = V_{out}$

① Clipping against left edge of the window



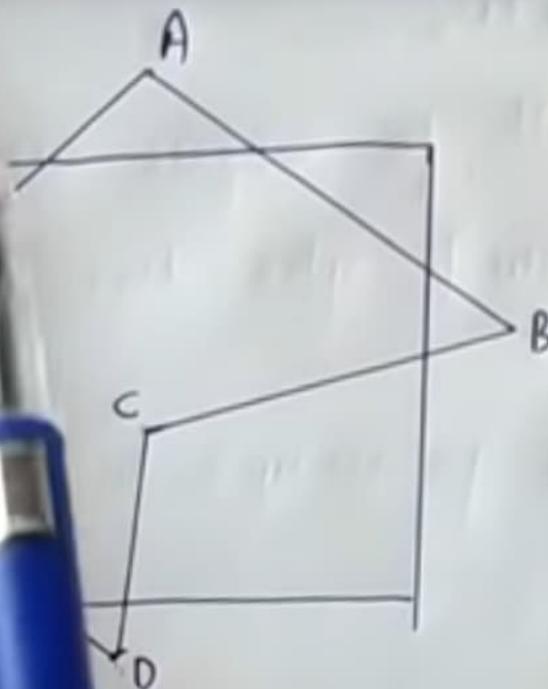
vertex	case	output	
AB	in→in	B	
BC	in→in	C	
CD	in→in	D	
DE	in→out	D'	
EA	out→in	E'A	} new vertices

② clipping against right edge of window

clipping	
OIP	
A'' A'	new vertex
B'	
C	
B' C	
C C'	
C'	

vertex	case	OIP
AB	in→out	A'
BC	out→in	B' C
CD	in→in	D
DD'	in→in	D'
D'E'	in→in	E'
E'A	in→in	A

① Clipping against left edge of the window



vertex	case	output	
AB	in → in	B	
BC	in → in	C	
CD	in → in	D	
DE	in → cut	D'	
EA	cut → in	E'A	} new vertices

② clipping against right edge of window

clipping	
OIP	
A'' A'	new vertex
B'	
C	
B' C	
C C'	
C'	

vertex	case	OIP
AB	in → out	A'
BC	out → in	B' C
CD	in → in	D
DD'	in → in	D'
D'E'	in → in	E'
E'A	in → in	A

2) Connectivity / Adjacency

Two pixels that are neighbours and have the same gray level are adjacent.

a) 4-adjacency

Binary image

0	1	0	1
0	0	1	0
0	0	1	0
1	0	0	0

b) 8-adjacency

Gray-scale image

54	10	100	8
81	150	2	34
201	200	3	45
7	70	147	56

$$V = \{1\}$$

$$V = \{1, 2, 3, \dots, 10\}$$

c) $N_8(p)$ 8 -neighbours : union of 4-neighbours and diagonal neighbours

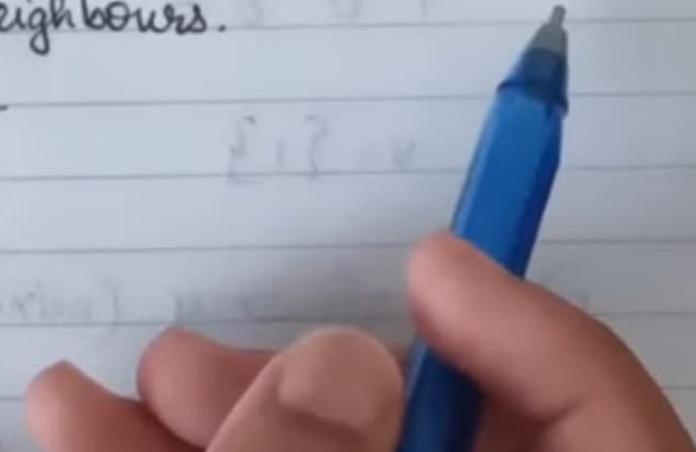
$(x-1, y+1)$	$(x, y+1)$	$(x+1, y+1)$
$(x-1, y)$	(x, y)	$(x+1, y)$
$(x-1, y-1)$	$(x, y-1)$	$(x+1, y-1)$

a) $N_4(p)$ 4-neighbours : the set of horizontal and vertical neighbours

	$(x, y+1)$	
$(x-1, y)$	(x, y)	$(x+1, y)$
	$(x, y-1)$	

b) $N_D(p)$ diagonal neighbours : the set of 4 diagonal neighbours.

$(x-1, y+1)$		$(x+1, y+1)$
	(x, y)	
$(x-1, y-1)$		$(x+1, y-1)$



SR. NO.	BASIS	BEAM PENETRATION	SHADOW MASK
1.	Colors produced	In this method, there is the production of only four colors i.e., red, green, yellow, orange.	In this method, there is the production of millions of colors.
2.	Color dependency	As in this method only four colors are produced it is because of the speed of the electron gun.	As in this method millions of colors are produced because it depends upon the intensity value of the three available guns.
3.	Number of electron guns used.	In this method, only one electron gun is used.	In this methods, three electron guns are used; i.e red, green and blue.
4.	Picture quality	As we know in this different colors and shades are not possible. So, it's picture quality is poor.	As we know in this different colors and shades are possible. So, it's picture quality is quite good.
5.	Realistic view	This method is not suitable for providing the realistic view.	This method is suitable for providing the realistic view.
6.	Resolution	This method provides high resolution.	Whereas, this method does not able to provide high resolution.
7.	Cost	It is cheaper than shadow mask method.	It is an expensive method.
8.	Application	It is used in random scan system to display color.	It is used in raster scan system to display color.

Color CRT Monitor:

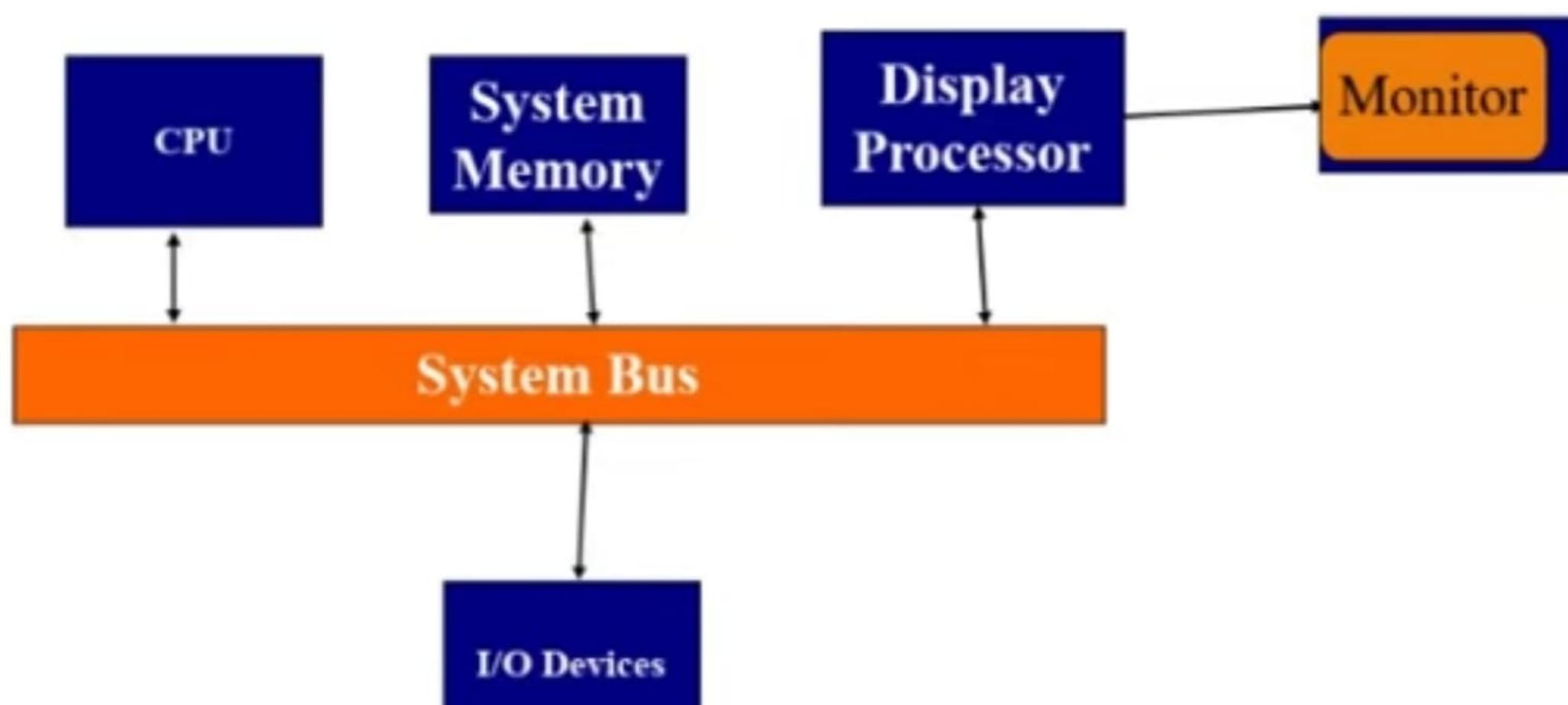
- ▶ Color CRT Monitors:
- ▶ The CRT Monitor display by using a combination of phosphors. The phosphors are different colors.
- ▶ This was one the earlier CRTs to produce color displays. Coating phosphors of different compounds can produce different colored pictures. But the basic problem of graphics is not to produce a picture of a predetermined color, but to produce color pictures, with the color characteristics chosen at run time.
- ▶ The basic principle behind colored displays is that combining the 3 basic colors – Red, Blue and Green, can produce every color. By choosing different ratios of these three colors we can produce different colors – millions of them in-fact. We also have basic phosphors, which can produce these basic colors. So, one should have a technology to combine them in different combinations.
- ▶ There are two popular approaches for producing color displays with a CRT are:
- ▶ Beam Penetration Method
- ▶ Shadow-Mask Method

Random Scan System

- ▶ **Advantages:**
 - ▶ High Resolution
 - ▶ Draw smooth line Drawing
 - ▶ Less Memory Required

- ▶ **Disadvantages:**
 - ▶ Realistic images with different shades cannot be drawn.
 - ▶ Colour limitations.

► Figure: Graphics System



Raster Scan System

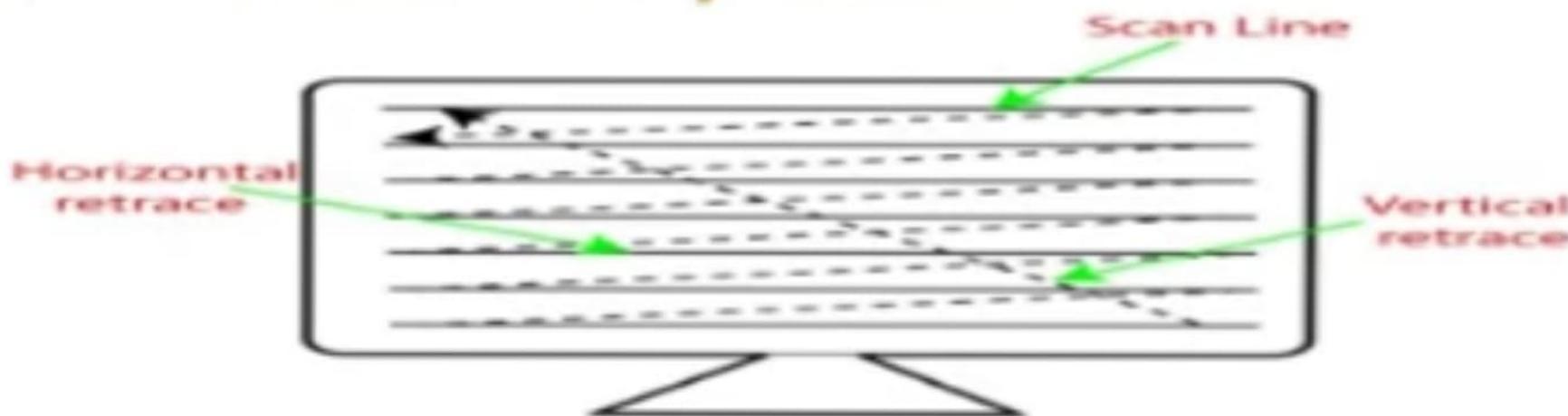
- **Advantages:**

- Real image
- Many colors to be produced
- Dark scenes can be pictured

- **Disadvantages:**

- Less resolution
- Display picture line by line
- More costly

Raster Scan System



Here, the beam is swept back and forth from the left to the right across the screen. When the beam is moved from left to the right, it is ON.

The beam is OFF, when it is moved from the right to the left as shown by dotted line in figure. When the beam reaches the bottom of the screen, it is made OFF and rapidly retracted back to the top left to start again.

A display produced in this way is called as raster scan.

In raster scan display a special area of memory is dedicated to graphics only. This memory area is called frame buffer.

This frame buffer stores the intensity values for all the screen points. Each screen point is called a pixel (picture element).

Raster Scan System

- ▶ **Raster Scan:** It is a scanning technique in which the electron beam moves along the screen. It moves from top to bottom, covering one line at a time.
- ▶ A raster scan is based on pixel intensity control display as a rectangular box on the screen called a **raster**.
- ▶ Picture description is stored in the memory area called as **Refresh buffer, or Frame Buffer**.
- ▶ Frame buffer is also known as **Raster or Bitmap**. Raster scan provides the refresh rate of 60 to 80 frames per second.

- ▶ **For Example: Television**
 - ▶ The beam refreshing has two types:
 - ▶ 1.Horizontal Retracing
 - ▶ 2.Vertical Retracing

$$\begin{aligned}
 ① \quad & x = x_i + t\Delta x \\
 & y = y_i + t\Delta y \\
 ② \quad & x_{wmin} \leq x \leq x_{wmax} \quad \text{--- } ① \\
 & y_{wmin} \leq y \leq y_{wmax} \quad \text{--- } ②
 \end{aligned}$$

Liang-Burkely Line Clipping

$B'(x, y)$

③ If $p_c = 0$
Then line is parallel to window
 $\Rightarrow q_c < 0$
Then line is completely outside

If $p_c < 0$ $t_1 = \max(0, \frac{y - y_1}{p_c})$
 $\frac{y - y_1}{p_c} p_c > 0$ $t_2 = \min(0, \frac{y - y_2}{p_c})$
 $\Rightarrow t_1 > t_2$ then terminate

$$y \geq 2$$

$$-4 \leq -2$$

$$x_{wmin} \leq x \Rightarrow x_{wmin} \leq x_i + t\Delta x \Rightarrow -(t\Delta x \geq x_{wmin} - x_i) \Rightarrow -t\Delta x \leq x_i - x_{wmin}$$

$$x_{wmax} \geq x \Rightarrow x_{wmax} \geq x_i + t\Delta x \Rightarrow t\Delta x \leq x_{wmax} - x_i$$

$$y_{wmin} \leq y$$

$$y_{wmax} \geq y$$

$$t p_k \leq q_k$$

$p_1 = -4$	$p_2 = 4$	$p_3 = 4$	$p_4 = -4$
$q_1 = -1$	$q_2 = 5$	$q_3 = 2$	$q_4 = 3$

$$\begin{aligned}
 p_1 &= -\Delta x \\
 h &= x_i - x_{wmin}
 \end{aligned}$$

$$\begin{aligned}
 p_2 &= \Delta x \\
 h &= x_i - x_{wmax}
 \end{aligned}$$

$$\begin{aligned}
 p_3 &= \Delta y \\
 h &= y_i - y_{wmin}
 \end{aligned}$$

$$\begin{aligned}
 p_4 &= -\Delta y \\
 h &= y_i - y_{wmax}
 \end{aligned}$$

$$\begin{aligned}
 & \text{If } t_1 < t_2 \text{ then move to step } 1, 0, 0, 0 \\
 & t_1 = \max(0, \frac{y - y_1}{p_c}) = 0 \\
 & t_2 = \min(0, \frac{y - y_2}{p_c}) = 0
 \end{aligned}$$

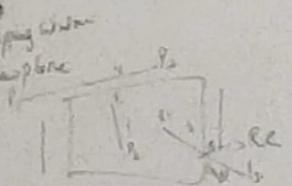
$$\begin{aligned}
 & \frac{-4 + 4 + 4 - 4}{4} = 0 \text{ for } t = 0 \\
 & t_1 = 1.7
 \end{aligned}$$

Line Clipping
- Line Shaded
- Long Dashed

Dot Line
- Shaded Dots

Color Shaded

1001	1000	1010
0011	0000	0010
0111	0100	0110



$$\text{Case 3: } P_1 = 0000 \checkmark \\ P_2 = 0110 \checkmark \\ 0000$$

Line needs to be
clipped

$$\text{Case 2: } P_1 = 1001 \\ P_2 = 1000 \\ 1000 \rightarrow$$

Line is totally
outside the window
Remove the line.

No clip
Line is inside the window

PC P2 fetch the region code
EP

$$P_1 = 0000$$

$$P_1 = \underline{0000} \rightarrow$$

No clip
Line is inside the window